$$\begin{split} &\lim_{x\to 0} \left(\frac{a_1^x + a_2^x + a_3^x + \dots + a_n^x}{n}\right)^{\frac{1}{x}} \\ &= \lim_{x\to 0} e^{\left(\frac{1}{x}\ln\frac{a_1^x + a_2^x + a_3^x + \dots + a_n^x}{n}\right)} \\ &= \lim_{x\to 0} e^{\left(\frac{1}{x}\ln\left(1 + \frac{a_1^x + a_2^x + a_3^x + \dots + a_n^x - n}{n}\right)\right)} \\ &= \lim_{x\to 0} e^{\left(\frac{1}{x}\left(\frac{a_1^x + a_2^x + a_3^x + \dots + a_n^x - n}{n}\right)\right)} \\ &= \lim_{x\to 0} e^{\left(\frac{1}{x}\left(\frac{a_1^x + a_2^x + a_3^x + \dots + a_n^x - n}{n}\right)\right)} \\ &= \lim_{x\to 0} e^{\left(\frac{a_1^x + a_2^x + a_3^x + \dots + a_n^x + a_n^x + n + a_n^x + a_n$$