

### Problem 0: Homework checklist

- ✓I didn't talk with any one about this homework.
- ✓Source-code are included at the end of this document.

### Problem 1: Operations

- $$\begin{bmatrix} 1 & 1 & 2 \\ 3 & 5 & 8 \\ 13 & 21 & 34 \end{bmatrix} \begin{bmatrix} 1 & -2 & 3 \\ -4 & 5 & -6 \\ 7 & -8 & 9 \end{bmatrix} = \begin{bmatrix} 11 & -13 & 15 \\ 39 & -45 & 51 \\ 167 & -193 & 219 \end{bmatrix}$$
- $\mathbf{x} = \text{ones}(1000, 1)$   $\mathbf{y} = [1:1000]'$   $\mathbf{x}^T \mathbf{y} = 500500.0$

### Problem 4: Image downsampling

- $\mathbf{y} = \mathbf{A}\mathbf{x}$  so  $\mathbf{A}$  must be a  $4 \times 16$  matrix.  $y_i = \sum_{j=1}^{16} A_{ij}x_j$   
 $y_1 = (x_1 + x_2 + x_5 + x_6)/4$   
 $y_2 = (x_3 + x_4 + x_7 + x_8)/4$   
 $y_3 = (x_9 + x_{10} + x_{13} + x_{14})/4$   
 $y_4 = (x_{11} + x_{12} + x_{15} + x_{16})/4.$

Then

$$\begin{aligned} \mathbf{A}_{11} &= \mathbf{A}_{12} = \mathbf{A}_{15} = \mathbf{A}_{16} = 0.25 \\ \mathbf{A}_{23} &= \mathbf{A}_{24} = \mathbf{A}_{27} = \mathbf{A}_{28} = 0.25 \\ \mathbf{A}_{39} &= \mathbf{A}_{3,10} = \mathbf{A}_{3,13} = \mathbf{A}_{3,14} = 0.25 \\ \mathbf{A}_{4,11} &= \mathbf{A}_{4,12} = \mathbf{A}_{4,15} = \mathbf{A}_{4,16} = 0.25 \end{aligned}$$

$$\mathbf{A} = \begin{bmatrix} 0.25 & 0.25 & 0 & 0 & 0.25 & 0.25 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0.25 & 0.25 & 0 & 0 & 0.25 & 0.25 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0.25 & 0.25 & 0 & 0 & 0.25 & 0.25 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0.25 & 0.25 & 0 & 0 & 0.25 & 0.25 \end{bmatrix}$$

- The sum of diagonal elements of  $\mathbf{X}$  is 24.2686
- Color image: Grey image:
- Reshape command will reshape the input array into a  $m \times n$  matrix, and return the new matrix.

