

# Problem X: Maximum Satisfiability

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## Problem Description

You are given  $n$  Boolean variables  $x_1, \dots, x_n$ , each taking a value in  $\{0, 1\}$ , and  $m$  weighted clauses  $C_1, C_2, \dots, C_m$  with corresponding weights  $w_1, \dots, w_m$ . A *literal* is either a variable  $x_i$  or its negation  $\neg x_i$ . A *clause* is a disjunction (logical “or”) of one or more literals, and a Boolean formula in *conjunctive normal form (CNF)* is the conjunction (logical “and”) of all clauses:

$$\phi = C_1 \wedge C_2 \wedge \dots \wedge C_m.$$

The formula  $\phi$  is said to be *satisfiable* if there exists an assignment of truth values to variables that makes all clauses true. Your task is to determine whether  $\phi$  is satisfiable. If it is not satisfiable, find the maximum total weight of clauses that can be simultaneously satisfied by some truth assignment.

## Input

The first line contains two integers  $n$  and  $m$  ( $1 \leq n \leq 20$ ,  $0 \leq m \leq 100$ ).

Each of the next  $m$  lines describes one clause. The line begins with an integer  $\ell$  ( $1 \leq \ell \leq 20$ ), the number of literals in the clause, followed by a positive integer  $w$  ( $0 < w \leq 10^6$ ), the weight of the clause, followed by  $\ell$  integers representing the literals themselves.

A positive integer  $i$  denotes the literal  $x_i$ , while a negative integer  $-i$  denotes the literal  $\neg x_i$ . Variable indices are 1-based.

## Output

Print a single line:

- **satisfiable** if there exists a truth assignment that satisfies all clauses, or
- **not satisfiable W** otherwise, where  $W$  is the maximum total weight of simultaneously satisfiable clauses.

## Examples

### Sample Input 1

```
3 2
2 1 1 -2
1 2 3
```

### Sample Output 1

```
satisfiable
```

### Sample Input 2

```
3 3
2 5 1 2
1 4 -1
1 3 -2
```

### Sample Output 2

```
not satisfiable 9
```