BFS DFS

Ideas/Issues

Appendix

COMP2521 25T1

Graphs (II) Graph Traversal

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bfs and dfs path checking path finding

BFS

Ideas/Issues

Appendix

Common problems on graphs:

- Is there a path between two vertices?
- What is the shortest path between two vertices?
- Which vertices are reachable from a particular vertex?
- Is the graph connected?
- Is there a cycle?
- How many connected components are there?
- Is there a simple path/cycle that passes through all vertices?

DFS

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Appendix

All of the above problems can be solved by a systematic exploration of a graph via its edges.

This systematic exploration is called traversal or search.

Traversal BFS and DFS

DFS

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Appendix

Two primary methods for graph traversal/search:

Breadth-first search (BFS)

- Prioritises exploring widely over exploring deeply
 - "Go wide"
- Implemented iteratively (using a queue)

Depth-first search (DFS)

- Prioritises exploring deeply over exploring widely
 - "Go deep"
- Implemented recursively or iteratively (using a stack)

Graph Traversal BFS and DFS

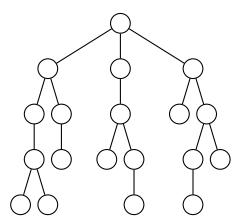
DFS

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Appendix

In what order would BFS and DFS visit the nodes of this tree?

(Assume that nodes towards the left have higher priority)



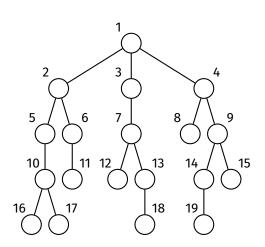
Graph Traversal BFS and DFS

BFS DFS

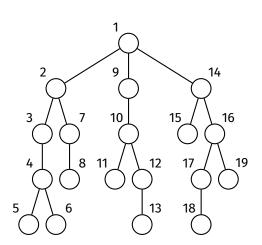
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Breadth-first search



Depth-first search



Traversal
BFS and DFS

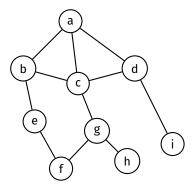
BFS DFS

Ideas/Issues

Appendix

In what order would BFS and DFS visit the vertices of this graph?

(Assume that nodes containing smaller letters have higher priority)



BFS vs. DFS in a graph

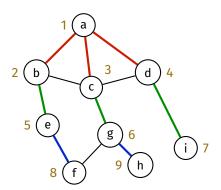
Graph Traversal BFS and DFS

BFS DFS

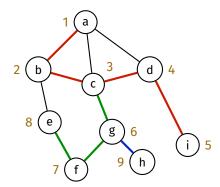
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Breadth-first search



Depth-first search



BFS

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Breadth-first search visits vertices in order of distance from the starting vertex.

BFS is implemented iteratively using a queue.

Data structures

Graph Traversal

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Data structures used in BFS:

- Visited array
 - To keep track of which vertices have been visited
- Predecessor array
 - To keep track of the predecessor of each vertex
 - The predecessor of v is the vertex from which we reached v
 - i.e., the vertex before v on the path to v
- Queue
 - First-in-first-out data structure
 - Stores unvisited vertices in the order that they should be visited

Algorithm

Graph Traversal

BFS Example Pseudocode

Pseudocodo Analysis Path Findin

DF3

Ideas/Issues

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Algorithm:

- 1 Create/initialise data structures:
 - Create visited array, initialised to false
 - Create predecessor array, initialised to -1
 - Create empty queue
- 2 Mark starting vertex as visited and enqueue it
- 3 While the queue is not empty:
 - Dequeue a vertex
 - Let this vertex be v
 - **2 Explore** v that is, for each of v's unvisited neighbours:
 - Mark it as visited
 - 2 Set its predecessor to v
 - 3 Enqueue it

Example

Graph Traversal

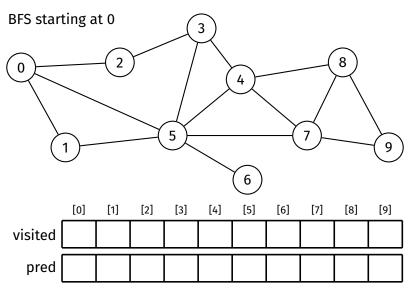
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queue





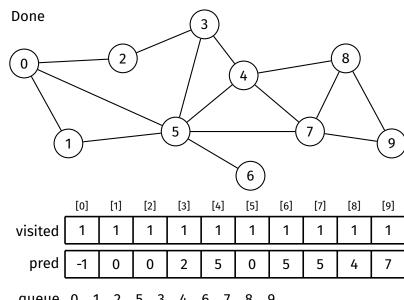
Example

Graph Traversal BFS

Example Pseudocode Analysis Path Finding

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queue



Pseudocode

```
Graph
Traversal
```

```
BFS
Example
Pseudocode
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Path Finding
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```

```
bfs(G, src):
    Input: graph G, starting vertex src
    create visited array, initialised to false
    create predecessor array, initialised to -1
    create queue Q
    visited[src] = true
    enqueue src into Q
    while Q is not empty:
        v = dequeue from Q
        for each neighbour w of v in G where visited \lceil w \rceil = \text{false}:
            visited[w] = true
            predecessor[w] = v
            enqueue w into Q
```

Simplification

Graph Traversal

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When using a predecessor array in BFS, the predecessor array can double as a visited array

predecessor[v] = -1 means v is not visited

Simplification

```
Graph
Traversal
```

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```
bfs(G, src):
    Input: graph G, starting vertex src
    create predecessor array, initialised to -1
    create queue Q
    predecessor[src] = src // <- mark src as visited
    enqueue src into Q
    while Q is not empty:
        v = dequeue from Q
        for each neighbour w of v in G where predecessor[w] = -1:
            predecessor[w] = v
            enqueue w into \mathcal{Q}
```

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BFS is O(V + E) when using the adjacency list representation:

- Typical queue implementation has O(1) enqueue and dequeue
- Each vertex is visited at most once $\Rightarrow O(V)$
- For each vertex, all of its edges are considered once $\Rightarrow O(E)$

BFS

Pseudoco

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A BFS finds the shortest path between the starting vertex and all other vertices.

Shortest path in terms of the number of edges

The shortest path between src and dest can be found by tracing backwards through the predecessor array (from dest to src).

BFS

Example Pseudocode

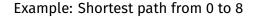
Analysis

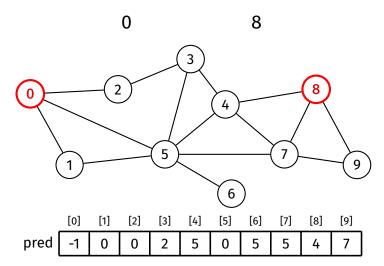
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BFS

Example Pseudocode

Analysis

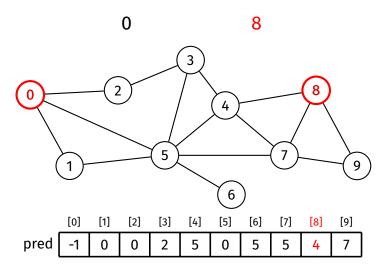
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BFS

Example Pseudocode

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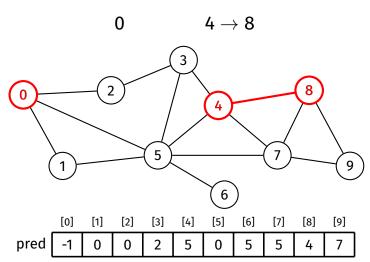
Path Finding

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BFS

Example Pseudocode

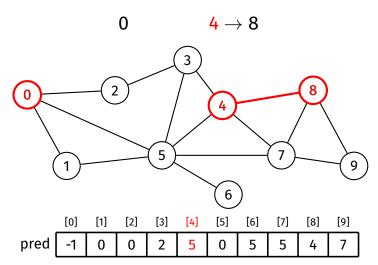
Analysis

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BFS

Example Pseudocode

Analysis

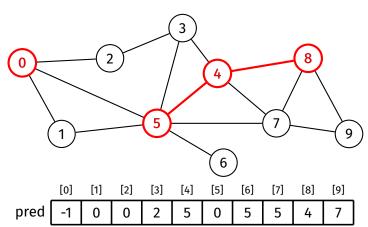
Path Finding

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$$0 \qquad 5 \rightarrow 4 \rightarrow 8$$



BFS

Example Pseudocode

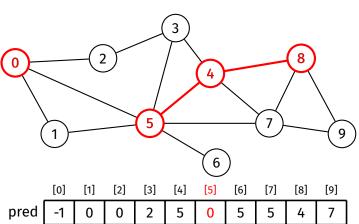
Analysis
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$$0 \qquad \qquad 5 \rightarrow 4 \rightarrow 8$$



BFS

Example Pseudocode

Analysis

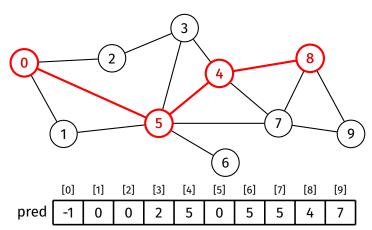
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$$0\longrightarrow 5\rightarrow 4\rightarrow 8$$



Path-Finding with BFS

```
Graph
Traversal
```

Pseudocode Analysis

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Appendix

```
bfsFindPath(G, src, dest):
   Input: graph G, vertices src and dest
... BFS starting from src ...

if predecessor[dest] \neq -1:
   v = dest
   while v \neq src:
      print v, "<-"
   v = predecessor[v]

print src
```

BFS

DFS

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Depth-first search goes as far down one path as possible until it reaches a dead end, then backtracks until it finds a new path to take, then repeats

DFS can be implemented recursively or iteratively.

Graph Traversal

BFS

Recursi

Pseudocode Example Analysis Path checking Path finding Iterative

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Appendix

Depth-first search is described recursively as:

- 1 Mark current vertex as visited
 - The first time, this is the starting vertex
- 2 For each neighbour of the current vertex:
 - If it has not been visited:
 - Recursively traverse starting from that vertex

The recursion naturally induces backtracking.

```
Graph
Traversal
```

BFS

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Graph Traversal

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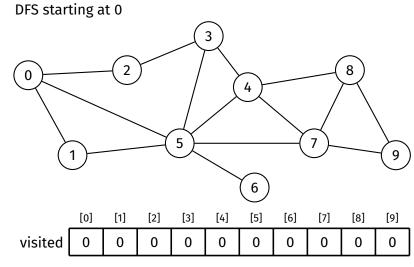
DFS Recursive

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visit order

Example

Graph Traversal

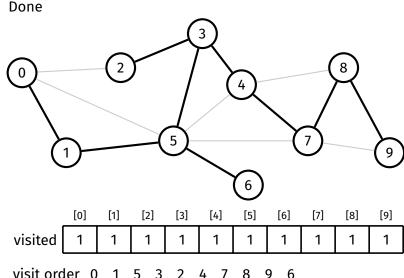
BFS

DFS

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visit order 0 1 5

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Recursive DFS is O(V + E) when using the adjacency list representation:

- Each vertex is visited at most once $\Rightarrow O(V)$
 - Function is called on each vertex at most once
- For each vertex, all of its edges are considered once $\Rightarrow O(E)$

Path-Checking with Recursive DFS

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Recursive DFS can be adapted to check if a path exists between two vertices.

Idea:

- To check if a path exists between *src* and *dest*:
 - If src = dest, then there is a path (the empty path)
 - ullet Otherwise, for each neighbour of src, recursively check if there is a path from that neighbour to dest

BFS

DFS Recursive

Pseudocod

Analysis

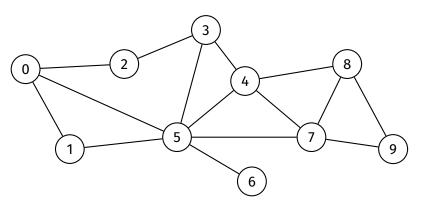
Path checking

Iterative

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Appendix

Does there exist a path between 0 and 7 in this graph?



BFS

DFS Recursive

Pseudocode Example Analysis

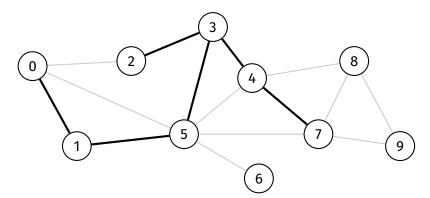
Path checking

Path finding Iterative

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Answer: Yes



Path-Checking with Recursive DFS

Pseudocode

```
Traversal
           dfsHasPath(G, src, dest):
BFS
               Input: graph G, vertices src and dest
               Output: true if there is a path from src to dest
                        false otherwise
               create visited array, initialised to false
Path checking
               return dfsHasPathRec(G, src, dest, visited)
Ideas/Issues
           dfsHasPathRec(G, v, dest, visited):
Appendix
               Input: graph G, vertices v and dest, visited array
               visited[v] = true
               if v = dest:
                    return true
               for each neighbour w of v in G:
                    if visited[w] = false:
                        if dfsHasPathRec(G, w, dest, visited):
                            return true
               return false
```

Traversal

BFS

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Appendix

O(V + E) when using the adjacency list representation:

Algorithm is just a modified recursive DFS with return statements

Path-Finding with Recursive DFS

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How to get the path?

Idea:

- Record the predecessor of each vertex during the DFS
- Trace backwards through the path after the DFS

```
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```

BFS

```
DFS
Recursive
```

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```
dfsFindPath(G, src, dest):
    Input: graph G, vertices src and dest
    create predecessor array, initialised to -1
    predecessor[src] = src
    if dfsFindPathRec(G, src, dest, predecessor):
        v = dest
        while v \neq src:
            print v, "<-"
            v = predecessor[v]
        print src
```

```
Graph
Traversal
```

```
BFS
```

```
Recursive
Pseudocode
```

Example Analysis

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```
dfsFindPathRec(G, v, dest, predecessor):
   if v = dest:
        return true

for each neighbour w of v in G:
    if predecessor[w] = -1:
        predecessor[w] = v
        if dfsFindPathRec(G, w, dest, predecessor):
        return true
```

return false

BFS

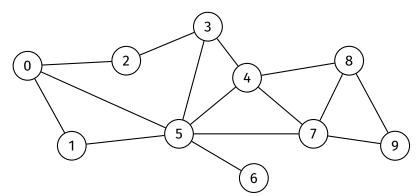
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Find a path from 0 to 7



Path-Finding with Recursive DFS

Example

Graph Traversal

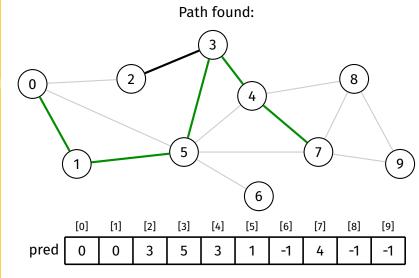
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Iterative Ideas/Issues

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Clearly, DFS is not guaranteed to find the shortest path.

Iterative Depth-First Search

Graph Traversal

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Iterative

Analysi

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Appendix

DFS can be implemented iteratively.

Iterative DFS is similar to BFS, but there are a few crucial differences:

- DFS uses a stack instead of a queue
- DFS marks a vertex as visited after removing it from the stack, not when adding it (which is what BFS does, but with a queue)

```
Graph
Traversal
BFS
DFS
```

Pseudocode Analysis

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Appendix

```
dfs(G, src):
    Input: graph G, vertex src
    create visited array, initialised to false
    create predecessor array, initialised to -1
    create stack S
    push src onto S
    while S is not empty:
        v = pop from S
        if visited[v] = true:
            continue // i.e., return to start of loop
        visited[v] = true
        for each neighbour w of v in G where visited \lceil w \rceil = \text{false}:
            predecessor[w] = v
            push w onto S
```

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Post

Iterative Pseudoc

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Appendix

Iterative DFS is O(V + E) when using the adjacency list representation.

- Typical stack implementation has O(1) push and pop
- Each vertex visited at most once $\Rightarrow O(V)$
- For each vertex, all of its edges are considered $\Rightarrow O(E)$

BFS

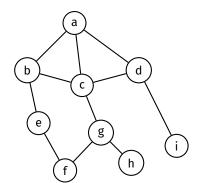
DFS

Ideas/Issues Spanning Trees Disconnected

Appendix

The edges traversed in a graph traversal form a spanning tree.

Consider the following graph:



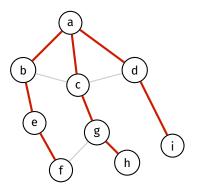
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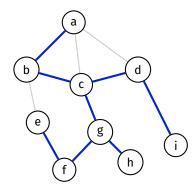
Spanning Trees
Disconnected

Appendix

A traversal starting at vertex 'a' forms the following spanning trees:



Breadth-first search



Depth-first search

BFS DFS

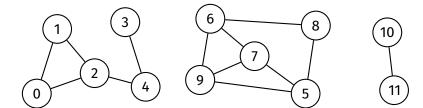
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Ideas/Issues

Disconnected Graphs

Appendix

If a graph is not connected, a graph traversal starting from a given vertex will not traverse the entire graph



BFS

Ideas/Issues

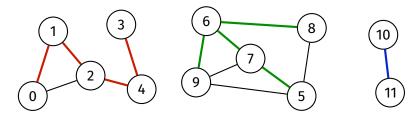
Disconnected Graphs

Appendix

Solution

After initial traversal is complete, perform traversal again on an unvisited vertex, repeat until all vertices are visited

This produces a spanning forest



Disconnected Graphs

```
Graph
Traversal
```

BFS DFS

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Graphs

Appendix

```
dfs(G):
    Input: graph G

    create predecessor array, initialised to -1

for each vertex v in G:
    if predecessor[v] = -1:
        dfsRec(G, v, predecessor)
...
```

BFS DFS

. . .

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https://forms.office.com/r/2BW7BasQ77



BFS

DFS

Ideas/Issues

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BFS Example

DEC

DFS Example

Path-Checking Example

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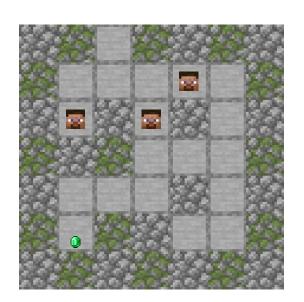
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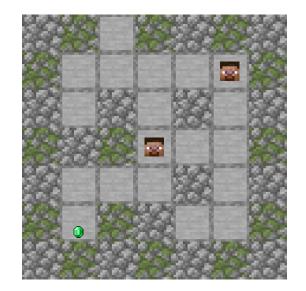
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DFS Example



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DFS

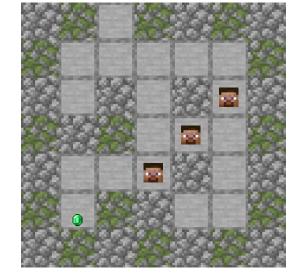
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DFS

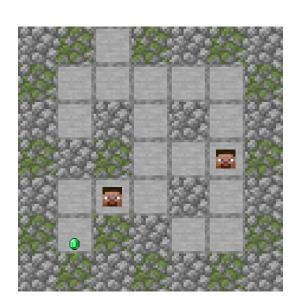
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BFS

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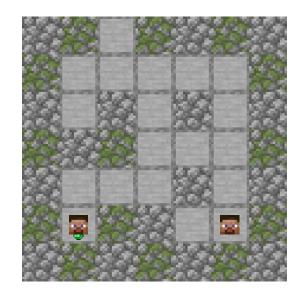
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Path-Checking Example

How do we avoid revisiting the same tiles?

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DFS Exam

Path-Checkin

How do we avoid revisiting the same tiles?

Mark tiles as they are visited!

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DFS Example



BFS

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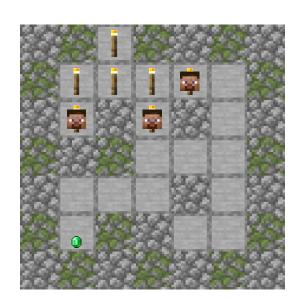
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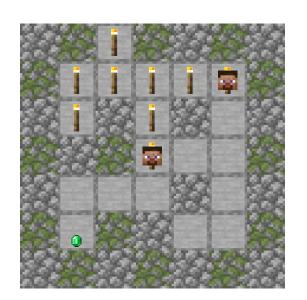
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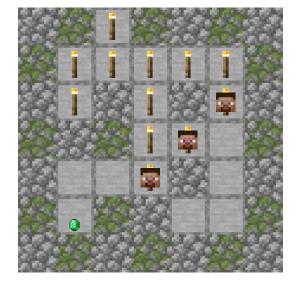
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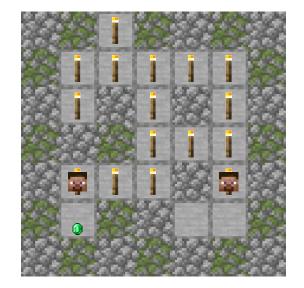
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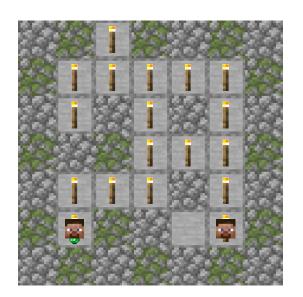
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Path-Checking Example

How do we find our way back to the entrance?

Traversal

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How do we find our way back to the entrance?

For each tile that we visit, keep note of the tile we were on directly before it! This is called the predecessor.

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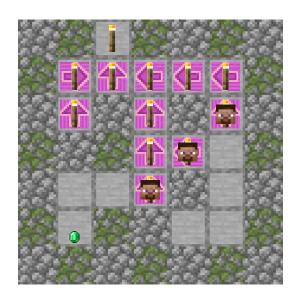
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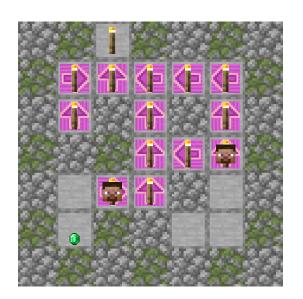
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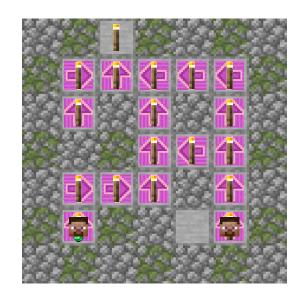
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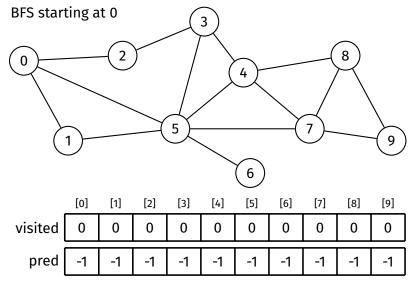
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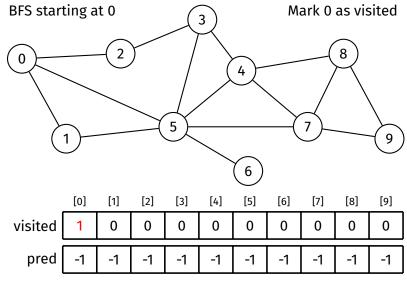
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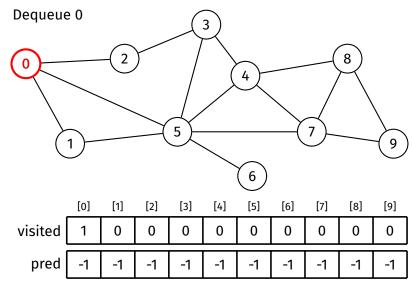
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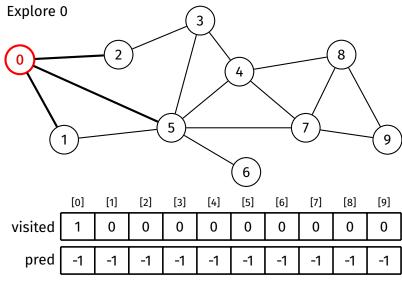
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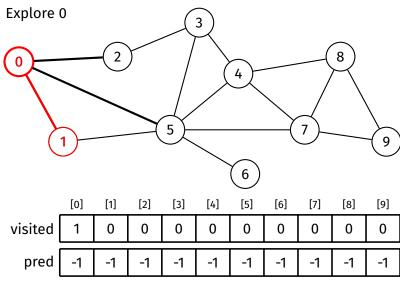
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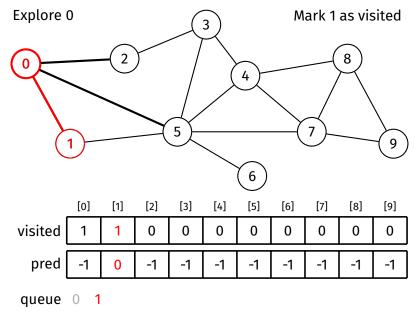
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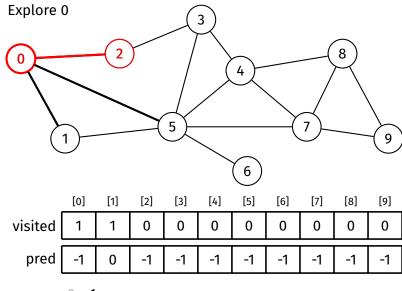
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queue 0 1

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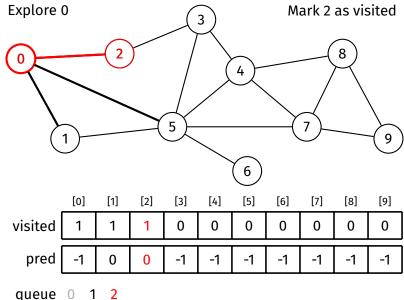
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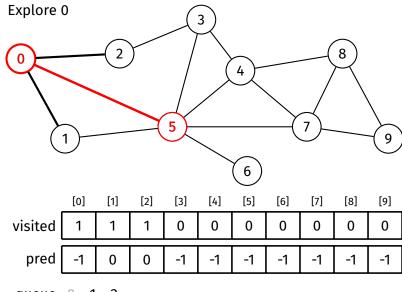
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queue 0 1 2



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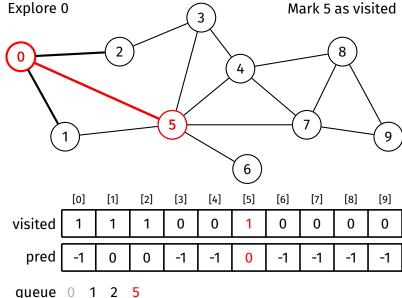
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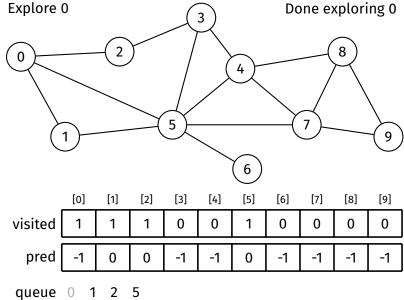
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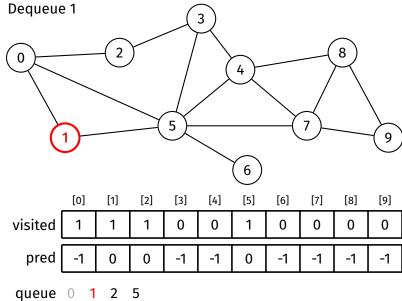
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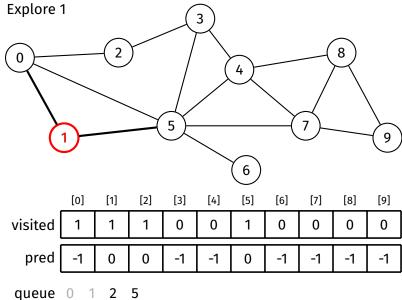
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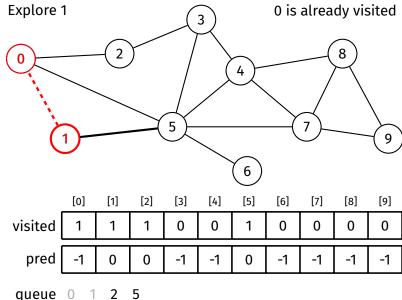
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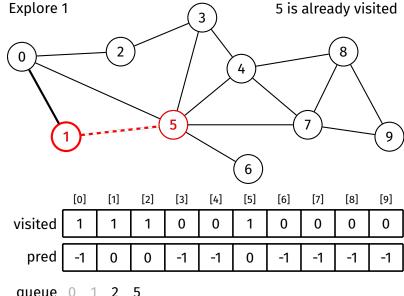
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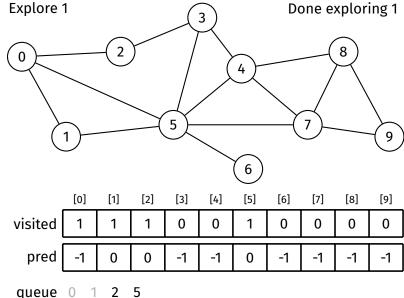
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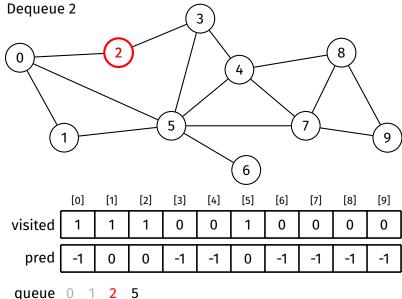
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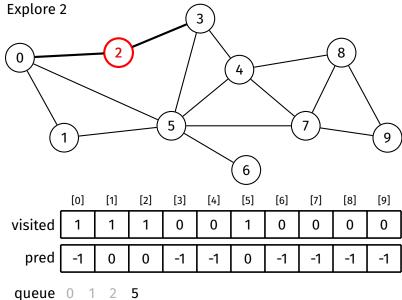
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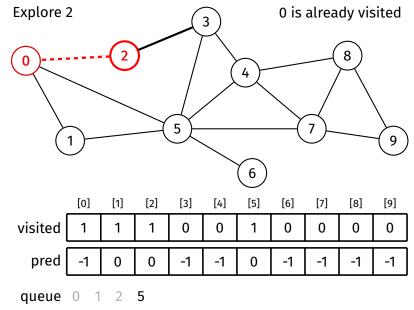
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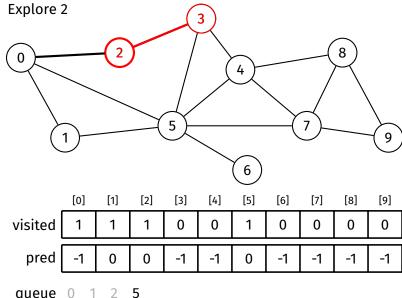
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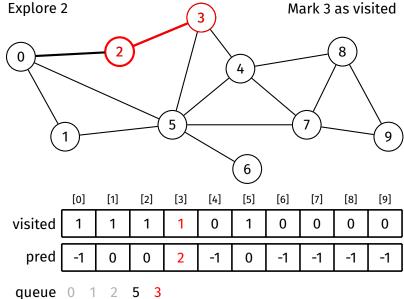
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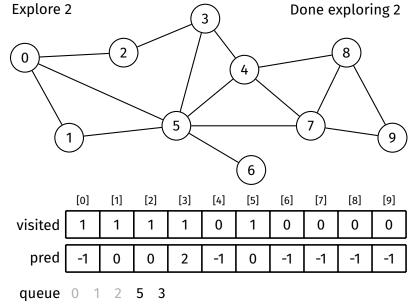
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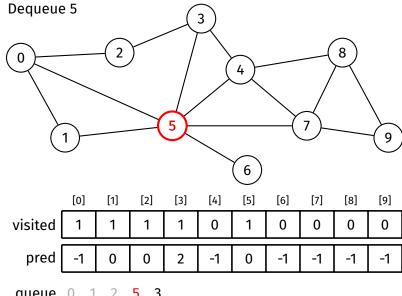
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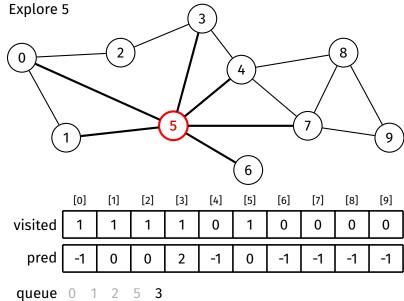
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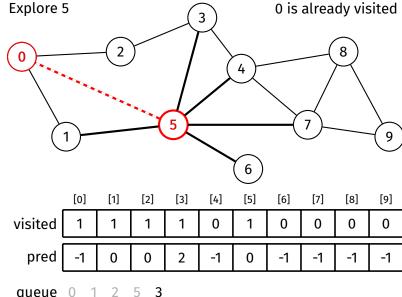
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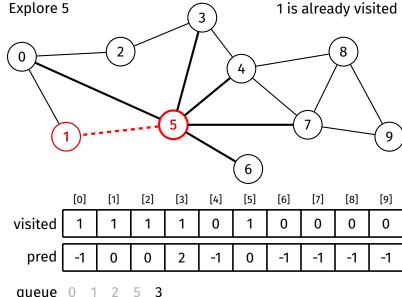
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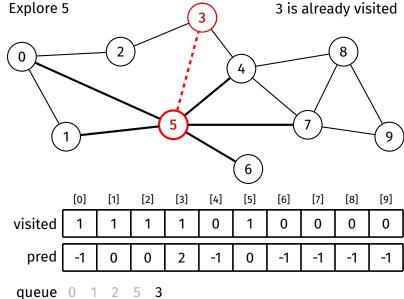
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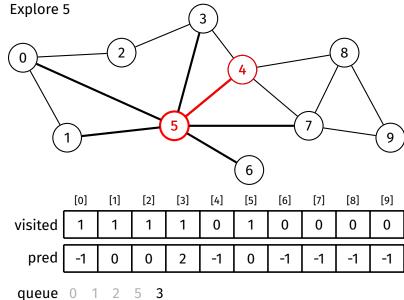
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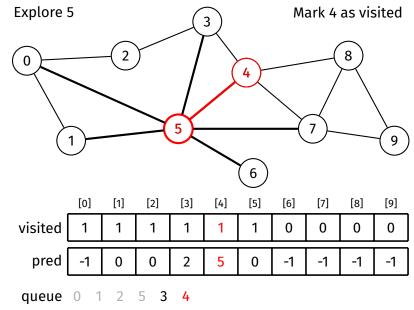
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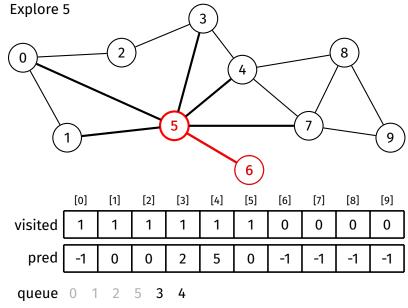
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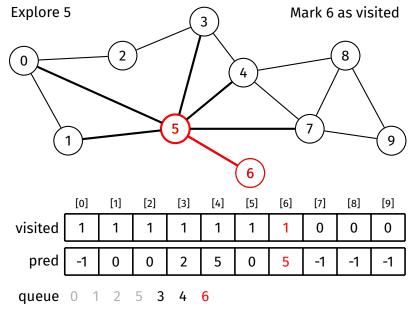
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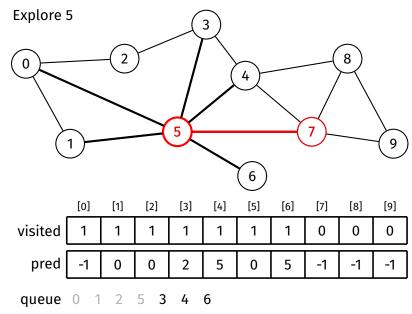
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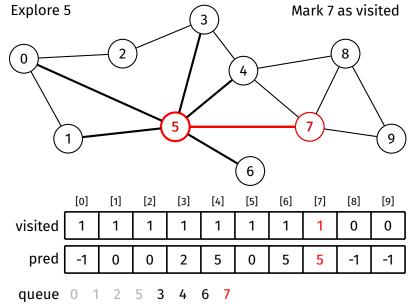
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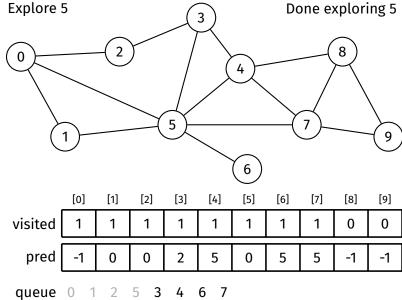
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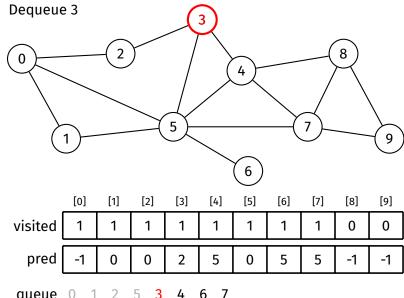
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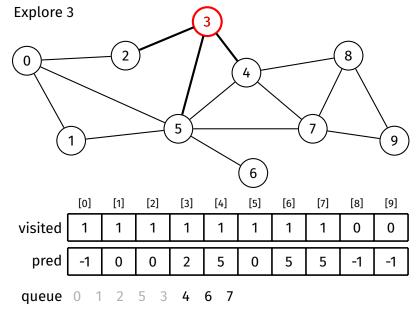
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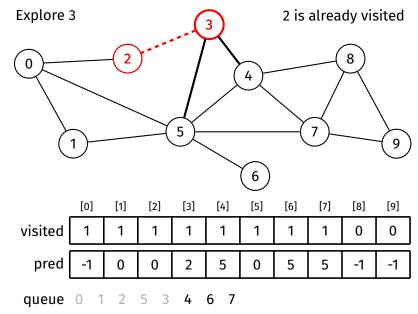
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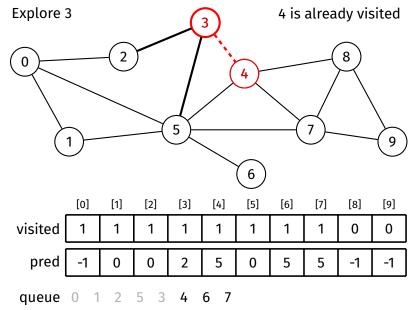
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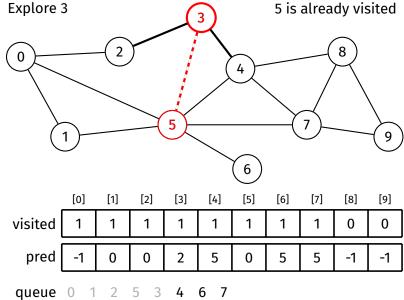
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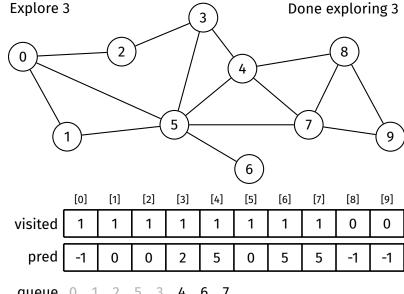
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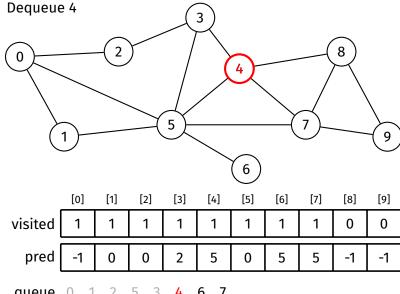
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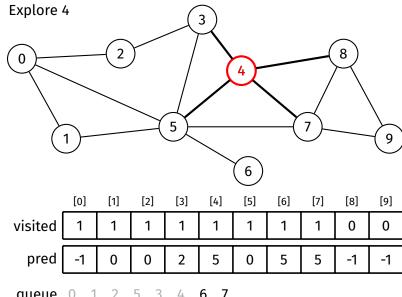
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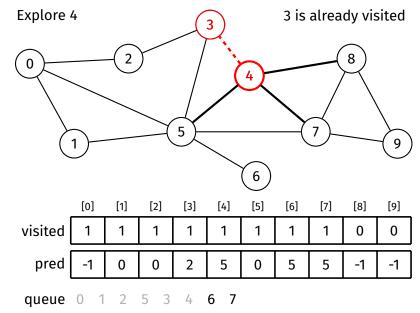
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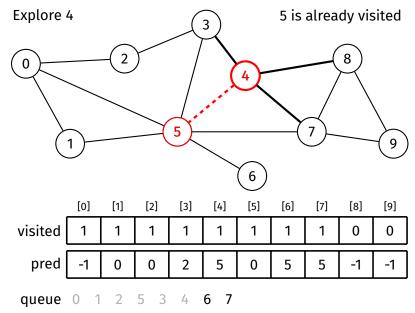
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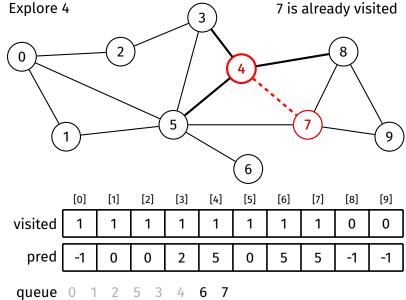
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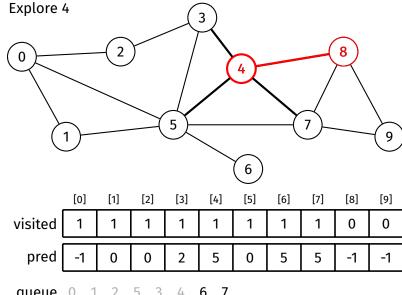
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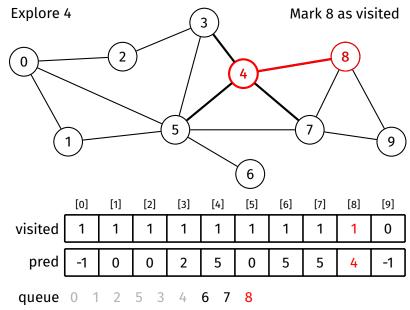
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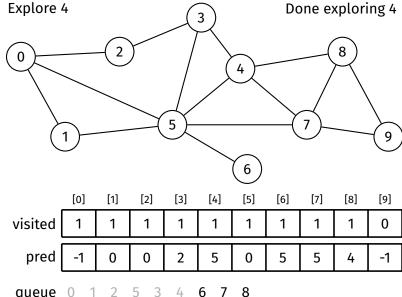
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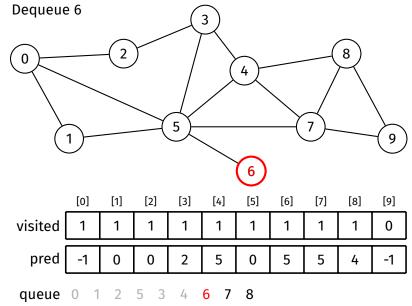
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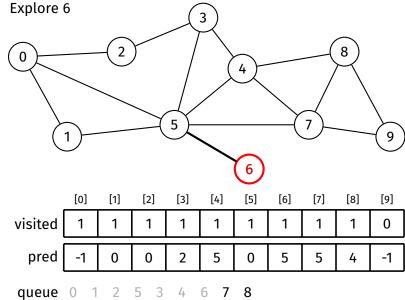
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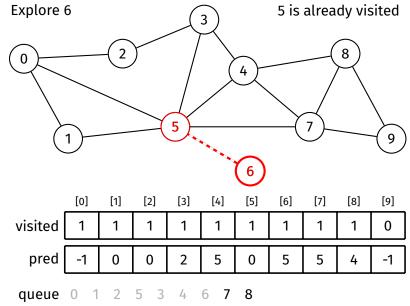
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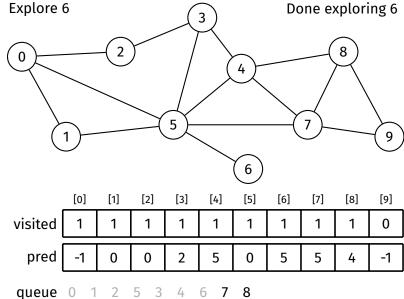
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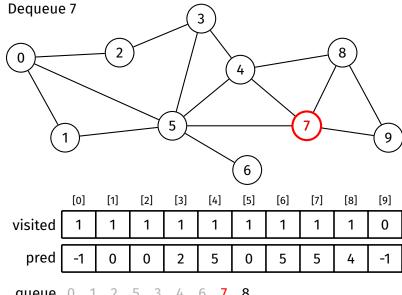
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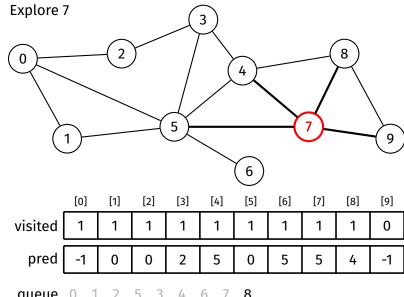
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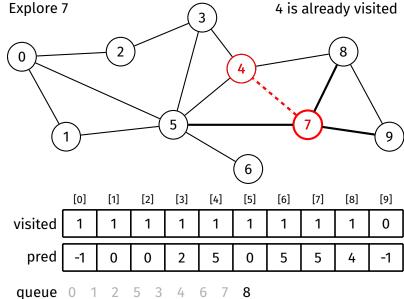
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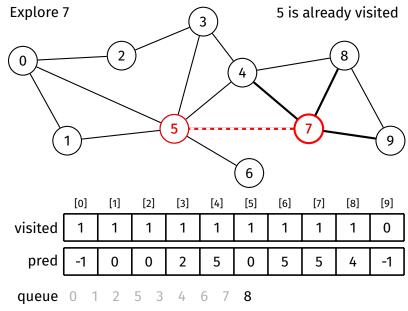
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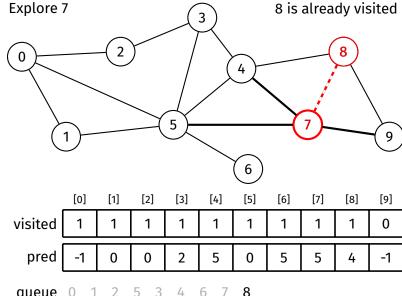
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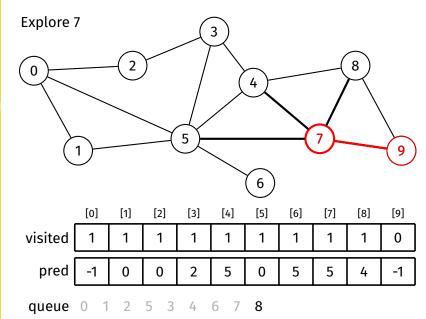
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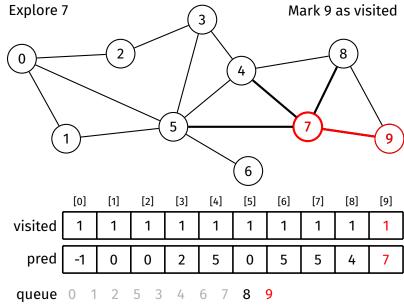
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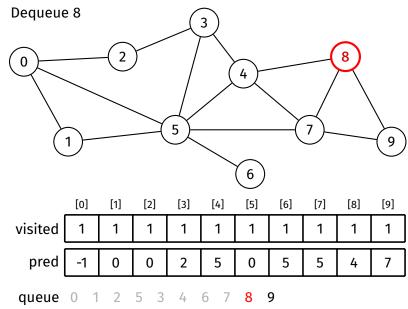
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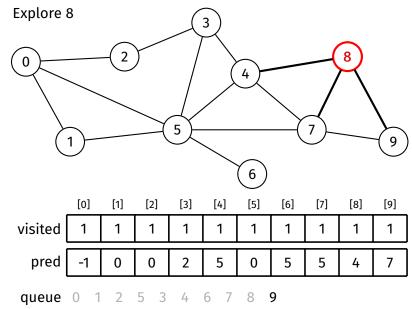
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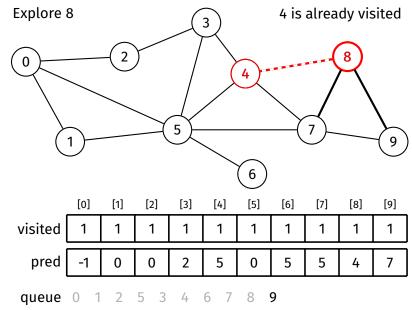
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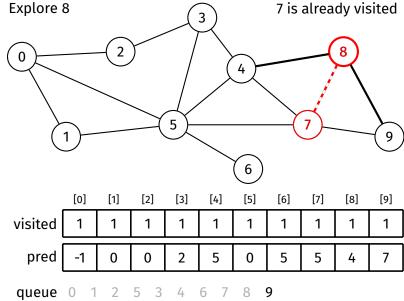
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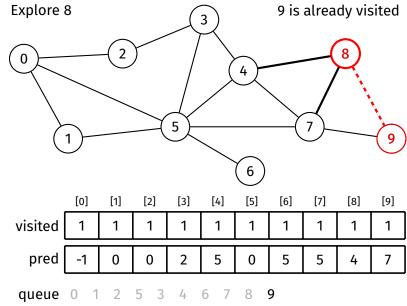
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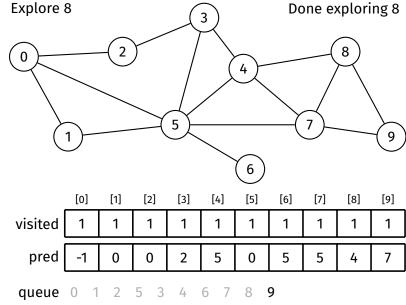
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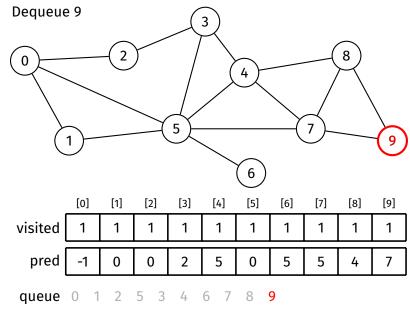
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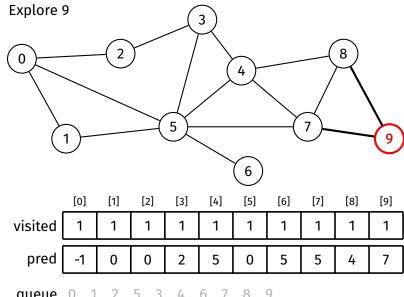
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0 1 2 5 3 4 6 7 8 9 queue



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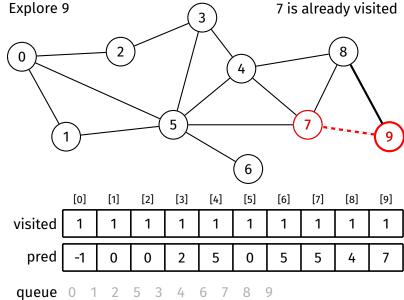
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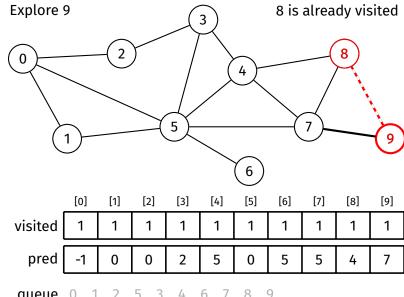
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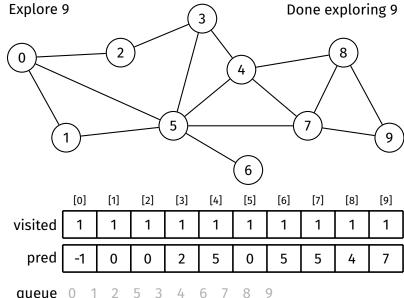
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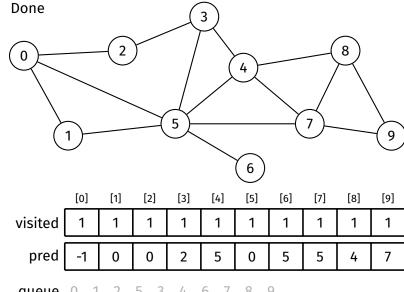
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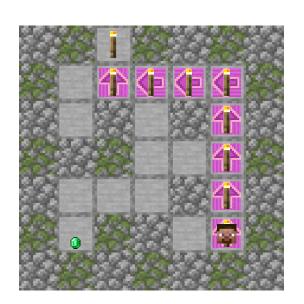
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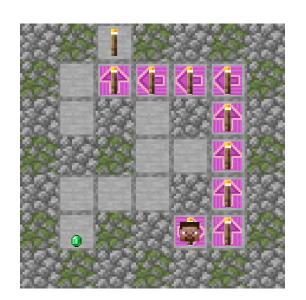
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DFS

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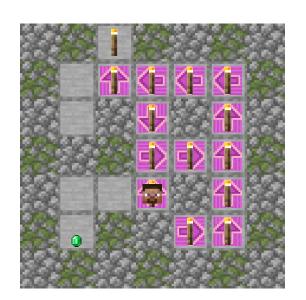
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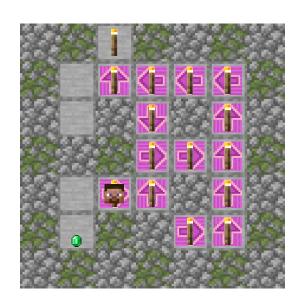
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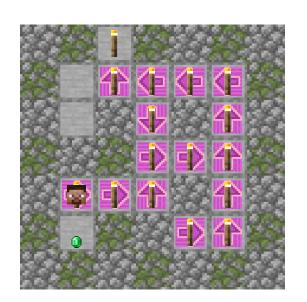
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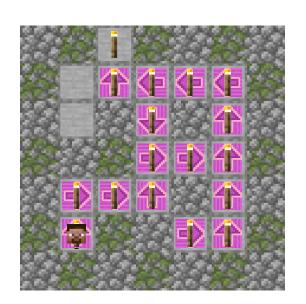
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DFS Example



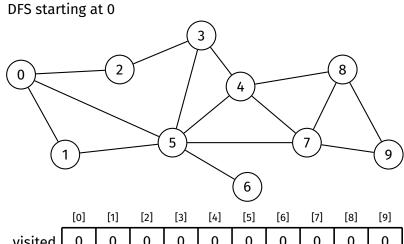
BFS DFS

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BFS Example

DFS Example Path-Checking



visited 0 0 0 0 0 0

visit order

call stack

BFS

DFS

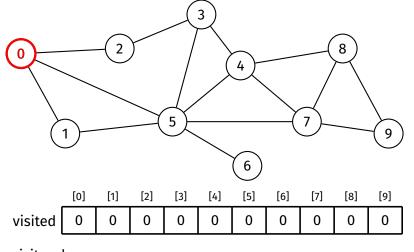
Ideas/Issues

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BFS Example

DFS DFS Example

Path-Checking



dfs(0)

call stack

visit order

BFS

DFS

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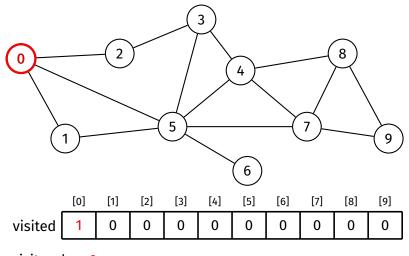
Appendix

BFS

BFS Example DFS

DFS Example

Path-Checking



visit order 0

Mark 0 as visited

dfs(0) call stack

BFS DFS

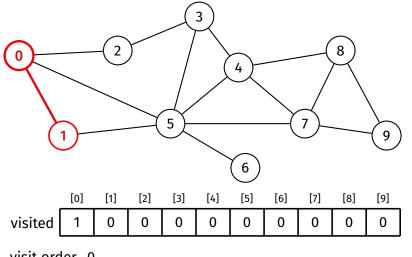
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BFS Example

DFS Example

Path-Checking



visit order 0

1 has not been visited

dfs(0)

call stack

BFS

DFS

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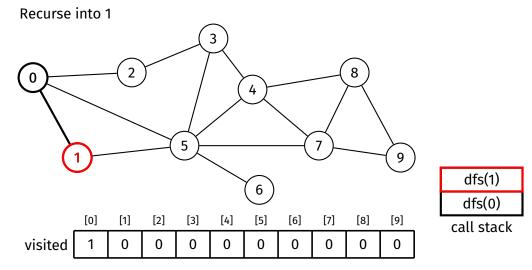
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BFS Example DFS

DFS Example

Path-Checking



visit order 0

BFS DFS

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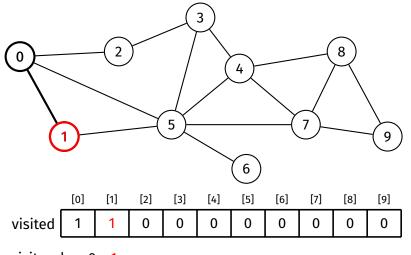
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BFS Example

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DFS Example

Path-Checking



dfs(1) dfs(0)

call stack

visit order 0 1

Mark 1 as visited

BFS

DFS

Ideas/Issues

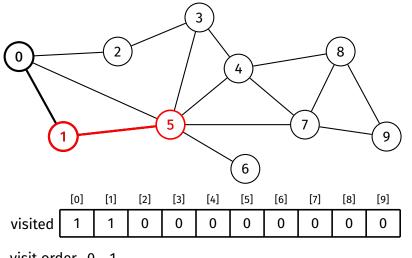
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BFS Example

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DFS Example

Path-Checking



visit order 0 1

5 has not been visited

dfs(1)

dfs(0)

call stack

BFS

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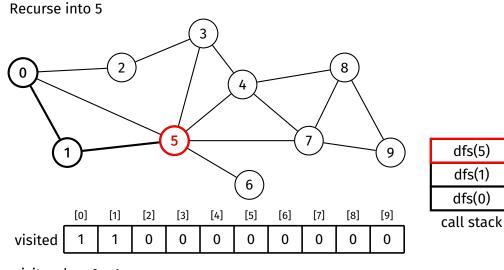
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Path-Checking



visit order 0 1

BFS

DFS

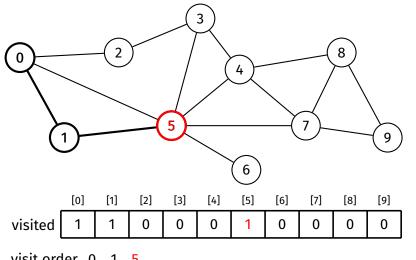
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BFS Example

DFS DFS Example

Path-Checking



dfs(5) dfs(1) dfs(0)

call stack

visit order 0 1 5

Mark 5 as visited

BFS DFS

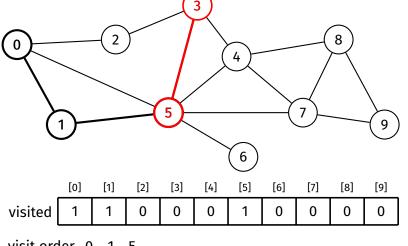
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BFS Example

DFS DFS Example

Path-Checking



dfs(5) dfs(1) dfs(0)call stack

visit order 0 1 5

3 has not been visited

BFS

DFS

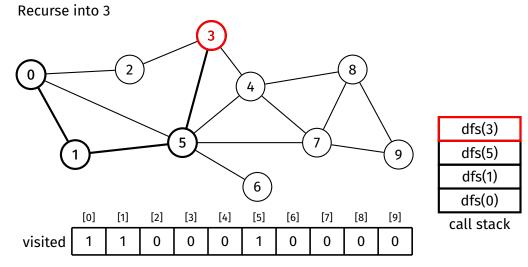
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Path-Checking

5 6 [0] [1] [2] [3] [4] [5] [6] [7] [8] [9] visited 0 0 0 0

dfs(3) dfs(5) dfs(1) dfs(0)

call stack

visit order 0 1 5 3

Mark 3 as visited

BFS

DFS

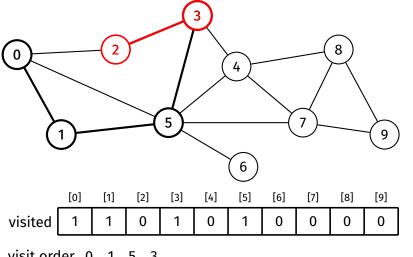
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BFS Example

DFS DFS Example

Path-Checking



call stack

dfs(3)

dfs(5) dfs(1)

dfs(0)

visit order 0 1 5 3

2 has not been visited

BFS

DFS

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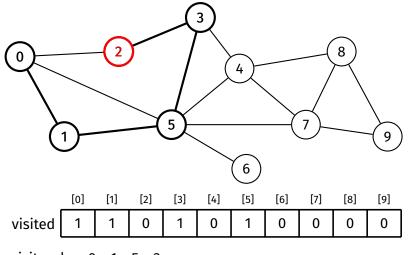
BFS

BFS Example

DFS

DFS Example

Path-Checking



dfs(5)
dfs(1)
dfs(0)
call stack

dfs(2)

dfs(3)

visit order 0 1 5 3

Recurse into 2

BFS

DFS

Ideas/Issues

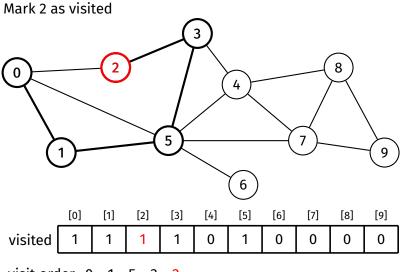
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DFS

DFS Example

Path-Checking



dfs(3)dfs(5) dfs(1) dfs(0)call stack

dfs(2)

Return

Graph Traversal

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DFS DFS Example

Path-Checking

Appendix BFS Example

5 6 [0] [1] [2] [3] [4] [5] [6] [7] [8] [9] visited 0 0 0 0

dfs(3)dfs(5) dfs(1) dfs(0)call stack

BFS

DFS

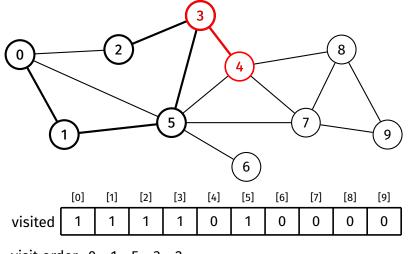
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BFS Example DFS

DFS Example

Path-Checking



dfs(5) dfs(1) dfs(0)call stack

dfs(3)

visit order 0 1

4 has not been visited

dfs(3)

dfs(5) dfs(1)

dfs(0)

call stack

Graph Traversal

BFS

DFS

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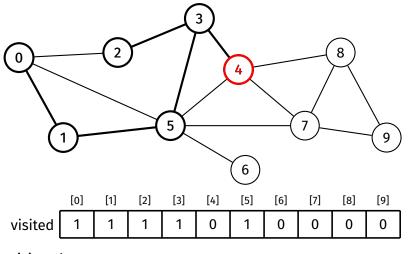
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BFS Example

DFS

DFS Example

Path-Checking



L

visit order 0 1 5 3 2

Recurse into 4

dfs(3)

dfs(5) dfs(1)

dfs(0)

call stack

Graph Traversal

BFS

DFS

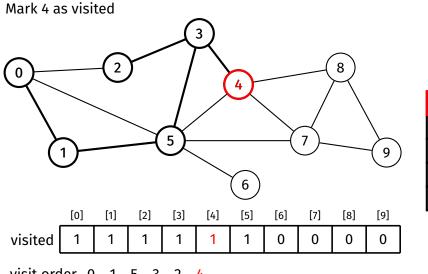
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BFS Example DFS

DFS Example

Path-Checking



visit order 0 5 3 2 4

dfs(3)

dfs(5) dfs(1)

Graph Traversal

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DFS

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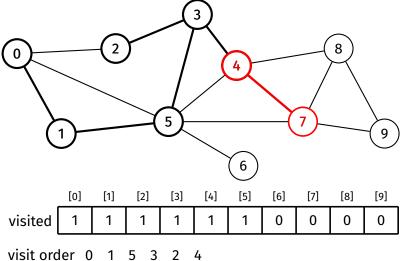
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BFS Example

DFS

DFS Example

Path-Checking



dfs(0)call stack

7 has not been visited

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dfs(7)

dfs(4)

dfs(3)

dfs(5) dfs(1)

dfs(0)

Graph Traversal

BFS

DFS

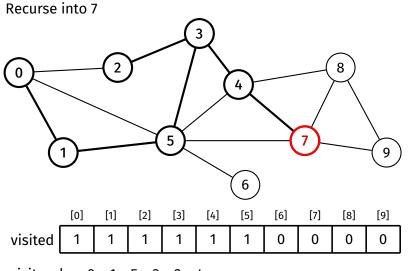
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DFS DFS Example

Path-Checking



call stack

dfs(7)

dfs(4)

dfs(3)

dfs(5) dfs(1)

dfs(0)

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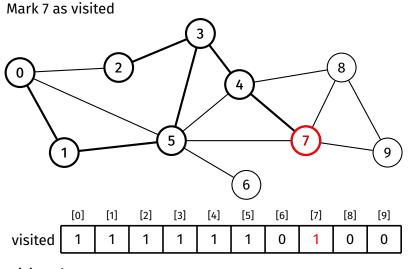
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DFS Example

Path-Checking



call stack

BFS DFS

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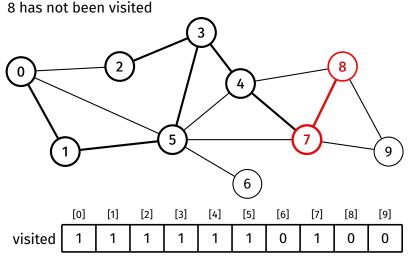
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DFS

DFS Example

Path-Checking



visit order 0 1 5 3 2 4 7

dfs(5)
dfs(1)
dfs(0)
call stack

dfs(7)

dfs(4)

dfs(3)

dfs(8)

dfs(7)

dfs(4)

dfs(3)

dfs(5) dfs(1)

dfs(0)

call stack

Graph Traversal

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DFS Example

Path-Checking

Recurse into 8 5 6 [0] [1] [2] [3] [4] [5] [6] [7] [8] [9] visited 0 0 0

dfs(8)

dfs(7)

dfs(4)

dfs(3)

dfs(5) dfs(1)

dfs(0)

call stack

Graph Traversal

BFS

DFS

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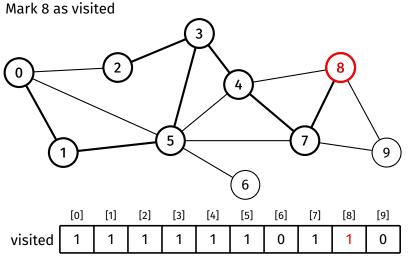
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BFS Example

DFS Example

Path-Checking



visit order 0 1 5 3 2 4 7 8

Traversal

BFS

DFS

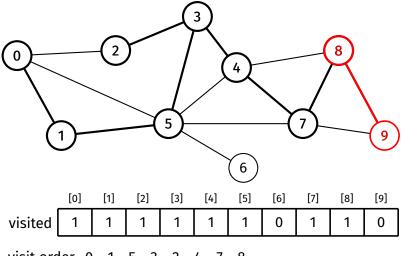
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DFS Example Path-Checking



dfs(4) dfs(3)dfs(5) dfs(1) dfs(0)call stack

dfs(8)

dfs(7)

visit order 0 1 5 3 2

9 has not been visited

Traversal

BFS

DFS

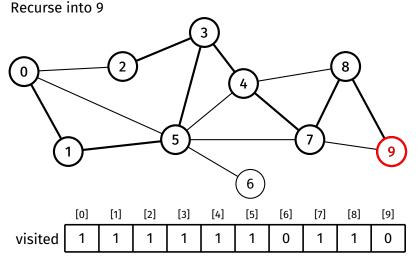
Ideas/Issues

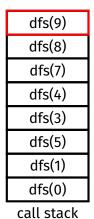
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DFS Example Path-Checking





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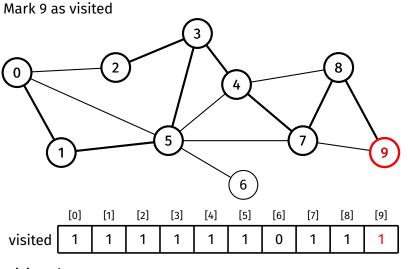
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DFS Example

Path-Checking



visit order 0 1 5 3 2 4 7 8 9



dfs(8)

dfs(7)

dfs(4)

Graph Traversal

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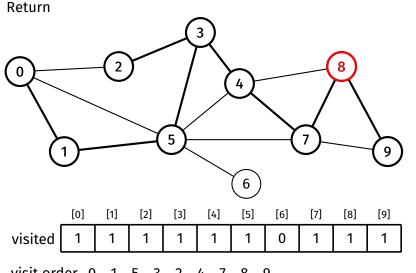
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BFS Example

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DFS Example Path-Checking



dfs(3)dfs(5) dfs(1) dfs(0)call stack

dfs(7)

dfs(4)

dfs(3)

dfs(5) dfs(1)

dfs(0)

Return

Graph Traversal

BFS

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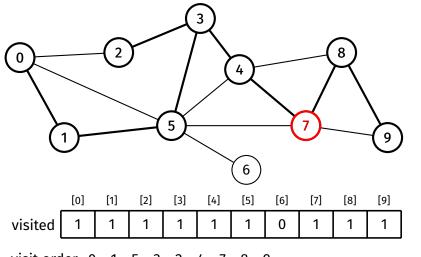
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DFS Example

Path-Checking



call stack

dfs(3)

dfs(5) dfs(1)

dfs(0)

call stack

Return

Graph Traversal

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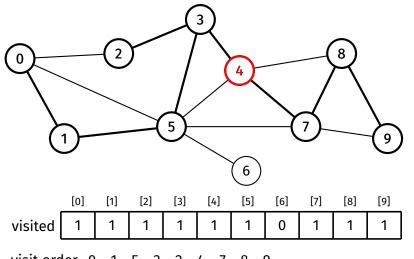
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DFS Example

Path-Checking



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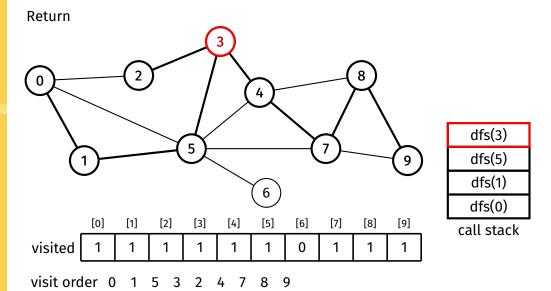
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Path-Checking



Return

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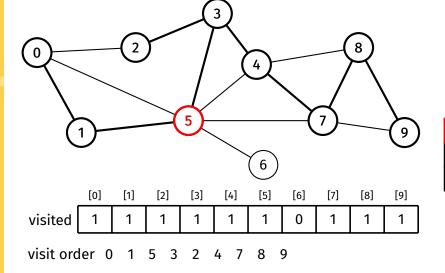
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BFS Example

DFS Example

Path-Checking



dfs(5) dfs(1) dfs(0) call stack

BFS

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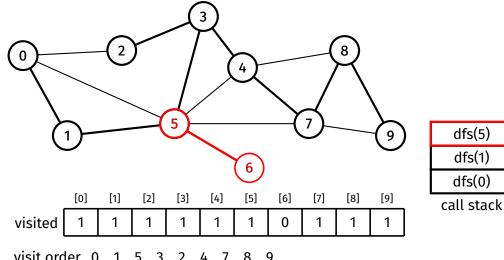
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BFS Example

DFS Example

Path-Checking



visit order 0 1 5 3 2

6 has not been visited

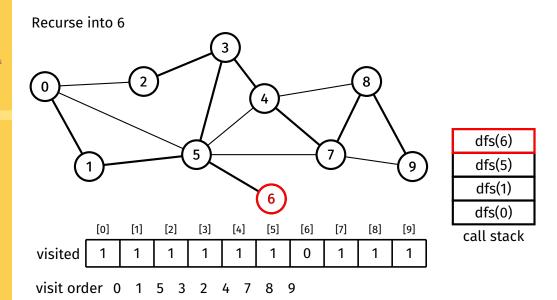
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BFS Example DFS DFS Example Path-Checking



BFS DFS

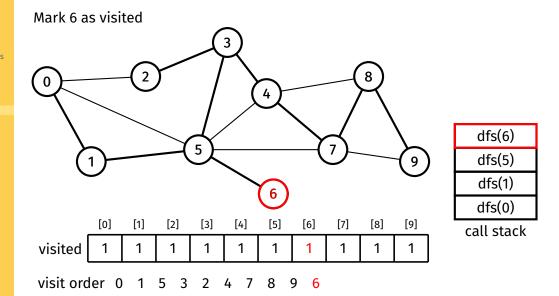
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BFS Example

DFS DFS Example

Path-Checking



dfs(5)

dfs(1)

dfs(0)

call stack

Return

Graph Traversal

BFS

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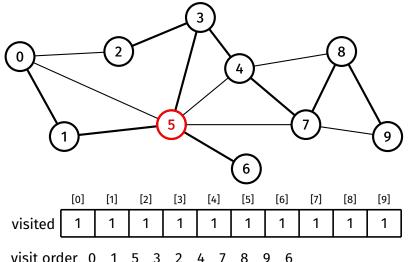
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BFS Example DFS

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Path-Checking



Return

Graph Traversal

BFS

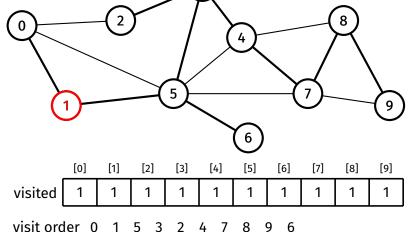
DFS

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DFS Example Path-Checking

BFS Example DFS



dfs(1) dfs(0)call stack

Return

Graph Traversal

BFS

DFS

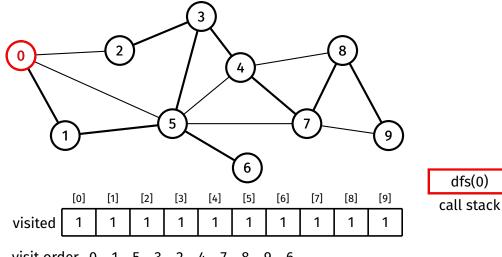
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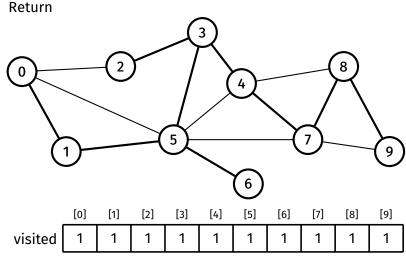
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BFS Example

DFS DFS Example Path-Checking



visit order 0 1 5 3 2

Example

Graph Traversal

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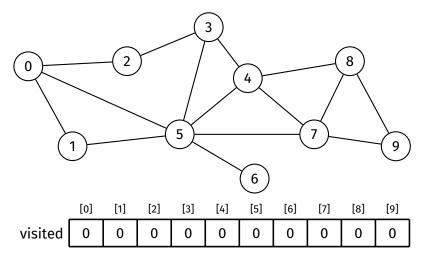
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DFS

DFS Exa

Path-Checking Example

Is there a path between 0 and 7?



Example

Graph Traversal

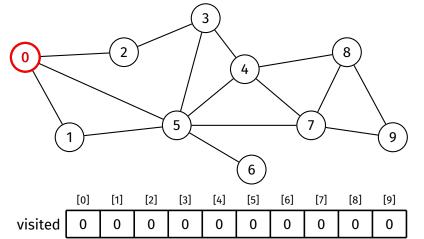
BFS DFS

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BFS Example

Path-Checking Example



path(0, 7)?

Example

Graph Traversal

BFS DFS

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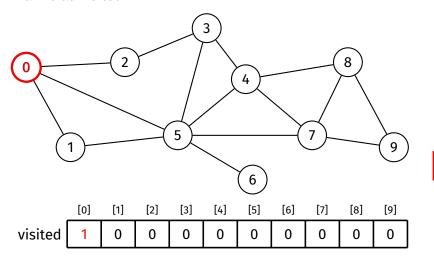
Appendix BES

BES Examp

DFS

Path-Checking Example

Mark 0 as visited



path(0, 7)?

Example

Graph Traversal

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Appendix BES

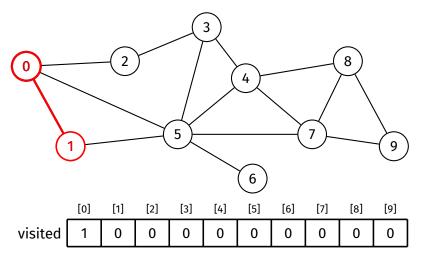
BFS Examp

DES Form

Path-Checking

Path-Checkir Example

1 has not been visited



path(0, 7)?

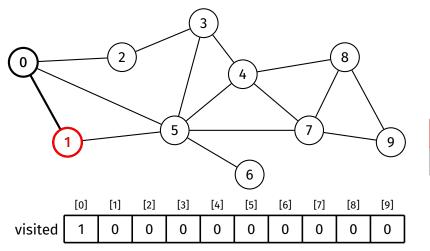
BFS DFS

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Appendix

Path-Checking Example

Recurse into 1



Path-Checking with Recursive DFS

Example

Graph Traversal

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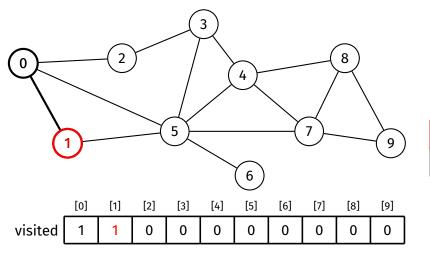
BFS Examp

DFS

Path-Checking

Path-Checkin Example

Mark 1 as visited



Path-Checking with Recursive DFS

Example

Graph Traversal

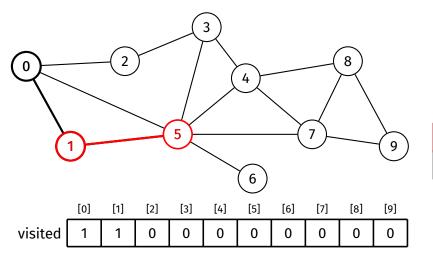
BFS DFS

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Path-Checking Example

5 has not been visited



BFS DFS

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Appendix BFS

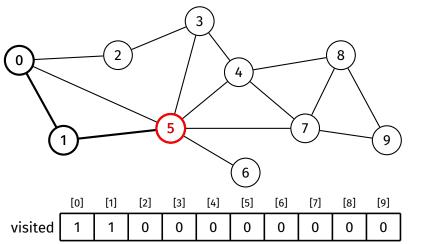
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Path-Checking Example

Recurse into 5





Path-Checking with Recursive DFS

Example

Graph Traversal

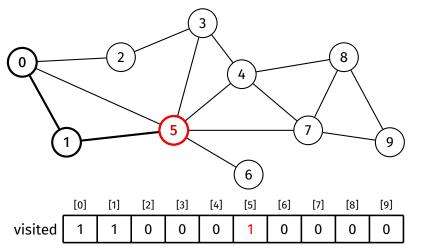
BFS DFS

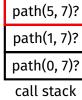
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Path-Checking Example

Mark 5 as visited





BFS DFS

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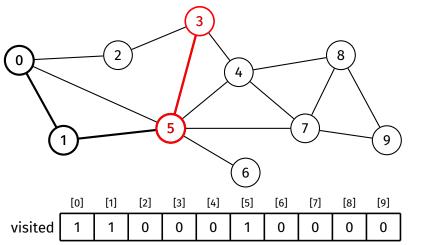
BES Examp

DFS

Path-Checki

Path-Checking Example

3 has not been visited





BFS DFS

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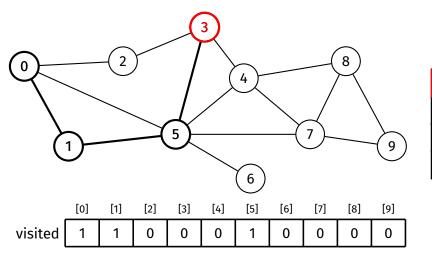
BFS Examp

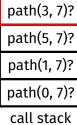
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Path-Checki

Path-Checking Example

Recurse into 3





BFS DFS

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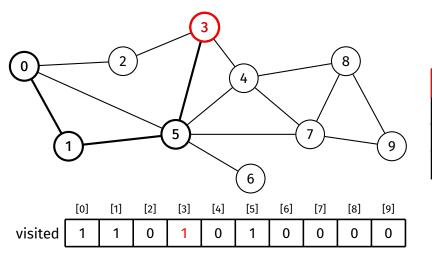
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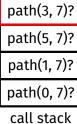
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DFS Exa

Path-Checking Example

Mark 3 as visited





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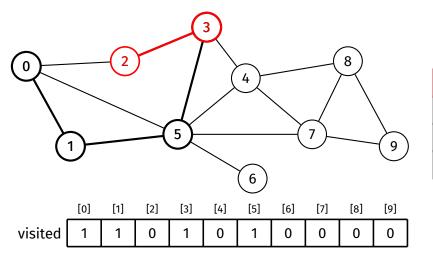
DEC Evamo

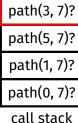
DFS

DFS Example Dath-Chocki

Path-Checking Example

2 has not been visited





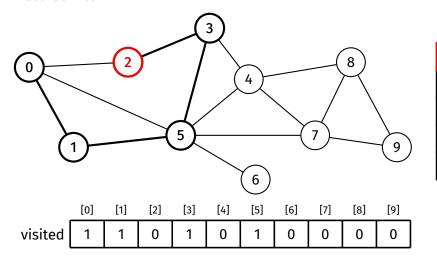
BFS DFS

Ideas/Issues

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Path-Checking Example

Recurse into 2



path(2, 7)?
path(3, 7)?
path(5, 7)?
path(1, 7)?
path(0, 7)?
call stack

BFS DFS

Ideas/Issues

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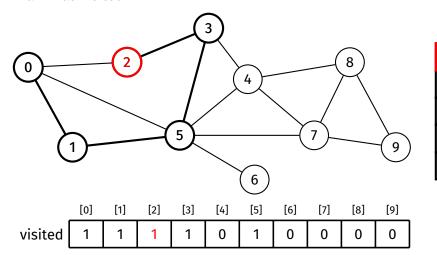
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BFS Examp

DFS Examp

Path-Checking Example

Mark 2 as visited



path(3, 7)?
path(5, 7)?
path(1, 7)?
path(0, 7)?
call stack

path(2, 7)?

BFS DFS

Ideas/Issues

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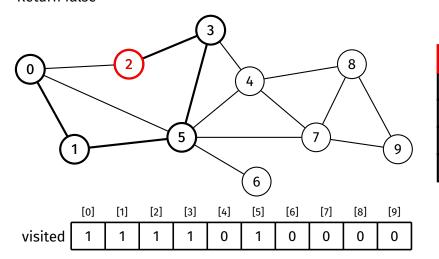
BFS Example

DFS

DFS Exampl

Path-Checking Example

Return false



path(2, 7)?
path(3, 7)?
path(5, 7)?
path(1, 7)?
path(0, 7)?
call stack

Path-Checking with Recursive DFS

Example

Graph Traversal

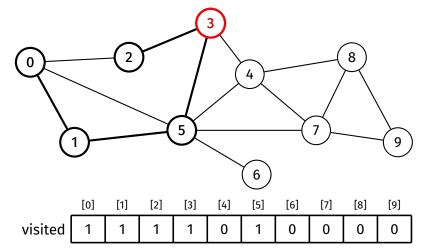
BFS DFS

Ideas/Issues

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Path-Checking

Example



path(3, 7)? path(5, 7)? path(1, 7)? path(0, 7)? call stack

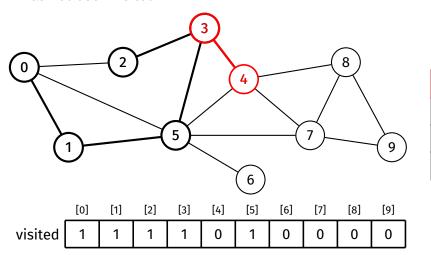
BFS DFS

Ideas/Issues

Appendix

Path-Checking Example

4 has not been visited



path(3, 7)?
path(5, 7)?
path(1, 7)?
path(0, 7)?
call stack

BFS DFS

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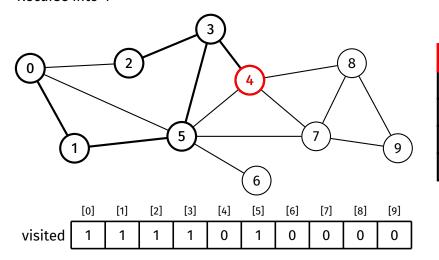
BES Evamn

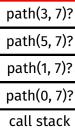
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DFS Examp

Path-Checking Example

Recurse into 4





path(4, 7)?

BFS DFS

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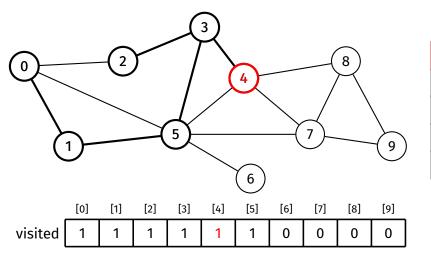
BFS

DIS Examp

DFS Examp

Path-Checking Example

Mark 4 as visited



ραιι(+, //:
path(3, 7)?
path(5, 7)?
path(1, 7)?
path(0, 7)?
call stack

nath(4 7)?

BFS DFS

Ideas/Issues

Appendix BES

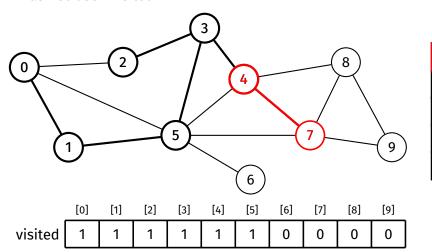
DEC Evamo

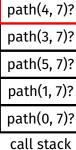
DFS

DFS Exampl

Path-Checking Example

7 has not been visited





BFS DFS

Ideas/Issues

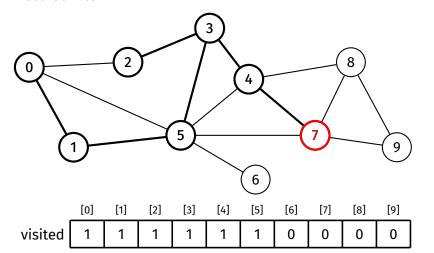
Appendix BES

BFS Exampl

DFS

Path-Checking Example

Recurse into 7



path(7, 7)?

path(4, 7)?

path(3, 7)?

path(5, 7)?

path(1, 7)?

path(0, 7)?

call stack

BFS DFS

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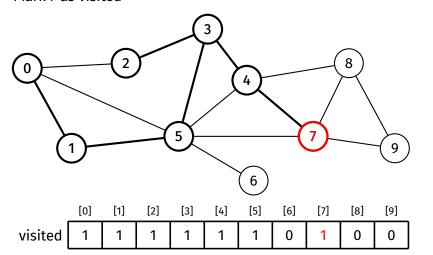
DEC Evamo

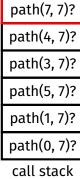
DFS

DFS Exampl

Path-Checking Example

Mark 7 as visited





BFS DFS

Ideas/Issues

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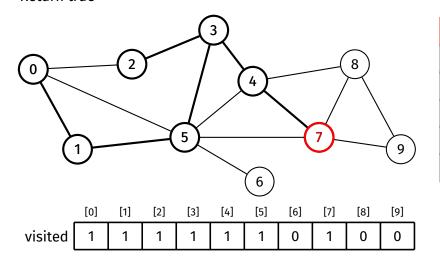
BFS Example

DES

DFS Exam

Path-Checking Example

Return true



path(4, 7)?
path(3, 7)?
path(5, 7)?
path(1, 7)?
path(0, 7)?
call stack

path(7, 7)?

BFS DFS

Ideas/Issues

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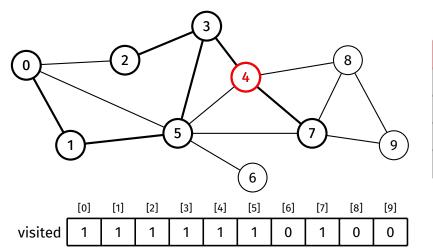
BFS Example

DFS

DFS Exampl

Path-Checking Example

Return true



patii(+, 7).
path(3, 7)?
path(5, 7)?
path(1, 7)?
path(0, 7)?
call stack

nath(4 7)?

BFS DFS

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lueas/issue

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BFS

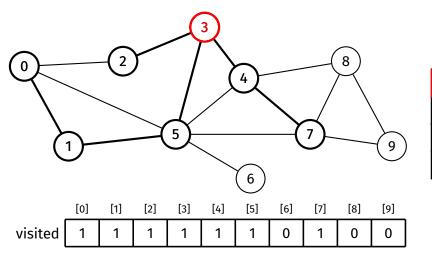
BES EXAMI

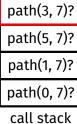
DES Exa

Path-Checking

Path-Checkir Example

Return true





BFS DFS

Ideas/Issues

Appendix BES

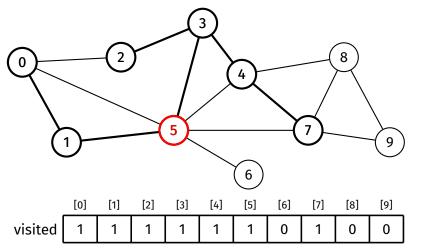
RFS Evamn

DFS

DFS Example Dath-Chocki

Path-Checking Example

Return true





BFS DFS

Ideas/Issues

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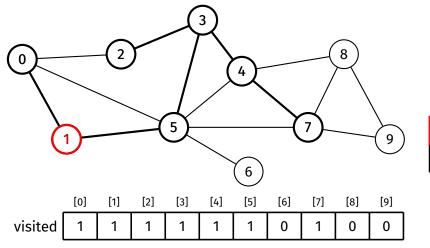
DEC Evamo

DFS

DFS Examp

Path-Checking Example

Return true



BFS DFS

Ideas/Issues

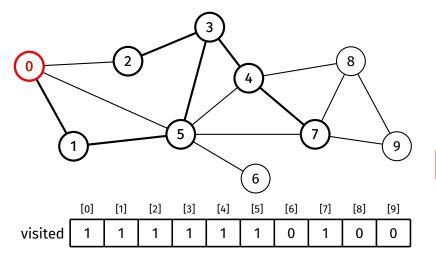
Appendix BFS

BFS Examp

DFS

Path-Checking Example

Return true



path(0, 7)?

call stack

Path-Checking with Recursive DFS

Example

Graph Traversal

BFS DFS

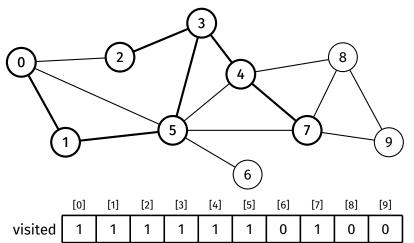
Ideas/Issues

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BFS Example

Path-Checking Example

Answer: Yes



call stack