

We want  $E[X]$ .

$$E[X] = E\left[\sum_{i=1}^{n-1} \sum_{j=i+1}^n X_{ij}\right]$$

$$= \sum_{i=1}^{n-1} \sum_{j=i+1}^n E[X_{ij}]$$

$$= \sum_{i=1}^{n-1} \sum_{j=i+1}^n \frac{1}{2}$$

$$= \binom{n}{2} \frac{1}{2}$$

$$= \frac{n(n-1)}{2} \cdot \frac{1}{2}$$

$$= \frac{n(n-1)}{4}$$

Expected number of inversions is  $n(n-1)/4$

4.  $p(A) = 0.32$

$p(B) = 0.25$

$p(C) = 0.2$

$p(D) = 0.18$

$p(E) = 0.05$

$c(A) = 00$

$c(B) = 10$

$c(C) = 110$

$c(D) = 01$

$c(E) = 111$

$$\begin{aligned} \text{Average code length} &= 0.32(2) + 0.25(2) + 0.2(3) + 0.18(2) + 0.05(3) \\ &= 2.25 \end{aligned}$$