Backhaul For Low-Altitude UAVs in Urban Environments

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Abstract—**Unmanned Aerial Vehicles (UAVs) acting as access points in cellular networks require wireless backhauls to the core network. In this paper we employ stochastic geometry to carry out an analysis of the UAV backhaul performance that can be achieved with a network of dedicated ground stations. We provide analytical expressions for the probability of successfully establishing a backhaul and the expected data rate over the backhaul link, given either an LTE or a millimeter-wave backhaul. We demonstrate that increasing the density of the ground station network gives diminishing returns on the performance of the UAV backhaul, and that for an LTE backhaul the ground stations can benefit from being co-located with an existing base station network.**

Keywords—*UAV networks, wireless backhaul, Poisson point process, stochastic geometry*

I. INTRODUCTION

Access points mounted on unmanned aerial vehicles (UAVs) are being proposed as a potential solution to data demand and congestion issues that are expected to arise in next-generation wireless networks [1]. The benefit of these UAV networks compared to existing static infrastructure is the flexibility of their deployment, which allows them to configure themselves around user hotspots or gaps in coverage. These UAV networks additionally differ from existing infrastructure in how they connect into the core network; whereas fixed infrastructure can make use of wired backhaul links, often fiber optics, the UAVs must use dedicated wireless links for a backhaul. These links may be established using millimeter-waves [2], free-space optical channels [3] or using sub-6GHz technologies such as LTE. Emerging research in the wireless community suggests that existing LTE base stations (BSs) that are intended for ground user service are capable of also providing backhaul for UAV networks [4]. However, we expect that as UAV networks become more widespread and play a greater role in serving the end user network, operators will opt to deploy dedicated backhaul infrastructure, referred to as ground stations (GSs), to support these networks. UAVs have very different performance requirements and behave very differently to the typical user equipment; the question of how to deploy these GS networks and whether they can take advantage of existing terrestrial infrastructure is an important one.

One of the first works to consider low-altitude UAVs operating alongside terrestrial BS networks is [5]. The authors simulate a network outage scenario where UAVs substitute offline BSs, with the UAVs wirelessly backhauling into adjacent, functioning BSs. The authors assume a hexagonal grid of BSs and demonstrate achieveable data rates in the downlink as a function of UAV distance to their backhaul. The works in [6] and [7] approach the problem of UAV position optimisation by considering a single end user, UAV and backhaul in isolation, with the UAV adjusting its position to optimise its end user and backhaul links. Stochastic geometry has also started to see use as a tool for modelling and analysing UAV-BS wireless links. In our previous work in [8] (which extends our work in [9]) we investigated the performance of a UAV network when the UAVs opportunistically backhaul through LTE BSs designed to serve end users on the ground. We considered both the backhaul link as well as the link between the UAV and the end user, and we demonstrated that, while the two different links have optimal performance at differing UAV heights, it is possible to maximise the performance of both links by allowing UAVs to adjust their individual heights. A similar analysis of the UAV-BS link was carried out in [10], where the authors consider the performance of UAV-BS links in different environments, given down-tilted BS antennas and omnidirectional UAV antennas. The authors conclude that the UAV-BS link is vulnerable to interference due to the high LOS probability, and suggest that both UAVs and BSs reduce their heights above ground to improve performance.

While a limited number of results have been published on the interaction between UAV networks and existing terrestrial BS networks, to date there is a lack of work on analysing the performance of a dedicated GS network that is deployed for providing backhaul to UAV networks. Our contribution in this paper is to use stochastic geometry to analyse the backhaul performance of GSs serving a low-altitude UAV network in an urban environment. We consider the use of both 2GHz LTE and millimeter-wave technology to support the backhaul link, with the GSs using frequency bands that are orthogonal to the underlying BS networks. Our analysis takes into account directional antenna alignment in 3D space between a typical UAV in the network and its associated backhaul GS as well as other interfering GSs, and it captures the effect of generalised multipath fading as well as line-of-sight (LOS) blocking due to buildings in the environment. We explore the effect of GS density as well as their height above ground on the probability of a typical UAV being able to establish a backhaul, given different operating heights of the UAV. We initially assume that the GSs are deployed independently of existing terrestrial infrastructure; in the numerical results section we show that, when using an LTE link for the backhaul, the GS infrastructure performs best when deployed at the same altitude as existing LTE infrastructure, highlighting how the LTE GS network may benefit from being co-located with existing LTE BSs. The analysis in this work allows us to address basic network
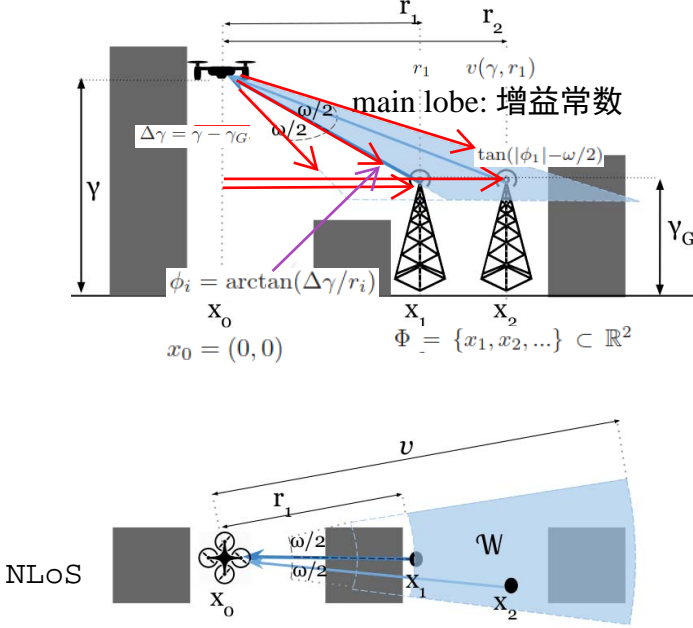
Fig. 1. Side and top view showing a UAV in an urban environment at a height γ, positioned above x_0 with antenna beamwidth ω. The UAV selects the nearest GS at x_1 for its backhaul and centers its antenna main lobe on the GS location; the blue area $\mathcal{W}$ illuminated by the main lobe denotes the region where interferers may be found. The GS at x_2 falls inside this area and produces interference.

design questions that would be relevant to a network operator interested in providing backhaul infrastructure for a network of UAVs.

II. SYSTEM MODEL

In this section we set up a system model of a network of GSs providing backhaul to UAVs. We consider two technologies for the backhaul channel, LTE in the 2GHz band and millimeter-wave. We model the network of GSs as a Poisson point process (PPP) $\Phi = \{x_1, x_2, ...\} \subset \mathbb{R}^2$ of intensity λ where elements $x_i \in \mathbb{R}^2$ represent the projections of the GS locations onto the $\mathbb{R}^2$ plane. The GSs have a height γ_G above ground. We consider a single reference UAV, positioned above the origin $x_0 = (0,0)$ at a height γ. Let $r_i = ||x_i||$ denote the horizontal distance between the GS i and the reference UAV, and let $\phi_i = \arctan(\Delta\gamma/r_i)$ denote the vertical angle, where $\Delta\gamma = \gamma - \gamma_G$.

The UAV is equipped with a directional antenna for communicating with its associated backhaul GS. The antenna has a horizontal and vertical beamwidth ω and a rectangular radiation pattern; using the approximations (2-26) and (2-49) in [11] and assuming perfect radiation efficiency the antenna gain can be expressed as $\eta(\omega) = 16\pi/(\omega^2)$ inside of the main lobe and $\eta(\omega) = 0$ outside. The UAV selects the nearest GS as its serving GS; we denote this GS as x_1 and its distance to the UAV as r_1. The UAV orients itself to align its backhaul antenna towards x_1; the antenna radiation pattern illuminates an area behind x_1 which we denote as $\mathcal{W} \subset \mathbb{R}^2$. This area takes the shape of a ring sector of arc angle equal to ω and major and minor radii $v(\gamma, r_1)$ and r_1, respectively, where

$$v(\gamma, r_1) = \begin{cases} \frac{|\Delta\gamma|}{\tan(|\phi_1|-\omega/2)} & \text{if } \omega/2 < |\phi_1| < \pi/2 - \omega/2 \\ \frac{|\Delta\gamma|}{\tan(\pi/2-\omega)} & \text{if } |\phi_1| > \pi/2 - \omega/2 \\ \infty & \text{otherwise} \end{cases}$$

(1)

with $|.|$ denoting absolute value. For the case where $\omega \geq \pi/2$, the major radius $v(\gamma, r_1)$ will always be infinite. We denote the set of GSs that fall inside the area $\mathcal{W}$ as $\Phi_{\mathcal{W}} = \{x \in \Phi : x \in \mathcal{W}\}$. The GSs in the set $\Phi_{\mathcal{W}}$ are capable of causing interference to the reference UAV, as their signals may be received by the UAV with non-zero gain. Note that $\Phi_{\mathcal{W}}$ is a PPP with the same intensity λ.

The wireless channels between the reference UAV and the GSs will be affected by buildings, which form obstacles and break LOS links. We adopt the model in [12], which defines an urban environment as a collection of buildings arranged in a square grid. There are β buildings per square kilometer, the fraction of area occupied by buildings to the total area is δ, and each building has a height which is a Rayleigh-distributed random variable with scale parameter κ. The probability of the reference UAV having LOS to the GS i is given in [12] as

$$\mathbb{P}_{LOS}(r_i) = \prod_{n=0}^{\max(0, d_i-1)} \left(1 - \exp\left(-\frac{\left(\max(\gamma, \gamma_G) - \frac{(n+1/2)|\Delta\gamma|}{d_i}\right)^2}{2\kappa^2} \right) \right)$$

(2)

where $d_i = \lfloor r_i\sqrt{\beta\delta} \rfloor$. We can express the SINR at the reference UAV as

$$\text{SINR} = \frac{p H_{t_1} \eta(\omega) \mu c (r_1^2 + \Delta\gamma^2)^{-\alpha_{t_1}/2}}{I_L + I_N + \sigma^2}$$

(3)

where p is GS transmit power, H_{t_1} is the random multipath fading component, α_{t_1} is the pathloss exponent, $t_1 \in \{L, N\}$ is an indicator variable which denotes whether the UAV has LOS or NLOS to its serving GS, μ is the serving GS antenna gain defined in the next subsections, c is the near-field pathloss, σ^2 is the noise power, and I_L and I_N are the aggregate LOS and NLOS interference, respectively.

The backhaul data rate, in Mbits/sec, can be calculated from the SINR using the Shannon capacity bound

$$\mathcal{R} = b\log_2(1 + \text{SINR})$$

(4)

where b denotes the bandwidth of the backhaul channel. We define an SINR threshold θ for the UAV backhaul link; if SINR $< \theta$ this represents the UAV failing to establish a backhaul of the required channel quality and therefore being in an outage state.

两种backhaul模式

A. LTE Backhaul

For the LTE backhaul case we assume that the GSs are equipped with tri-sector antennas similar to those already in use in terrestrial BSs, as this allows them to serve UAVs in any horizontal direction. For tractability we model the horizontal antenna gain μ_h of these antennas as having a constant value. The antennas are tilted up towards the sky, to model the behaviour of the antennas in the vertical plane we adopt the 3GPP model [13], such that

$$\mu_v(\phi_i) = 10^{-\min\left(12\left(\frac{\phi_i - \phi_T}{10}\right)^2, 20\right)/10}, \tag{5}$$

$$\mu_l(\phi_i) = \max\left(\mu_h \mu_v(\phi_i), 10^{-2.5}\right), \tag{6}$$
$$\phi_i = \arctan(\Delta\gamma/r_i)$$

where $\mu_v(\phi_i)$ is the vertical antenna gain, ϕ_T is the vertical uptilt angle of the GS antenna (in degrees) and $\mu_l(\phi_i)$ is the total antenna gain.

B. Millimeter-wave Backhaul

For the millimeter-wave backhaul we assume each GS is equipped with an antenna array that uses beamforming to direct a directional beam towards the UAV to which it provides a backhaul link. We adopt a similar approach to modelling the GS antenna array as in [14] and [15]. The GS antenna is modelled as having a single directional beam with a beamwidth of ω_G and a gain of μ_m inside the main lobe, and a gain of 0 outside. The reference UAV will always experience an antenna gain of μ_m from its serving GS. The beam patterns of the remaining GSs will appear to be pointed in random directions with respect to the reference UAV; as a result each interfering GS will have non-zero antenna gain to the reference UAV with a certain probability ζ.

III. ANALYTICAL RESULTS

In this section we derive an analytical expression for the probability that the reference UAV will receive a signal from the GS network with an SINR above θ, thereby establishing a backhaul. We refer to this as the backhaul probability. To derive an expression for the backhaul probability we need an expression for the conditional backhaul probability given the serving GS of the reference UAV has either LOS or NLOS to the reference UAV, and given it is located at a horizontal distance r_1 from the UAV. We then decondition this conditional backhaul probability with respect to the LOS probability of the serving GS as well as its horizontal distance. The LOS probability for a given horizontal distance r_1 is given in Eq. (2). Given a PPP distribution of GSs the serving GS horizontal distance random variable R_1 is known to be Rayleigh-distributed with scale parameter $1/\sqrt{2\pi\lambda}$.

A. Aggregate LOS & NLOS Interference

LTE backhaul The interferers will belong to the set $\Phi_{\mathcal{W}}$. We partition this set into two sets which contain the LOS and NLOS interfering GSs, denoted as $\Phi_{\mathcal{W}L} \subset \Phi_{\mathcal{W}}$ and $\Phi_{\mathcal{W}N} \subset \Phi_{\mathcal{W}}$, respectively. These two sets are inhomogeneous PPPs with intensity functions $\lambda_L(x) = \mathbb{P}_{LOS}(||x||)\lambda$ and $\lambda_N(x) = (1 - \mathbb{P}_{LOS}(||x||))\lambda$. Note that we drop the

密度随距离变化 **LoS和NLoS的GS集合**

index i as the GS coordinates have the same distribution irrespective of their index values. For an LTE backhaul the aggregate LOS and NLOS interference is expressed as $I_L = \sum_{x \in \Phi_{\mathcal{W}L}} pH_L\eta(\omega)\mu_l(\phi)c(||x||^2 + \Delta\gamma^2)^{-\alpha_L/2}$ and $I_N = \sum_{x \in \Phi_{\mathcal{W}N}} pH_N\eta(\omega)\mu_l(\phi)c(||x||^2 + \Delta\gamma^2)^{-\alpha_N/2}$, recalling that $\phi = \arctan(\Delta\gamma/||x||)$.

millimeter-wave backhaul As defined in the system model, the millimeter-wave interfering GSs will only create interference at the reference UAV if their directional beams happen to align with the UAV location, which occurs with probability ζ. As a result of this $\Phi_{\mathcal{W}L}$ and $\Phi_{\mathcal{W}N}$ have intensity functions $\lambda_L(x) = \mathbb{P}_{LOS}(||x||)\zeta\lambda$ and $\lambda_N(x) = (1 - \mathbb{P}_{LOS}(||x||))\zeta\lambda$. The aggregate LOS and NLOS interference is then expressed as $I_L = \sum_{x \in \Phi_{\mathcal{W}L}} pH_L\eta(\omega)\mu_m c(||x||^2 + \Delta\gamma^2)^{-\alpha_L/2}$ and $I_N = \sum_{x \in \Phi_{\mathcal{W}N}} pH_N\eta(\omega)\mu_m c(||x||^2 + \Delta\gamma^2)^{-\alpha_N/2}$.

B. Conditional Backhaul Probability

The expression for the backhaul probability, given serving GS distance r_1 and an LOS channel to the serving GS, follows the derivation provided by us in [9] as

条件:水平距离r1,LoS

$$\mathbb{P}(\text{SINR} \geq \theta | R_1 = r_1, t_1 = \text{L}) =$$ **关于ri的函数**

$$\sum_{n=0}^{m_L-1} \frac{s_L^n}{n!}(-1)^n \cdot \sum_{i_L+i_N+i_\sigma=n} \frac{n!}{i_L!i_N!i_\sigma!}$$
$$\cdot (-(p\eta(\omega)c)^{-1}\sigma^2)^{i_\sigma} \exp(-(p\eta(\omega)c)^{-1}s_L\sigma^2)$$
$$\cdot \frac{d^{i_L}\mathcal{L}_{I_L}((p\eta(\omega)c)^{-1}s_L)}{ds_L^{i_L}} \frac{d^{i_N}\mathcal{L}_{I_N}((p\eta(\omega)c)^{-1}s_L)}{ds_L^{i_N}}, \tag{7}$$

where $s_L = m_L\theta\mu^{-1}(r_1^2 + \Delta\gamma^2)^{\alpha_L/2}$, m_L is the Nakagami-m fading term for a LOS channel, $\mathcal{L}_{I_L}$ and $\mathcal{L}_{I_N}$ are the Laplace transforms of the aggregate LOS and NLOS interference, respectively, and the second sum is over all the combinations of non-negative integers i_L, i_N and i_σ that add up to n. μ takes the value of either $\mu_l(\phi_1)$ or μ_m depending on whether we are considering LTE or millimeter-wave backhaul. The conditional backhaul probability given an NLOS serving GS $\mathbb{P}(\text{SINR} \geq \theta | R_1 = r_1, t_1 = \text{N})$ is calculated as in Eq. (7) with m_N, α_N and s_N replacing m_L, α_L and s_L.

C. Laplace Transform of Aggregate Interference

LTE backhaul The Laplace transform of the aggregate LOS interference $\mathcal{L}_{I_L}((p\eta(\omega)c)^{-1}s_L)$ given an LOS serving GS is expressed as

$$\mathbb{E}\left[\exp\left(-(p\eta(\omega)c)^{-1}s_L I_L\right)\right]$$
$$= \mathbb{E}_{\Phi_{\mathcal{W}L}}\left[\prod_{x \in \Phi_{\mathcal{W}L}} \mathbb{E}_{H_L}\left[\exp\left(-H_L g(||x||, s_L, \alpha_L)\right)\right]\right]$$

$$\overset{(a)}{=} \mathbb{E}_{\Phi_{\mathcal{W}L}}\left[\prod_{x\in\Phi_{\mathcal{W}L}}\left(\frac{m_L}{\boxed{g(||x||,s_L,\alpha_L)}+m_L}\right)^{m_L}\right]$$

关于x的函数

$$\overset{(b)}{=} \exp\left(-\underset{\mathcal{W}}{\int}\left(1-\left(\frac{m_L}{\boxed{g(||x||,s_L,\alpha_L)}+m_L}\right)^{m_L}\right)\boxed{\lambda_L(x)}\mathrm{d}x\right)$$

$\mathcal{W}$ 区域积分

$$\overset{(c)}{=} \exp\left(-\lambda\omega\int_{r_1}^{v(\gamma,r_1)}\left(1-\left(\frac{m_L}{\boxed{g(r,s_L,\alpha_L)}+m_L}\right)^{m_L}\right)\boxed{\mathbb{P}_{LOS}(r)}r\mathrm{d}r\right)$$

(8)

where

$$\phi_i = \arctan(\Delta\gamma/r_i)$$

$$g(||x||,s_L,\alpha_L) = s_L\mu_l(\phi)(\boxed{||x||^2}+\Delta\gamma^2)^{-\alpha_L/2},$$

(a) comes from the power-series representation of the Nakagami-m distribution, (b) comes from the probability generating functional of the PPP [16], (c) comes from switching to polar coordinates where $r = ||x||$, $\boxed{\lambda_L(x) = \mathbb{P}_{LOS}(||x||)\lambda}$, and the integral is over $\mathcal{W}$ which has major and minor radius of $v(\gamma,r_1)$ and r_1, and an angular arc of ω. Note that the Laplace transform for the NLOS interferers $\mathcal{L}_{I_N}((p\eta(\omega)c)^{-1}s_L)$ is solved by simply substituting $\lambda_L(x)$ with $\lambda_N(x)$, m_L with m_N and $g(r,s_L,\alpha_L)$ with $g(r,s_L,\alpha_N)$ in Eq. (8) and solving as shown. The above integration is for the case when the serving GS is LOS; if the serving GS is NLOS we substitute s_L with s_N as defined in the previous subsection.

millimeter-wave backhaul The Laplace transform of the LOS interferers for a millimeter-wave backhaul is derived as in Eq. (8), with the intensity λ being multiplied by ζ (as explained in the previous subsection), and with $\mu_l(\phi)$ being replaced with μ_m. Note that, unlike $\mu_l(\phi)$, μ_m is a constant value with respect to r; as a result of this it is possible to represent the integral in Eq. (8) in closed-form for the case of millimeter-wave backhaul. We begin by recognising that $\mathbb{P}_{LOS}(r)$ is a step function. We use this fact to separate the integral above into a sum of weighted integrals, resulting in the following expression

$$\omega\zeta\lambda\sum_{j=\lfloor r_1\sqrt{\beta\delta}\rfloor}^{\lfloor v(\gamma,r_1)\sqrt{\beta\delta}\rfloor}\mathbb{P}_{LOS}(l)\int_l^u\left(1-\left(\frac{m_L}{g(r,s_L,\alpha_L)+m_L}\right)^{m_L}\right)r\mathrm{d}r$$

(9)

where $l = \max(r_1, j/\sqrt{\beta\delta})$ and $u = \min(v(\gamma,r_1),(j+1)/\sqrt{\beta\delta})$. Using the derivations (11) in [9]

$$\int_l^u\left(1-\left(\frac{m_L}{g(r,s_L,\alpha_L)+m_L}\right)^{m_L}\right)r\mathrm{d}r = \frac{1}{2}\sum_{k=1}^{m_L}\binom{m_L}{k}(-1)^{k+1}$$

$$\cdot\left((u^2+\Delta\gamma^2)_2\mathrm{F}_1\left(k,\frac{2}{\alpha_L};1+\frac{2}{\alpha_L};-\frac{m_L(u^2+\Delta\gamma^2)^{\alpha_L/2}}{\mu_m s_L}\right)\right.$$

$$\left.-(l^2+\Delta\gamma^2)_2\mathrm{F}_1\left(k,\frac{2}{\alpha_L};1+\frac{2}{\alpha_L};-\frac{m_L(l^2+\Delta\gamma^2)^{\alpha_L/2}}{\mu_m s_L}\right)\right),$$

(10)

Inserting this solution into Eq. (9) we obtain an expression for the Laplace transform of the LOS interferers Eq. (8).

D. Backhaul Probability and Expected Rate

To obtain the overall backhaul probability for the reference UAV in the network we decondition the conditional backhaul probability as defined in the previous subsection with respect to the indicator variable t_1 (we use the LOS probability function in Eq. (2)). We then decondition with respect to the horizontal distance random variable R_1.

$$\mathbb{P}(\mathrm{SINR}\geq\theta) = \int_0^\infty\left(\mathbb{P}(\mathrm{SINR}\geq\theta|R_1=r_1,t_1=\mathrm{L})\mathbb{P}_{LOS}(r_1)\right.$$

$$\left.+\mathbb{P}(\mathrm{SINR}\geq\theta|R_1=r_1,t_1=\mathrm{N})(1-\mathbb{P}_{LOS}(r_1))\right)f_{R_1}(r_1)\mathrm{d}r_1.$$

(11)

The expected rate for the backhaul can be calculated using the backhaul probability as

$$\mathbb{E}[\mathcal{R}] = b\int_0^\infty\mathbb{P}(\mathrm{SINR}\geq 2^s-1)\mathrm{d}s.$$

(12)

IV. NUMERICAL RESULTS

In this section we explore the trade-offs that occur between the parameters of the GS network and the resulting backhaul probability of the reference UAV. We generate our results using the analytical expressions given in the previous section and validate them via Monte Carlo (MC) trials. In the following figures solid lines denote the results obtained via the mathematical analysis and markers denote results obtained via MC trials. Unless stated otherwise the parameters used for the numerical results are taken from Table I.

In Fig. 2 and Fig. 3 we demonstrate how increasing the density of the GSs improves the backhaul probability of the UAV, for the LTE and the millimeter-wave backhaul cases, respectively. We consider the upper limit for the GS density to be $5/\mathrm{km}^2$, which corresponds to the density of a terrestrial BS network in an urban environment [13]. For all cases the backhaul probability increases monotonically, with more GSs giving diminishing returns on the improved performance. Note that we set the millimeter-wave interference probability

TABLE I. NUMERICAL RESULT PARAMETERS

Parameter	LTE Backhaul	mmWave Backhaul
Carrier Freq	2 GHz	73 GHz
Bandwidth	20 MHz	1000 MHz
ω	30 deg	10 deg
α_L	2.1	2
α_N	4	3.5 [17]
m_L	1	3
m_N	1	1
p	40 W	10 W [18]
c	-38.4 dB [14]	-69.7 dB
μ_h	-5 dB	N/A
μ_m	N/A	32 dB
ζ	N/A	0
θ	10 dB	10 dB
σ^2	$8\cdot10^{-13}$ W [14]	$4\cdot10^{-11}$ W
ϕ_T	$\arctan(\Delta\gamma/\mathbb{E}[R_1])$	N/A
ω_G	N/A	10 deg
γ_G	30 m	30 m
β	300 /km^2	300 /km^2
δ	0.5	0.5
κ	20 m	20 m

parameter ζ to zero, to reflect the fact the millimeter-wave antennas have very narrow beamwidths and therefore have an extremely low probability of alignment occuring by chance. As a result of this the millimeter-wave signal is noise limited, with a resulting higher backhaul probability for the UAV compared to the interference-limited LTE signals. Although the LTE backhaul is interference-limited, increasing the density of GSs has an overall positive effect on the backhaul probability, for the range of GS densities under consideration. These results suggest that a good UAV backhaul probability can be achieved when the density of GSs is only a fraction of the density of the existing BS network; if the GSs are to be co-located with the BS sites then this result demonstrates that a network operator only has to upgrade a fraction of the existing BS network to be able to provide a backhaul for a network of UAVs.

In Fig. 4 we plot the expected data rate supported by the UAV backhaul as a function of the density of GSs, when considering an LTE backhaul. We can see that the expected rate initially increases as we increase the density of the GSs. However, due to the effect of interference the expected rate appears to behave differently depending on the UAV height. For the lowest UAV height the LOS probability on the interfering GSs is low due to building blockage, and therefore the rate monotonically increases with increased GS density. At the mid-range heights (60 and 80 m) the UAVs have a higher LOS probability on the interfering GSs; as a result increasing the density of the GSs improves the signal from the serving GS, but at the same time increases the aggregate interference. For the large heights (100 and 120 m) the UAV has a steep vertical angle to its serving GS, which results in a smaller area $\mathcal{W}$ illuminated by the UAV antenna and which limits interference. The height the UAVs will operate at will be largely determined by the end user link [8]; however, an operator may wish to avoid operating the UAVs within the range of heights which cause deteriorated backhaul performance, if such an option exists.

In Fig. 5 we consider the effect of the GS height on the backhaul probability of an LTE backhaul, for different UAV heights. We immediately observe that for larger GS heights the backhaul probability appears to deteriorate for all but the lowest UAV height. This effect is due to the increasing
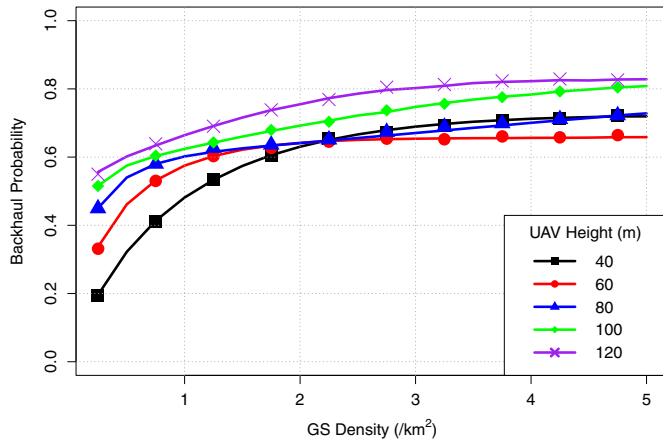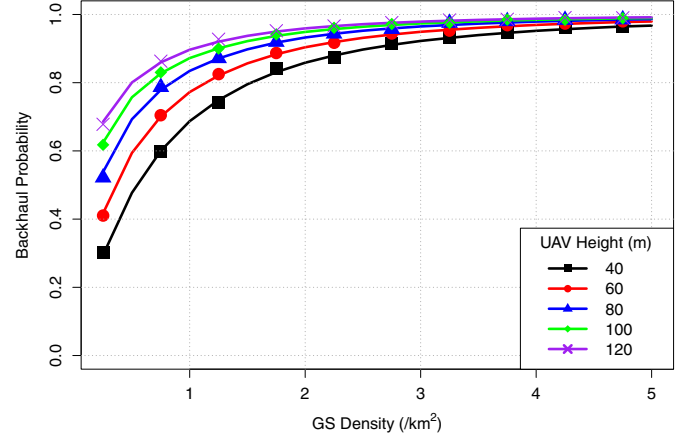

Fig. 3. Backhaul probability for a millimeter-wave backhaul as a function of the GS density, given θ of 10dB.
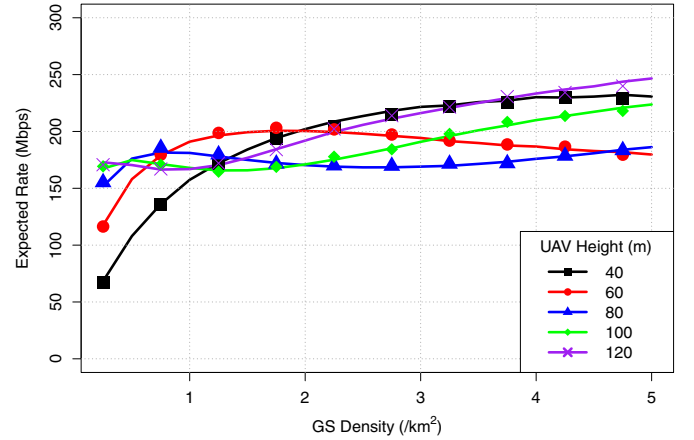

Fig. 4. Expected data rate of an LTE backhaul as a function of GS density.

interference that is experienced by a typical UAV as the GS heights increase; the improved wireless channel to the serving GS does not compensate for the improved wireless channels to the interfering GSs. The GS height cutoff point above which the interference deteriorates appears to be around 30 m, which corresponds to the height of LTE BSs in urban environments as proposed by the 3GPP model [13]. These results suggest that when deploying dedicated GSs for backhauling the UAVs using the LTE band the operators should avoid placing the GSs any higher than the standard height used for the current terrestrial BS network, which also suggests that existing BS sites are suitable for hosting the backhaul GSs. It is also worth noting that the backhaul probability only marginally decreases for GS heights lower than 30 m; this suggests that it is possible to provide UAV backhaul using GSs that are positioned at heights very close to ground level.

In Fig. 6 we show the effect of the GS height on the backhaul probability when the backhaul uses a millimeter-wave signal. We see that the backhaul probability monotonically increases with increased GS height. This is due to the increase in the LOS probability between the UAV and the serving GS. Recall that for a millimeter-wave signal high-
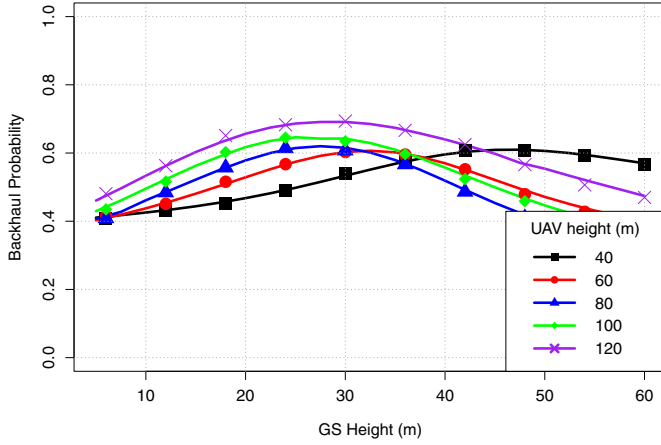

Fig. 2. Backhaul probability for an LTE backhaul as a function of the GS density, given θ of 10dB.

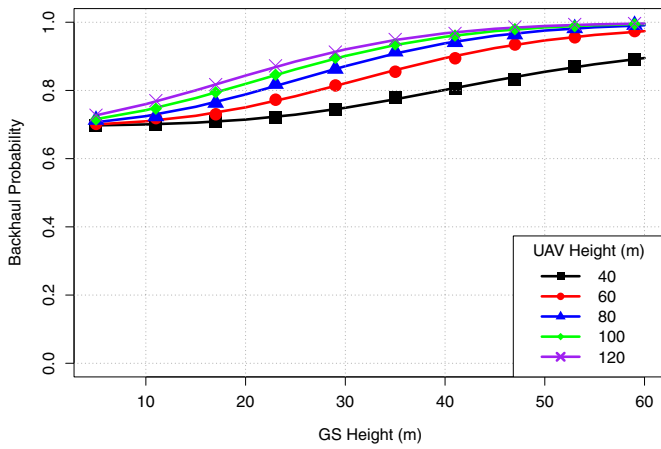Fig. 5. Backhaul probability for an LTE backhaul, given a GS density of 1.25 /km^2 and θ of 10dB.

Fig. 6. Backhaul probability for a millimeter-wave backhaul, given a GS density of 1.25 /km^2 and θ of 10dB.

directionality antennas are assumed on the part of both the UAV as well as the backhaul, and as a result of this the UAV is assumed to receive no interference from other GSs, even when those GSs have LOS to the UAV. It follows then that the network operator should consider deploying the GSs as high as possible above the ground to maximise backhaul performance, which makes the existing BS sites sub-optimal for hosting the GS equipment, in contrast to the LTE backhaul case. As in the previous plots, we observe that greater UAV heights correspond to larger backhaul probability, showing the importance of operating UAVs at heights which can strike a balance between ensuring a good signal for the end user while simultaneously allowing the UAVs to meet their backhaul requirements.

V. CONCLUSION

In this paper we have used stochastic geometry to model a network of GSs that provide wireless backhaul to UAVs in an urban environment. Our model takes into account network parameters such as GS density and antenna characteristics, along with environmental parameters such as building density. We demonstrated that a good backhaul probability for the

UAVs can be achieved with a GS density that is lower than the typical BS network density in an urban environment, and that LTE and millimeter-wave backhauls require different GS heights to maximise performance.

In subsequent works we will consider more detailed models of the millimeter-wave channel which take into account factors such as shadowing, atmospheric and building signal absorption, as well as the impact of antenna misalignment.

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