UWO CS2214 Jan. 19, 2019

Assignment #1
Due: Jan. 29, 2017, by 23:55
Submission: on the OWL web site of the course

Format of the submission. You must submit a single file which must be in **PDF** format. All other formats (text or Miscrosoft word format) will be **ignored** and considered as **null**. You are strongly encouraged to type your solutions using a text editor. To this end, we suggest the following options:

- 1. Miscrosoft word and convert your document to PDF
- 2. the typesetting system LATEX; see https://www.latex-project.org/and https://en.wikipedia.org/wiki/LaTeX#Example to learn about LATEX; see https://www.tug.org/begin.html to get started
- 3. using a software tool for typing mathematical symbols, for instance http://math.typeit.org/
- 4. using a Handwriting recognition system such as those equipping tablet PCs

Hand-writing and scanning your answers is allowed but not encouraged:

- 1. if you go this route please use a scanning printer and **do not take a** picture of your answers with your phone,
- 2. if the quality of the obtained PDF is too poor, your submission will be **ignored** and considered as **null**.

Problem 1 (Undertsamding implication) [20 marks] Let p, q be two Boolean variables. By definition, the implication $p \longrightarrow q$ is true if and only if p is false or q is true. Based on that, we have established the following practical tautologies:

根据定义只有q是false 是错的时候 才会错

1.
$$(p \longrightarrow q) \iff (\neg q \longrightarrow \neg p)$$

$$2. \ (p \leftrightarrow q) \iff ((p \longrightarrow q) \land (q \longrightarrow p))$$

Would these two tautologies still be true if we were changing the truth value of the implication $p \longrightarrow q$ to that of

- 1. $p \wedge q$?
- 2. $p \vee q$?

Justify your answer. Another way of phrasing the question would be the following. Wuld the above tautologies still be tautologies if we were

- 1. repacing \longrightarrow with \land ?
- 2. repacing \longrightarrow with \vee ?

Problem 2 (Proving theorems!) [20 marks] For each of the following statements, translate it into predicate logic and prove it, if the statement is true, or disprove it, otherwise: 如果是错的你要反驳他 证明其为虚假的

- 1. for any two even integers, there exists a third integer (even or odd) the double of which is equal to the sum of the first two integers.
- 2. for any two odd integers, there exists a third integer (even or odd) the triple of which is equal to the sum of the first two integers.

Problem 3 (Finding a treasure!) [20 marks] In the back of an old cupboard you discover a note signed by a pirate famous for his bizarre sense of humour and love of logical puzzles. In the note he wrote that he had hidden treasure somewhere on the property. He listed five true statements and challenged the reader to use them to figure out the location of the treasure.

- 1. If there is an old shipwreck near the beach, then the treasure is buried under a coconut palm tree.
- 2. There is a coconut palm tree growing either at the far end of the island or near the cave.
- 3. Either there is a shipwreck near the beach, or the treasure is hidden in a cave.
- 4. If there is a coconut palm tree at the far end of the island, then there is no shipwreck on the beach
- 5. There is no coconut palm tree near the cave.

Problem 4 (Deciding consistency) [20 marks] A set of propositions is consistent if there is an assignment of truth values to each of the propositional variables, that makes all propositions true. Is the following set of propositions consistent?

- 1. The system is in multiuser state if and only if it is operating normally.
- 2. If the system is operating normally, the kernel is functioning.
- 3. The kernel is not functioning or the system is in interrupt mode.
- 4. If the system is not in multiuser state, then it is in interrupt mode.
- 5. The system is in interrupt mode.

Problem 5 (Deciding satisfiability) [20 marks] Let p, q, r be three Boolean variables. For each of the following propositional formulas determine whether it is satisfiable or not. p = Tq = T and r = F

1.
$$p \wedge (q \vee \neg p) \wedge (\neg q \vee \neg r)$$

2.
$$p \wedge (q \vee \neg p) \wedge (\neg q \vee \neg p)$$
 not satisfiable

任意两个偶数 都能找到一个 数的double 是他们的sum for any two even int, the double of a third int is equal the sum