Pattern Recognition, Homework 1

**Deadline: March 31, 23:55**

**Part. 1, Coding (70%)**:

In this coding assignment, you are required to implement linear regression by using only [NumPy](https://numpy.org/), then train your model using **gradient descent** on the provided dataset, and evaluate the performance on testing data. Find the sample code and data on the GitHub page

<https://github.com/NCTU-VRDL/CS_ILE5065/tree/main/HW1>

**Please note that only NumPy can be used to implement your model, you will****get 0 pointsby calling sklearn.linear\_model.LinearRegression. Moreover, please train your regression model using gradient descent, not the closed-form solution.**

1. (15%) Implement the linear regression model and train it by using **gradient descent** with [**mean absolute error**](https://en.wikipedia.org/wiki/Mean_absolute_error) and [**mean square error**](https://en.wikipedia.org/wiki/Mean_squared_error) as the objective function, respectively
2. (15%) Plot the [learning curve](https://miro.medium.com/max/1718/1*69r3IZNMnWPngwzbeSTz_Q.png) of the training with both losses in the same figure, you should find that loss decreases and converges after a few iterations (x-axis=iteration, y-axis=loss, [Matplotlib](https://matplotlib.org/) or other plot tools is available to use)
3. (15%) What’re the mean square error and mean absolute errorbetween your predictions and the ground truths on the testing data (prediction=model(x\_test), ground truth=y\_test)
4. (10%) What’re the [weights (β1) and intercepts (β0)](https://miro.medium.com/max/2872/1*_TqRJ9SmwFzRigJhMiN2uw.png) of your linear model trained from both losses?
5. (10%) Please explain the difference between gradient descent, mini-batch gradient descent, and stochastic gradient descent?
6. (5%) All your codes should follow the [PEP8 coding style](https://www.python.org/dev/peps/pep-0008/) and with clear comments

**Part. 2, Questions (30%):**

1. (10%) Suppose that we have three colored boxes R (red), B (blue), and G (green). Box R contains 3 apples, 4 oranges, and 3 guavas, box B contains 2 apples, 0 orange, and 2 guavas, and box G contains 12 apples, 4 oranges, and 4 guavas. If a box is chosen at random with probabilities p(R)=0.2, p(B)=0.4, p(G)=0.4, and a piece of fruit is removed from the box (with equal probability of selecting any of the items in the box), then what is the probability of selecting guava? If we observe that the selected fruit is in fact an apple, what is the probability that it came from the blue box?
2. (10%) Using the definition show that satisfies .
3. (10%) Consider two variables and with joint distribution . Prove the following result

Here denotes the expectation of under the conditional , with a similar notation for the conditional variance.

Hint: Please check the definitions of the expectation operator, the sum rule, and the product rule.