

# COMP30024 Artificial Intelligence Project 1 Report

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## search problem formulation

- **State**: player pieces and obstacle pieces' location on board
- **Action**: player can move, jump or exit one player piece per turn defined in specification
- **Goal Test**: no player's piece on board
- **Path Cost**: 1 cost per action

## search algorithms

### terminology

- **b**: branching factor for search tree
- **d**: length for the solution path in search tree
- **$\delta$** : relative error in heuristic =  $|h^*(s) - h(s)|$
- **dist<sub>SLD</sub>**: straight line distance in hexe

### a\* search

- time complexity
  - best case  $\in O(d)$  if we disregard the complexity of the heuristic calculation
  - average case  $\in O(b^{\delta d})$  (from lecture)
  - worst case  $\in O(b^d)$  (because it is uniform cost search now)
- space complexity  $\in O(b^{\delta d})$  (because "keep all nodes in memory")
- completeness
  - Yes, as we are guaranteed in the specification "at least one winning sequence of actions exists"
- optimality
  - Yes, as long as  $h(s) \leq h^*(s) \forall s \in \text{state space}$

### heuristic function

- $h(\text{state}) = \sum_{\text{piece} \in \text{player}} (\lceil \text{dist}_{\text{SLD}}(\text{piece}) / 2 \rceil + 1)$
- admissibility:
  - Discussing Red player is similar for Green and Blue player as they are parallel cases. So we can only discuss Red player case at here.  
Fastest path for a single piece on board to reach in goal hexe is that the piece can jump to goal hexe as much as possible and then exit. i.e.  $h(\text{piece to goal hexe}) = \# \text{ jump action} = \lceil \frac{\text{number of move action}}{2} \rceil$ .  
Where  $\# \text{ move action}$  can be measured by SLD distance  
 $\therefore \# \text{ jump action}$  is the ideal(lower bound of) length of path for the piece to reach the goal hexe as described above  
 $\therefore h^*(\text{piece}) \geq \# \text{ jump action} + 1$ . Note: plus 1 for exit action  
 $\therefore h^*(\text{state}) \geq \sum_{\text{piece} \in \text{player}} h(\text{piece}) = \sum_{\text{piece} \in \text{player}} (\lceil \text{dist}_{\text{SLD}}(\text{piece}) / 2 \rceil + 1)$

### problem feature impact

## **search tree**

- branching factor
- depth

## **other features of the input impact on search algorithm**

- time complexity
- space complexity