## Determining the Mobility of Charge Carriers in Organic Semiconductors

#### Masters' Thesis

Submitted in partial fulfillment of the requirements of BITS F421T Thesis

By

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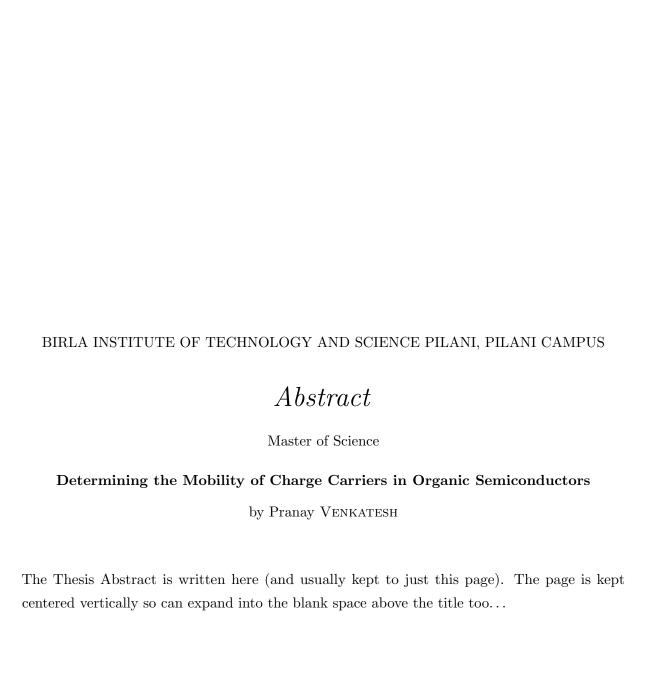
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## Acknowledgements

The acknowledgements and the people to thank go here, don't forget to include your project advisor. . .

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## Abbreviations

LAH List Abbreviations Here

## **Physical Constants**

Speed of Light  $~c~=~2.997~924~58\times10^8~\mathrm{ms^{-S}}$  (exact)

*Glossary* xii

Dedicate this to someone, anyone.

## Introduction

#### 1.1 Semiconductor Materials

#### 1.2 Electronic Structure

The electronic structure is the solution of the quantum states of electrons in a given chemical system. Typically, this involves determining the energies and wavefunctions of the various states. This can be done by solving the Schrödinger equation for molecules.

#### 1.3 Phonons

#### 1.4 Path Integrals

## Organic Semiconductor Materials

- 2.1 Introduction
- 2.2 Rubrene
- 2.3 Y6

## Polarons

- 3.1 Introduction
- 3.2 Pekar's Polaron
- 3.3 Fröhlich Polaron
- 3.4 Holstein Polaron

# Path Integrals and Quantum Dynamics

#### 4.1 Introduction

If we want to understand the electronic properties of materials, our limited understanding of analytically solvable quantum systems does not get us very far. There's only a limited number of systems with analytical solutions.

As in the case of classical mechanics, any realistic depiction of quantum systems would require understanding how the system couples with an environment, which influences it heavily. Open quantum system theory hence helps us with this problem since we can learn what happens to systems that interact with an environment and how that affects their dynamics. The easiest models of open quantum systems are called "system-bath" models where you have a (reasonably) solvable system coupled to a bath that represents the effects of an environment.

For studying electron-phonon systems, we need to construct models whereby we can understand what happens to the electrons when they interact with an ionic lattice as an environment. This chapter starts by covering the general theory of open quantum systems and the best ways to treat their evolution. We then move on to the path integral formulation and discuss how that helps us with the quantum dynamics of system-bath models. Once we have constructed these path integral equations, we move onto evaluating the path integrals using Monte Carlo simulations.

#### 4.2 Dynamics of Open Quantum Systems

For isolated quantum systems, the dynamics can be described by the time-dependent Schrödinger equation (TDSE):

$$-i\hbar \frac{\partial}{\partial t} |\Psi(x,t)\rangle = \mathcal{H} |\Psi(x,t)\rangle \tag{4.1}$$

The average values of a time-dependent observable A is given by

$$A(t) = \langle \Psi(t) | \hat{A} | \Psi(t) \rangle \tag{4.2}$$

One of our objectives is to figure out how a quantum-mechanical system moves from an initial state  $t_0$  to a final state. A convenient tool to describe the states of macroscopic systems that can be formed from a mixture of pure states  $\{\Psi_{\nu}\}$  is the density operator  $\hat{W}$ , given by

$$\hat{W} = \sum_{\nu} w_{\nu} |\Psi_{\nu}\rangle \langle \Psi_{\nu}| \tag{4.3}$$

which is a summation over the projection operators onto the pure states with a probability weight of  $w_{\nu}$ . Expectations for observables can now be determined by :  $\langle \hat{A} \rangle = Tr\{\hat{W}\hat{A}\}$ .

First let us try to construct an equation of motion for the density operator.

#### 4.2.1 Liouville-von Neumann Equation

John von Neumann extended the classical Lioville equation for phase space trajectories to quantum statistics.

The time propagation of the wavefunctions in eq. 4.1 can be written as

$$|\Psi(t)\rangle = U(t, t_0) |\Psi(t_0)\rangle \tag{4.4}$$

where

$$U(t, t_0) = \exp\left(-\frac{i\mathcal{H}(t - t_0)}{\hbar}\right)$$

.

We can substitute eq 4.4 in in eq 4.3 to obtain a time-dependent equation for the density operator.

$$\hat{W}(t) = \sum_{\nu} w_{\nu} U(t, t_0) |\Psi(t_0)\rangle \langle \Psi(t_0)| U^{\dagger}(t, t_0) = \sum_{\nu} U(t, t_0) W(t_0) U^{\dagger}(t, t_0)$$
(4.5)

To derive a time-derivative equation, take a partial derivative on both sides with respect to t:

$$\frac{\partial}{\partial t}\hat{W}(t) = -\frac{i}{\hbar}(\mathcal{H}\hat{W} - \hat{W}\mathcal{H}) = -\frac{i}{\hbar}[\mathcal{H}, \hat{W}(t)] \tag{4.6}$$

Equation 4.6 is called the Liouville-von Neumann equation and is the simplest equation for the evolution of macroscopic quantum systems. For brevity we can use the notation of super-operator  $\mathcal{L} = \frac{1}{\hbar}[H,(.)]$  to get

$$\frac{\partial}{\partial t}\hat{W} = -i\mathcal{L}\hat{W}$$

#### 4.2.2 System-Bath Models and The Reduced Density Matrix

For models where we have a system coupled to a bath, we will represent our Hamiltonian in the form :

$$\mathcal{H} = \mathcal{H}_S + \mathcal{H}_R + \mathcal{H}_{int} \tag{4.7}$$

Where  $\mathcal{H}_S$  is the Hamiltonian of the relevant system, represented only in terms of system coordinates  $s = \{s_j\}$  and momenta  $p = \{p_j\}$ ,  $\mathcal{H}_R$  is the Hamiltonian of the reservoir having coordinates  $Z = \{Z_{\xi}\}$  and momenta  $P = \{P_{\xi}\}$ .  $\mathcal{H}_{int}$  is the linear coupling term of the system and the reservoir.

For harmonic baths, the reservoir Hamiltonian reads

$$\mathcal{H}_R = \sum_{\xi} \frac{P_{\xi}^2}{2M} + \frac{1}{2} M \omega_{\xi}^2$$

Since the system and bath are coupled, we cannot come up with a factorization scheme to separate the wavefunction out into system and bath co-ordinates. However, we can work out some kind of separation for the statistical operator.

Consider matrix elements of the statistical operator :

$$W(s, z; s', z'; t) = \langle s | (\langle Z | \hat{W} | Z' \rangle) | s' \rangle$$

If we want to write out a statistical operator in the state-space of the system co-ordinates alone, it would look like:

$$\rho(s, s'; t) = \int dZ < s |(\langle Z | \hat{W} | Z' \rangle)| s' \rangle$$
(4.8)

These can be considered as the matrix elements of a Reduced Density Operator (RDO):

$$\hat{\rho}(t) = \int dZ \langle Z | \hat{W}(t) | Z \rangle \tag{4.9}$$

This is a partial trace of the statistical operator over the reservoir coordinates. If we instead had a basis set  $\{|\alpha\rangle\}$  that represented the reservoir states, we could write the RDO as:

$$\hat{\rho}(t) = \sum_{\alpha} \langle \alpha | \hat{W}(t) | \alpha \rangle = \text{Tr}_{R} \{ \hat{W}(t) \}$$
(4.10)

The matrix elements of the RDO can be defined using any basis that represents the system. If  $|a\rangle$  and  $|b\rangle$  are members of a basis of the system state-space, we can get the relevent matrix element  $\rho_{ab}$  by

$$\rho_{ab}(t) = \langle a | \, \rho(t) \, | b \rangle \tag{4.11}$$

This defines the elements of the Reduced Density Matrix (RDM).

If we have an electron interacting with a bath of harmonic modes with frequencies  $\{\omega_i\}$ , then we can abstract out the effect of this bath using the spectral density function:

$$J(\omega) = \sum_{\xi} g_{\xi}^2 \delta(\omega - \omega_{\xi}) \tag{4.12}$$

Where  $g_{\xi}$  is the coupling coefficient for each mode.

#### 4.2.3 Quantum Master Equations

#### 4.2.4 Adiabatic and Markov Approximations

#### 4.3 Path Integral Treatment of Open Quantum Systems

For a general Hamiltonian in cartesian co-ordinates

$$\mathcal{H} = \sum_{j} \frac{p_{j}^{2}}{2m_{j}} + V(x_{1}, ..., x_{n})$$

To propagate this system from an initial  $(t_0, x_0)$  to a final  $(t_f, x_f)$ , let us split the time scale t into N short time chunks  $\Delta t \equiv \frac{t}{N}$ . Now the time-evolution operator can be written as:

$$e^{-i\mathcal{H}t/\hbar} = e^{-i\mathcal{H}\Delta t/\hbar} \dots e^{-i\mathcal{H}\Delta t/\hbar} = \prod_{k=1}^{N} e^{-i\mathcal{H}(t_k - t_{k-1})/\hbar}$$
(4.13)

where  $t_k = kt/N$ .

Using

$$\int dx_k |\psi_k\rangle \langle \psi_k| = 1$$

between successive steps we get:

$$\langle x_f | e^{-i\mathcal{H}t/\hbar} | x_0 \rangle = \int dx_1 ... \int dx_{N-1} \prod_{k=1}^N \langle x_k | e^{-i\mathcal{H}(t_k - t_{k-1})/\hbar} | x_{k-1} \rangle$$
 (4.14)

This is an exact representation for any value of N.  $x_f \equiv x_N$  is the final point in the propagation.

To evaluate this integral, we need an approximation to evaluate the short time propagator in a time-step  $\Delta t$ . If operators A and B do not commute, we cannot use the rule of exponential of a sum of operators equals the product of exponentials of the operators. The expansion of  $e^{A+B}$  developed by Suzuki and Trotter helps us alleviate this problem. They found that:

$$e^{\delta(A+B)} = e^{\delta A}e^{\delta B} + O(\delta^2) \tag{4.15}$$

The error term  $O(\delta^2)$  vanishes when we take the limit of  $\delta \to 0$ .

As a guess way to split the Hamiltonian if we separate out the kinetic term  $\mathcal{T}$  and the potential term  $\mathcal{V}$  in the following way :

$$e^{-i\mathcal{H}\Delta t/\hbar} \approx e^{-i\mathcal{V}\Delta t/2\hbar} e^{-i\mathcal{T}\Delta t/\hbar} e^{-i\mathcal{V}\Delta t/2\hbar}$$
 (4.16)

We can evaluate the kinetic part exactly to get:

$$\langle x_k | e^{-i\mathcal{H}\Delta t/\hbar} | x_{k-1} \rangle = \prod_{j=1}^n \left( \frac{m_j}{2\pi i\hbar \Delta t} \right)^{1/2} \exp\left( \frac{i}{\hbar} \frac{m_j}{2\Delta t} (x_{j,k} - x_{j,k-1})^2 \right)$$
(4.17)

Plugging this into the propagation expression we get:

$$\langle x_f | e^{-i\mathcal{H}t/\hbar} | x_0 \rangle \approx \prod_{j=1}^n \left( \frac{m_j N}{2\pi i\hbar t} \right)^{1/2} \int d^n x_1 \dots \int d^n x_{N-1}$$

$$\exp \left( \frac{i}{\hbar} \sum_{k=1}^N \left( \sum_{j=1}^n \frac{m_j N}{2t} (x_{j,k} - x_{j,k-1})^2 - \frac{t}{2N} [\mathcal{V}(x_k) + (V_{k-1})] \right) \right)$$
(4.18)

This equation is the "primitive" discretized path integral expression. As we use more sophisticated methods to split the Hamiltonian we will get better discretized expressions to work with.

When we take the limit of  $N \to \infty$ , we get an equality.

$$\langle x_f | e^{-i\mathcal{H}t/\hbar} | x_0 \rangle = \int \mathcal{D}x \exp\left(\frac{i}{\hbar}S[x]\right)$$
 (4.19)

Where S[x] is the action functional  $\int \mathcal{L}[x,t]dt$  of the path. This is the well-known Feynman path integral expression. We will however be dealing with discretized path integral expressions to understand the dynamics of systems we're interested in.

We cannot use monte carlo methods to sample the primitive discretization of the path integral since it is a highly oscillatory function. Typically the phase terms cancel each other out dramatically in this oscillating function and Monte carlo schemes carried over long time periods fail to capture all the information necessary. This is called the Monte carlo "sign problem".

We take three approaches to try and deal with this. The first is to substitute the time term with another variable so that the phase factor (and consequently the integrand) becomes real. The second approach is to use a better Trotter splitting scheme to generate well-behaved propagators to simulate long time dynamics. The third uses a method from complex analysis known as "analytic continuation" to determine the observables of interest.

#### 4.4 Imaginary Time Path Integral Monte-Carlo

This is the first of the approaches we take to tackle the sign problem that arises in evaluating path integrals using monte carlo simulations.

#### 4.5 Real Time Path Integral Dynamics

One of the major issues with performing real-time path integral monte carlo simulations is the infamous sign problem, as mentioned earlier. To alleviate the sign problem, we employ a method

developed by Makri and co-workers [QuAPI and QCPI citations] to develop equations that converge when attempting to numerically sample discretized path integral expressions using Monte Carlo simulations.

#### 4.5.1 Quasi-Adiabatic Propagator Path Integral (QuAPI)

#### 4.5.2 Quantum-Classical Path Integral (QCPI)

#### 4.5.3 Evaluating the Real-Time Path Integrals

#### 4.5.4 Determining Observables

#### 4.5.4.1 Mobility

For determining the mobility of the polarons in these systems we use the Einstein-Smoluchowski relation :

$$\mu = \beta q D \tag{4.20}$$

Where  $\mu$  is the mobility, q is the charge, D is the diffusion coefficient and  $\beta = \frac{1}{k_B T}$ .

For getting the mobility we use a method developed by Blumberger and co-workers [Blumberger mobility cite].

The diffusion coefficient can be got from the Mean Square Displacement (MSD) as follows:

$$D = \frac{1}{2} \lim_{t \to \infty} \frac{dMSD}{dt} \tag{4.21}$$

In the diffusive regime, the MSD is a linear function of time, so we simply take the slope of MSD vs t calculations for calculating mobility.

There are multiple definitions for how to compute the MSD for quantum dynamics simulations [cite relevant papers] but we have chosen to use the following:

$$MSD(t) = \sum_{k=1}^{M} P_k(t)(x_k(t) - x(0))^2$$
(4.22)

Here,  $P_k(t) = \rho_{kk}$  is the population of site k at time t. This calculation of MSD is typically averaged over multiple simulations of the dynamics calculation.

#### 4.5.4.2 Polaron Radius

#### 4.5.4.3 Self-Energy

#### 4.6 Analytic Continuation Method

We can also obtain the mobility of polarons using a combination of imaginary and (short) real time path integral monte carlo simulations using an analytic continuation [Vukmirovic ref].

The Holstein polaron Hamiltonian for an electron coupled to phonon modes in a lattice is given by:

$$\mathcal{H} = \sum_{n} \left[ -J(c_n^{\dagger} c_{n+1} + c_{n+1}^{\dagger} c_n) + \left( \frac{P_n^2}{2M} + \frac{1}{2} M \omega_n^2 Z_n^2 \right) + g_n c_n^{\dagger} c_n Z_n \right]$$
(4.23)

Where  $c_n$  and  $c_{n+1}$  represent the annihilation operators in second-quantization representation for electrons at lattice sites n and n+1 respectively.

We can split this as  $\mathcal{H} = \mathcal{H}_0 + \mathcal{H}_1 + \mathcal{H}_2$  where  $\mathcal{H}_2$  is the first term representing electron energies,  $\mathcal{H}_0 = \sum_n \frac{P_n^2}{2M}$  and  $\mathcal{H}_1$  contains the other terms.

The DC mobility  $\mu$  is given by the Kubo formula :

$$\mu = \frac{\beta}{2} \int_{-\infty}^{\infty} dt < j(t)j(0) > \tag{4.24}$$

Where j is the current density operator.

For two arbitrary operators A and B the time-correlation function (TCF) is given by:

$$\langle A(t)B \rangle = Z^{-1} \operatorname{Tr} \left[ e^{-\beta \mathcal{H}} e^{it\mathcal{H}} A e^{-it\mathcal{H}} B \right]$$
 (4.25)

If we split beta into m intervals  $(\tau = \beta/m)$  and t into Q intervals  $(t = \Delta t/Q)$  and perform a Suzuki-Trotter decomposition of the Hamiltonian based on the splitting mentioned earlier, we can write the TCF as:

$$\langle A(t)B \rangle = Z^{-1} \operatorname{Tr} \left[ (e^{-\tau \mathcal{H}_0} e^{-\tau \mathcal{H}_1} e^{-\tau \mathcal{H}_2})^m (e^{i\Delta t \mathcal{H}_0} e^{it\mathcal{H}_1} e^{i\Delta t \mathcal{H}_2})^Q A (e^{-i\Delta t \mathcal{H}_0} e^{-i\Delta t \mathcal{H}_1} e^{-i\Delta t \mathcal{H}_2})^Q B \right]$$

$$(4.26)$$

If we consider the basis states to be a direct product of electron momenta and phonon coordinates :

$$|k; \{X\}\rangle = |k\rangle |X_1\rangle |X_1\rangle \dots |X_N\rangle \tag{4.27}$$

We can derive a path integral expression for the TCF and sample it using Monte carlo calculations performed over both a short real time t and over imaginary time.

To get the mobility, we construct the inverse equation of the current density TCF:

$$\langle j(t_c)j(0)\rangle = \int_{-\infty}^{\infty} d\omega \frac{1}{\pi} \frac{\omega e^{-i\omega t_c}}{1 - e^{-\beta\omega}} Re\mu(\omega)$$
 (4.28)

Where  $t_c$  represents both the imaginary time  $t_c = -it$  where  $0 \le t \le \beta$  and short real times  $t_c = t$ .

To perform the analytic continuation, we first discretize this integral equation:

$$\mathbf{j} = \mathbf{K} \cdot \mathbf{m} \tag{4.29}$$

Where  $\mathbf{j}$  represents the discretized current density TCF elements in real and imaginary time.  $\mathbf{m}$  is the discretized representation of the real part of the mobility.  $\mathbf{K}$  is a linear operator that takes care of the integral term. We need to get  $\mathbf{m}$ , knowing  $\mathbf{K}$  (from discrete fourier transforms) and  $\mathbf{j}$  (from the real and imaginary time monte carlo calculations). We get  $\mathbf{m}$  by performing a Singular Value Decomposition of  $\mathbf{K}$  and using the factors to derive the elements of  $\mathbf{m}$ .

## Modelling Real Materials

#### 5.1 Introduction

To model real materials

- 5.2 Electronic Structure Data
- 5.3 Phonon Modes
- 5.4 Coupling Constants
- 5.5 Constructing Reference Hamiltonians
- 5.6 Modelling Dynamics

## Results

#### 6.1 Pentacene

In this example, we model the dynamics of the pentacene dimer and tetramer using the path integral non-adiabatic dynamics techniques as mentioned.

To study charge transfer processes in molecular aggregates, we use a one-dimensional nearest-neighbours (NN) Hamiltonian of the form [Borelli Ref]. :

$$\mathcal{H} = \sum_{n,m}^{N_e} \epsilon_{nm} |n\rangle \langle m| + \sum_{k=1}^{F} \frac{\omega_k}{2} (P_k^2 + Z_k^2) + \sum_{n,k}^{N_e,F} g_k^{(n)} Z_k |n\rangle \langle n|$$
 (6.1)

Here  $\epsilon_{nm}$  represents the members of a matrix of electronic energies and couplings. For the nearest-neighbour pentacene model we are considering we use a value of  $\epsilon_{12} = 300cm^{-1}$ . The "system" part of the Hamiltonian ( $\mathcal{H}_s$ ) is described by the first term of electron couplings. The second term represents the energies of the vibrational modes, treated as harmonic in this case. The third term is the linear coupling between each electron and the vibrational mode at site k. The vibrational frequencies and linear coupling terms are determined by Density Functional Theory calculations [Borelli Hopping Ref].

The effects of the bath are taken into consideration by the spectral density. We model the interactions as an effective Debye spectral density with reorganization energy  $\lambda = 100cm^{-1}$  and characteristic frequency  $\gamma = 50cm^{-1}$ .

Using calculations from the Quantum-Classical Path Integral method, we can see the propagation of the density matrix. We can use this data to obtain the populations of the various sites (diagonal elements) and the coherences between the sites (off-diagonal elements).

Chapter 6. Results

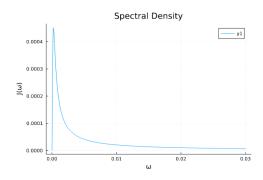
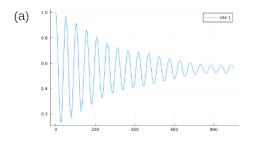
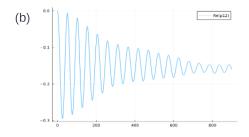


FIGURE 6.1: Debye Spectral Density for Pentacene





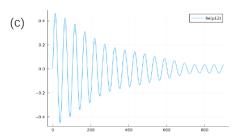


Figure 6.2: Density Matrix Elements of Pentacene dimer. (a)  $\rho_{11}$  population of site 1 (b)  $Re(\rho_{12})$  Real part of coherence (c)  $Im(\rho_{12})$  Imaginary part of coherence

Chapter 6. Results

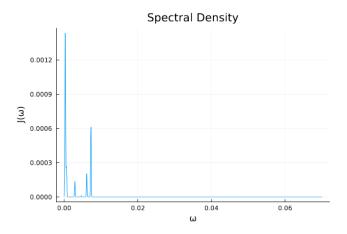


FIGURE 6.3: Spectral Density (with Gaussian broadening) for Rubrene

#### 6.2 Rubrene

Here, we attempt to model the dynamics of the Holstein-Peierls polaron in rubrene using the model developed by Ordejon, et al [Ordejon citation], where the Hamiltonian is given by :

$$\mathcal{H} = \sum_{M,N} \epsilon_{MN} a_M^{\dagger} a_N + \sum_{Q=(Z,P)} \omega_Q (b_Q^{\dagger} b_Q + \frac{1}{2}) + \sum_{Q,M,N} \omega_Q g_{MN}^Q (b_{-Q} + b_Q^{\dagger}) a_M^{\dagger} a_N$$
 (6.2)

The effects of the bath are taken into consideration by the spectral density  $J(\omega) = \sum_i g_i^2 \delta(\omega - \omega_i)$ . We use a Gaussian line-shape broadening to model the spectral density  $J(\omega)$ .

We consider a simplified 1-dimensional chain of 10 rubrene sites with interactions between the nearest 2 neighbours.

By evaluating the QuAPI integral using tensor-train Monte carlo computations, we obtain the values of the RDM elements over time. We can use the diagonal elements to get the site populations. Chapter 6. Results

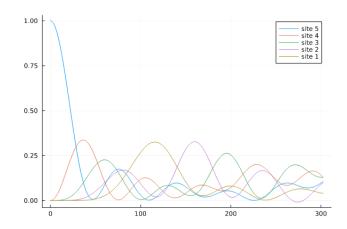


FIGURE 6.4: Populations of various sites in rubrene over time

## Appendix A

## Feynman Variational Approach to the Polaron Problem