明天 7:30-9:30 pm 期间中考试。

多项式 乘法. $f(x) = a_0 + a_1 x + \cdots + a_0 x^d \qquad deg \leq d$ $g(x) = b_0 + b_1 x + \cdots + b_0 x d \qquad deg \leq d$ $f \cdot g = a_0 b_0 + (a_1 b_0 + b_1 a_0) x$ $+ \left(\sum_{l} a_{l} b_{k-l}\right) x^{k-l}$ $f \cdot g = a_0 b_0 + a_0 b_0 +$

$$\frac{f}{(x,y)} = \frac{x_0, x_1 \cdots x_d}{x_1 + x_j}, \frac{x_1 + x_j}{y_1 + y_j}$$

$$\frac{f(x,y)}{f(x_d)} = \frac{\left(\frac{x_1 + x_2}{x_1 + x_1} \cdots x_d}{x_d + x_d}\right) \left(\frac{a_0}{a_1}\right)$$

$$\frac{f(x_d)}{f(x_d)} = \frac{f(x_d)}{f(x_d)}$$

$$\begin{array}{c}
\left(\begin{array}{c}
a_{\alpha}\\
\vdots\\
a_{\alpha}
\end{array}\right) = M^{-1} \cdot \begin{pmatrix}
f(x_{\alpha})\\
\vdots\\
f(x_{\alpha})\\
\end{array}\right)$$

$$h(x) = \int |x| \cdot j(x)$$
 deg $\leq 2d$.

$$\left(h(x_i) = f(x_i) g(x_i)\right) \qquad O(d) \approx \frac{1}{2} \frac{3}{4}.$$

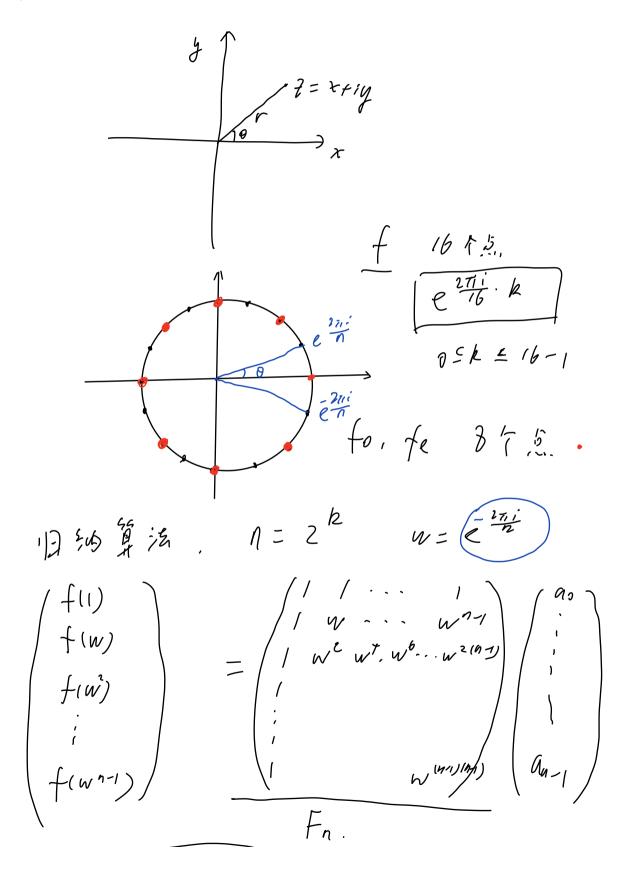
$$f(x) = x^{6} + 3x^{3} + 2x^{2} + x + 1$$

$$= \frac{(x^{6} + 2x^{2} + 1) + (3x^{3} + x)}{f_{2}(x^{2})}$$

$$\frac{dy}{f_{2}} = \frac{d}{dy} = \frac{(x^{2})}{f_{2}(x^{2})} + x_{1} = \frac{(x^{2})}{f_{2}(x^{2})} + x_{2} = \frac{(x^{2})}{f_{2}(x^{2})} + x_{$$

$$f = \frac{1}{x_1} - \frac{1}{x_2} = \frac{1}{x_2} = \frac{1}{x_2}$$

$$f = \frac{1}{x_2} - \frac{1}{x_2} = \frac{1}{x_2}$$



定理:
$$(\overline{F_n})^T \cdot F_n = n \cdot I_n$$
. $\overline{F_n}$ 是 F_n 中旬个元素作系矩

$$i \stackrel{?}{\downarrow} \stackrel{$$

$$= \left(\begin{array}{c} \overline{V_i}^T \cdot V_j \\ \end{array} \right)$$

$$\overline{V_i}^T V_j = \sum_{k=0}^{n-1} (\overline{w}^i)^k (w^j)^k$$

$$= \sum_{k=0}^{n-1} (W^{-i} \cdot W^{j})^{k}$$

$$|W|^2 = \overline{W} \cdot W = 1$$

$$(W^{j-1})^k$$
, $h=0$, ... $n-1$, $2\pi 40$ 3 .
 $\frac{\beta_{-}}{\beta_{-}} \chi^n - 1 = 0$ FG π π .
 $\frac{\beta_{-}}{\beta_{-}} (W^{j-1})^k = 0$.

$$W^{j-1} \stackrel{?}{\not=} X \xrightarrow{(j,i,n)} -1 \text{ BS } \#$$

$$\sum_{k=0}^{n} (w^{j-i})^{k} = 0$$

$$F_{n}^{-1} = \frac{1}{n} (\overline{F_{n}}^{T})$$

$$F_{n}^{-1} \stackrel{f(v)}{=} n \left(\frac{1}{|W|} (\overline{w})^{2}, \dots (\overline{w})^{n} \right)$$

$$\overline{W} = e^{\frac{2\pi i}{n}} \text{ Leccesive } 1/3 \leq 18 \stackrel{n}{\not=} = 2$$

$$O(n \log n)$$

年度得第一个
$$\left(\frac{Q_{0}}{Q_{1}-1}\right)$$
 $=$ $\left(\frac{I_{n}}{I_{n}}, \frac{Q_{n}}{Q_{n}}\right)$ $\left(\frac{F_{n}}{F_{n}}\right)$ $\left(\frac{F_{n}}{F_{n}}\right)$ $\left(\frac{F_{n}}{F_{n}}\right)$ $\left(\frac{F_{n}}{F_{n}}\right)$ $\left(\frac{F_{n}}{F_{n}}\right)$

 $D_{h} = \begin{pmatrix} 1 & w_{2n} & w_{2n} & w_{2n} & w_{2n} & w_{2n} \\ & & & & & & & \\ \hline P_{u} & = & \begin{pmatrix} \overline{1}_{n} & D_{n} & w_{2n} & w_{2n} \\ & \overline{1}_{n} & -D_{n} & w_{2n} & w_{2n} \\ & & & & & \\ \hline P_{u} & = & \begin{pmatrix} \overline{1}_{n} & D_{n} & w_{2n} & w_{2n} \\ & \overline{1}_{n} & -D_{n} & w_{2n} & w_{2n} \\ & & & & \\ \hline P_{u} & = & \begin{pmatrix} \overline{1}_{n} & w_{2n} & w_{2n} \\ & \overline{1}_{n} & w_{2n} & w_{2n} \\ & & & & \\ \hline P_{u} & &$

通常 DFT.

Distrete Fourier Transform

 $W_n = e^{-\frac{2\pi i}{n}}$ $\int_{0}^{\infty} \frac{f(x)}{4x}$ $\int_{0}^{\infty} \frac{dx}{dx} = \frac{1}{n}$

$$\frac{\sqrt{1}}{\sqrt{1}} f(x_n), \quad x_n = \frac{k \cdot 7}{n}$$

$$k = 0 \cdot \cdots \cdot n - 1.$$

$$\begin{pmatrix} f_0 \\ \vdots \\ f_{n-1} \end{pmatrix} \in \mathbb{R}^7, \quad (\mathbb{C}^n)$$

$$\begin{array}{cccc}
DFT : & C^{n} \longrightarrow & C^{n} \\
\begin{pmatrix} f_{0} \\ \vdots \\ f_{n-1} \end{pmatrix} & & \downarrow & \downarrow \\
\begin{pmatrix} f_{n} \\ \vdots \\ f_{n-1} \end{pmatrix} & & = \begin{pmatrix} f_{n} \\ \vdots \\ f_{n-1} \end{pmatrix}
\end{array}$$

$$\begin{pmatrix}
\hat{f}_{0} \\
\hat{f}_{h-1}
\end{pmatrix} \longrightarrow \begin{pmatrix}
\hat{f}_{0} \\
\hat{f}_{h}
\end{pmatrix}$$

$$\frac{1}{4} (\bar{F}_{h})^{7}$$

$$\underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} at\right)}_{=\frac{2\pi i}{2\pi i}} \underbrace{\left(\int_{-2\pi i}^{2\pi i} at - e^{-2\pi i} a$$

$$\frac{1}{\sqrt{n}} = \frac{1}{\sqrt{n}} = \frac{1}{\sqrt{n}}$$

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$$= \sum_{l=0}^{n-1} e^{2\pi i \frac{(aT-k)l}{n}}$$

$$= \sum_{l=0}^{n-1} e^{2\pi i \frac{(aT-k)l}{n}}$$

$$= \sum_{l=0}^{n-1} \frac{(aT-k)l}{n}$$

$$f = \sin(2\pi f, t) + \sin(2\pi f_1 t)$$

 $f_1 = 50$, $f_2 = 120$
 $f + Noise$, $T = 1$, $N = 1000$

