

The Fourth Week Report

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1 Questions Remained

1.1 What is Forward and Back propagation?

In short, forward propagation is a way we used to count the value of compound functions. And back propagation is used to count the derivative of compound functions. We needn't complicate them.

1.2 How can we express the derivative of $\sigma(z)$?

By taking the derivative of $\sigma(z)$, we can easily get the result: $\sigma'(z) = \sigma(z)(1 - \sigma)$. Further, we can gain the consequence:

$$dz = \frac{\partial L}{\partial z} = \frac{\partial L}{\partial a} \cdot \frac{\partial a}{\partial z} \quad (1)$$

$$= \left(-\frac{y}{a} + \frac{1-y}{1-a}\right) \cdot a(1-a) \quad (2)$$

$$= a - y \quad (3)$$

$$dw = \frac{\partial L(w, b)}{\partial w} = \frac{\partial L}{\partial z} \cdot \frac{\partial z}{\partial w} \quad (4)$$

$$= dz \cdot x \quad (5)$$

$$= x(a - y) \quad (6)$$

$$db = \frac{\partial L}{\partial b} = \frac{\partial L}{\partial z} \cdot \frac{\partial z}{\partial b} \quad (7)$$

$$= 1 \cdot dz \quad (8)$$

$$= a - y \quad (9)$$

1.3 Some uses of numpy. ¹

1. Creat a vector:

```
1 x = np.array([...])
```

2. Call some frequently-used functions

```
1 np.exp(x)
2 np.log(x)
```

3. Get the shape of matrices

```
1 x.shape[0] # the number of rows
2 x.shape[1] # the number of column
```

4. Change the dimension

```
1 x.reshape((row,col))
```

¹The source of package "pythonhighlight":<https://github.com/chenfeng123456/python-latex-highlighting>

5. Count the length of each row

```
1 x_norm = np.linalg.norm(x, axis=1, keepdims = True)
```

6. Matrix-matrix or matrix-vector multiplication

```
1 # matrix multiplication:  
2 # x1.shape = (a, m), x2.shape = (m, b)  
3 np.dot(x1,x2)  
4 # multiply the elements in corresponding locations  
5 # x1.shape = (a, m), x2.shape = (a, m)  
6 np.multiply(x1, x2)
```

7. Gain random numbers

- Get one number

```
1 n = numpy.random.random()
```

- Get a matrix

```
1 n = numpy.random.random(size=(3, 2))
```

- Generate random numbers between 0 and 1

```
1 np.random.rand(2,3) # (2,3) show the dimension
```

- Generate the same random numbers

```
1  '''  
2  Set the same seed every time,  
3  and we can get the same random numbers  
4  '''  
5  numpy.random.seed(num)  
6  numpy.random.rand(the_length_of_array)
```

1.4 What do high bias and high variance mean?

High bias means that your model can't fit your train set well and high variance means your model overfit the train set so that it can't fit other data well.

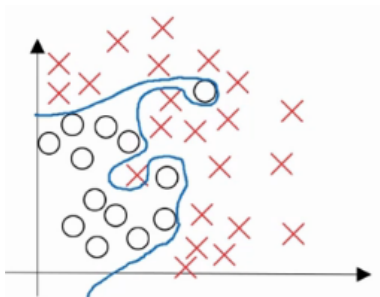


Figure 1: Overfitting

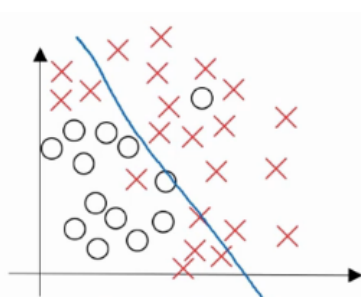


Figure 2: Underfitting

1.5 How does regularization prevent overfitting?

Regularization is able to reduce overfitting by adding the regularization term, $\frac{\lambda}{2m}||w||_2^2$. So the derivative $\frac{\partial L}{\partial W}$ turns into: $dW^{[l]} = (form_backprop) + \frac{\lambda}{m}W^{[l]}$. Then we can get the update of grads as follows:

$$W^{[l]} := W^{[l]} - \alpha[(form_backprop) + \frac{\lambda}{m}W^{[l]}] \quad (10)$$

$$= W^{[l]} - \alpha\frac{\lambda}{m}W^{[l]} - \alpha(form_backprop) \quad (11)$$

$$= (1 - \frac{\alpha\lambda}{m})W^{[l]} - \alpha(form_backprop) \quad (12)$$

If λ is big enough, the weight matrix W can be very small, and so does the Z . As the [Figure 3](#) shows, when Z is relatively small, $\tanh(Z)$ could be almost linear. We have known that when $g(x)$ is linear, no matter how deep the neural network is, what it counts is always a linear function which can't fit very complicate data.

Of course we need't keep Z so small all the time, but we can find a reasonable range that makes our model "just right".

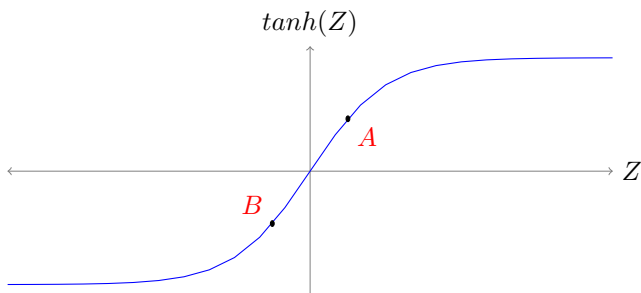


Figure 3: $\tanh(Z)$ function

2 Works

This week, I also do the homework of course1. It isn't an easy process. I had to add tons of codes to ensure that the works can run correctly in my computer. And there are still some codes remained to be understood, which I think I will do again.

It is worth mentioning that I finished all the codes ultimately but couldn't get the right output. Fortunately, I finally found the answer on the Internet(see [Code Listing 1](#)).

Code Listing 1: The solution of vanishing gradients

```

1 #解决了。应该是参数问题。
2 import numpy as np
3 def initialize_parameters_deep(layer_dims):
4     """
    """
  
```

```

5  Arguments:
6  layer_dims — python array (list) containing the dimensions of each layer in our
              network
7
8  Returns:
9  parameters — python dictionary containing your parameters "W1", "b1", ..., "WL",
              "bL":
10                 Wl — weight matrix of shape (layer_dims[l], layer_dims[l-1])
11                 bl — bias vector of shape (layer_dims[l], 1)
12
13  """
14
15  np.random.seed(1)
16  parameters = {}
17  L = len(layer_dims) # number of layers in the network
18
19  for l in range(1, L):
20      parameters['W' + str(l)] = np.random.randn(layer_dims[l], layer_dims[l - 1]) /
21          np.sqrt(
22              layer_dims[l - 1]) # *0.01
23      parameters['b' + str(l)] = np.zeros((layer_dims[l], 1))
24
25      assert (parameters['W' + str(l)].shape == (layer_dims[l], layer_dims[l - 1]))
26      assert (parameters['b' + str(l)].shape == (layer_dims[l], 1))
27
28  return parameters

```

3 Learning summary

Because I have watched too fast before (I finished the first and the second course within two or three weeks) and lacked practice, I didn't understand much about the videos. So I decided to watch them again and do more exercise. Now a week has passed, and I have figure out many problems which have been confusing me for a long time. The next week I'll stick to the plan and finish the second coure's homework.