

# Risk-Aware Security-Constrained Unit Commitment: Taming the Curse of Real-Time Volatility and Consumer Exposure

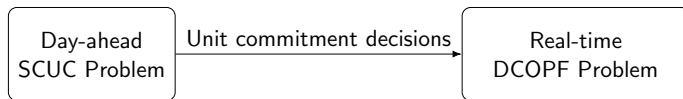
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# Two-Stage Wholesale Electricity Market



- **Day-ahead market:** security-constrained unit commitment (SCUC)
  - ▶ Currently uses a deterministic model
- **Real-time market:** DC optimal power flow
- Volatility in real-time market
  - ▶ Demand
  - ▶ Renewable (wind) production

# Prior Work: SCUC and Demand/Renewable Uncertainty

- Two-stage stochastic programming
  - ▶ Demand uncertainty: Carpentier et al. [1996], Takriti et al. [1996]
  - ▶ Renewable generation: Dvorkin et al. [2014], Morales et al. [2009], Sundar et al. [2016], Wang and Hobbs [2015], Wu et al. [2007]
  - ▶ Bottleneck: large number of scenarios. Struggling with 10 scenarios for our data.
- Adaptive robust optimization models for SCUC
  - ▶ Polyhedral uncertainty sets: Bertsimas et al. [2012], Jiang et al. [2011]
  - ▶ Data-driven uncertainty sets: Velloso et al. [2019], Ning and You [2019]

# Our Goal: Protect Consumers from Price Spikes in Real-Time Market

- Consumer payment at bus  $i$ :
  - Day-ahead (DA) payment:  $(\text{DA price at } i) \times (\text{DA load at } i)$
  - Real-time (RT) consumer exposure:**  
 $(\text{RT price at } i) \times \max\{(\text{RT load at } i - \text{DA load at } i), 0\}$

RT Load – DA Load

	RT LMP		
	Low or negative	Medium	High
	Low or negative	Medium	High
High		<b>HIGH</b>	<b>VERY HIGH</b>
Medium			<b>HIGH</b>
Low or negative			

- Challenge: **Very high RT price** if there is shortfall in wind

# Contributions

- A SCUC model that reduces **worst-case consumer exposure**
  - ▶ **Minimal modification**; preserves two-stage market structure
  - ▶ Real-time uncertainty added as a **penalty term** in the SCUC ( “Mean-variance portfolio optimization” )
  - ▶ Uncertainty set via principal component analysis (PCA), capturing **locational correlation**
- Solve the **nonconvex** model for NYISO case study (1819 buses, 362 generators)
  - ▶ Problem-specific **logic-based Benders decomposition (LBBD) cuts**
  - ▶ Grid search
  - ▶ Branch-and-cut

① Introduction

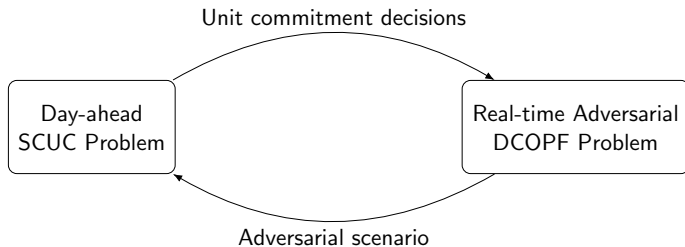
② Model

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# Risk-Aware Security-Constrained Unit Commitment



- A better representation of the impact of RT volatility on system cost

# The Model

$$\min \sum_{t \in \mathcal{T}^{\text{DA}}} \left( \sum_{g \in \mathcal{G}} (h_{gt} + C_g^{\text{Start}} v_{gt} + C_g^{\text{Down}} w_{gt}) + \sum_{i \in \mathcal{N}} C^{\text{VOLL}} p_{it}^{\text{Unmet}} \right) + \rho \hat{V}(\mathbf{y}) \rightarrow \text{DA cost} + \text{penalty on worst-case consumer exposure}$$

s.t. DA constraints: load, capacity, transmission, ramping  $\rightarrow$  SCUC constraints

$$\hat{V}(\mathbf{y}) = \max_{\omega \in \Omega} \frac{1}{N^{\text{tp}}} \sum_{t \in \mathcal{T}^{\text{RT}}} \sum_{i \in \mathcal{N}} \lambda_{it}(\mathbf{y}, \omega) (d_{it}^{\text{RT}} - \bar{D}_{it})^+$$

$h_{gt}$ :	Piecewise linear operating cost
$v_{gt}$ :	Binary start-up decision
$w_{gt}$ :	Binary shut-down decision
$p_{it}^{\text{Unmet}}$ :	Unmet load
$\hat{V}(\mathbf{y})$ :	Worst-case RT consumer exposure
$\lambda_{it}(\mathbf{y}, \omega)$ :	RT LMP
$d_{it}^{\text{RT}}$ :	RT load



# Adversarial Real-time Problem

$$\begin{aligned} \text{DCOPF-A}(\mathbf{y}^*) &:= \max_{\boldsymbol{\omega} \in \Omega} \quad \frac{1}{N^{\text{tp}}} \sum_{t \in \mathcal{T}^{\text{RT}}} \sum_{i \in \mathcal{N}} \lambda_{it}(\mathbf{y}^*, \boldsymbol{\omega}) (d_{it}^{\text{RT}} - \bar{D}_{it})^+ \\ \text{s.t.} \quad &\lambda_{it}(\mathbf{y}^*, \boldsymbol{\omega}) \text{ is an optimal solution of DCOPF-D}(\mathbf{y}^*, \boldsymbol{\omega}). \end{aligned}$$

- $\lambda_{it}(\mathbf{y}^*, \boldsymbol{\omega})$ : RT market equilibrium price
- Uncertainty set  $\Omega$ : using PCA to capture covariance of loads and renewable outputs

# Data-Driven Uncertainty Set

- PCA
  - ▶ Covariance matrix of data for **recent past**, one per time period
  - ▶  $K$  largest leading modes

$$d_{it}^{\text{RT}} = \bar{D}_{it} + \sum_{k=1}^K Q_{kit}^d \alpha_{kt}^d \quad \forall i \in \mathcal{N}, t \in \mathcal{T}^{\text{RT}} \rightarrow \text{RT load}$$

$$p_{gt}^{\text{max,RT}} = \bar{p}_{gt}^{\text{max}} + \sum_{k=1}^K Q_{kgt}^w \alpha_{kt}^w \quad \forall g \in \mathcal{G}^{\text{Wind}}, t \in \mathcal{T}^{\text{RT}} \rightarrow \text{RT wind output}$$

$$\left| \sum_{k=1}^K \alpha_{kt}^{\text{ind}} \right| \leq \Sigma^{\text{ind}} \quad \forall t \in \mathcal{T}^{\text{RT}}, \text{ind} \in \{d, w\} \rightarrow \text{Bound on stressors}$$

$$|\alpha_{kt}^{\text{ind}}| \leq R^{\text{ind}} \quad \forall k = 1, \dots, K; t \in \mathcal{T}^{\text{RT}}, \text{ind} \in \{d, w\} \rightarrow \text{Bound on stressors}$$

$$d_{it}^{\text{RT}} \geq 0 \quad \forall i \in \mathcal{N}, t \in \mathcal{T}^{\text{RT}}$$

$$p_{gt}^{\text{max,RT}} \geq 0 \quad \forall g \in \mathcal{G}^{\text{Wind}}, t \in \mathcal{T}^{\text{RT}}.$$

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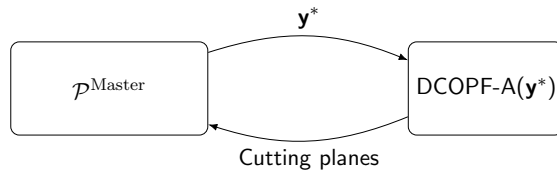
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# The Decomposition Algorithm

- A mixed-integer nonconvex optimization model
  - ▶  $\mathbf{y}$
  - ▶ KKT conditions



- $\mathcal{P}^{\text{Master}}$ : Relax the constraint  $\hat{V}(\mathbf{y}) = \max_{\boldsymbol{\omega} \in \Omega} \frac{1}{N^{\text{tp}}} \sum_{t \in \mathcal{T}^{\text{RT}}} \sum_{i \in \mathcal{N}} \lambda_{it}(\mathbf{y}, \boldsymbol{\omega})(d_{it}^{\text{RT}} - \bar{D}_{it})^+$
- Add under-estimators of  $\hat{V}(\mathbf{y})$  via cutting planes
  - ▶ But  $\text{DCOPF-A}(\mathbf{y}^*)$  is nonconvex...

# Cutting Planes

- Idea:  $\hat{V}^*(\mathbf{y}^*) \rightarrow$  under-estimator for  $\mathbf{y}^*$  **and neighboring  $\mathbf{y}$ 's**
- **No-good cut**:  $\hat{V}(\mathbf{y}) \geq \hat{V}^*(\mathbf{y}^*) \left(1 - \sum_{t \in \mathcal{T}^{\text{RT}}|\text{Hour}} \left(\sum_{g \in \mathcal{I}_{1t}} (1 - y_{gt}) + \sum_{g \in \mathcal{I}_{0t}} y_{gt}\right)\right).$
- **Integer L-shaped cut**:  $\hat{V}(\mathbf{y}) \geq \hat{V}^*(\mathbf{y}^*) + a \sum_{t \in \mathcal{T}^{\text{RT}}|\text{Hour}} \left(\sum_{g \in \mathcal{I}_{1t}} y_{gt} - \sum_{g \in \mathcal{I}_{0t}} y_{gt} - |\mathcal{I}_{1t}|\right)$ 
  - ▶ Nontrivial lower bound for 1-neighbors of  $\mathbf{y}^*$
  - ▶  $a = \max(\hat{V}^* - \hat{V}_1, (\hat{V}^* - \hat{V}_0)/2)$
  - ▶  $\hat{V}_1$ : the minimum value of  $\hat{V}$  when exactly one generator changes its commitment decision
  - ▶  $\hat{V}_0$ : a lower bound on  $\hat{V}$  under a feasible commitment decision
- **Logic-based Benders decomposition (LBBD) cut** (problem specific):  

$$\hat{V}(\mathbf{y}) \geq \sum_{t \in \mathcal{T}^{\text{RT}}|\text{Hour}} \left(\hat{V}_t^*(\mathbf{y}^*) \left(1 - \sum_{g \in \mathcal{I}_{0t}} y_{gt}\right)\right)$$
  - ▶ Nontrivial lower bound when all off-generators remains off

# Validity of the LBBD Cut

## Proposition

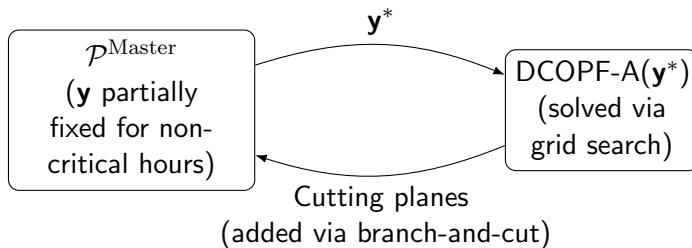
*When there is no congestion in the network and the ramping constraints are not binding in the real-time market:*

- *The LBBD cut  $\hat{V}(\mathbf{y}) \geq \sum_{t \in \mathcal{T}^{\text{RT}} | \text{Hour}} \left( \hat{V}_t^*(\mathbf{y}^*) \left( 1 - \sum_{g \in \mathcal{I}_{0t}} y_{gt} \right) \right)$  provides a correct lower bound for  $\hat{V}(\mathbf{y})$ .*
- *Also, it provides the exact value of  $\hat{V}(\mathbf{y})$  at the current solution  $\mathbf{y}^*$ .*
- Consider  $\mathcal{I}'_{0t}$
- Case 1:  $\mathcal{I}'_{0t} \subset \mathcal{I}_{0t}$ : open more generators  $\rightarrow$  nonpositive RHS
- Case 2:  $\mathcal{I}_{0t} \subseteq \mathcal{I}'_{0t}$ : turn off generators  $\rightarrow$  Less capacity, LMP will not decrease  $\rightarrow \hat{V}_t^*(\mathbf{y}^*)$  is a lower bound
- Congestion: Some LMPs may drop in Case 2
- Ramping: LMP depends on the production levels of the previous time period

# Solving DCOPF-A( $\mathbf{y}^*$ )

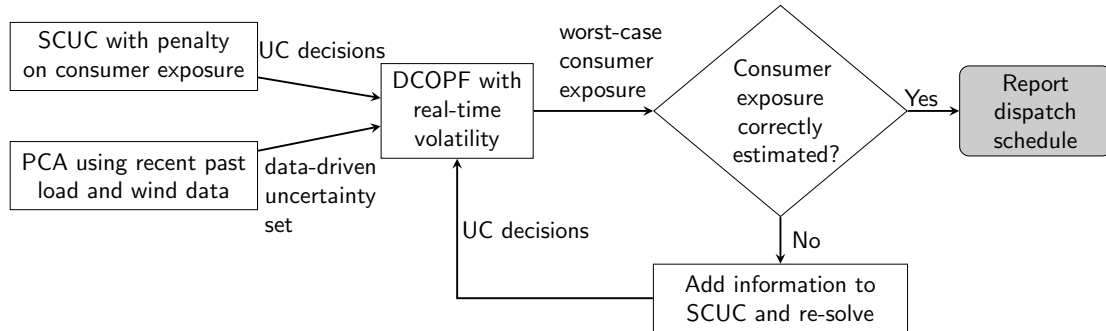
- Direct solve with Knitro or Gurobi: not scalable
- McCormick relaxation: not very tight, limited cost reduction
- Grid search
  - ▶ Iterate through a set of fixed stressors (i.e, “grids”) ( $\tilde{\alpha}_{kt}^d, \tilde{\alpha}_{kt}^w$ )
  - ▶ Solve DCOPF( $\mathbf{y}^*, \tilde{\omega}$ )

# Implementation Details





# Obtaining Risk-Aware Day-ahead Schedule with Our Method



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# NYISO Case Study

- Realistic **NYISO data set**: 1819 buses, 2207 lines, 362 generators and 38 wind farms
- Linux workstation with Intel Xeon processor and 250 GB memory (Palmetto Clusters)
- Gurobi 10.0.1; time limit of 24 hours; all solved **under 0.5% optimality gap**

## Risk-Aware vs. Deterministic Models

- **Cost saving** for most instances
- **Larger savings** under higher volatility
- Relatively small increase in DA cost
- Lower  $\rho \rightarrow$  less cost savings when volatility is lower/higher  $\rightarrow$  more conservative decisions

$R^d$	$R^w$	Save (k\$)	Deter. cost (M\$)	Cost red. (%)	DA cost diff (\$)	Consr. exp. (k\$)
0.1	0.2	0.00	5.37	0.00	0.00	8.53
0.1	0.4	0.12	5.37	0.00	116.16	8.53
0.1	0.6	0.00	5.37	0.00	0.00	8.89
0.1	0.8	42.29	5.41	0.78	116.16	8.89
0.1	1.0	42.28	5.41	0.78	123.50	8.89
0.2	0.2	114.71	5.50	2.09	116.16	17.78
0.2	0.4	114.14	5.50	2.08	688.03	17.78
0.2	0.6	115.74	5.50	2.11	1446.22	16.76
0.2	0.8	108.58	5.50	1.98	8130.20	17.78
0.2	1.0	115.64	5.50	2.10	1072.06	17.78

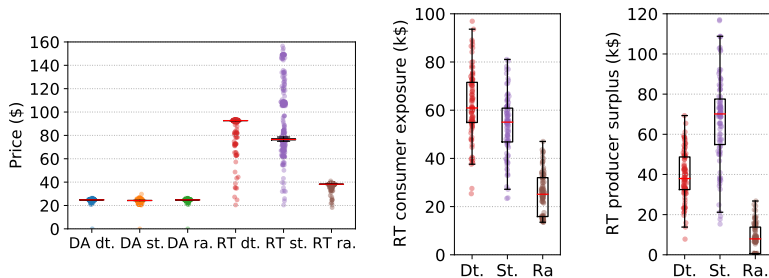
## Risk-Aware vs. Stochastic Models

- Two-stage stochastic programming SCUC model
  - ▶ Objective: Minimize Expected cost +  $\rho$  CVaR
  - ▶ 10 scenarios, 48-hour time limit, with warm start
  - ▶ L-shaped via branch-and-cut not useful
- Stochastic model: **higher** DA cost & consumer exposure

$R^d$	$R^w$	Opt. gap (%)	Save (k\$)	Cost red. (%)	DA cost diff (k\$)	Sto constr. exp. (k\$)
0.1	0.2	3.69	243.93	4.34	-185.95	66.51
0.1	0.4	2.22	158.57	2.87	-114.88	52.22
0.1	0.6	3.30	234.16	4.18	-176.80	66.25
0.1	0.8	2.55	190.63	3.43	-133.17	66.36
0.1	1.0	2.32	178.97	3.22	-120.88	66.99
0.2	0.2	0.55	136.20	2.47	-20.62	133.36
0.2	0.4	1.00	151.53	2.74	-36.65	133.36
0.2	0.6	3.29	289.53	5.11	-173.80	132.49
0.2	0.8	0.40	121.72	2.21	-5.53	133.97
0.2	1.0	0.72	146.50	2.65	-31.19	134.16

# Out-of-Sample Tests

- Perturbed adverse stressors: sample vector  $\alpha^{ind} = (\alpha_{1t}^{ind}, \alpha_{2t}^{ind}, \alpha_{3t}^{ind})$  with **fixed norm**
  - ▶ DA LMPs are similar
  - ▶ Our model: lowest RT LMPs, consumer exposure, and producer surplus
- Uniformly distributed stressors: sample  $\alpha_{kt}^{ind}$  in  $[-R^{ind}, R^{ind}]$



# Summary

- Modify SCUC to reduce **RT consumer exposure** due to load and wind volatility
- **Data-driven PCA-based** uncertainty set for correlation of uncertain data
- Algorithmic development for **nonconvex** optimization problem
- **Large-scale** NYISO case study
- **Cost saving** across various levels of variation, without substantial expenses for dispatch
- Published on IEEE Transactions on Energy Markets, Policy and Regulation (2024)