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Comments on "Ellipse area calculations and their applicability in posturography" (Schubert and Kirchner, vol.39, pages 518-522, 2014)



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Dear Editor:

I would like to congratulate the authors for the article regarding the calculation of the so-called ellipse area [1]. As the authors indicated, the algorithms employed to calculate the area of the 95% prediction ellipse using the chi-square or the Rayleigh distribution are in fact only exact when the number of samples of the bivariate variable tends to infinite (when each univariate variable is assumed to have a normal distribution) [2]. As the authors also observed, for a typical data size in posturography, 30 s of data sampled at 100 Hz (3000 samples), this approximation is probably good enough, since the error is only 0.1%. The problem appears when the data size is much less: for 100 samples, the error is 2.5%, and for 10 samples, the error is 26%. These last two cases are unlikely scenarios in posturography, but possible for an unadvised user; and besides, the prediction ellipse area can be employed in any other data analysis. The authors described the calculation (see the supplementary data in [1]) but did not publish any algorithm to compute the exact 95% prediction ellipse area. They only made available the algorithm with the known approximation (i.e., they used the chi-square distribution and not the F distribution for the exact calculation). To fill this lacuna, at the end of this letter it is presented a computer program to calculate the exact 95% prediction ellipse area [2] for a Matlab-like environment software

(p/2 + 1)*prod(saxes)

and the same algorithm implemented in the Python language, a free and open source software. The program input, the variable 'data', has 'n' rows (the number of samples) and two columns for a bivariate data. In fact, this computer program is written to also calculate the hypervolume of a hyper-ellipsoid (with p dimensions) if 'data' has p columns. Briefly, the volume of the hyperellipsoid is calculated with the same equation for the volume of a p-dimensional ball (http://en.wikipedia.org/wiki/Volume_of_an_n-ball) with the radius replaced by the semi-axes of the hyper-ellipsoid. The variable 'hypervolume' contains the calculated ellipse area for 2-D data or the hypervolume for p-dimensional

The webpage 'Prediction ellipse and prediction ellipsoid' at the website https://github.com/demotu/BMC contains a detailed explanation about the prediction ellipse and a more complete code written in Python to compute and plot the results and other variables.

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[[]n, p] = size(data);covar = cov(data);[U, S, V] = svd(covar);f95 = finv(.95,p,n-p)*(n-1)*p*(n+1)/n/(n-p);

[%] Matlab code to calculate the hypervolume of the exact 95% prediction hyper-ellipsoid: % 2-D array dimensions % covariance matrix of data % singular value decomposition % F 95 percent point function saxes = sqrt(diag(S)*f95);% semi-axes lengths hypervolume = pi^(p/2)/gamma

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Python code to calculate the hypervolume of the exact 95% prediction hyper-ellipsoid: import numpy as np from scipy.stats import f as F from scipy.special import gamma n, p = np.asarray(data).shape cov = np.cov(data, rowvar = 0)U, s, Vt = np.linalg.svd(cov) f95 = F.ppf(.95,p,n-p)*(n-1)* $p^*(n + 1)/n/(n - p)$ saxes = np.sqrt(s*f95)hypervolume = np.pi**(p/2)/ gamma(p/2 + 1)*np.prod(saxes)

hypervolume

- # import Numpy package
- # import F distribution
- # import Gamma function
- # 2-D array dimensions
- # covariance matrix of data # singular value decomposition
- # F 95 percent point function
 - # semi-axes lengths

Conflicts of interest statement

There author declares no conflicts of interest.

References

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