Maclaurin Series

$$e^{x} = 1 + x + \frac{1}{2}x^{2} + o(x^{2}) = \sum_{n=0}^{\infty} \frac{1}{n!}x^{n}, \ x \in (-\infty, +\infty)$$
 (1)

$$\sin x = x - \frac{1}{6}x^3 + o(x^3) = \sum_{n=0}^{\infty} \frac{(-1)^n}{(2n+1)!} x^{2n+1}, \ x \in (-\infty, +\infty)$$
 (2)

$$\stackrel{Derivation}{\Longrightarrow} \cos x \qquad = 1 - \frac{1}{2}x^2 + o(x^3) \qquad = \sum_{n=0}^{\infty} \frac{(-1)^n}{(2n)!} x^{2n}, \ x \in (-\infty, +\infty)$$
 (3)

$$\arcsin x = x + \frac{1}{6}x^3 + o(x^3) = \sum_{n=0}^{\infty} \frac{(2n)!}{4^n(n!)^2(2n+1)} x^{2n+1}, \ x \in [-1,1]$$
 (4)

$$\tan x = x + \frac{1}{3}x^3 + o(x^3) = \sum_{n=1}^{\infty} \frac{B_{2n}(-4)^n (1-4^n)}{(2n)!} x^{2n-1}, \ x \in (-\frac{\pi}{2}, \frac{\pi}{2})$$
 (5)

$$\arctan x = x - \frac{1}{3}x^3 + o(x^3) = \sum_{n=0}^{\infty} \frac{(-1)^n}{2n+1} x^{2n+1}, \ x \in [-1, 1]$$
 (6)

$$(1+x)^{\alpha} = 1 + \alpha x + \frac{\alpha(\alpha-1)}{2}x^2 + o(x^2) = \sum_{n=0}^{\infty} C_{\alpha}^n x^n, \ x \in (-1,1)$$
 (7)

$$\ln(1+x) = x - \frac{1}{2}x^2 + o(x^2) = \sum_{n=0}^{\infty} \frac{(-1)^n}{n+1} x^{n+1}, \ x \in (-1,1]$$
 (8)

Derivation
$$\frac{1}{1+x}$$
 = $1-x+x^2+o(x^2)$ = $\sum_{n=0}^{\infty} (-1)^n x^n, \ x \in (-1,1)$ (9)

$$\stackrel{x \to (-x)}{\Longrightarrow} \frac{1}{1-x} = 1 + x + x^2 + o(x^2) = \sum_{n=0}^{\infty} x^n, \ x \in (-1,1)$$
 (10)