



**NANYANG  
TECHNOLOGICAL  
UNIVERSITY**

# **CE1107/CZ1107: DATA STRUCTURES AND ALGORITHMS**

## **Binary Trees**

**College of Engineering**

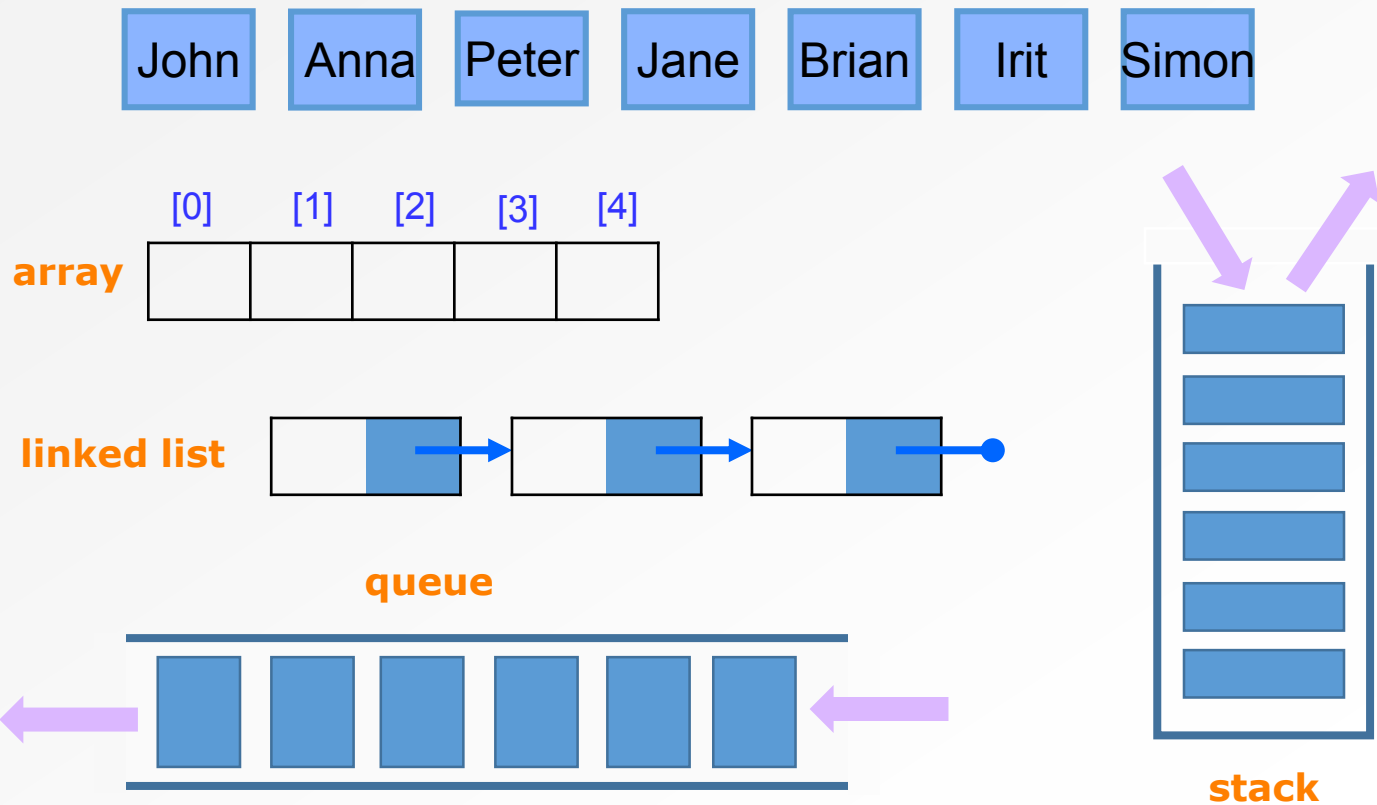
School of Computer Science and Engineering

- **Non-linear data structures**

- Tree data structure
  - Binary trees
- Implement binary tree nodes in C
- Binary Tree Traversal
- Tree traversal order
  - Pre-order
  - In-order
  - Post-order
- Application examples
  - Count nodes in a binary tree
  - Find grandchild nodes
  - Calculate height of every node
- Level-by-level traversal
- Preorder traversal with a stack

# LINEAR DATA STRUCTURE

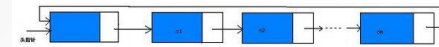
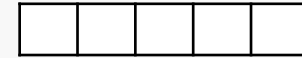
- Array, linked list, queue, stack



# DATA STRUCTURES SO FAR...

- Linear

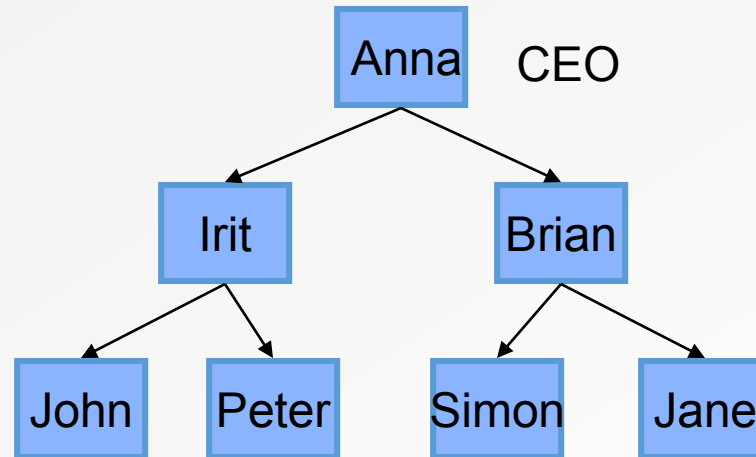
- Items all arranged one after another
- Random access
  - Arrays
- Sequential access
  - Linked list
- Limited-access sequential
  - Stacks
  - Queues



- Used them to store lists of numbers, lists of people, lists of moves, etc
  - Linear data

# NON-LINEAR DATA STRUCTURE

- Suppose you have a set of names



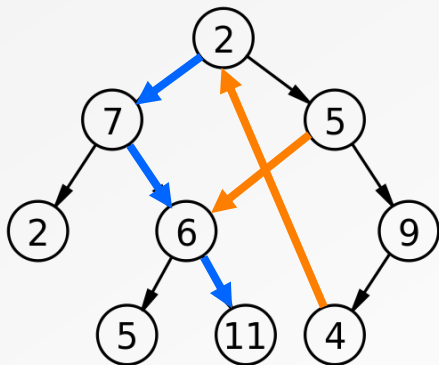
## Tree

- Company organization

Not good to use linear data structure to store hierarchical relationships

# TREE DATA STRUCTURE

- Still using nodes + links representation
- New idea:
  - Each node can have links to more than one other node
  - **No loop** (with loop, becomes class)



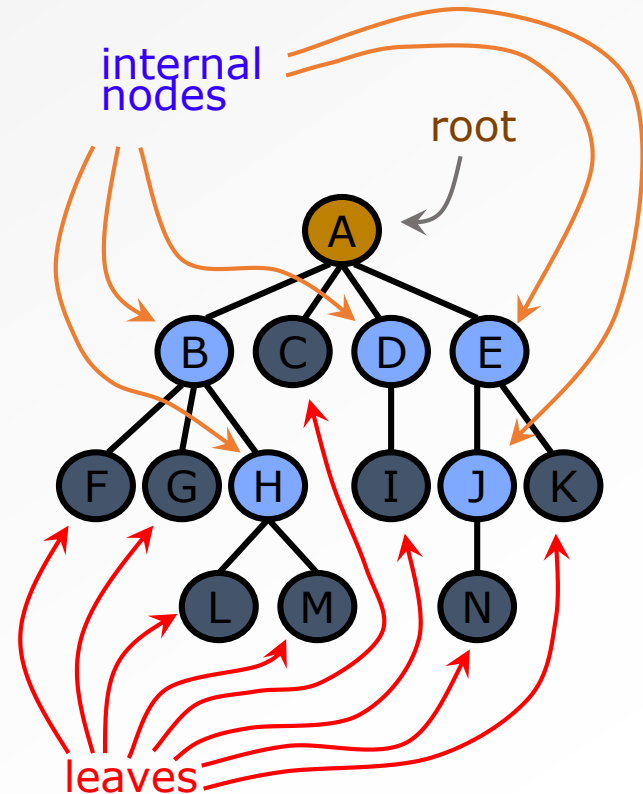
**Observe that:**

- **If we follow one path of a tree, we get a linked list**

- Non-linear data structures
- **Tree data structure**
  - **Binary trees**
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# TREE DATA STRUCTURE

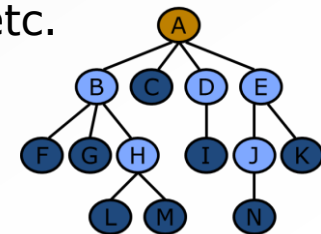
- A tree is composed of nodes
- Each node contains a value
- Types of nodes
  - **Root:** only one in a tree, has no parent.
  - Internal (non-leaf):  
Nodes with children are called **internal nodes**
  - Leaf:  
nodes without children are called **leaves**





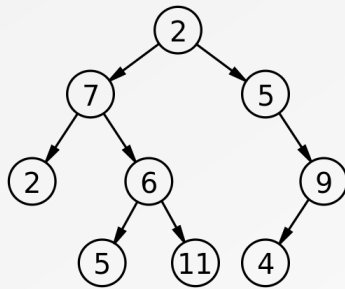
# WHY TREES?

- Model layouts with hierarchical relationships between items
  - Chain of command in the army
  - Personnel structure in a company
  - (Binary tree structure is limited because each node can have **at most two children**)
- Tree structures also allow us to
  - Some problems require a tree structure: some games, most optimization problems, etc.
  - Allow us to do the following very quickly: (we'll see that in the following lectures)
    - **Search for a node with a given value**
    - **Add a given value to a list**
    - **Delete a given value from a list**

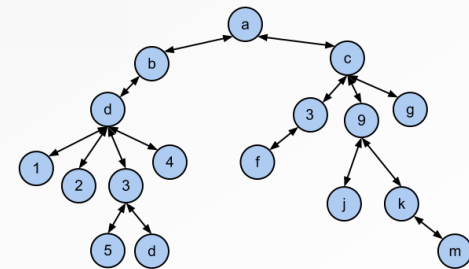


# TREE DATA STRUCTURE

- Tree data structure looks like... a tree:
  - Only one root node (no nodes points to it)
  - Each node branches out to some number of nodes
  - Each node has only one "parent" node – the node pointing to it (except the root node)



**Binary tree**

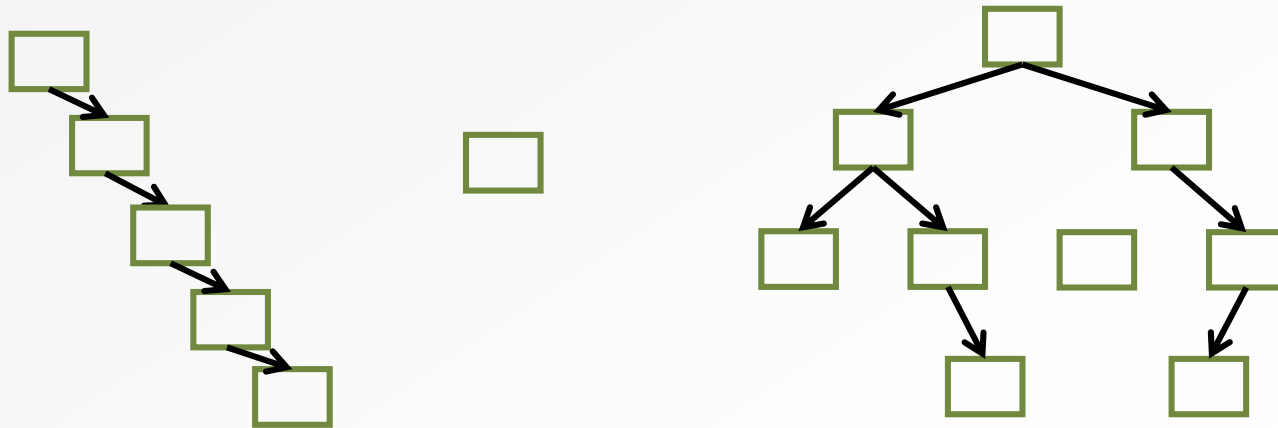


**General tree**

- General tree
  - Each node can have links to any number of other nodes
- **Binary tree (we'll work with this in our course)**
  - **Each node can have links to at most two other nodes**

# POSSIBLE TREE CONFIGURATIONS

- We'll see later why not all trees configurations are desirable/useful
- Has to do with balance of a tree



- Non-linear data structures
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  - Binary trees
- **Implement binary tree nodes in C**
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- Tree traversal order
  - Pre-order
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# IMPLEMENTATION

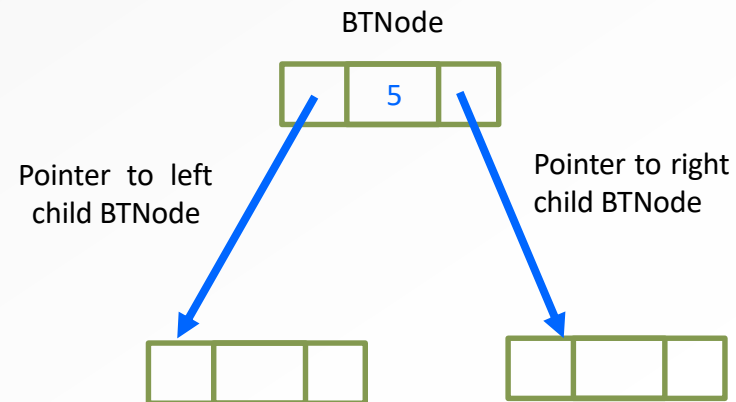
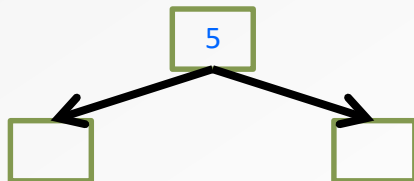
- Recall implementation of LinkedList

- Node has link to **at most one** other node
- Defined a ListNode with one **next** pointer and a data **item**

```
typedef struct _listnode{  
    int item;  
    struct _listnode *next;  
}ListNode;
```

- BinaryTree

- Node has link to **at most TWO** other nodes
- Define a BTreeNode with
  - Two pointers
  - A data item

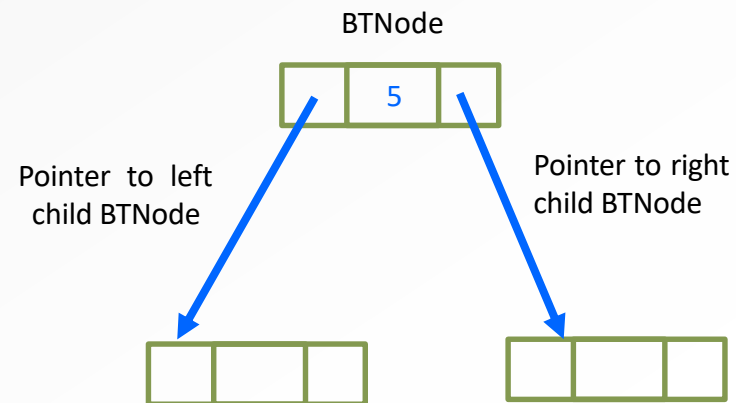


# BTNode

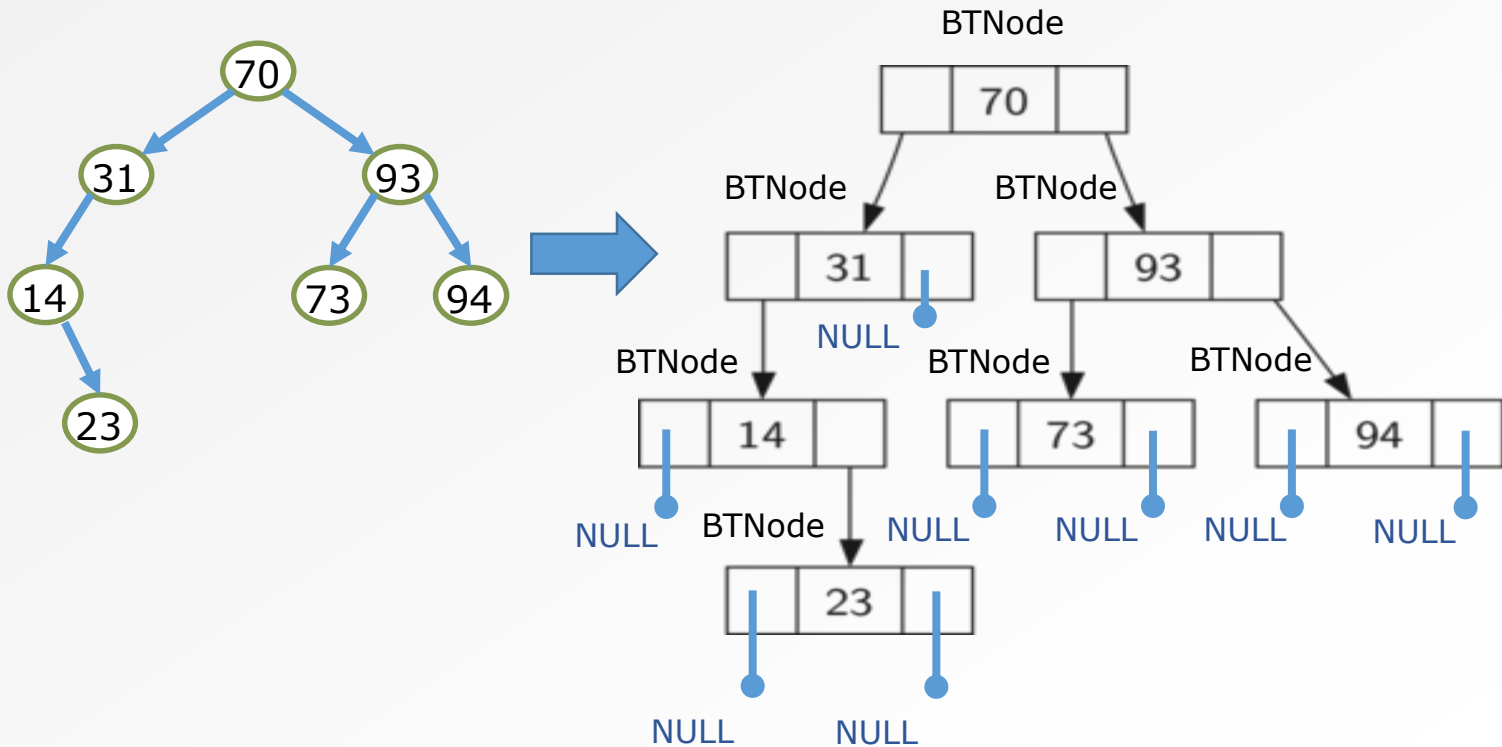
- Start with a simple BTNode that stores an integer
  - The type of item can be character, string, or structure, etc.

```
typedef struct _bnode{  
    int item;  
  
    struct _bnode *left;  
    struct _bnode *right;  
} BTNode;
```

```
typedef struct _listnode{  
    int item;  
    struct _listnode *next;  
} ListNode;
```



# EXAMPLE BINARY TREE

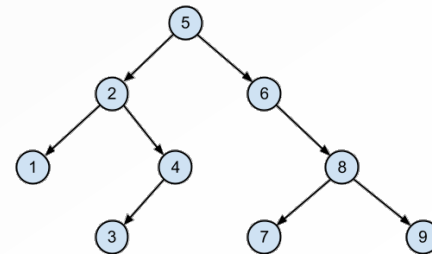


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- **Binary Tree Traversal**
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# TREE TRAVERSAL

- Given a linear data structure and a particular item, very obvious what the “next” item is
  - Each node has an obvious “previous” and “next” node
- Trees are non-linear structures
  - How to extract data from a binary tree?
  - What is the traversal sequence?  
left/left/left, then left/left/right, then...?
- Need a systematic way to visit every node in the tree
  - Clearly defined steps
  - No repeated visits to nodes



# TREE TRAVERSAL

- Why is this important?
  - Tree traversal is foundation for many functions
- Very common function template:

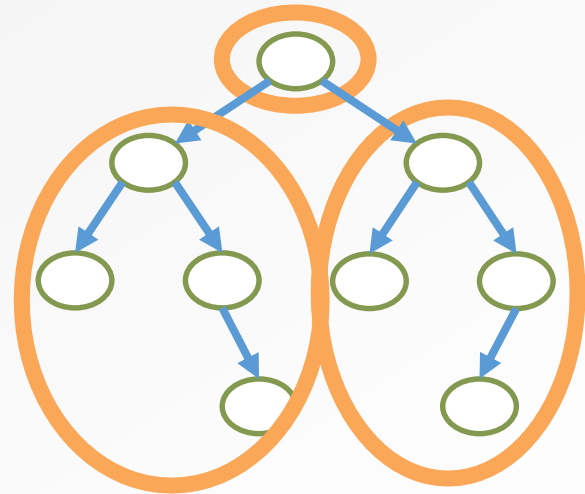
Traverse tree

- At each node, perform some operation

- Example task: count # of nodes in a tree

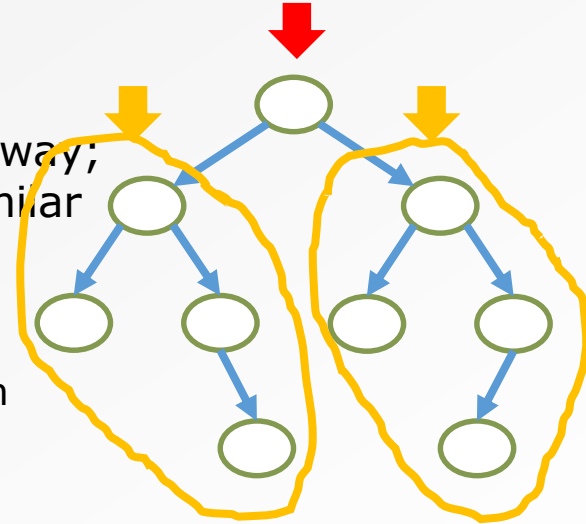
At every node N, size of that subtree

= size of N's left subtree  
+ size of N's right subtree  
+ N itself



# TREE TRAVERSAL

- Tree traversal is recursive
  - Recursion: is the process of repeating items in a self-similar way; divide a problem into several similar sub-problems.
  - At each node
    - Visit the node and both children
- Initial case + repeating case
  - (Visit root) + (visit children)
- When combined, guarantees that all nodes will be visited once and only once



# TREE TRAVERSAL PROCESS

```
TreeTraversal(Node N):
```

```
  Visit N;
```

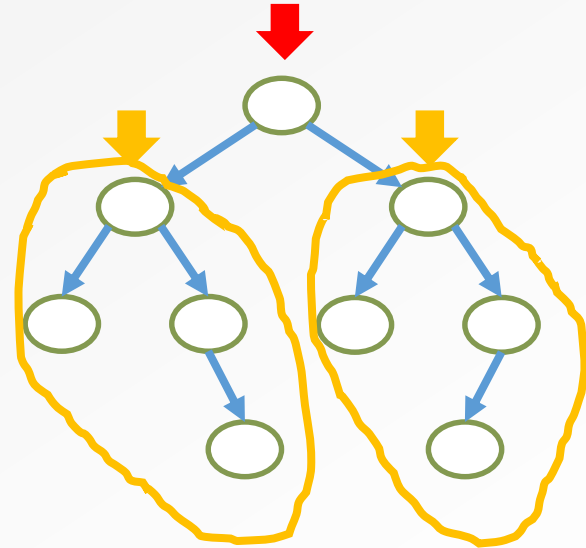
```
  If (N has left child)
```

```
    TreeTraversal(LeftChild);
```

```
  If (N has right child)
```

```
    TreeTraversal(RightChild);
```

```
  Return; // return to parent
```

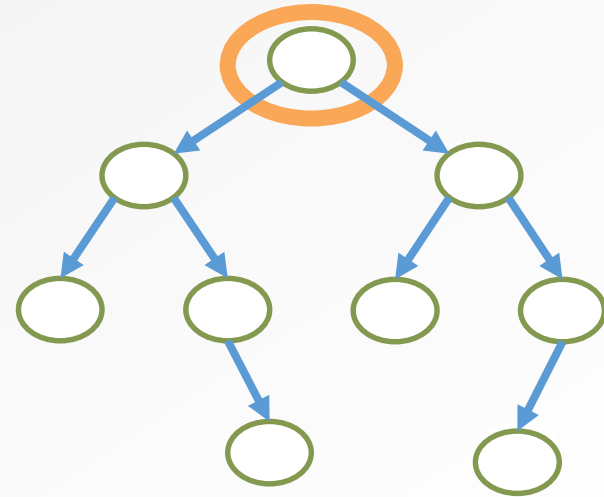


# TREE TRAVERSAL TEMPLATE #1

## Pseudocode

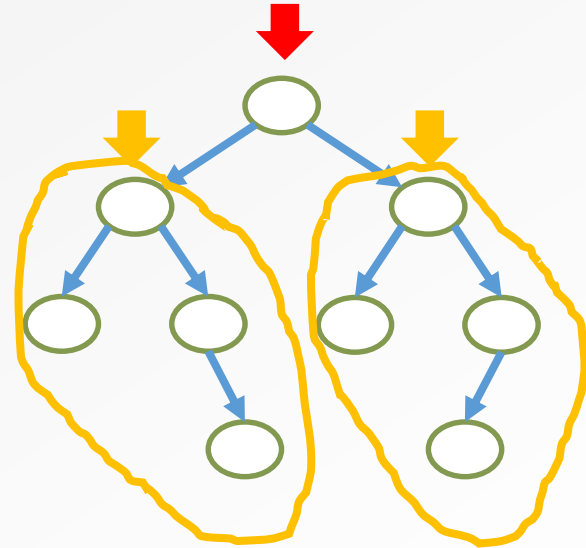
```
TreeTraversal(Node N):  
    Visit N;  
    If (N has left child)  
        TreeTraversal(LeftChild);  
    If (N has right child)  
        TreeTraversal(RightChild);  
    Return; // return to parent
```

In main(), call TreeTraversal(root)



# TREE TRAVERSAL TEMPLATE #2

- Current function:
  - Need to check for existence of left and right children before following them
- New version:
  - Always follow links to children
  - Then check if the link is NULL
  - In other words, not actually pointing at a BTNode



# TREE TRAVERSAL TEMPLATE #2

## Pseudocode

TreeTraversal2(Node N):

    If N==NULL return;

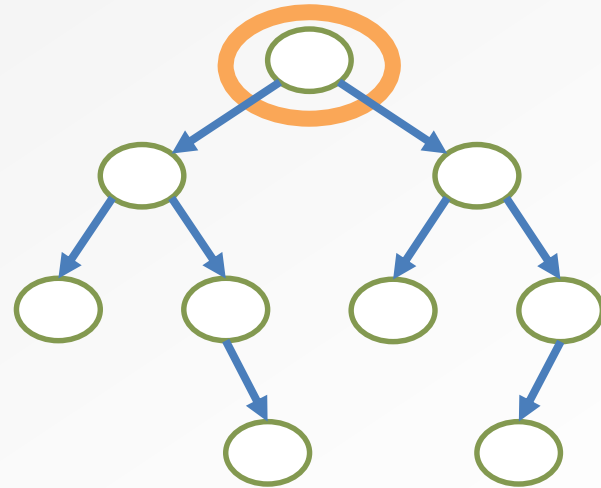
    Visit N;

    TreeTraversal2(LeftChild);

    TreeTraversal2(RightChild);

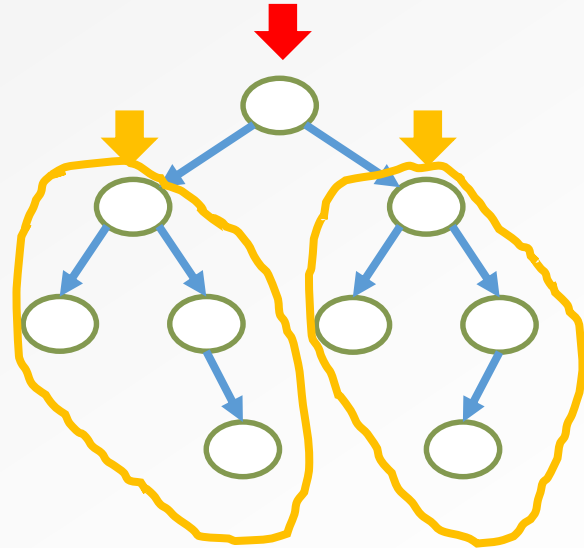
    Return; // return to parent

In main(), call TreeTraversal2(root)



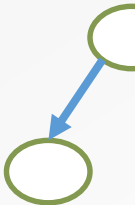
# TreeTraversal2() IMPLEMENTATION

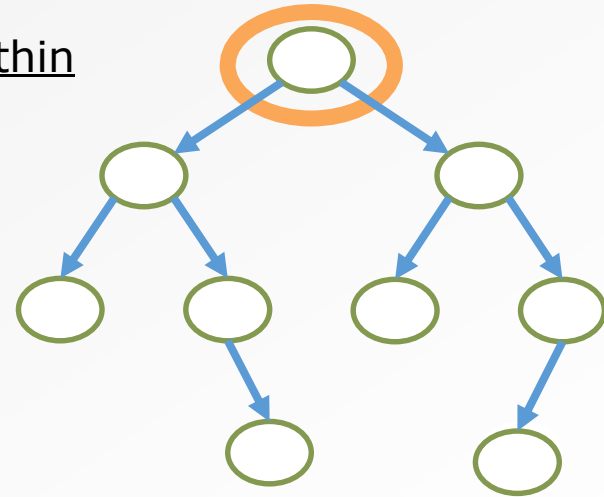
```
Void TreeTraversal2(BTNode *cur){  
    If (cur == NULL) return;  
    PrintNode(cur); // visit cur  
    TreeTraversal2(cur->left);  
    TreeTraversal2(cur->right);  
}
```





## TREETRAVERSAL() FEATURES

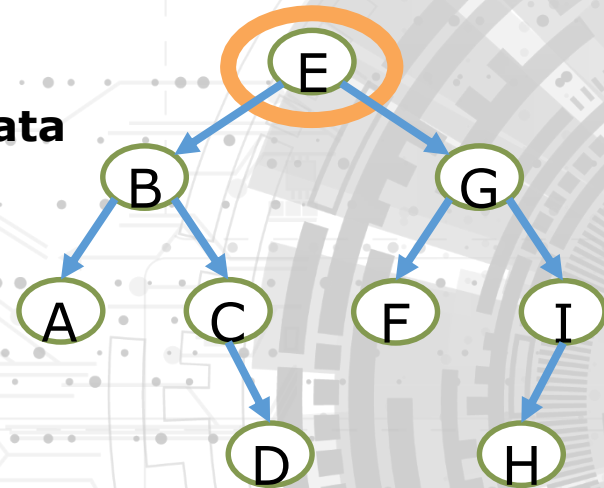
- Recursive
    - TreeTraversal() is called from within its own body
    - initial call TreeTraversal(root)
  - Depth-first
    - The traversal goes as deep as possible before backtracking and going sideways
    - Not level-by-level! (that is called breadth-first)
- 
- ```
graph TD; A(( )) --> B(( ))
```



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# THREE “STANDARD” WAYS TO TRAVERSAL

- Pre-order
  - **Process the current node's data**
  - **Visit the left child subtree**
  - **Visit the right child subtree**
- In-order
- Post-order



# THREE "STANDARD" WAYS TO TRAVERSAL

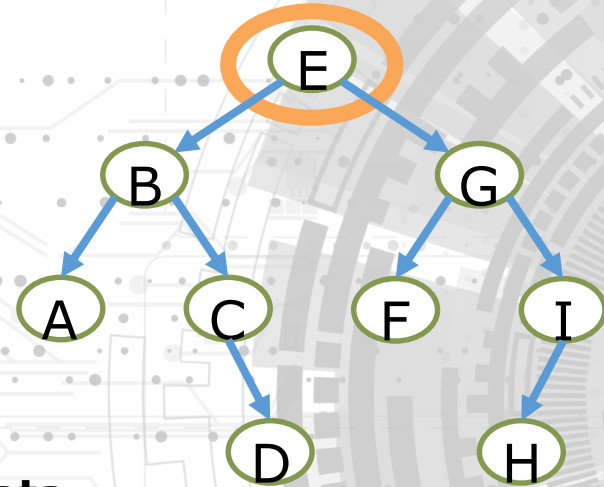
- Pre-order

- Process the current node's data
- Visit the left child subtree
- Visit the right child subtree

- In-order

- **Visit the left child subtree**
- **Process the current node's data**
- **Visit the right child subtree**

- Post-order



# THREE “STANDARD” WAYS TO TRAVERSAL

- Pre-order

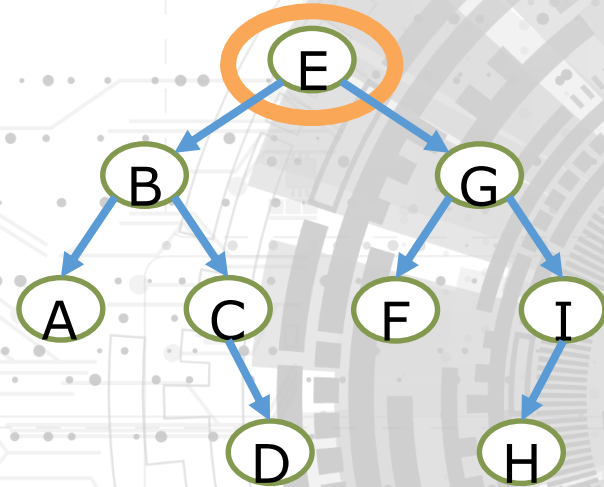
- Process the current node's data
- Visit the left child subtree
- Visit the right child subtree

- In-order

- Visit the left child subtree
- Process the current node's data
- Visit the right child subtree

- **Post-order**

- **Visit the left child subtree**
- **Visit the right child subtree**
- **Process the current node's data**



# TREE TRAVERSAL - PRINT

- Recall the TreeTraversal() template (TT) – **Pre-order** :
  - Simple task at each node: print out data in that node

```
void TreeTraversal(BTNode *cur){  
    if (cur == NULL)  
        return;  
  
    // Do something with the current node's data  
  
    TreeTraversal(cur->left); //Visit the left child node  
    TreeTraversal(cur->right); //Visit the right child node  
}
```

# TREE TRAVERSAL - PRINT

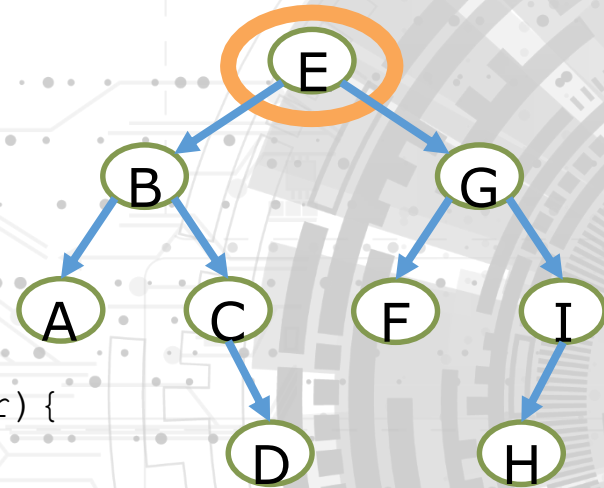
- Recall the TreeTraversal() template (TT) – **Pre-order** :
  - Simple task at each node: print out data in that node

```
void TreeTraversal(BTNode *cur){  
    if (cur == NULL)  
        return;  
  
    printf("%c", cur->item);  
  
    TreeTraversal(cur->left); //Visit the left child node  
    TreeTraversal(cur->right); //Visit the right child node  
}
```

# TREE TRAVERSAL PRE-ORDER: PRINT

Output:

E B A C D G F I H



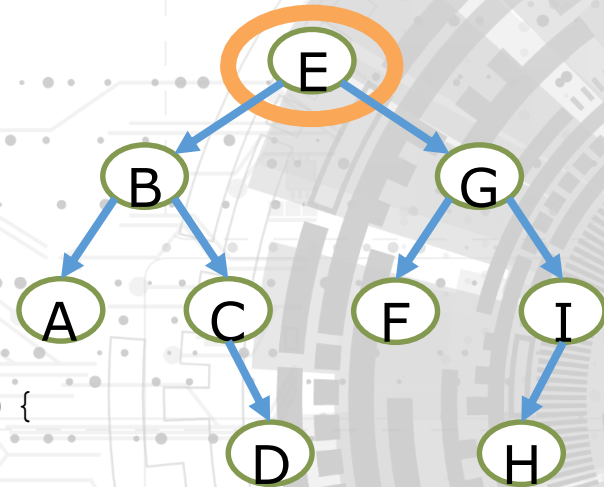
```
void TreeTraversal_pre(BTNode *cur) {  
    if (cur == NULL)  
        return;  
  
    printf("%c  ", cur->item);  
  
    TreeTraversal_pre(cur->left); //Visit the left child node  
    TreeTraversal_pre(cur->right); //Visit the right child node  
}
```



# TREE TRAVERSAL IN-ORDER: PRINT

Output:

A B C D E F G H I

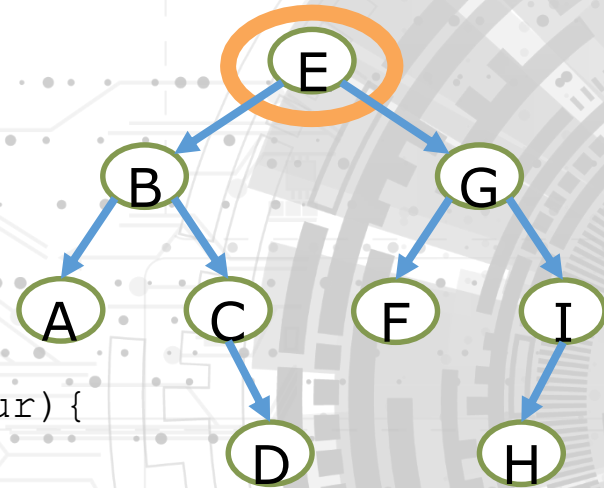


```
void TreeTraversal_in(BTNode *cur){  
    if (cur == NULL)  
        return;  
  
    TreeTraversal_in(cur->left); //Visit the left child node  
    printf("%c  ", cur->item);  
    TreeTraversal_in(cur->right); //Visit the right child node  
}
```

# TREE TRAVERSAL POST-ORDER: PRINT

Output:

A D C B F H I G E



```
void TreeTraversal_post(BTNode *cur){  
    if (cur == NULL)  
        return;  
  
    TreeTraversal_post(cur->left); //Visit the left child node  
    TreeTraversal_post(cur->right); //Visit the right child node  
    printf("%c ", cur->item);  
}
```

# PRE-ORDER, IN-ORDER AND POST-ORDER

Pre-Order Traversal

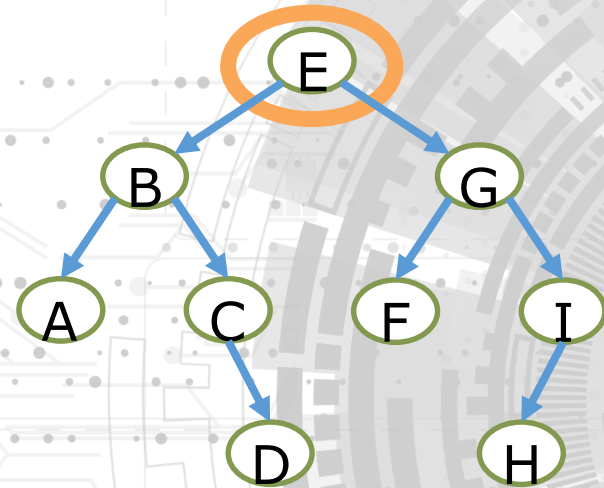
E B A C D G F I H

In-Order Traversal

A B C D E F G H I

Post-Order Traversal

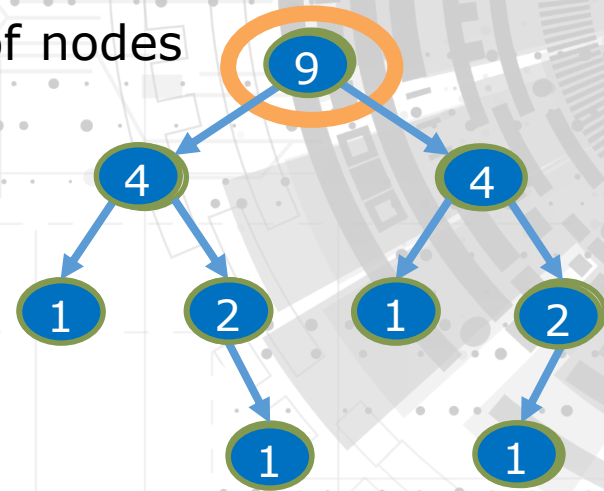
A D C B F H I G E



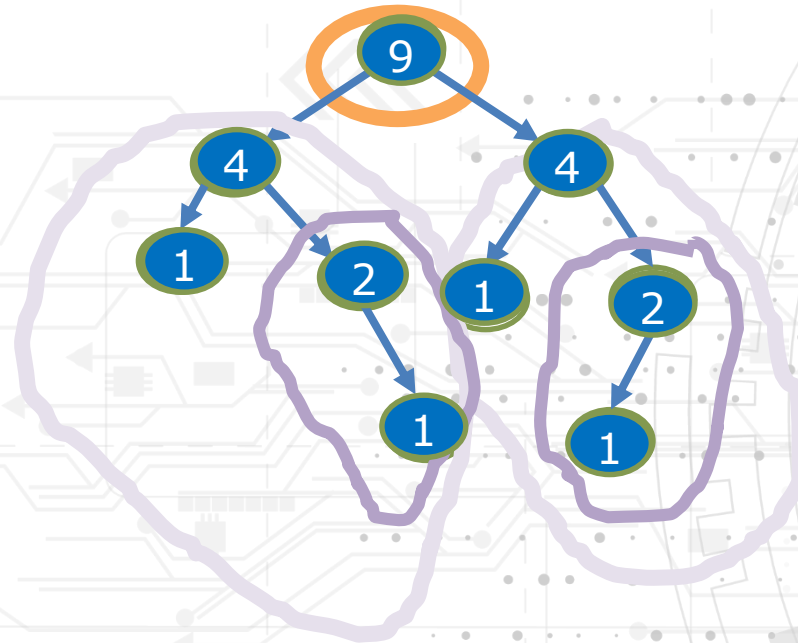
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# COUNT NODES IN A BINARY TREE

- Recursive definition:
  - Number of nodes in a tree  
= 1  
+ number of nodes in left subtree  
+ number of nodes in right subtree
- Each node returns the number of nodes in its subtree



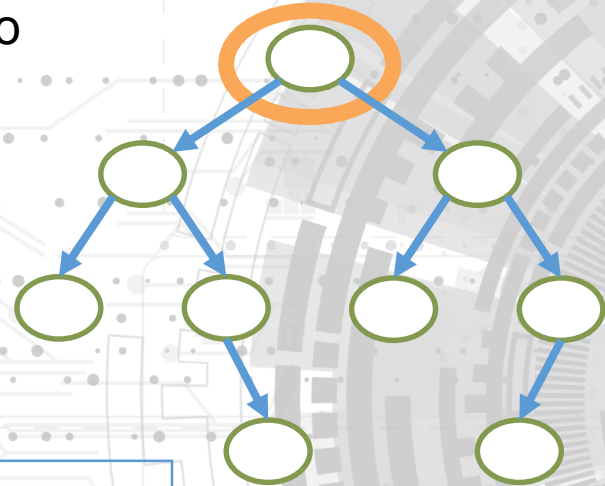
# COUNT NODES IN A BINARY TREE



- Each node returns the number of nodes in its own subtree
- Leaf nodes return 1  
Information **propagates upwards** as TreeTraversal returns from visiting leaf nodes
- Which is the first/last count to be returned?

# countNode()

- Return the size of your subtree to your parent node
- Leaf nodes must return 1 to parent node
- Root node returns size of entire tree

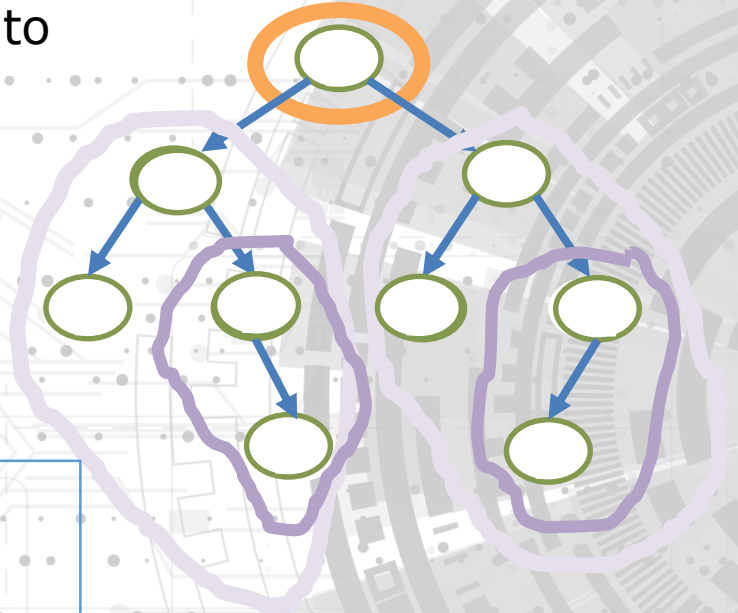


```
void TreeTraversal(BTNode *cur) {  
    if (cur == NULL)  
        return;  
    //may do something with cur;  
    TreeTraversal(cur->left);  
    TreeTraversal(cur->right);  
    //may do something with cur;  
}
```

# countNode()

- Return the size of your subtree to your parent node
- Leaf nodes must return 1 to parent node
- Root node returns size of entire tree

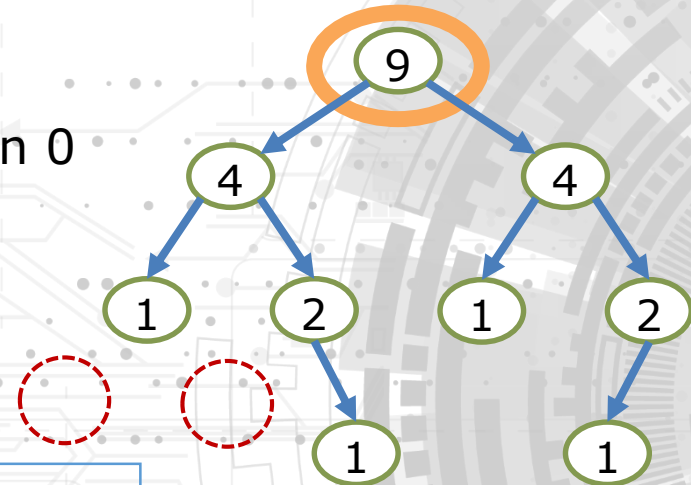
```
int countNode(BTNode *cur) {  
    if (cur == NULL)  
        return ???;  
  
    countNode(cur->left);  
    countNode(cur->right);  
    ??? //sum and get total;  
}
```





# countNode()

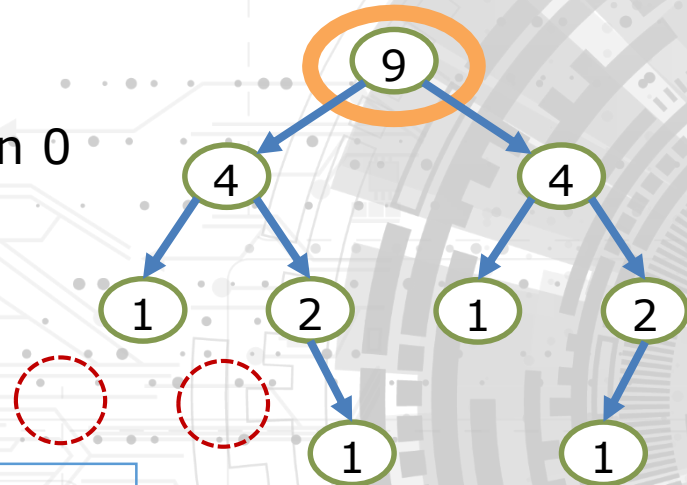
- Leaf nodes must return 1
  - "Null" nodes should return 0
- Leaf node returns  $1 + 0 + 0$



```
int countNode(BTNode *cur) {  
    if (cur == NULL)  
        return 0;  
  
    l = countNode(cur->left);  
    r = countNode(cur->right);  
    return l+r+1;  
}
```

# countNode()

- Leaf nodes must return 1
  - "Null" nodes should return 0
- Leaf node returns  $1 + 0 + 0$



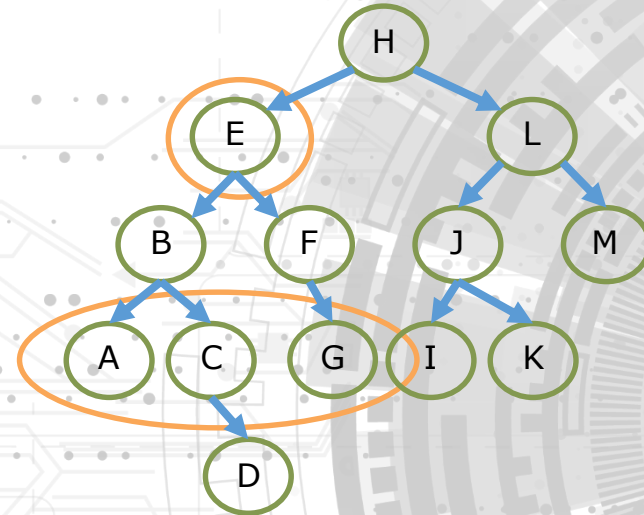
```
int countNode(BTNode *cur) {  
    if (cur == NULL)  
        return 0;  
  
    return (countNode(cur->left)  
            + countNode(cur->right)  
            + 1);  
}
```

# OUTLINE

- Non-linear data structures
- Tree data structure
  - Binary trees
- Implement binary tree nodes in C
- Binary Tree Traversal
- Tree traversal order
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  - In-order
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# FIND GRANDCHILDREN

- Given a node X, find all the nodes that are X's grandchildren
- Given node E, we should return grandchild nodes A, C, and G
- What if we want to find **k-level grandchildren**?
  - **Need a way to keep track of how many levels down we've gone**

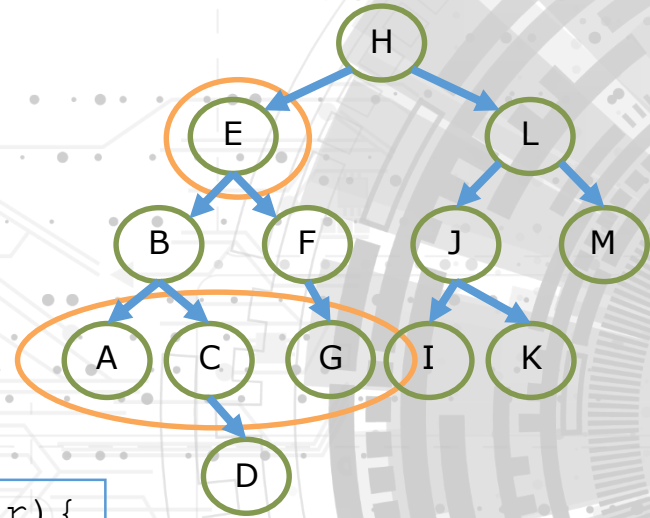


**X->left->left**  
**X->left->right**  
**X->right->left**  
**X->right->right**

**2-level grandchildren**

# FIND GRANDCHILDREN

- We want to go down **k** “levels”
- Use a counter to track how far down we’ve gone
- At each TreeTraversal(child), increment counter



```
void TreeTraversal(BTNode *cur) {  
    if (cur == NULL)  
        return;  
  
    // check counter  
  
    TreeTraversal(cur->left);  
    TreeTraversal(cur->right);  
}
```

Do something with the current node's data

Visit the left child node

Visit the right child node

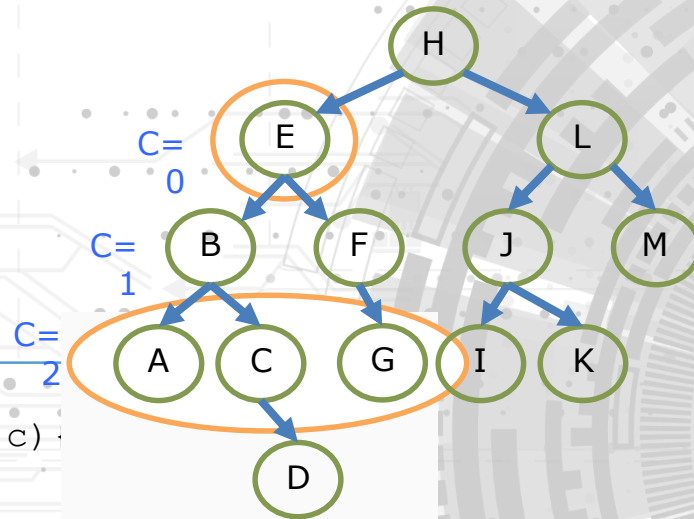
# FIND GRANDCHILDREN

```
void main( ){ ...
```

```
    if (X == null) return;  
    findgrandchildren(X, 0);
```

```
}
```

```
1. void findgrandchildren(  
    BTNode *cur, int c)  
2.  
3.     if (cur == NULL) return;  
4.  
5.     if (c == k){  
6.         printf("%d ", cur->item);  
7.         return;  
8.     }  
9.     if (c < k){  
10.        findgrandchildren(cur->left, c+1);  
11.        findgrandchildren(cur->right, c+1);  
12.    }
```

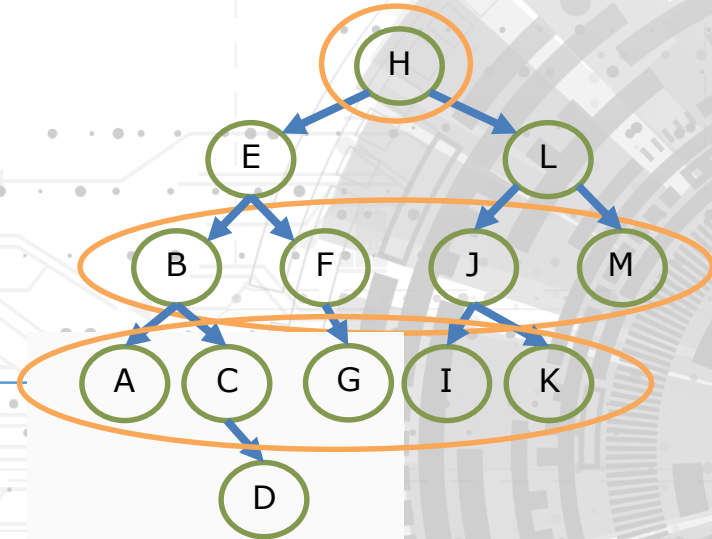


# FIND GRANDCHILDREN

```
void main( ){ ...
```

```
    if (X = null) return;  
    findgrandchildren(X,0);  
}
```

```
void findgrandchildren(  
    BTreeNode *cur, int c){  
    if (cur == NULL) return;  
  
    if (c == k){  
        printf("%d ", cur->item);  
        return;  
    }  
  
    if (c < k){  
        findgrandchildren(cur->left, c+1);  
        findgrandchildren(cur->right, c+1);  
    }  
}
```



if  $k=2$ , we call  
`findgrandchildren(H,0)`,  
what is the output?

How about  $k=3$ ?

How about

`findgrandchildren(H,1)`?

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- Application examples
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  - **Calculate height of every node**
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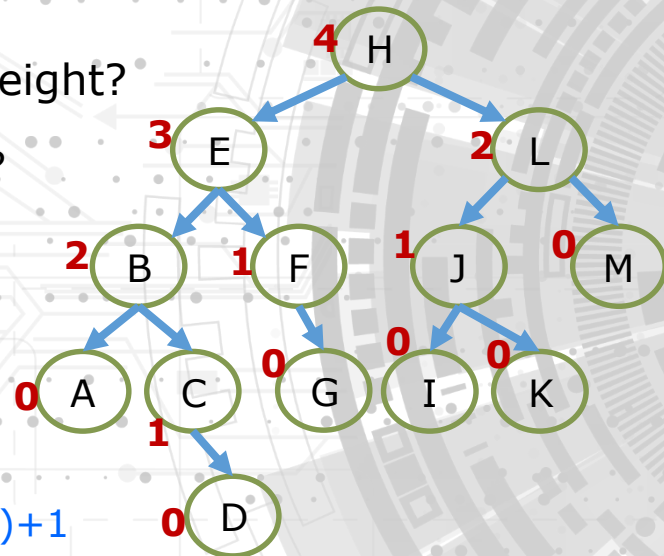
# CALCULATE HEIGHT OF EVERY NODE

- **Height** of a node = number of links from that node to the deepest leaf node
- How does each node calculate its height?
  - What is the height of node D, C, H?

- We found:

- leaf.height = 0
- Non-leaf node X

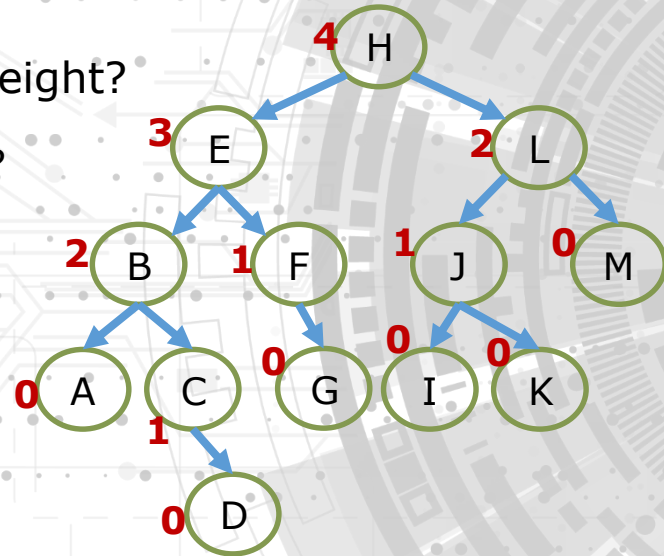
$$X.\text{height} = \max(X.\text{left.height}, X.\text{right.height}) + 1$$



- Does information propagate upwards or downwards?

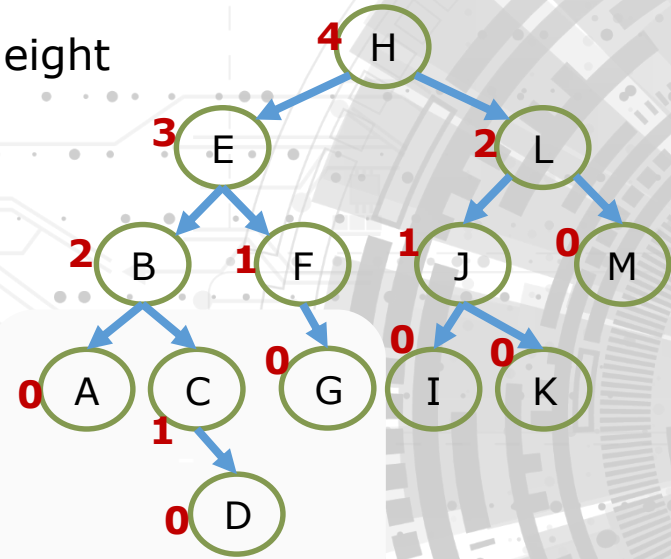
# CALCULATE HEIGHT OF EVERY NODE

- **Height** of a node = number of links from that node to the deepest leaf node
- How does each node calculate its height?
  - What is the height of node D, C, H?
- Go through entire tree:  
calculate and store height of  
each node in the item field



# CALCULATE HEIGHT OF EVERY NODE

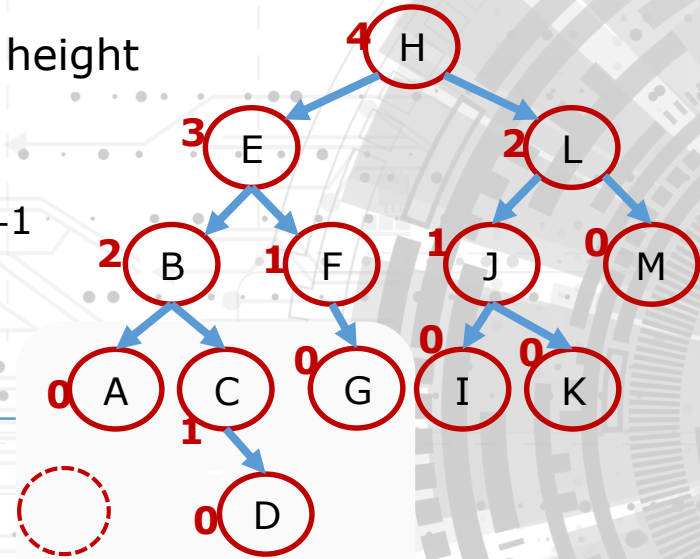
- We want each node to report its height
  - Leaf node must report 0



```
int TreeTraversal(BTNode *cur){  
    if(cur == NULL)  
        return 0;  
  
    int l = TreeTraversal(cur->left);  
    int r = TreeTraversal(cur->right);  
  
    // do something here. Max( left, right)?  
  
    return 1 + max(l, r);  
}
```

# CALCULATE HEIGHT OF EVERY NODE

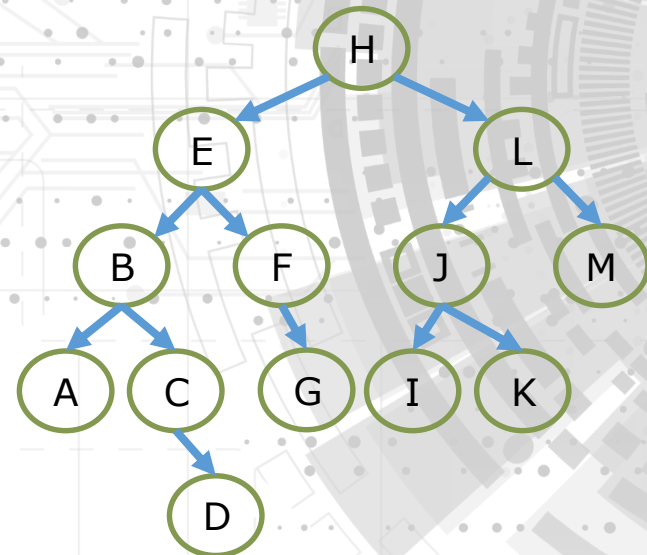
- We want each node to report its height
  - Leaf node must report 0
  - At "null" condition, must report -1



```
int TreeTraversal(BTNode *cur){  
    if(cur == NULL)  
        return -1;  
  
    int l = TreeTraversal(cur->left);  
    int r = TreeTraversal(cur->right);  
  
    int c = max (l, r) + 1;  
  
    return c;  
}
```

# QUESTIONS

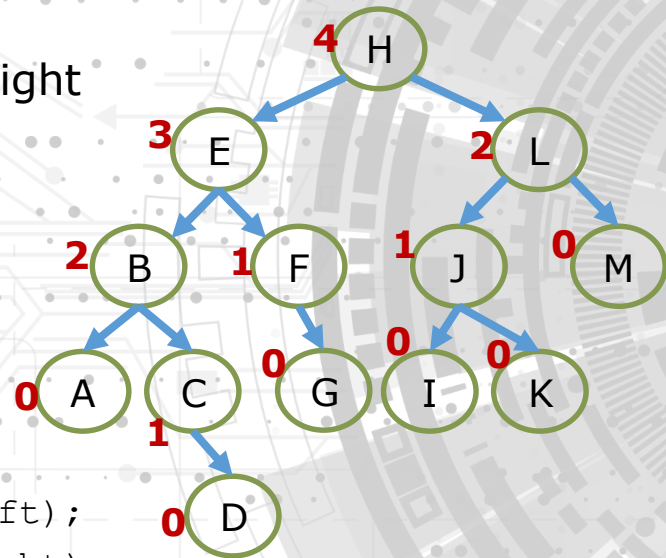
- Does the tree traversal order matter?
- **Depth** of a node = number of links from that node to the root node. How does each node calculate its depth?



# CALCULATE HEIGHT OF EVERY NODE

- **Height** of a node = number of links from that node to the deepest leaf node
- We want each node to report its height
  - Leaf node must report 0
  - At "null" condition, must report -1

```
int TreeTraversal(BTNode *cur){  
    if(cur == NULL)  
        return -1;  
  
    int l = TreeTraversal(cur->left);  
    int r = TreeTraversal(cur->right);  
  
    int c = max (l, r) + 1;  
  
    return c;  
}
```



# QUESTIONS

- Does the tree traversal order matter?
- **Height** of a node = number of links from that node to the deepest leaf node
- **Depth** of a node = number of links from that node to the root node. How does each node calculate its depth?

```
void TreeTraversal(BTNode *cur, int d){  
    if(cur == NULL)  
        return;  
  
    //print cur->item and d;  
  
    TreeTraversal(cur->left, d+1);  
    TreeTraversal(cur->right, d+1);  
  
    return;  
}
```



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- Application examples
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  - Calculate height of every node
- **Level-by-level traversal**
- Preorder traversal with a stack



# LEVEL-BY-LEVEL: BREADTH-FIRST SEARCH



Depth-first search

begins at the root and explores as far as possible along each branch before backtracking

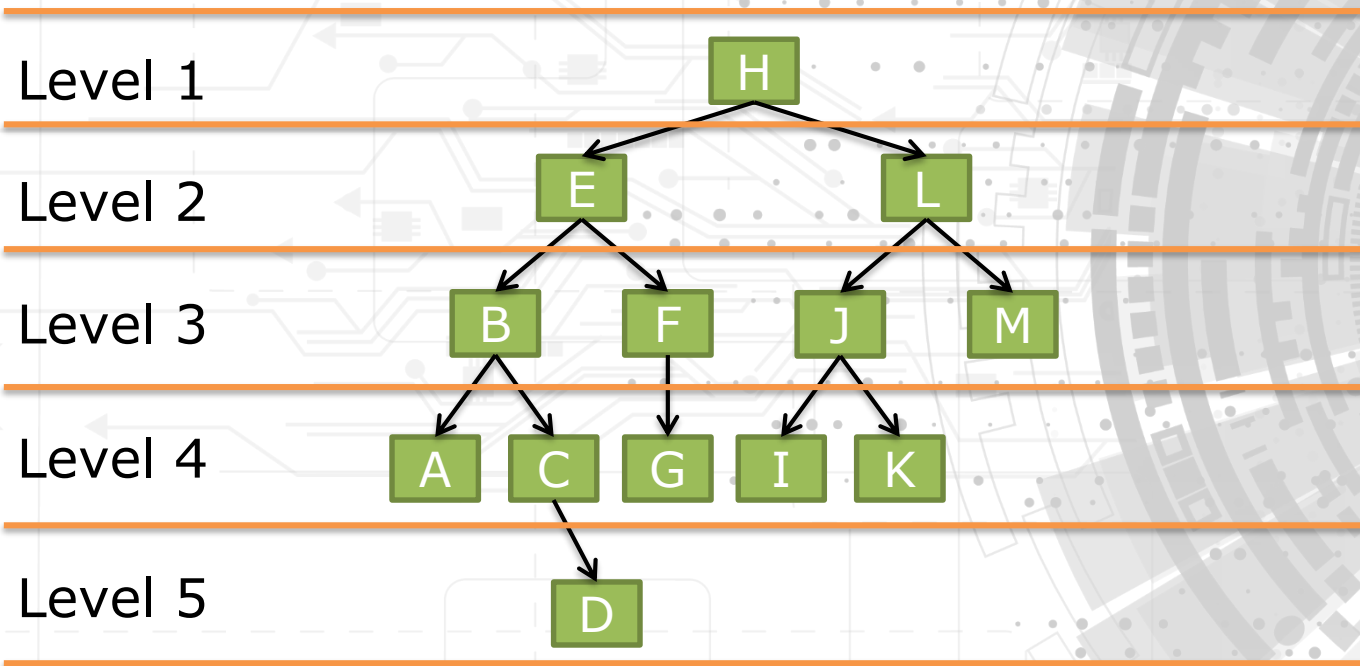
E.g. the post-order traversal



Breadth-first search

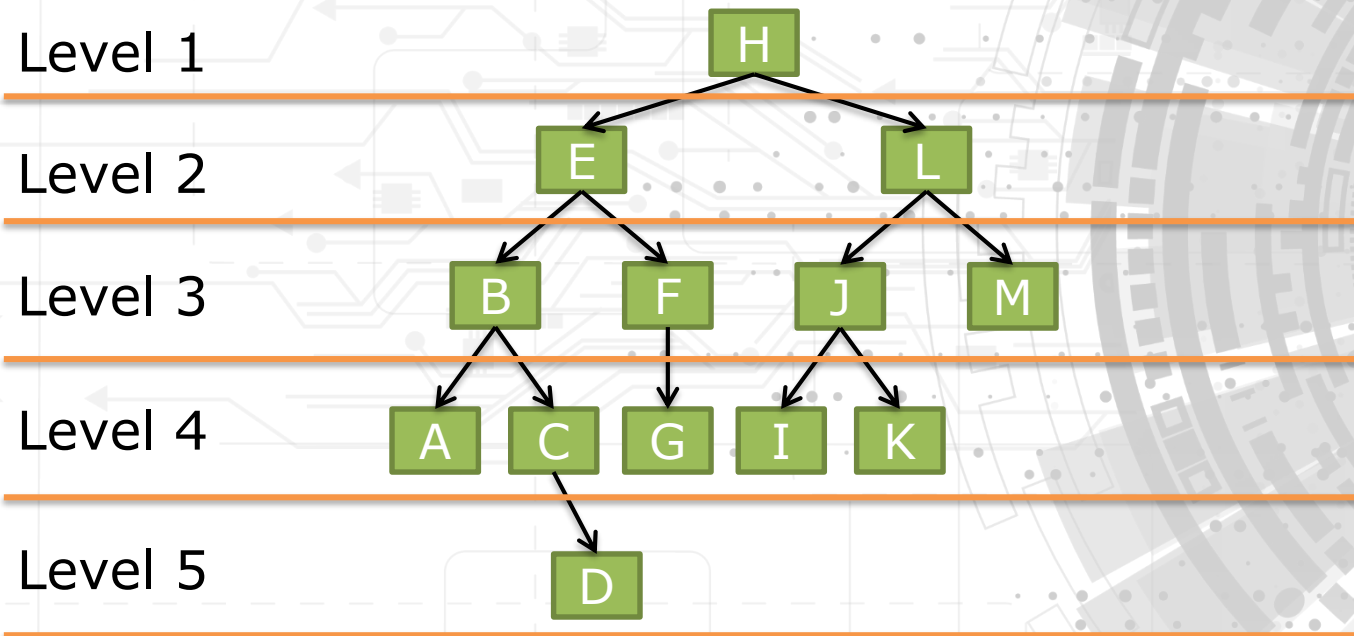
begins at a root node and inspects all its children nodes. Then for each of those children nodes in turn, it inspects their children nodes, and so on.

# LEVEL-BY-LEVEL TREE TRAVERSAL



# LEVEL-BY-LEVEL TREE TRAVERSAL

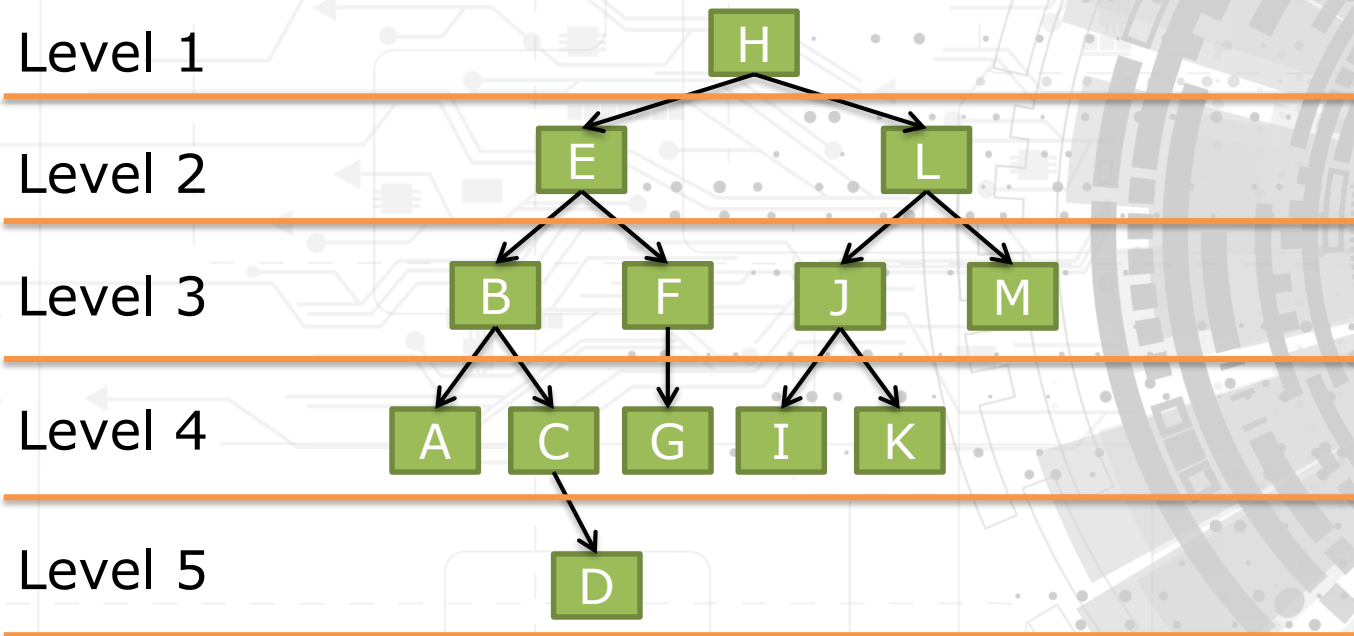
- Hint: Make use of another data structure



Nodes stored in order accessed in tree...

# LEVEL-BY-LEVEL TREE TRAVERSAL

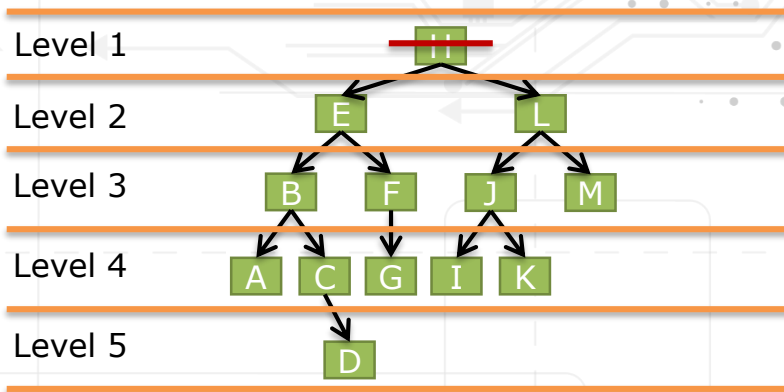
- Use a queue! Root node should be first



Nodes stored in order accessed in tree

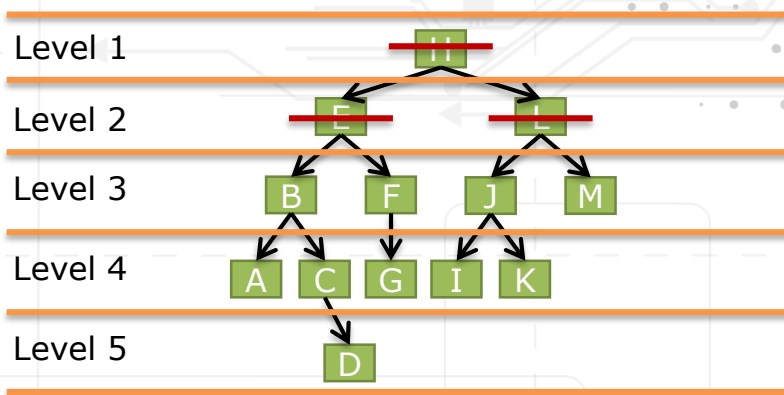
# LEVEL-BY-LEVEL TREE TRAVERSAL

- Enqueue the root, H



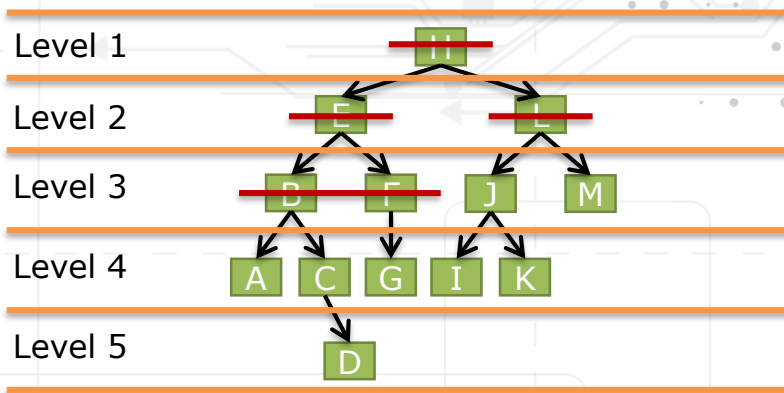
# LEVEL-BY-LEVEL TREE TRAVERSAL

- Enqueue the root, H
- Dequeue H, and enqueue H's children



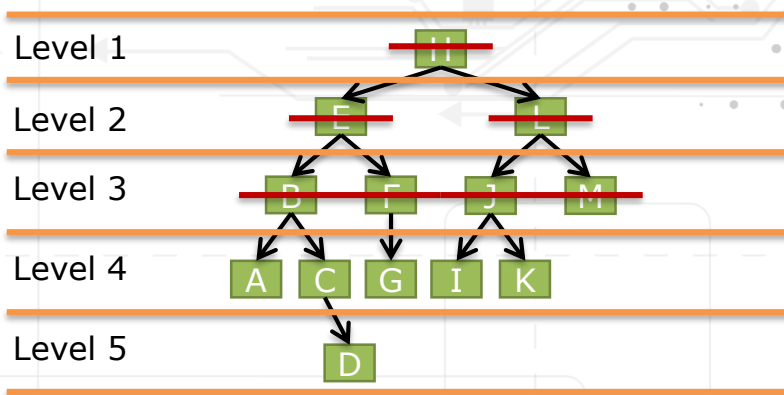
# LEVEL-BY-LEVEL TREE TRAVERSAL

- Enqueue the root, H
- Dequeue H, and enqueue H's children
- Dequeue E, and enqueue E's children



# LEVEL-BY-LEVEL TREE TRAVERSAL

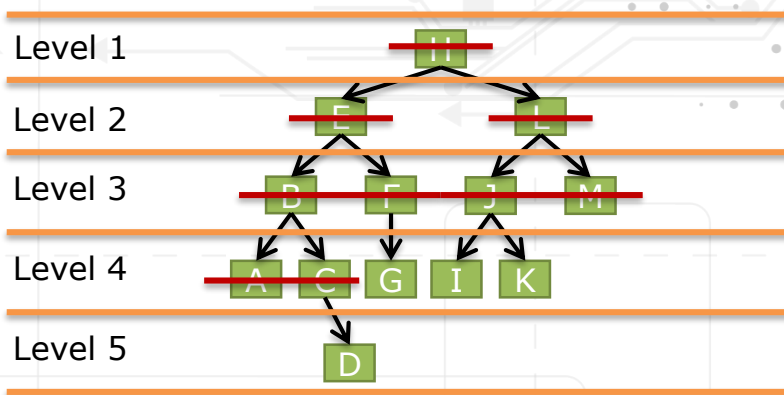
- Enqueue the root, H
- Dequeue H, and enqueue H's children
- Dequeue E, and enqueue E's children
- Dequeue L, and enqueue L's children





# LEVEL-BY-LEVEL TREE TRAVERSAL

- Enqueue the root, H
- Dequeue H, and enqueue H's children
- Dequeue E, and enqueue E's children
- Dequeue L, and enqueue L's children
- Dequeue B, and enqueue B's children



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- **Preorder traversal with a stack**

# PREORDER TRAVERSAL WITH A STACK

Push the root onto the stack.

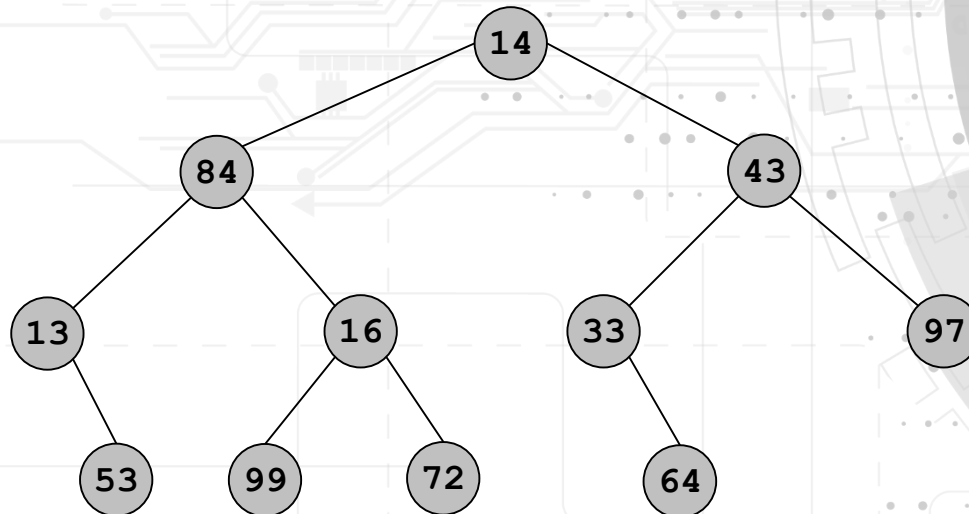
While the stack is not empty

- pop the stack and visit it
- push its two children



14

Stack



# PREORDER TRAVERSAL WITH A STACK

Push the root onto the stack.

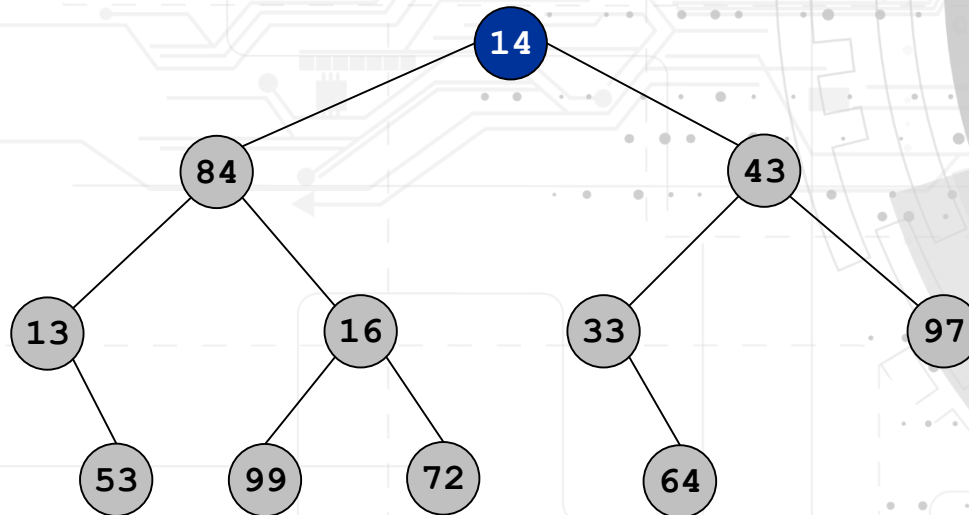
While the stack is not empty

- pop the stack and visit it
- push its two children

14

84  
43

Stack



# PREORDER TRAVERSAL WITH A STACK

Push the root onto the stack.

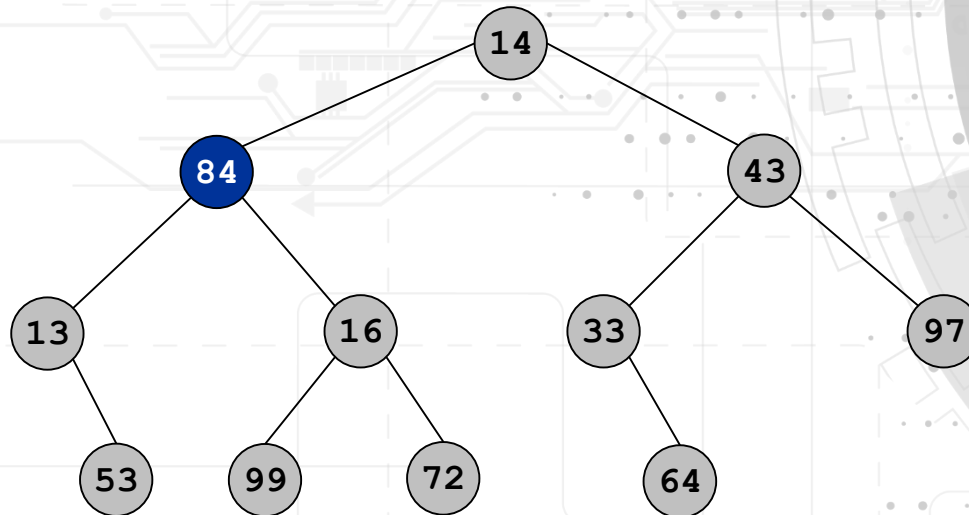
While the stack is not empty

- pop the stack and visit it
- push its two children

14 84

13  
16  
43

Stack



# PREORDER TRAVERSAL WITH A STACK

Push the root onto the stack.

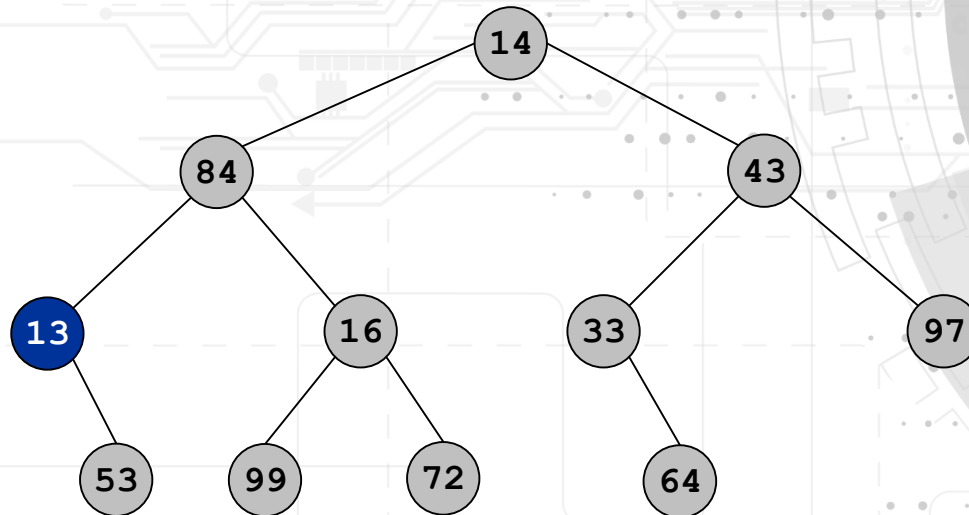
While the stack is not empty

- pop the stack and visit it
- push its two children

14 84 13

53  
16  
43

Stack



# PREORDER TRAVERSAL WITH A STACK

Push the root onto the stack.

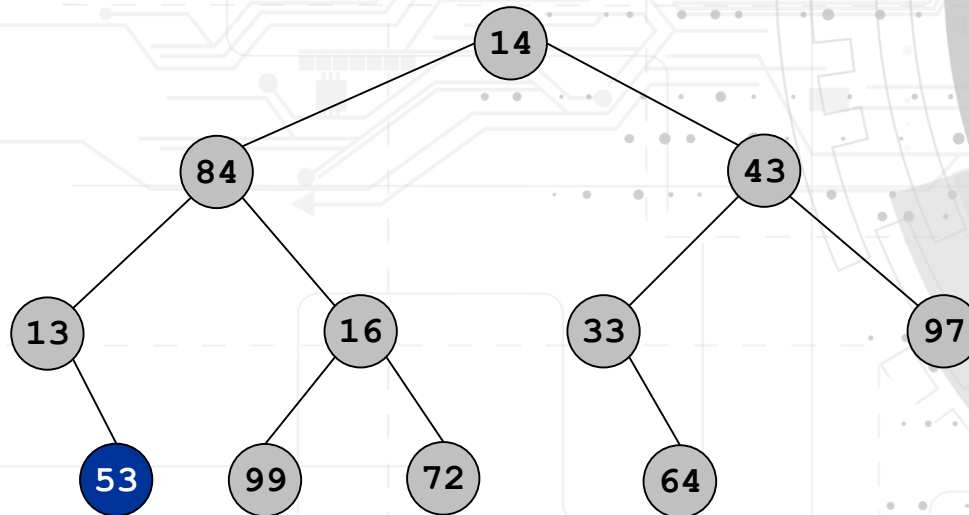
While the stack is not empty

- pop the stack and visit it
- push its two children

14 84 13 53

16  
43

Stack



# PREORDER TRAVERSAL WITH A STACK

Push the root onto the stack.

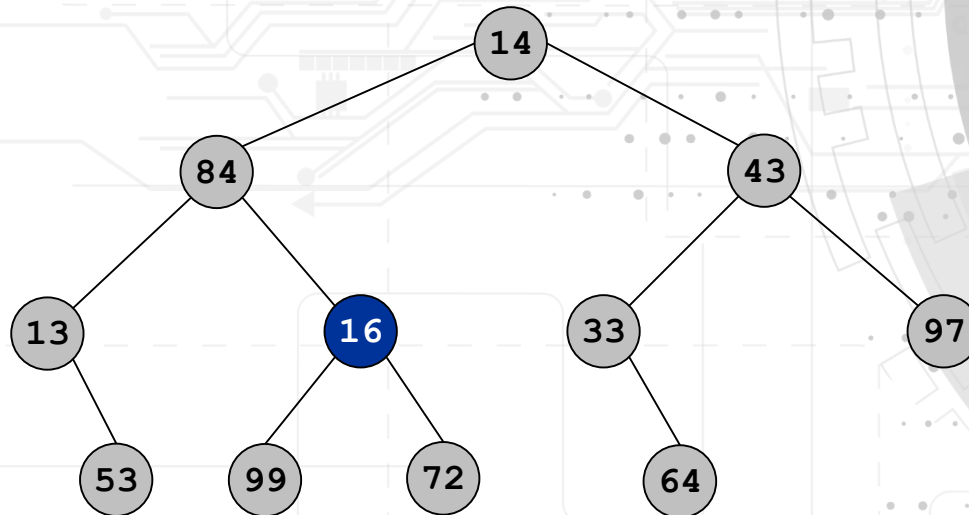
While the stack is not empty

- pop the stack and visit it
- push its two children

14 84 13 53 16

99  
72  
43

Stack





# PREORDER TRAVERSAL WITH A STACK

Push the root onto the stack.

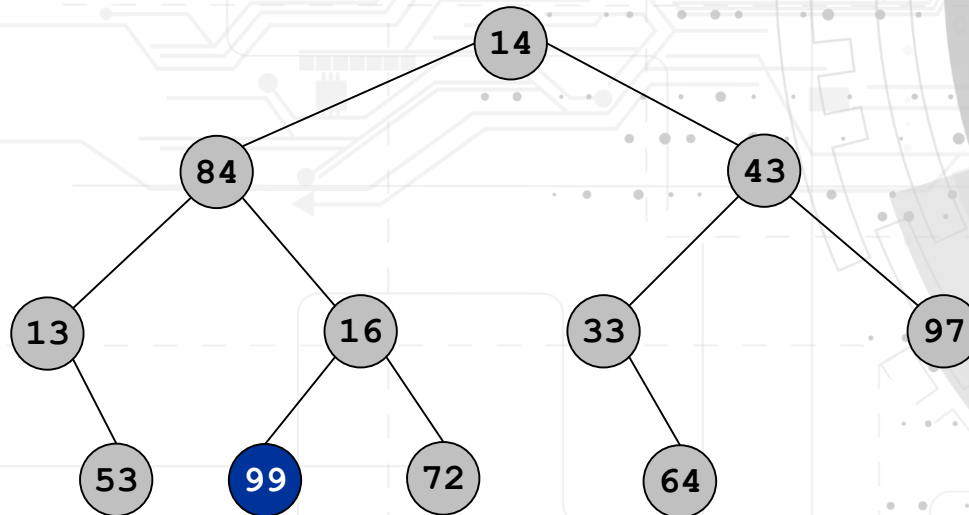
While the stack is not empty

- pop the stack and visit it
- push its two children

14 84 13 53 16 99

72  
43

Stack



# PREORDER TRAVERSAL WITH A STACK

Push the root onto the stack.

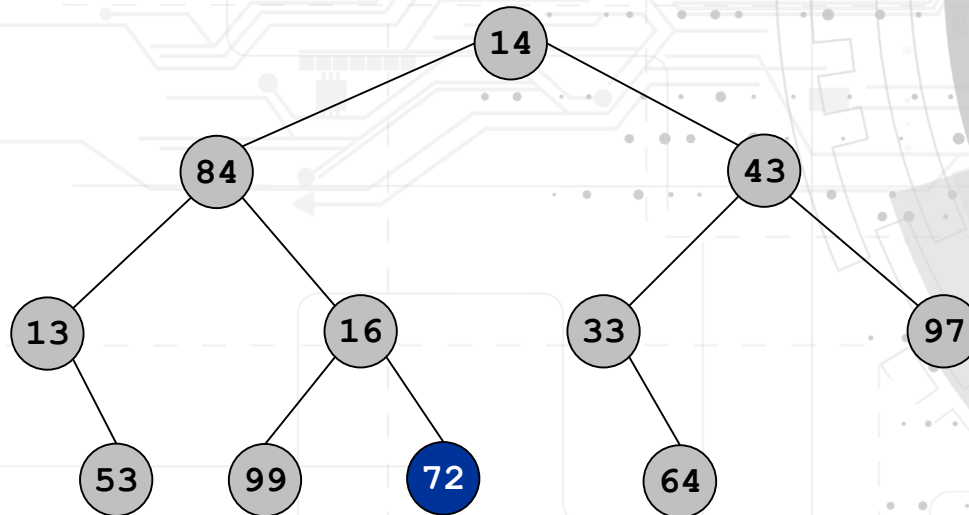
While the stack is not empty

- pop the stack and visit it
- push its two children

14 84 13 53 16 99 72

43

Stack



# PREORDER TRAVERSAL WITH A STACK

Push the root onto the stack.

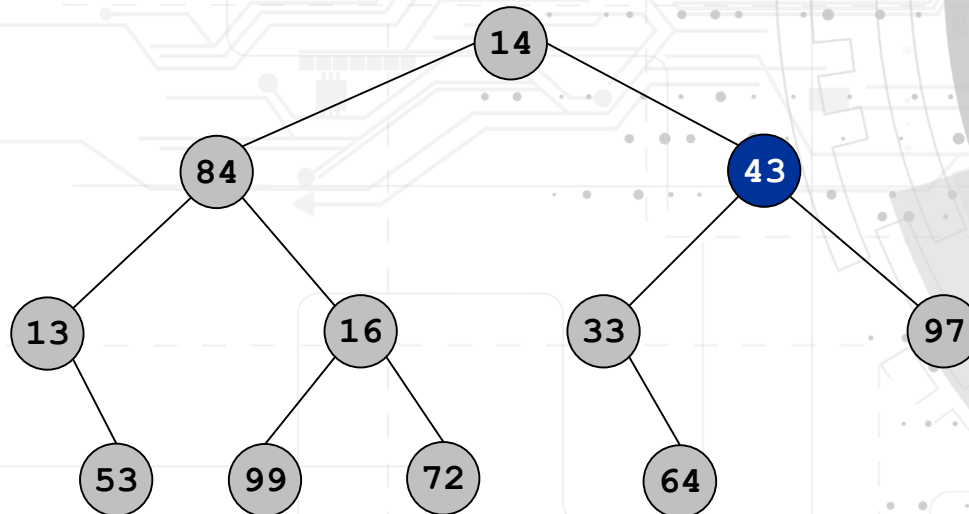
While the stack is not empty

- pop the stack and visit it
- push its two children

14 84 13 53 16 99 72 43

33  
97

Stack



# PREORDER TRAVERSAL WITH A STACK

Push the root onto the stack.

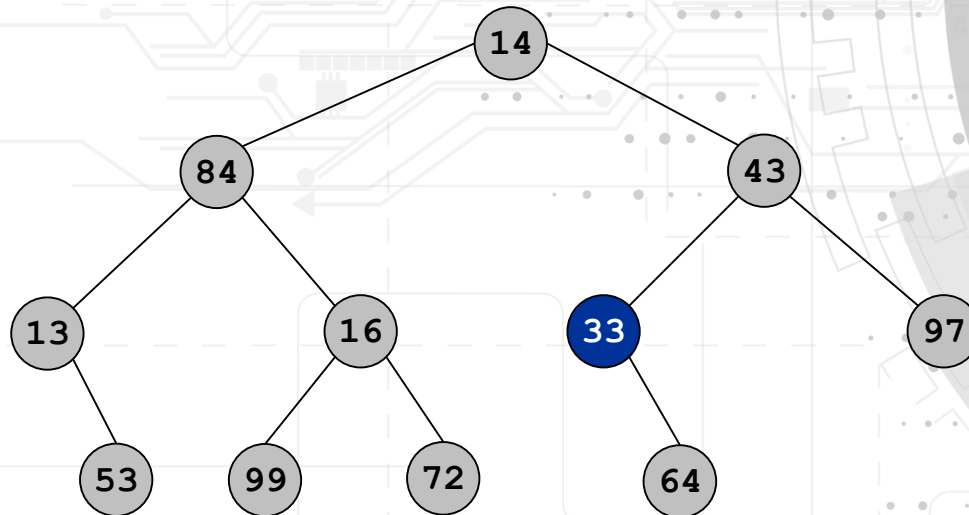
While the stack is not empty

- pop the stack and visit it
- push its two children

14 84 13 53 16 99 72 43 33

64  
97

Stack



# PREORDER TRAVERSAL WITH A STACK

Push the root onto the stack.

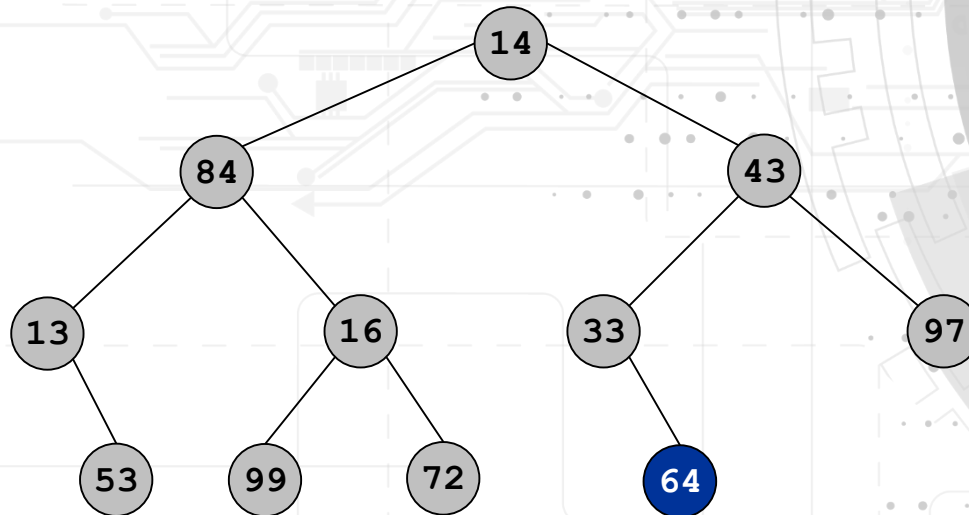
While the stack is not empty

- pop the stack and visit it
- push its two children

14 84 13 53 16 99 72 43 33 64

97

Stack



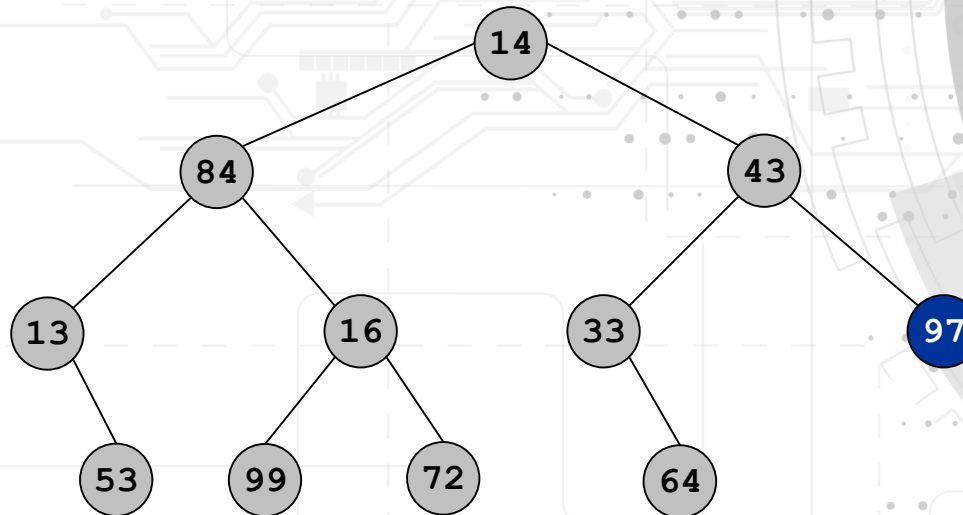
# PREORDER TRAVERSAL WITH A STACK

Push the root onto the stack.

While the stack is not empty

- pop the stack and visit it
- push its two children

14 84 13 53 16 99 72 43 33 64 97



Stack

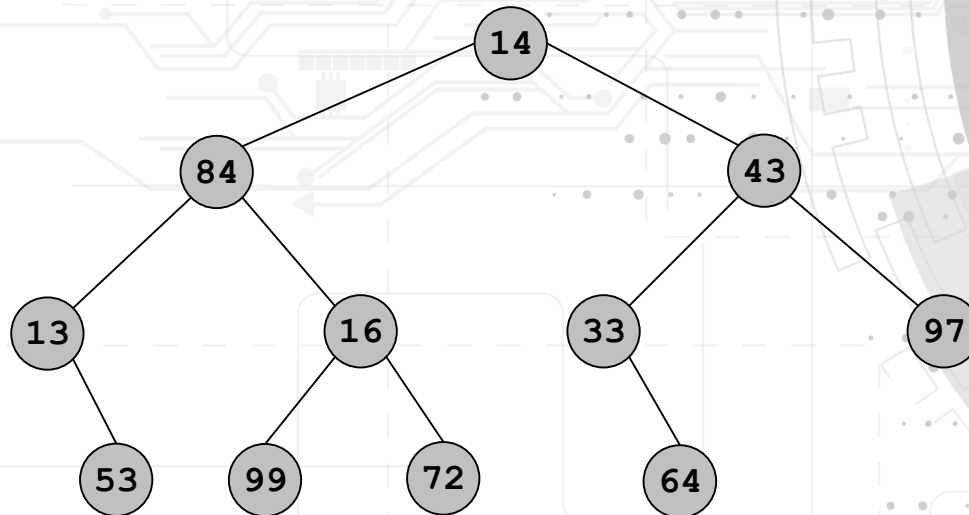
# PREORDER TRAVERSAL WITH A STACK

Push the root onto the stack.

While the stack is not empty

- pop the stack and visit it
- push its two children

14 84 13 53 16 99 72 43 33 64 97



Stack

# YOU SHOULD BE ABLE TO

- Binary tree Traverse:
  - Pre-order
  - In-order
  - Post-order
- Write recursive binary tree functions using the TreeTraversal template as a starting point
- Based on the traversal of the binary tree, do a lot of things: print, count numbers, count height/depth, find grandchildren,..., etc.