

Introduction to Data Science Course

Evaluation

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Assessment

- ◎ Accuracy: The predictive capability of the classifier
- ◎ Effectiveness:
 - Cost to create the model
 - Cost to use the model
- ◎ Robustness: ability to solve noise or missing value
- ◎ Scale: Efficiency with Big Data
- ◎ Understandable
- ◎ Other properties: Tree size, number of laws, quality of law...

Accuracy

◎ The dataset is divided into two completely independent parts.

- Training set
- Test set

◎ Measures to evaluate accuracy: confusion matrix, fault rate,...

◎ The method of estimating the accuracy of the classifier:

- Holdout method, Random Subsampling

Cross-validation

Bootstrap

Some concepts (1/2)

◎ Let's:

- Positive tuples are samples belonging to a major class that is concerned
- Negative tuples are the models that belong to the remaining classes

◎ P is the number of positive sample, N is number of negative samples in the test set.

◎ TP (True Positives): number of positive samples are classified correctly

◎ TN (True Negatives): number of negative samples are classified correctly

Some concepts (2/2)

- ◎ FP (False Positives): number of negative samples are classified incorrectly to positive samples
- ◎ FN (False Negatives): number of positive samples are classified incorrectly to negative samples.

		Predicted class		
		+	−	Total
Actual class	+	TP	FN	P
	−	FP	TN	N
	Total	P'	N'	$P + N$

Confusion Matrix

Confusion Matrix

A\P	C	¬C	
C	TP	FN	P
¬C	FP	TN	N
	P'	N'	All

- ⊙ Data in computer store, positive samples P are samples with `buys_computer = yes`

Actual class\Predicted class	<code>buy_computer = yes</code>	<code>buy_computer = no</code>	Total
<code>buy_computer = yes</code>	6954	46	7000
<code>buy_computer = no</code>	412	2588	3000
Total	7366	2634	10000

- ⊙ Determine TP, TN, FP, FN?
- ⊙ Ideally, the sub diagonal should be 0 or approximately 0

Accuracy

◎ Accuracy: sample rate in test set is classified correctly.

$$accuracy = \frac{TP + TN}{P + N}$$

◎ Example:

- $accuracy = (6954 + 2588) / 10000 = 0.95$

Actual class\Predicted class	buy_computer = yes	buy_computer = no	Total
buy_computer = yes	6954	46	7000
buy_computer = no	412	2588	3000
Total	7366	2634	10000

Error Rate

- ◎ Error Rate: The sample rate was incorrectly classified in the test set (= 1 - accuracy)

$$\text{error rate} = \frac{FP + FN}{P + N}$$

- ◎ Example:

- error rate = (412 + 46)/ 10000 = 0.05

Actual class\Predicted class	buy_computer = yes	buy_computer = no	Total
buy_computer = yes	6954	46	7000
buy_computer = no	412	2588	3000
Total	7366	2634	10000

Class imbalance (1/2)

◎ Classes of interest can be rare compared to other classes

◎ Example:

- In the phishing detection application, the class of interest is "fraud" but occurs much less than those of the class "Nonfraudulant".
- In diagnosis, the class of interest is "cancer", the sample rate is labeled "yes" much lower than the label "no".



Class imbalance (2/2)

- ◎ Classifier is correct in negative samples but completely incorrect in positive samples
 - ◎ Example:
 - A classifier of accuracy 99% shows a very high probability of prediction. However, if the wrong 1% belongs to the positive sample, 99% becomes pointless
- Resolution by measure sensitivity and specificity

Sensitivity và Specificity

- ◎ Sensitivity: correct positive sample recognition ratio

$$\text{sensitivity} = \frac{TP}{P}$$

- ◎ Specificity: correct negative sample recognition ratio

$$\text{specificity} = \frac{TN}{N}$$

Sensitivity vs. Specificity

- ◎ The classifier has a high accuracy of 96.40%.
- ◎ However, the ability to identify positive samples is quite low because of low sensitivity.

<i>Classes</i>	<i>yes</i>	<i>no</i>	<i>Total</i>	<i>Recognition (%)</i>
<i>yes</i>	90	210	300	30.00
<i>no</i>	140	9560	9700	98.56
Total	230	9770	10,000	96.40

Precision vs. Recall

- ◎ Precision: is the proportion of the class that assigns a label to positive is actually positive.

$$precision = \frac{TP}{TP + FP}$$

- ◎ Recall: is the positive sample rate assigned by the classifier.

$$recall = \frac{TP}{TP + FN} = \frac{TP}{P}$$

Precision and Recall

◎ Precision(yes) = $90/230 = 39.13\%$

◎ Recall(yes) = $90/300 = 30.00\%$

<i>Classes</i>	<i>yes</i>	<i>no</i>	<i>Total</i>
<i>yes</i>	90	210	300
<i>no</i>	140	9560	9700
Total	230	9770	10,000

Precision and Recall

◎ Highest precision is 1.0:

- Showing each sample that the marking class belongs to the positive is actually positive.
- Unable to show the number of positive samples is classified incorrectly

◎ Highest recall is 1.0:

- Showing all positive samples is labeled properly.
- Unable to present how many other samples are mislabeled in the positive.

F-Score

- ◎ F-score: A combination of precision and recall

$$F = \frac{2 \times \text{precision} \times \text{recall}}{\text{precision} + \text{recall}}$$

- ◎ F-score is harmonic mean between precision and recall
- ◎ Equally weighted between precision and recall ($\beta=1$)
- ◎ If you want to one over another, you can set $\beta=2$, $\beta=0.5$

$$F_{\beta} = \frac{(1 + \beta^2) \times \text{precision} \times \text{recall}}{\beta^2 \times \text{precision} + \text{recall}}$$

Example

classes	buy_computer = yes	buy_computer = no	total	recognition(%)
buy_computer = yes	6954	46	7000	99.34
buy_computer = no	412	2588	3000	86.27
total	7366	2634	10000	95.42

F-measure(B-Yes)= 96.81%

Summary of the measurements

A\P	C	¬C	
C	TP	FN	P
¬C	FP	TN	N
	P'	N'	All

Measure	Formula
accuracy, recognition rate	$\frac{TP + TN}{P + N}$
error rate, misclassification rate	$\frac{FP + FN}{P + N}$
sensitivity, true positive rate, recall	$\frac{TP}{P}$
specificity, true negative rate	$\frac{TN}{N}$
precision	$\frac{TP}{TP + FP}$
F , F_1 , F -score, harmonic mean of precision and recall	$\frac{2 \times \text{precision} \times \text{recall}}{\text{precision} + \text{recall}}$
F_β , where β is a non-negative real number	$\frac{(1 + \beta^2) \times \text{precision} \times \text{recall}}{\beta^2 \times \text{precision} + \text{recall}}$

Exercise 3

- ◎ Data relating to the customer classification is deceptive or non-deceptive by a bank before lending:

		<i>Predict</i>		
<i>Actual</i>	Class	Deceptive	Non-deceptive	Total
	Deceptive	44	15	59
	Non-deceptive	20	146	166
	Tổng	64	161	225

- ◎ Suppose the class of interest is deceptive, create confusion matrix
- ◎ Calculating the measurements accuracy, error rate, sensitivity, specificity, precision, F-Score

Estimation methods



Reliability when estimating

- ◎ Whether the figures are calculated from the measurements that are reliable?
 - Depends on the type of data
 - Depend on how the data is collected
 - Depends on how to divide data into training and test episodes.
 - ...
- Method is required to reliably estimate the accuracy

Holdout Method

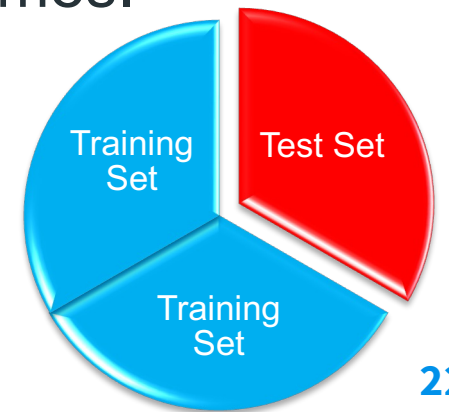
◎ Data is randomly divided into 2 independent sections

- Training set up 2/3 to draw the model
- Test set accounted for 1/3 to estimate accuracy

→ Samples may not represent all data, missing class in the experiment set

◎ Random sampling: is the variant of holdout

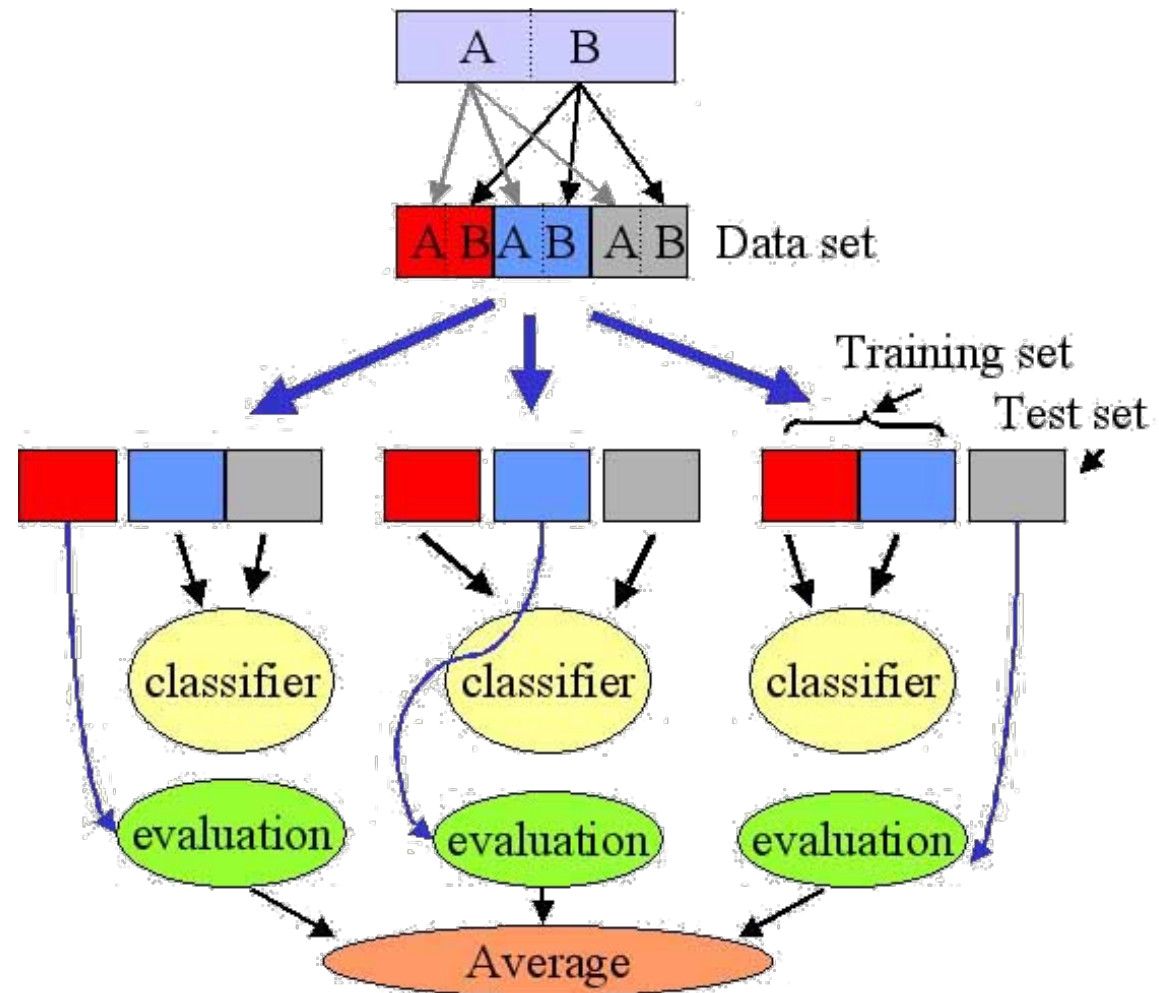
- Repeat holdout k times, the accuracy is the average of all times.



K-fold Cross-Validation

- ◎ Randomly divide the data into K-independent and roughly equal size. $D=\{D1, D2, \dots, Dk\}$
 - Perform k evaluation.
 - For the time i, the D_i episode was used as a test, the rest of the training
 - $K = 10$ commonly used
- ◎ Leave-one-out: is k fold with K is the number of samples (only applies when the data size is small)
- ◎ Stratified cross-validation: Distributing the classes of samples in each fold is roughly the same as the original data


K-fold Cross-Validation



Bootstrap

- ◎ Usually apply to small datasets
- ◎ Each time a sample is selected, it is likely to be picked again and added to the training set
- ◎ There are a few bootstrap methods, which are common **.632 Bootstrap**
 - The d-size dataset will be sampled Bootstrap d times. So training set has d samples. Samples that do not include the training will be used to test. About 63.2% of data fall into training assignments and 36.8% for test episodes (because according to probability $(1-1/d)^d \approx e^{-1} = 0.368$)
 - Repeats the sampling k times and the accuracy:

$$Acc(M) = \frac{1}{k} \sum_{i=1}^k (0.632 \times Acc(M_i)_{test_set} + 0.368 \times Acc(M_i)_{train_set})$$



The End