

Binary Search Tree

- External nodes do store items for our implementation
 - External nodes store items and children point to address 0 (null)
- An inorder traversal of a binary search tree visits the keys in increasing order

Binary Search Trees

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BST Operations

- makeFromEmpty initialize a new tree
- ◆ isEmpty return true if empty, false if not
- search (private) return pointer to node in which key is found, otherwise return NULL
- search(public) return true if key is found, otherwise return false
- ◆ findMin return smallest node value
- ◆ findMax return largest node value

Binary Search Trees

BST Operations

- insert insert a new node into the tree maintaining BST property. All inserts are done at a leaf
- remove remove a node from the tree maintaining BST property.
- display print a tree in an order traversal

Binary Search Trees

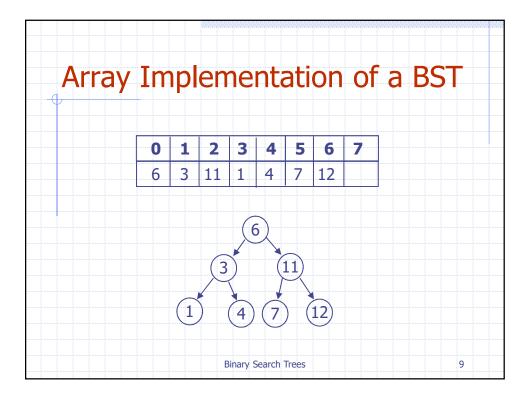
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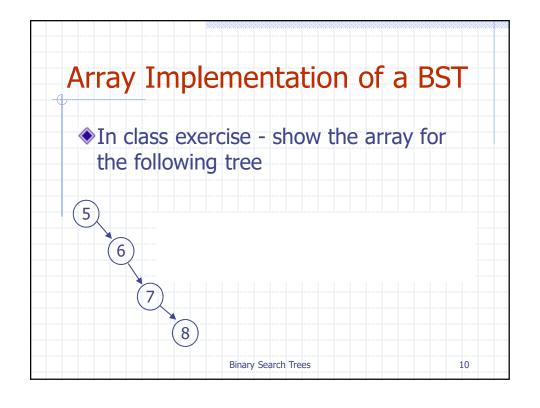
Array Implementation of a BST

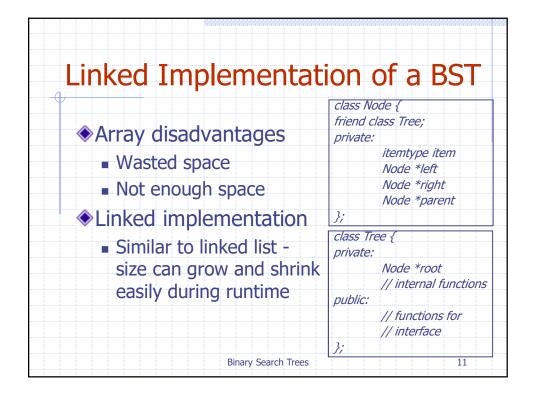
- A BST can be implemented with an array
- Given a node i
 - parent(i) = (i 1)/2
 - If i = 0, then no parent since root
 - leftChild(i) = 2i+1
 - If 2i+1 <= N, otherwise no child
 - rightChild(i) = 2i+2
 - If 2i+2 <= N, otherwise no child

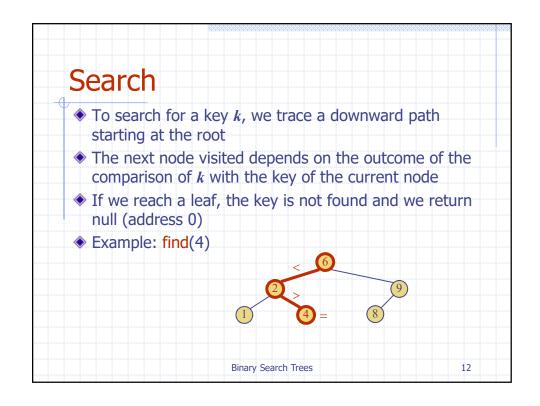
Binary Search Trees

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Search

Recursive implementation of search (private)

Node * search (Node *nodePtr, itemtype key)

if (!nodePtr)

return 0

else if (nodePtr->item == key)

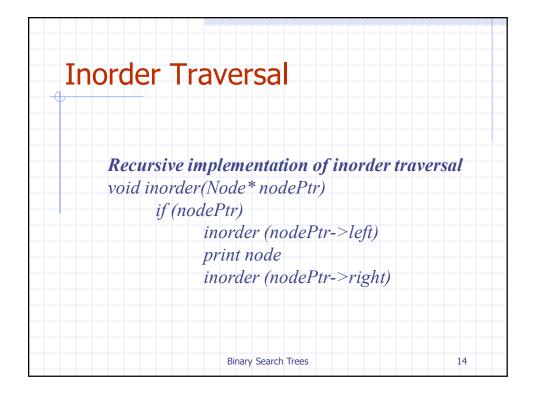
return nodePtr

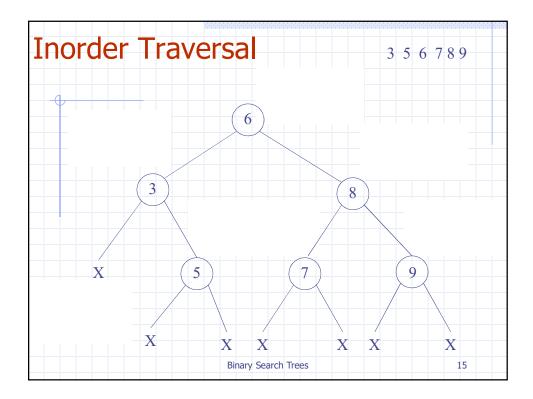
else if (nodePtr->item > key)

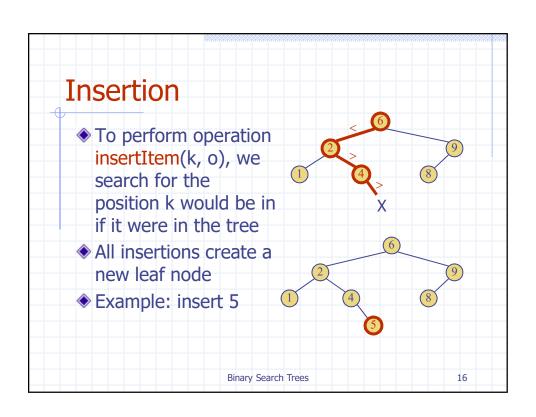
return search(nodePtr->left, key)

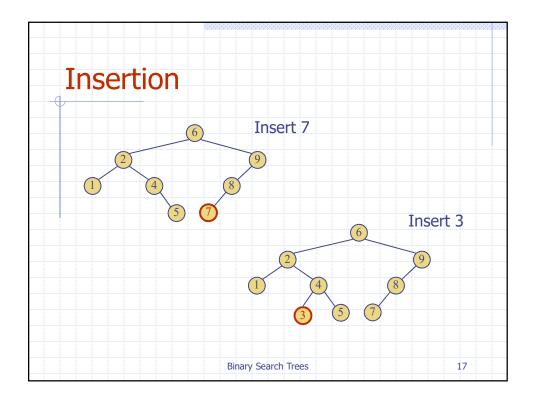
else

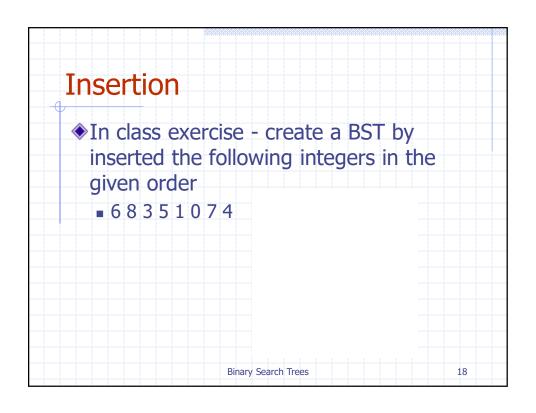
return search(nodePtr->right, key)
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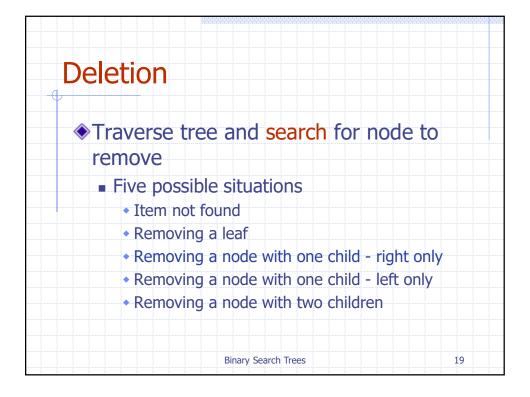


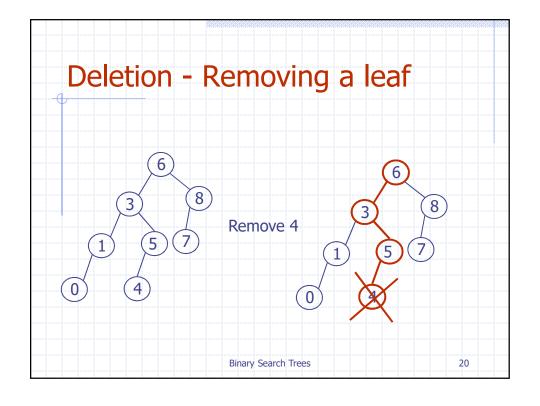












Deletion - Removing a node with children

- Otherwise the node has children find replacement node
 - If the left child exists
 - Replace node information with the *largest* value smaller than the value to remove
 - findMax(leftChild)
 - Else there is a right child
 - Replace node information with the smallest value larger than value to remove
 - findMin(rightChild)

Binary Search Trees

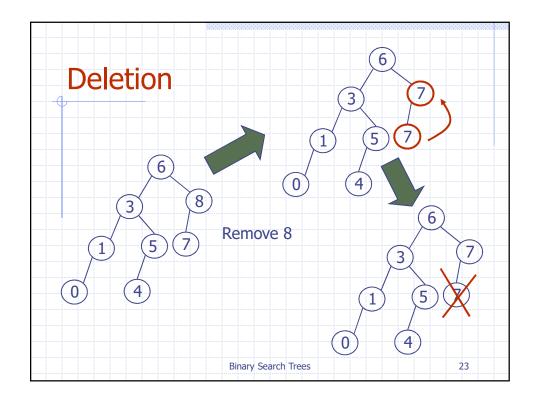
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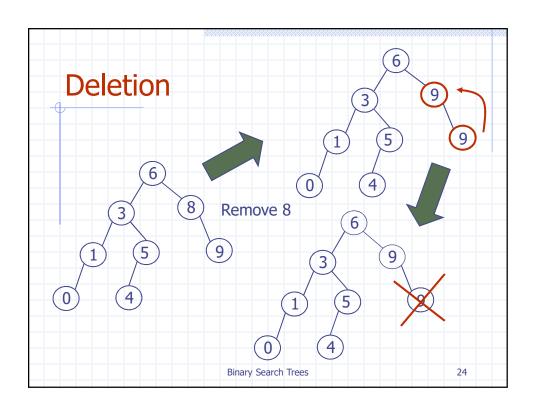
Deletion - Removing a node with children (continued)

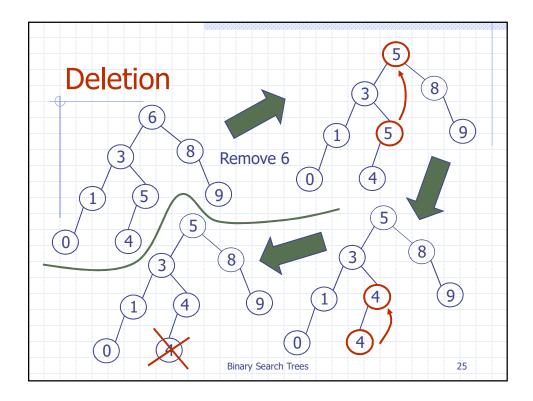
- Splice out replacement node (call remove recursively)
- Just copy in info of replacement node over the value to remove (overload = if necessary)
 - Note this is NOT the best solution if you have a large data structure. The overhead of the copy is too great and you should move the node instead.
- Delete replacement node if leaf

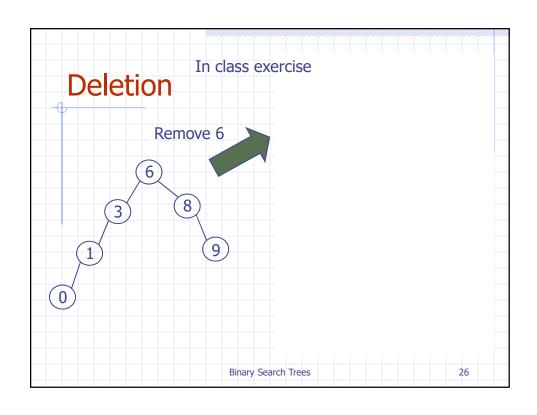
Binary Search Trees

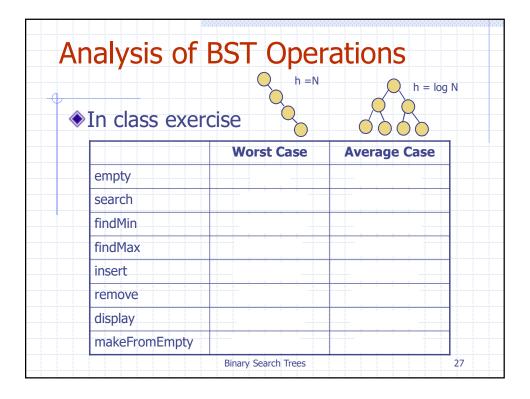
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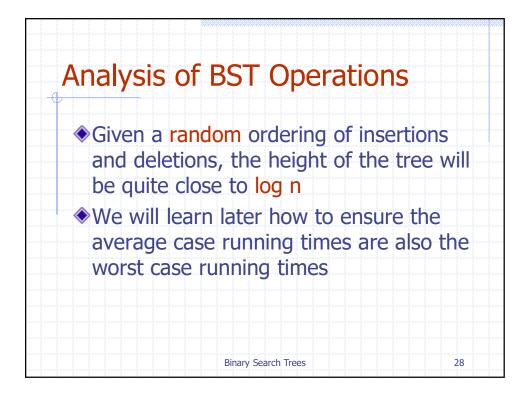












Treesort *Uses a BST to sort records efficiently *Use makeFromEmpty *Read in elements and insert in that order into a BST *Traverse inorder to read out nodes in ascending order *Runtime *Average case - O(N log N) *Worst case - O(N²)