Problem 4:

(a)

$$\mathbf{A} = \begin{bmatrix} 0 & 1 & 1 & 1 \\ 3 & 0 & 3 & -4 \\ 1 & 1 & 1 & 2 \\ 2 & 3 & 1 & 3 \end{bmatrix}$$
$$\mathbf{b} = \begin{bmatrix} 0 \\ 7 \\ 6 \\ 6 \end{bmatrix}$$

(i) Partial pivoting The output from my code is

$$\mathbf{x} = \begin{bmatrix} 4 \\ -3 \\ 1 \\ 2 \end{bmatrix}$$

(ii) Scaled pivoting The output from my code is

$$\mathbf{x} = \begin{bmatrix} 4 \\ -3 \\ 1 \\ 2 \end{bmatrix}$$

(b)

$$\mathbf{A} = \begin{bmatrix} 0.2115 & 2.296 & 2.715 & 3.215 \\ 0.4371 & 3.916 & 1.683 & 2.852 \\ 6.099 & 4.324 & 23.20 & 1.578 \\ 4.623 & 0.8926 & 15.32 & 5.305 \end{bmatrix}$$
$$\mathbf{b} = \begin{bmatrix} 8.438 \\ 8.8888 \\ 35.20 \\ 26.14 \end{bmatrix}$$

(i) Partial pivoting The output from my code is

$$\mathbf{x} = \begin{bmatrix} 0.999081 \\ 0.999913 \\ 1.00021 \\ 1.0001 \end{bmatrix}$$

(ii) Scaled pivoting The output from my code is

$$\mathbf{x} = \begin{bmatrix} 0.999081 \\ 0.999913 \\ 1.00021 \\ 1.0001 \end{bmatrix}$$

Problem 5:

$$\mathbf{A} = \begin{bmatrix} -9 & 11 & -21 & 63 & -252 \\ 70 & -69 & 141 & -421 & 1684 \\ -575 & 575 & -1149 & 3451 & -13801 \\ 3891 & -3891 & 7782 & -23345 & 93365 \\ 1024 & -1024 & 2048 & -6144 & 24572 \end{bmatrix}$$

$$\mathbf{b} = \begin{bmatrix} -356 \\ 2385 \\ -19551 \\ 132274 \\ 34812 \end{bmatrix}$$

The output of scaled pivoting result is

$$\mathbf{x} = \begin{bmatrix} 1 \\ -0.864667 \\ 0.0848896 \\ 5.27044 \\ 2.64978 \end{bmatrix}$$

Problem 6:

We can construct 12 equation if there are no external forces, 2 for each node:

$$\sum F_{1x} = F_1 \cos \alpha + F_3 \cos \gamma + F_H = 0$$

$$\sum F_{1y} = F_v + F_3 \cos \gamma + F_1 \sin \alpha = 0$$

$$\sum F_{2x} = F_8 \cos \beta + F_9 \cos \alpha - F_2 \cos \beta - F_1 \cos \alpha = 0$$

$$\sum F_{2y} = F_5 + F_2 \sin \beta + F_8 \sin \beta - F_1 \sin \alpha - F_9 \sin \alpha = 0$$

$$\sum F_{3x} = F_4 \cos \beta + F_2 \cos \beta - F_3 \cos \gamma = 0$$

$$\sum F_{3y} = F_4 \sin \beta - F_2 \sin \beta - F_3 \sin \gamma = 0$$

$$\sum F_{4x} = F_6 \cos \beta - F_4 \cos \beta = 0$$

$$\sum F_{4y} = -F_4 \sin \beta - F_6 \sin \beta - F_5 = 0$$

$$\sum F_{5x} = F_7 \cos \gamma - F_6 \cos \beta - F_8 \cos \beta = 0$$

$$\sum F_{5y} = F_6 \sin \beta - F_8 \sin \beta - F_7 \sin \gamma = 0$$

$$\sum F_{6x} = -F_7 \cos \gamma - F_9 \cos \alpha = 0$$

$$\sum F_{6y} = F_R + F_7 \sin \gamma + F_9 \sin \alpha = 0$$

Then the linear equation $A\mathbf{x} = \mathbf{b}$ becomes:

We know:

$$\sin \alpha = 0.447$$

$$\cos \alpha = 0.894$$

$$\sin \beta = 0.316$$

$$\cos \beta = 0.949$$

$$\sin \gamma = 0.707$$

$$\cos \gamma = 0.707$$

Then matrix A becomes:

For different configurations:

The results are shown:

$$F_a = \begin{bmatrix} -784.006 \\ -51.402 \\ -991.374 \\ -687.167 \\ -991.374 \\ -687.167 \\ -991.374 \\ -565.711 \\ -687.167 \\ -991.374 \\ -51.402 \\ -784.006 \\ 1051.35 \\ 1401.8 \end{bmatrix} \quad F_b = \begin{bmatrix} -2162.2 \\ -334.561 \\ -611.893 \\ -121.296 \\ -1923.341 \\ -923.341 \\ -121.296 \\ -1672.99 \\ -1125.07 \\ -1323.05 \\ 1051.35 \\ 1401.8 \end{bmatrix} \quad F_c = \begin{bmatrix} -189.822 \\ -610.785 \\ -684.362 \\ -273.791 \\ -273.791 \\ -273.791 \\ -149.06 \\ -1301.13 \\ 179.729 \\ -1028.97 \\ 1379.85 \\ 1399.11 \\ 1754.95 \\ 1839.8 \end{bmatrix} \quad F_d = \begin{bmatrix} 727.085 \\ -684.362 \\ 211.065 \\ -212.136 \\ 300.561 \\ -212.136 \\ 300.561 \\ -739.007 \\ -495.589 \\ -896.666 \\ 391.926 \\ -525.572 \\ -474.23 \\ -799.237 \end{bmatrix}$$

For the direction of the forces: negative values indicate forces point outward. Positive direction of F_V , F_H , F_R are as shown in the figure.