

CE2101/ CZ2101: Algorithm Design and Analysis

Week 4: Review Lecture

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Content

- Comparison of Sorting Algorithms
- Greedy Strategy
- Dijkstra's Algorithm



omparison of Sorting Algorithms

Time complexity comparison:

	Best	Average	Worst
Insertion Sort	n	n2	n2
Mergesort	n log n	n log n	n log n
Quicksort			
*Radix	n	n	n
Heapsort			

^{*} Radix sort is not required



Empirical Parformance

Compared by time (in milliseconds)

Insertion Sort	0.1	168	342	23,382	
Mergesort	2.0	2.3	2.2	30	
Quicksort	0.7	0.9	0.7	12	best performance
*Radix	1.6	1.6	1.6	18	perjarmana
Heapsort	3.4	3.5	3.6	49	umbers

Reference: Shaffer, C. A. (2001). A practical introduction to data structures and algorithm analysis. Upper Saddle River, NJ: Prentice Hall.

'UP' and **'DOWN**' columns show the performance for inputs of size 10,000 where the numbers are in ascending (sorted) and descending (reversely sorted) order. Figures are timings obtained using workstation running UNIX.



Greedy Strategy

- To solve optimization problems: min or max
- Make a best choice at each step by using only knowledge available at the time.
- The choice is not expensive and cannot be undone.
- Global optimum may not be guaranteed.



<u>Diiketra'e Algorithm</u>

- Single source shortest path on a weighted, directed graph.
- All weights must be nonnegative.





- Initialise d and pi
- Set S to empty
- 3. While there are still vertices in **V S**
 - i. Move **u**, the vertex in **V S** that has the shortest path estimate from source (smallest d), to **S**
 - ii. 5402: For all the neighbors of u in V S, update their estimates of shortest distances to the source (d)



Evarcica

Suppose our goal is to sort an array in ascending order, and in the input array A of size 600 there are no more than 10 inversions, i.e. pairs of array indices (i, j) such that i < j and A[i] > A[j]. Which of the sorting algorithms learnt in the lectures would you use to sort array A? Briefly justify your answer. [AY1718S1]

Insertion. (1. Switchle for almost sorted array)

12. 600 is considered small input size, inversion.



The *union* of two sets A and B is a set C such that an element x is in C if and only if x is in A or B. Note that, if x is in both A and B, then x will appear in the union C exactly once. Suppose that sets A and B are represented by two arrays, and both arrays have been sorted in ascending order. The sum of their sizes |A| + |B| is equal to n. Design an algorithm to compute the union of sets A and B in time O(n). Briefly describe your algorithm and analyse its worst-case time complexity. [AY1718S1]

similar to merge function

worst case: n elements > n-1 compares

* if have dupli lates, can screen once first



Evarcica

Describe a linear-time algorithm to rearrange an array of n integers so that all the negative keys will be moved to the left side of all the nonnegative keys. You should not use any auxiliary array for temporary storage of keys. Show that the running time of your algorithm is O(n). [AY1617S1]



Evercice

 A weighted directed graph G is represented by the array of adjacency lists shown below. List the shortest path from vertex b to each vertex, obtained by Dijkstra's algorithm when running on G. [AY1819S1]

$$a: \to (d, 1) \to (b, 2)$$

 $b: \to (d, 3) \to (e, 10)$
 $c: \to (a, 4) \to (f, 5)$
 $d: \to (e, 2) \to (c, 2) \to (g, 4) \to (f, 8)$
 $e: \to (g, 6)$
 $f:$
 $g: \to (f, 1)$



