## COM 530500 Network Science Homework #1

Due: Thursday, October 14, 2021 No late homework will be accepted.

班級: 通訊所

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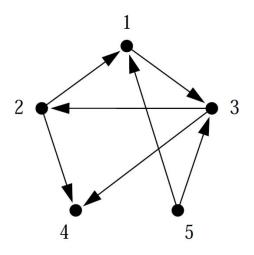
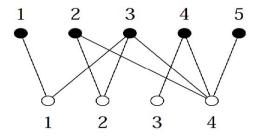


Figure 1: Network (a).

## Problem 1.(10%)

- (a) (5%) Write down the adjacency matrix of network (a).
- (b) (5%) Write down the cocitation matrix of network (a).

Solution: Type your answer here.



 $\Diamond$ 

Figure 2: Network (b).

## Problem 2.(10%)

(a) (5%) Write down the incidence matrix of network (b).

(b) (5%) Write down the projection matrix for the projection of network (b) onto its black vertices.

Solution: Type your answer here.

 $\Diamond$ 

**Problem 3.(10%)** Consider a bipartite network, with its two types of vertices. Suppose there are  $n_1$  vertices of type 1 and  $n_2$  vertices of type 2. Show that the mean degrees  $c_1$  and  $c_2$  of the two types are related by  $c_2 = \frac{n_1}{n_2}c_1$ .

Solution: Type your answer here.

 $\Diamond$ 

Problem 4.(20%) Given

$$A = \begin{pmatrix} 0 & 2 & -1 \\ 2 & 3 & -2 \\ -1 & -2 & 0 \end{pmatrix},$$

- (a) (10%) Find all eigenvalues of matrix A.
- (b) (10%) Find an orthogonal matrix U that diagonalizes A.

Solution: Type your answer here.

 $\Diamond$ 

**Problem 5.(15%)** Read the tutorial from Ping-En Lu's GitHub repository to install Python3 and python-igraph (if you need).

Paste your screenshots of "Hello, World!" of both Python 3 (5%) and python-igraph (5%), and write a brief report (5%). (For example, you can write down some problems you encountered, and how you solved them.)

Solution: Type your answer here.

**Problem 6.(35%)** Please download the **tvshow** dataset from Ping-En Lu's GitHub repository, and find the following information from this dataset.

- Number of nodes. (5%)
- Number of edges. (5%)
- Mean degree. (5%)
- Maximum degree. (5%)
- Diameter. (5%)

You need to upload your **python source code** to iLMS, and **write a brief report** (10%) including screenshots, README file, and descriptions of your code below the solution area. There will be no points for this problem if you do not upload your python source code to iLMS.

Solution: Type your answer here.