Report: 构建两层神经网络分类器

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github repo 链接: https://github.com/chenghengheng/CV-HW1 (https://github.com/chenghengheng/CV-HW1)

模型网盘下载地址: https://pan.baidu.com/s/1bAbrUL2hiJo4A0ywluG1mQ?pwd=w4h9 (https://pan.baidu.com/s/1bAbrUL2hiJo4A0ywluG1mQ?pwd=w4h9)

模型训练

数据集

采用mnist数据集,训练集大小60000 * 28 * 28,测试集大小10000 * 28 * 28。

为方便后续计算,对原始数据作以下处理:

• Reshape: 将每个样本对应的28 * 28的数据改写为784 * 1格式

• Standardize:对测试集进行归一化,并用测试集的均值和方差处理训练集

• Expand:训练过程中,将测试集的分类扩展为矩阵形式,矩阵的第i行对应 X_i 的分类,第j列为1对应真实标签,其他列都为0

训练

按标准正态分布随机设置初始的权重和偏置,通过随机梯度下降(SGD)方法更新参数。

设置100000次迭代,每次随机选择一组 $\{X_i,y_i\}$,计算当前参数下的loss,根据梯度更新w,b w=w-stepsize*gradient(w) b=b-stepsize*gradient(b)

• 激活函数: 使用tanh()作为激活函数

• loss: 采用交叉熵损失函数

$$L = \frac{1}{N} \sum_{i} -log(p(y_i))$$

• 反向传播: 输出层的误差项为 $2*(\hat{y}-y)$, 根据反向传播算法, 前一层的误差项为f'(z) $\bigcirc (W^T\delta)$

• 梯度计算: 上一层的激活值*误差项

• 学习率下降策略: 学习率按余弦函数下降

• L2正则化:为方便计算与编程,将正则化部分设置在对参数的更新中,在梯度项部分加上 λw

• 保存模型: 应用 numpy. savetxt 函数将参数保存为txt文件,应用模型时通过 numpy. loadtxt 导入参数

代码说明

para2.py 将训练过程封装为函数,通过修改变量调整学习率,隐藏层大小,正则化强度。

具体函数说明详见代码注释部分。

本文件 parameter&test.ipynb 包括参数查找,模型测试,可视化训练及测试 Loss,最终测试精度和对网络参数的可视化。

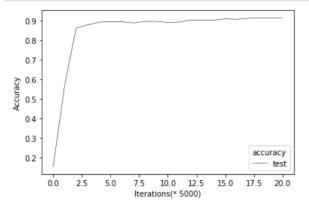
```
In [1]: | from para2 import * import tensorflow as tf import numpy as np import random import math
```

```
In [2]: N np. random. seed(1) random. seed(1)
```

```
d = d * d
             x_train = x_train.reshape(n, d)
              t, d1 = x_{test.shape}[0], x_{test.shape}[1]
             d1 = d1 * d1
              x_{test} = x_{test}. reshape(t, d1)
In [5]: \mathbf{M} \mid \text{nLabels} = \max(y_{\text{train}}) + 1
              yExpanded = binary(y train, nLabels)
             ytExpanded = binary(y_test, nLabels)
             X, mu, sigma = standardize(x train)
             Xtest = standardize_(x_test, mu, sigma)
         以上为数据处理部分
         参数查找
In [6]: M loss1, loss2, test = para(0.001, [50], 0.05, X, y train, n, d, Xtest, y test, t, nLabels, yExpanded, 1)
             Train iteration = 0, training error = 0.846717, test error = 0.847000
              Train iteration = 5000, training error = 0.432450, test error = 0.430100
             Train iteration = 10000, training error = 0.143167, test error = 0.138800
             Train iteration = 15000, training error = 0.121550, test error = 0.122200
             Train iteration = 20000, training error = 0.115267, test error = 0.108900
             Train iteration = 25000, training error = 0.110283, test error = 0.105800
             Train iteration = 30000, training error = 0.110067, test error = 0.106400
             Train iteration = 35000, training error = 0.112817, test error = 0.112500
              Train iteration = 40000, training error = 0.109667, test error = 0.104700
             Train iteration = 45000, training error = 0.104567, test error = 0.104500
             Train iteration = 50000, training error = 0.113783, test error = 0.110900
              Train iteration = 55000, training error = 0.108983, test error = 0.107900
             Train iteration = 60000, training error = 0.101267, test error = 0.097400
             Train iteration = 65000, training error = 0.099917, test error = 0.098300
             Train iteration = 70000, training error = 0.097667, test error = 0.098400
             Train iteration = 75000, training error = 0.094283, test error = 0.091300
             Train iteration = 80000, training error = 0.095133, test error = 0.094000
             Train iteration = 85000, training error = 0.091350, test error = 0.088600
              Train iteration = 90000, training error = 0.089500, test error = 0.087800
             Train iteration = 95000, training error = 0.086617, test error = 0.086100
             Training error with final model = 0.085867
             Test error with final model = 0.087300
In [7]: | loss1 = np. array(loss1)
              loss2 = np. array(loss2)
              test = np.array(test)
In [8]: | x = np. arange (19)
             plt.plot(x, loss1, color="red", label="train", linewidth=0.5)
             plt.plot(x, loss2, color="blue", label="test", linewidth=0.5)
             plt.legend(title="Loss")
             plt.xlabel('Iterations(* 5000)')
             plt.ylabel('Loss')
             plt.show()
                                                               Loss
                 2.00
                                                                 train
                                                                 test
                 1.75
                 1.50
               § 1.25
                 1.00
                 0.75
                 0.50
                      0.0
                            2.5
                                              10.0
                                                                 17.5
```

Iterations(* 5000)

In [4]: n, $d = x_{train.shape}[0]$, $x_{train.shape}[1]$



初始参数:初始学习率为0.001,隐藏层大小为50,正则化强度0.05。

Loss 及 accuracy 曲线如上图, 收敛较快。

以下,对隐藏层大小作调整测试。

```
In [10]: M | loss1, loss2, test = para(0.001, [100], 0.05, X, y_train, n, d, Xtest, y_test, t, nLabels, yExpanded, 2)
              Train iteration = 0, training error = 0.941617, test error = 0.943400
              Train iteration = 5000, training error = 0.365250, test error = 0.360300
              Train iteration = 10000, training error = 0.135650, test error = 0.128800
              Train iteration = 15000, training error = 0.139033, test error = 0.141600
              Train iteration = 20000, training error = 0.113633, test error = 0.110200
              Train iteration = 25000, training error = 0.111683, test error = 0.105800
              Train iteration = 30000, training error = 0.108667, test error = 0.102700
              Train iteration = 35000, training error = 0.115317, test error = 0.115400
              Train iteration = 40000, training error = 0.106650, test error = 0.100500
              Train iteration = 45000, training error = 0.105283, test error = 0.104900
              Train iteration = 50000, training error = 0.113667, test error = 0.110000
              Train iteration = 55000, training error = 0.108333, test error = 0.106800
              Train iteration = 60000, training error = 0.098650, test error = 0.094700
              Train iteration = 65000, training error = 0.101167, test error = 0.098500
              Train iteration = 70000, training error = 0.098417, test error = 0.099100
              Train iteration = 75000, training error = 0.092833, test error = 0.089600
              Train iteration = 80000, training error = 0.095333, test error = 0.093700
              Train iteration = 85000, training error = 0.088867, test error = 0.085900
              Train iteration = 90000, training error = 0.088150, test error = 0.087000
              Train iteration = 95000, training error = 0.085133, test error = 0.085600
              Training error with final model = 0.084500
              Test error with final model = 0.084000
```

```
In [11]: N loss1 = np.array(loss1)
loss2 = np.array(loss2)
test = np.array(test)
```

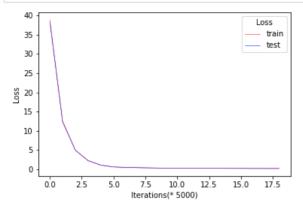
```
In [12]: \mathbf{N} = \text{np. arange}(19)
               plt.plot(x, loss1, color="red", label="train", linewidth=0.5)
               plt.plot(x, loss2, color="blue", label="test", linewidth=0.5)
               plt.legend(title="Loss")
               plt.xlabel('Iterations(* 5000)')
               plt.ylabel('Loss')
               plt.show()
                                                                  Loss
                  2.25
                                                                   train
                  2.00
                                                                   test
                  1.75
                  1.50
                Loss
                  1.25
                  1.00
                  0.75
                  0.50
                        0.0
                              2.5
                                                10.0
                                                      12.5
                                                             15.0
                                                                   17.5
                                         Iterations(* 5000)
In [13]: \forall y = np. arange (21)
               plt.plot(y, 1-test, color="black", label="test", linewidth=0.5)
               plt.legend(title="accuracy")
               plt.xlabel('Iterations(* 5000)')
               plt. ylabel('Accuracy')
               plt.show()
                  0.8
                  0.6
                Accuracy
6.0
                  0.2
                                                               accuracy
                                                                   test
                       0.0
                            2.5
                                  5.0
                                             10.0
                                                  12.5
                                                        15.0
                                                              17.5
                                                                   20.0
                                        7.5
                                        Iterations(* 5000)
In [14]: | loss1, loss2, test = para(0.001, [200], 0.05, X, y_train, n, d, Xtest, y_test, t, nLabels, yExpanded, 3)
               Train iteration = 0, training error = 0.920183, test error = 0.917400
               Train iteration = 5000, training error = 0.311400, test error = 0.302800
               Train iteration = 10000, training error = 0.135833, test error = 0.131100
               Train iteration = 15000, training error = 0.154800, test error = 0.153100
               Train iteration = 20000, training error = 0.131200, test error = 0.127600
               Train iteration = 25000, training error = 0.118850, test error = 0.112200
               Train iteration = 30000, training error = 0.113500, test error = 0.111000
               Train iteration = 35000, training error = 0.123300, test error = 0.122000
               Train iteration = 40000, training error = 0.111333, test error = 0.105100
               Train iteration = 45000, training error = 0.117817, test error = 0.115000
               Train iteration = 50000, training error = 0.122550, test error = 0.118400
               Train iteration = 55000, training error = 0.112517, test error = 0.109200
               Train iteration = 60000, training error = 0.102733, test error = 0.097700
               Train iteration = 65000, training error = 0.114917, test error = 0.108600
               Train iteration = 70000, training error = 0.103900, test error = 0.102100
               Train iteration = 75000, training error = 0.097100, test error = 0.093300
               Train iteration = 80000, training error = 0.099533, test error = 0.097000
               Train iteration = 85000, training error = 0.091417, test error = 0.089800
               Train iteration = 90000, training error = 0.090067, test error = 0.087400
               Train iteration = 95000, training error = 0.086850, test error = 0.088200
               Training error with final model = 0.085617
               Test error with final model = 0.085900
```

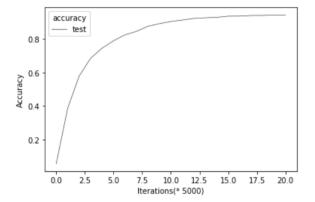
随着隐藏层大小从50增加到100,精度提升,隐藏层大小增加至200时,模型训练时长明显增加,但训练结果无改善。

Loss 及 accuracy 曲线如上图,收敛较快。

```
In [15]: Nossl, lossl, test = para(0.001, [100], 0.1, X, y train, n, d, Xtest, y test, t, nLabels, yExpanded, 5)
              Train iteration = 0, training error = 0.941617, test error = 0.943400
              Train iteration = 5000, training error = 0.163983, test error = 0.157100
              Train iteration = 10000, training error = 0.144950, test error = 0.133700
              Train iteration = 15000, training error = 0.172933, test error = 0.170700
              Train iteration = 20000, training error = 0.138617, test error = 0.133500
              Train iteration = 25000, training error = 0.132800, test error = 0.125800
              Train iteration = 30000, training error = 0.124000, test error = 0.116900
              Train iteration = 35000, training error = 0.153317, test error = 0.152600
              Train iteration = 40000, training error = 0.128050, test error = 0.119300
              Train iteration = 45000, training error = 0.125850, test error = 0.125500
              Train iteration = 50000, training error = 0.134350, test error = 0.129300
              Train iteration = 55000, training error = 0.130850, test error = 0.127500
              Train iteration = 60000, training error = 0.119050, test error = 0.112800
              Train iteration = 65000, training error = 0.122150, test error = 0.116200
              Train iteration = 70000, training error = 0.117150, test error = 0.114100
              Train iteration = 75000, training error = 0.110333, test error = 0.107900
              Train iteration = 80000, training error = 0.115533, test error = 0.112700
              Train iteration = 85000, training error = 0.106467, test error = 0.102800
              Train iteration = 90000, training error = 0.105033, test error = 0.100600
              Train iteration = 95000, training error = 0.102817, test error = 0.098600
              Training error with final model = 0.101217
              Test error with final model = 0.097300
In [16]: M loss1, loss2, test = para(0.001, [100], 0.01, X, y_train, n, d, Xtest, y_test, t, nLabels, yExpanded, 6)
              Train iteration = 0, training error = 0.941617, test error = 0.943400
              Train iteration = 5000, training error = 0.625883, test error = 0.613000
              Train iteration = 10000, training error = 0.432150, test error = 0.421300
              Train iteration = 15000, training error = 0.325700, test error = 0.314900
              Train iteration = 20000, training error = 0.256183, test error = 0.254900
              Train iteration = 25000, training error = 0.210333, test error = 0.210700
              Train iteration = 30000, training error = 0.173817, test error = 0.175300
              Train iteration = 35000, training error = 0.149717, test error = 0.154600
              Train iteration = 40000, training error = 0.124683, test error = 0.124200
              Train iteration = 45000, training error = 0.103650, test error = 0.108700
              Train iteration = 50000, training error = 0.095117, test error = 0.095800
              Train iteration = 55000, training error = 0.082033, test error = 0.087100
              Train iteration = 60000, training error = 0.075233, test error = 0.077400
              Train iteration = 65000, training error = 0.070083, test error = 0.073700
              Train iteration = 70000, training error = 0.067467, test error = 0.071100
              Train iteration = 75000, training error = 0.062050, test error = 0.064000
              Train iteration = 80000, training error = 0.060633, test error = 0.063600
              Train iteration = 85000, training error = 0.057100, test error = 0.059800
              Train iteration = 90000, training error = 0.056817, test error = 0.059600
              Train iteration = 95000, training error = 0.053217, test error = 0.057700
              Training error with final model = 0.052800
              Test error with final model = 0.056500
In [17]: \triangleright loss1 = np. array (loss1)
              loss2 = np. array(loss2)
              test = np.array(test)
```

```
In [18]: N x = np. arange(19)
plt. plot(x, loss1, color="red", label="train",linewidth=0.5)
plt. plot(x, loss2, color="blue", label="test",linewidth=0.5)
plt. legend(title="Loss")
plt. xlabel('Iterations(* 5000)')
plt. ylabel('Loss')
plt. show()
```





可以看出,本组参数在训练集的准确率有明显提升。

Loss 及 accuracy 曲线如上图,初始收敛较慢,但收敛结果更好。

最终测试错误率为0.056500.

以下,对初始步长 (学习率) 作调整测试。

```
In [20]: M loss1, loss2, test = para(0.01, [100], 0.01, X, y train, n, d, Xtest, y test, t, nLabels, yExpanded, 7)
              Train iteration = 0, training error = 0.941617, test error = 0.943400
              Train iteration = 5000, training error = 0.312133, test error = 0.311500
              Train iteration = 10000, training error = 0.281550, test error = 0.263700
              Train iteration = 15000, training error = 0.298233, test error = 0.297400
              Train iteration = 20000, training error = 0.327200, test error = 0.316400
              Train iteration = 25000, training error = 0.260167, test error = 0.255800
              Train iteration = 30000, training error = 0.404417, test error = 0.391100
              Train iteration = 35000, training error = 0.279950, test error = 0.279200
              Train iteration = 40000, training error = 0.236367, test error = 0.221700
              Train iteration = 45000, training error = 0.221333, test error = 0.215400
              Train iteration = 50000, training error = 0.255833, test error = 0.233400
              Train iteration = 55000, training error = 0.215367, test error = 0.207700
              Train iteration = 60000, training error = 0.217450, test error = 0.214700
              Train iteration = 65000, training error = 0.205967, test error = 0.203700
              Train iteration = 70000, training error = 0.169233, test error = 0.168100
              Train iteration = 75000, training error = 0.165783, test error = 0.158200
              Train iteration = 80000, training error = 0.147483, test error = 0.141200
              Train iteration = 85000, training error = 0.109883, test error = 0.106000
              Train iteration = 90000, training error = 0.092283, test error = 0.093100
              Train iteration = 95000, training error = 0.068700, test error = 0.073100
              Training error with final model = 0.057117
              Test error with final model = 0.061200
In [21]: M loss1, loss2, test = para(0.0001, [100], 0.01, X, y_train, n, d, Xtest, y_test, t, nLabels, yExpanded, 8)
              Train iteration = 0, training error = 0.941617, test error = 0.943400
              Train iteration = 5000, training error = 0.924150, test error = 0.924100
              Train iteration = 10000, training error = 0.903517, test error = 0.900200
              Train iteration = 15000, training error = 0.872533, test error = 0.871200
              Train iteration = 20000, training error = 0.836667, test error = 0.831500
              Train iteration = 25000, training error = 0.792467, test error = 0.786500
              Train iteration = 30000, training error = 0.755300, test error = 0.750600
              Train iteration = 35000, training error = 0.724417, test error = 0.717500
              Train iteration = 40000, training error = 0.694567, test error = 0.686800
              Train iteration = 45000, training error = 0.667750, test error = 0.659300
              Train iteration = 50000, training error = 0.644600, test error = 0.638300
              Train iteration = 55000, training error = 0.623333, test error = 0.617000
              Train iteration = 60000, training error = 0.605567, test error = 0.598400
              Train iteration = 65000, training error = 0.591033, test error = 0.583600
              Train iteration = 70000, training error = 0.578733, test error = 0.570500
```

经参数查找, 表现较好的一组参数是

初始学习率为0.001,隐藏层大小为100,正则化强度0.01。

Training error with final model = 0.546083 Test error with final model = 0.542300

Train iteration = 75000, training error = 0.567633, test error = 0.560800 Train iteration = 80000, training error = 0.559933, test error = 0.554400 Train iteration = 85000, training error = 0.54117, test error = 0.548600 Train iteration = 90000, training error = 0.549750, test error = 0.545500 Train iteration = 95000, training error = 0.547200, test error = 0.543500

测试

导入模型,用经过参数查找的模型进行测试,输出分类精度。

```
In [22]: M np.random.seed(1) random.seed(1) nHidden = [100] w = np.loadtxt("weights_100 hidden_0.001000 step_0.010000 lambda.txt") # 导入模型 b = np.loadtxt("bias_100 hidden_0.001000 step_0.010000 lambda.txt") yhat1 = predict(w, b, X, nHidden, nLabels) # 测试模型 print("Training error with final model = %f" % (sum(yhat1 != y_train) / n)) yhat2 = predict(w, b, Xtest, nHidden, nLabels) print("Test error with final model = %f" % (sum(yhat2 != y_test) / t)) acc = 1 - (sum(yhat2 != y_test) / t) print("\nTest accuracy with final model = %f" % acc) # 测试精度

Training error with final model = 0.052800 Test error with final model = 0.056500

Test accuracy with final model = 0.943500
```

```
In [23]: | import matplotlib.pyplot as plt

w = np.loadtxt("weights_100 hidden_0.001000 step_0.010000 lambda.txt")

w1 = w[:78400].reshape(100, 28, 28)

w2 = w[78400:].reshape(10, 10, 10)
```

网络参数可视化

对最优模型的参数进行可视化操作。

