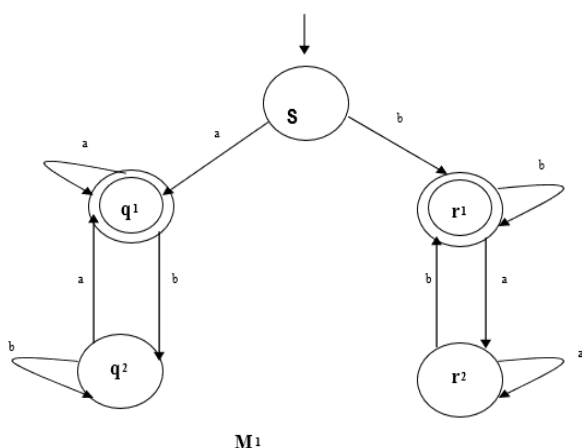


NAME: STANLEY NGUGI CHEGE REG NUMBER: SCT212-0065/2017

ASSIGNMENT 2: FINITE AUTOMATA

The figure below shows the state diagram of a finite automaton M_1 . Give the formal description of this automaton. (5 Marks)

Provide a conclusion on the language accepted by this machine



	Input Alphabet	
States	a	b
S	q1	r1
q1	q1	q2
q2	q1	q2
r1	r2	r1
r2	r2	r1

$$Q = \{S, q1, q2, r1, r2\}$$

$$\Sigma = \{a, b\}$$

$$\delta = \text{Transition Symbol}$$

$$q_0 = \{S\}$$

$$F = \{q1, r1\}$$

Possible path	Pattern
$S \xrightarrow{b} r_1$	b
$S \xrightarrow{b} r_1 \xrightarrow{b} r_1$	bb

$S \rightarrow b \rightarrow r_1 \rightarrow a \rightarrow r_2 \rightarrow b \rightarrow r_1$	<i>bab</i>
$S \rightarrow b \rightarrow r_1 \rightarrow a \rightarrow r_2 \rightarrow a \rightarrow r_2 \rightarrow b \rightarrow r_1$	<i>baab</i>
$S \rightarrow b \rightarrow r_1 \rightarrow b \rightarrow r_1 \rightarrow a \rightarrow r_2 \rightarrow b \rightarrow r_1$	<i>bbab</i>
$S \rightarrow b \rightarrow r_1 \rightarrow b \rightarrow r_1 \rightarrow a \rightarrow r_2 \rightarrow a \rightarrow r_2 \rightarrow b \rightarrow r_1$	<i>bbaab</i>
$S \rightarrow a \rightarrow q_1$	<i>a</i>
$S \rightarrow a \rightarrow q_1 \rightarrow b \rightarrow q_2 \rightarrow a \rightarrow q_1$	<i>aba</i>
$S \rightarrow a \rightarrow q_1 \rightarrow a \rightarrow q_1$	<i>aa</i>
$S \rightarrow a \rightarrow q_1 \rightarrow a \rightarrow q_1 \rightarrow b \rightarrow q_2 \rightarrow a \rightarrow q_1$	<i>aaba</i>
$S \rightarrow a \rightarrow q_1 \rightarrow a \rightarrow q_1 \rightarrow b \rightarrow q_2 \rightarrow b \rightarrow q_2 \rightarrow a \rightarrow q_1$	<i>aabba</i>

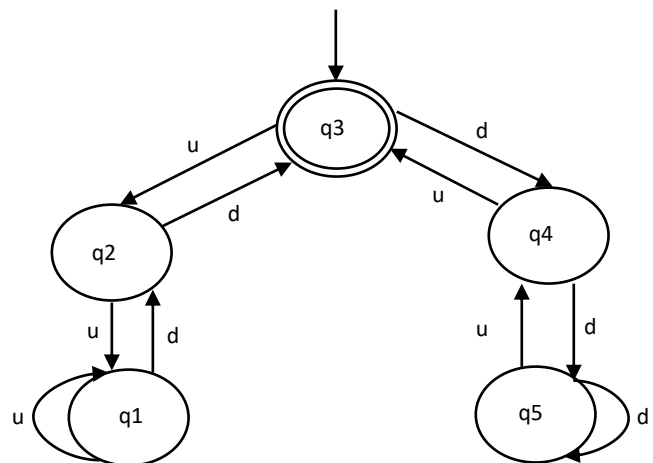
Conclusion

The machine accepts a language that starts with an “a” and ends with an “a” or a language that starts with a “b” and ends with a “b”.

Question Seven (from Logic & Truth Tables Lesson):

The formal description of a DFA is $(\{q_1, q_2, q_3, q_4, q_5\}, (u, d), \delta, q_3, \{q_3\})$, where δ is given by the following transition table. Give the state diagram of this machine. (8 Marks).

	u	d
q_1	q_1	q_2
q_2	q_1	q_3
q_3	q_2	q_4
q_4	q_3	q_5
q_5	q_4	q_5



Conclusion

The machine accepts a language that starts with double ‘u’ and ends with double ‘d’ or starts with double ‘d’ and ends with double ‘u’.