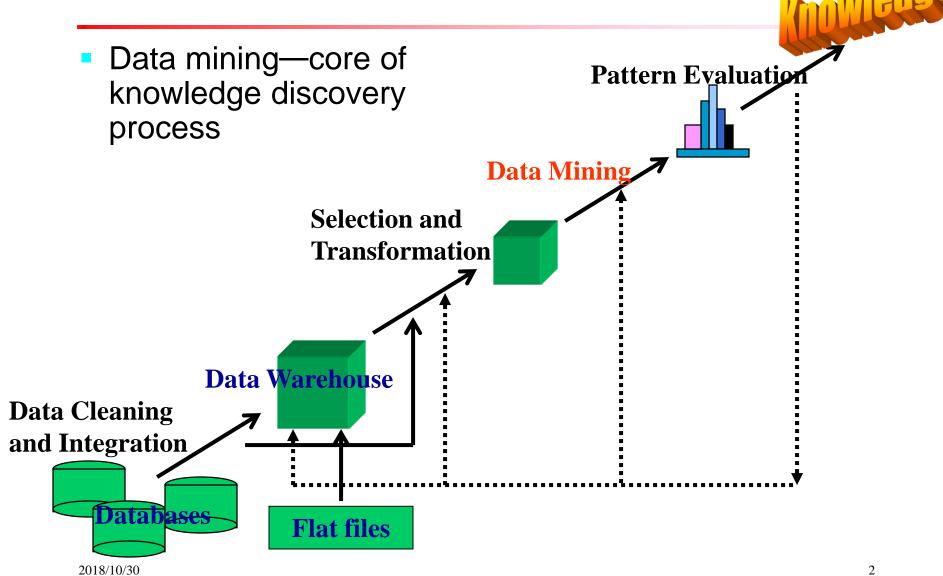
## **Data Mining**

Ying Liu, Prof., Ph.D

University of Chinese Academy of Sciences

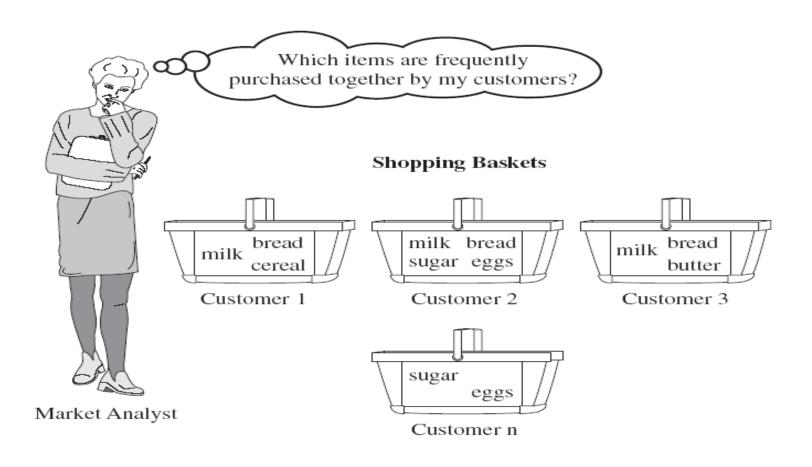
#### **Review**



# Mining Association Rules in Large Databases

- Basic concepts and a road map
- Mining single-dimensional Boolean association rules
- Mining multilevel association rules
- Mining multidimensional association rules
- Summary

## **Market Basket Analysis**



## What Is Association Rules Mining?

#### Association rules mining

 Finding frequent patterns, associations among sets of items or objects in transaction databases, relational databases, and other information repositories.

#### Examples

- What products were often purchased together? Beer and diapers?!
- What DNA segments often occur together in DNA sequences?

## What Is Association Rules Mining?

- Where does the data come from?
  - supermarket transactions, membership cards, discount coupons, customer complaint calls
- Applications
  - Basket data analysis
  - Cross-marketing
  - Catalog design
  - Sale campaign analysis
  - Web log (click stream) analysis
  - DNA sequence analysis

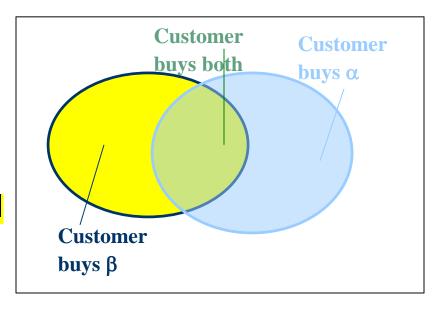
## **Basic Concepts**

Transaction-id	Items bought
10	A, B, D
20	A, C, D
30	A, D, E
40	B, E, F
50	B, C, D, E, F

- Item collection  $X = \{x_1, ..., x_m\}$
- Itemset: a set of items, k-itemset
- Transaction T ⊆ X, each T associates a unique Tid and items bought by a customer
- Rule form  $\alpha => \beta$ ,  $\alpha \subset X$ ,  $\beta \subset X$ ,  $\alpha \cap \beta = \emptyset$

## **Basic Concepts**

- support, s, probability that a transaction contains α and β
  - support  $(\alpha => \beta) = P(\alpha \cap \beta)$
- Frequent itemset, occurrence greater than a min\_support
- Frequent itemset mining, find all the rules  $\alpha => \beta$  satisfying min\_support
- Let sup<sub>min</sub> = 50%, frequent Itemsets {A:3, B:3, D:4, E:3, AD:3}
   support (A) = 3/5 = 60%, support (AD) = 3/5 = 60%



## **Basic Concepts**

confidence, c, conditional probability that a transaction having  $\alpha$  also contains  $\beta$ 

$$\frac{\mathsf{P}(\alpha \cap \beta)}{\mathsf{Confidence}(\alpha => \beta) = \mathsf{P}(\beta \mid \alpha) = \frac{\mathsf{P}(\alpha \cap \beta)}{\mathsf{P}(\alpha)} = \frac{\mathsf{count}(\alpha \cap \beta)}{\mathsf{count}(\alpha)}$$

- Measure of rule interestingness
- Rules satisfy min\_support and min\_confidence are strong
- Let sup<sub>min</sub> = 50%, conf<sub>min</sub> = 50%, frequent itemsets {A:3, B:3, D:4, E:3, AD:3} Association rules:

### **Interestingness Measure: Correlations (Lift)**

- play basketball ⇒ eat cereal [40%, 66.7%] is misleading
  - The overall % of students eating cereal is 75% > 66.7%.
- Measure of dependent/correlated events: lift

$$lift = \frac{P(A \cap B)}{P(A)P(B)}$$

	Basketball	Not basketball	Sum (row)
Cereal	2000	1750	3750
Not cereal	1000	250	1250
Sum(col.)	3000	2000	5000

$$lift(B,C) = \frac{2000/5000}{3000/5000*3750/5000} = 0.89 \quad lift(B,\neg C) = \frac{1000/5000}{3000/5000*1250/5000} = 1.33$$

## **Association Rule Mining: A Road Map**

- Boolean vs. quantitative associations (based on the types of values handled)
  - Boolean association rules, only concern presence or absence of items, buys(x, "SQLServer") ^ buys(x, "DMBook") => buys(x, "DBMiner") [0.2%, 60%]
  - Quantitative association rules, concern quantitative attributes, age(x, "30...39") ^ income(x, "42...48K") => buys(x, "high resolution TV") [1%, 75%]
- Single level vs. multiple-level analysis (based on the levels of abstraction involved)
  - age(x, "30...39") => buys(x, "laptop computer")
  - age(x, "30...39") => buys(x, "computer")
- Single dimension vs. multiple dimensional associations (based on dimensions involved)

# Mining Association Rules in Large Databases

- Basic concepts and a road map
- Mining single-dimensional Boolean association rules
- Mining multilevel association rules
- Mining multidimensional association rules
- Summary

## **Handling Exponential Complexity**

- Given n transactions and m different items:
  - Number of possible association rules:  $O(2^m)$
  - Computation complexity:  $O(nm2^m)$
- Apriori Principle
  - Collect single item counts, find large items
  - Find candidate pairs, count them => large pairs of items
  - Find candidate triplets, count them => large triplets of items, And so on...
  - Guiding Principle: Every subset of a frequent itemset has to be frequent
    - Used for pruning many candidates

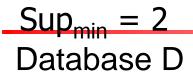
## **Apriori: A Candidate Generation-and-Test Approach**

- Apriori uses prior knowledge of frequent itemsets
- Iterative approach, level-wise search
- The Apriori property (downward closure property, antimonotone) of frequent patterns
  - Any subset of a frequent itemset must be frequent
  - If any itemset is infrequent, its superset should not be generated/tested
  - If {beer, diaper, nuts} is frequent, so is {beer, diaper}, every transaction having {beer, diaper, nuts} also contains {beer, diaper}
  - If {beer, diaper} is infrequent, {beer, diaper, nut} cannot be frequent at all

## **Apriori: A Candidate Generation-and-Test Approach**

#### Method:

- Initially, scan DB once to get frequent 1-itemset
- Generate length (k+1) candidate itemsets from length k frequent itemsets
- Test the candidates against DB
- Terminate when no frequent or candidate set can be generated



Tid	Items	
10	A, C, D	
20	B, C, E	
30	A, B, C, E	
40	B, E	

 $C_{I}$ 1st scan

Itemset	sup
{A}	2
{B}	3
{C}	3
{D}	1
{E}	3

	Itemset	sup
$L_1$	{A}	2
	{B}	3
<b>→</b> [	{C}	3
	{E}	3

Itemset	sup
{A, C}	2
{B, C}	2
{B, E}	3
{C, E}	2

2	Itemset	sup
	{A, B}	1
	{A, C}	2
	{A, E}	1
	{B, C}	2
	{B, E}	3
	{C, E}	2

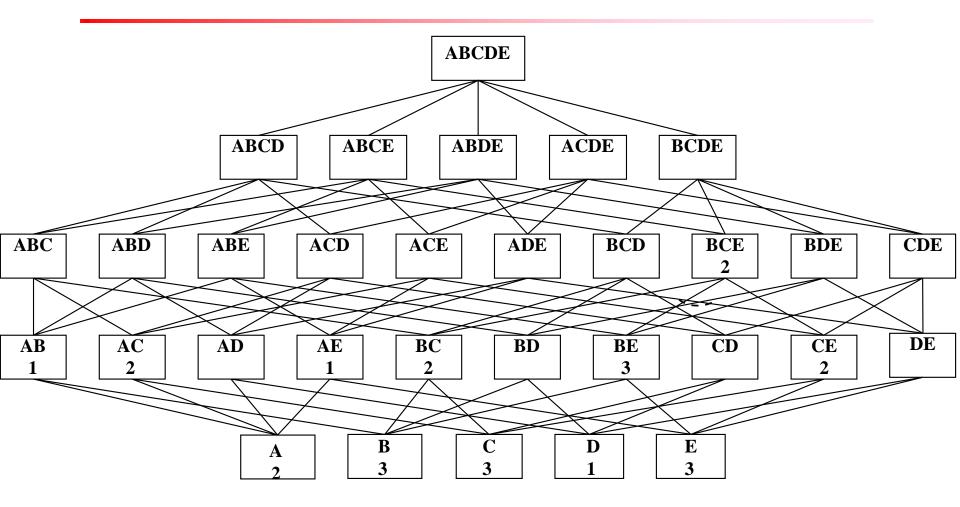
 $\begin{array}{c|c} C_2 \\ \hline 2^{\text{nd}} \ \text{scan} \\ \hline & \{\text{A, B}\} \\ \hline & \{\text{A, C}\} \\ \hline & \{\text{B, C}\} \\ \hline & \{\text{B, E}\} \\ \hline & \{\text{C, E}\} \\ \end{array}$ 

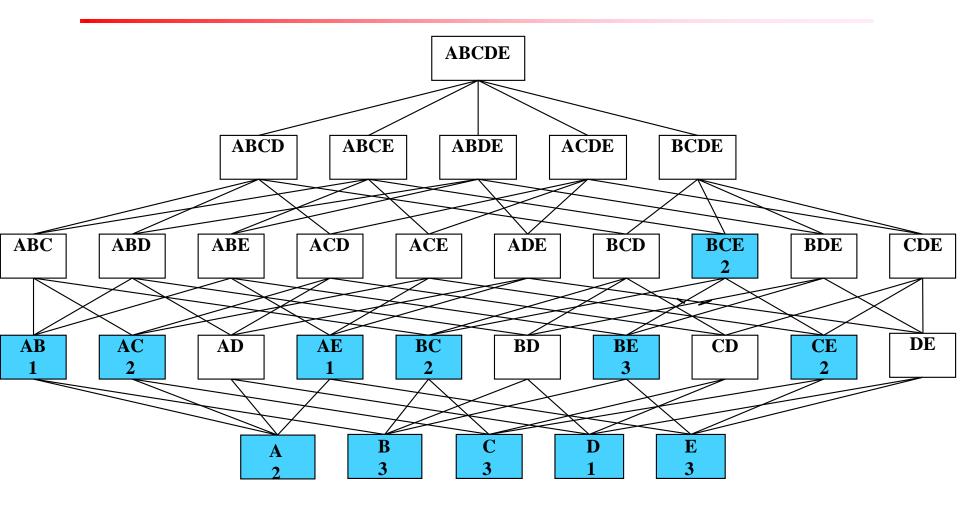
$C_3$	Itemset
2018/10/30	{B, C, E}

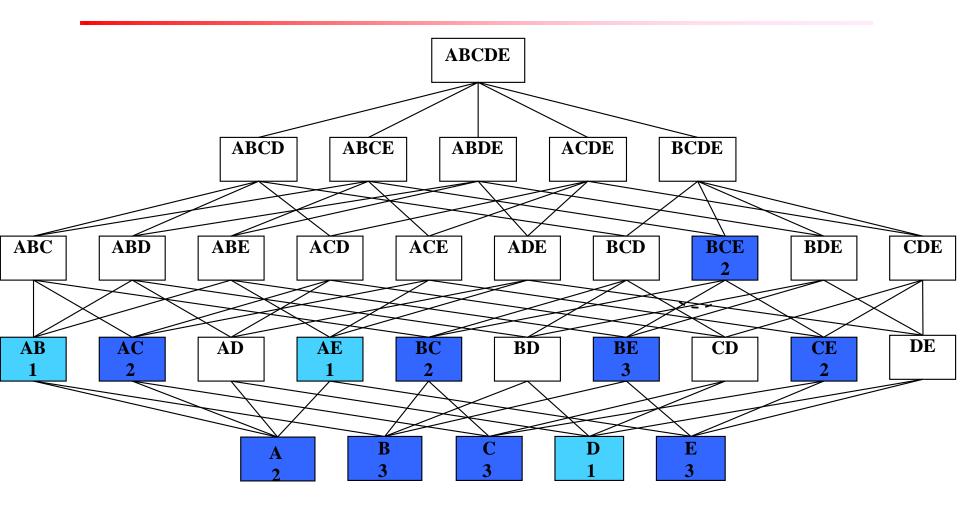
3<sup>rd</sup> scan<sup>3</sup>

Itemset	sup	
{B, C, E}	2	

Itemset	sup
{B, C, E}	2







## **Apriori Algorithm**

#### Pseudo-code $C_k$ : Candidate itemset of size k $L_k$ : frequent itemset of size k Input: Database *D*, *min\_sup* Output: frequent itemsets L $L_1 = \{ \text{frequent single items from } D \};$ for $(k = 2; L_{k-1}! = \varnothing; k++)$ do begin $C_k$ = candidates generated from $L_{k-1}$ ; for each transaction $t \in D$ do increment the count of all candidates in $C_k$ which are contained in t end $L_k$ = candidates in $C_k$ with min\_support end return $L = \bigcup_k L_k$ ;

#### **How to Generate Candidates?**

- How to generate candidates?
  - Step 1: self-joining L<sub>k</sub>
  - Step 2: pruning
- Example
  - L<sub>3</sub>={abc, abd, acd, ace, bcd}
  - Self-joining: L<sub>3</sub>\*L<sub>3</sub>
    - abc and abd -> abcd, acd and ace -> acde
  - Pruning:
    - acde is pruned because ade is not in L<sub>3</sub>
  - C<sub>4</sub>={abcd}

#### **How to Generate Candidates?**

- Suppose the items in  $L_{k-1}$  are listed in order

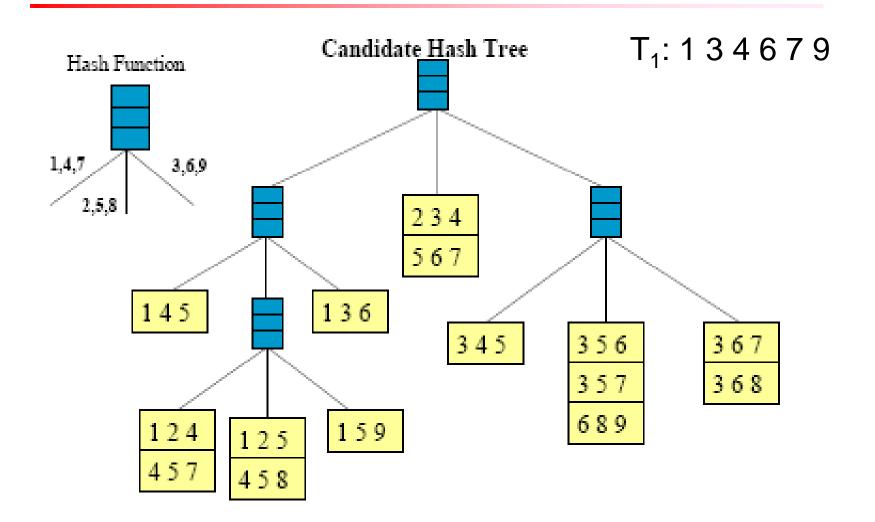
forall (k-1)-subsets s of c do

if  $(s \text{ is not in } L_{k-1})$  then delete c

## **How to Count Supports of Candidates?**

- Why counting supports of candidates a problem?
  - The total number of candidates can be very huge
  - One transaction may contain many candidates
- Method:
  - Candidate itemsets are stored in a hash-tree
  - Leaf node of hash-tree contains a list of itemsets and counts
  - Interior node contains a hash table

### **Example: Counting Supports of Candidates**



#### **Exercise**

1. A database has 9 transactions. Let *min\_sup* = 20%. Please present all the candidates and frequent itemsets at each iteration.

TID	List of items_IDs	
T100	11,12,15	
T200	12,14	
T300	12,13	
T400	11,12,14	
T500	I1,I3	
T600	12,13	
T700	I1,I3	
T800	11,12,13,15	
T900	11,12,13	

## **Challenges of Frequent Pattern Mining**

#### Challenges

- Multiple scans of transaction database
- Huge number of candidates
- Tedious workload of support counting for candidates

#### Improving Apriori

- Reduce passes of transaction database scans
- Shrink number of candidates
- Facilitate support counting of candidates

## **Partition: Scan Database Only Twice**

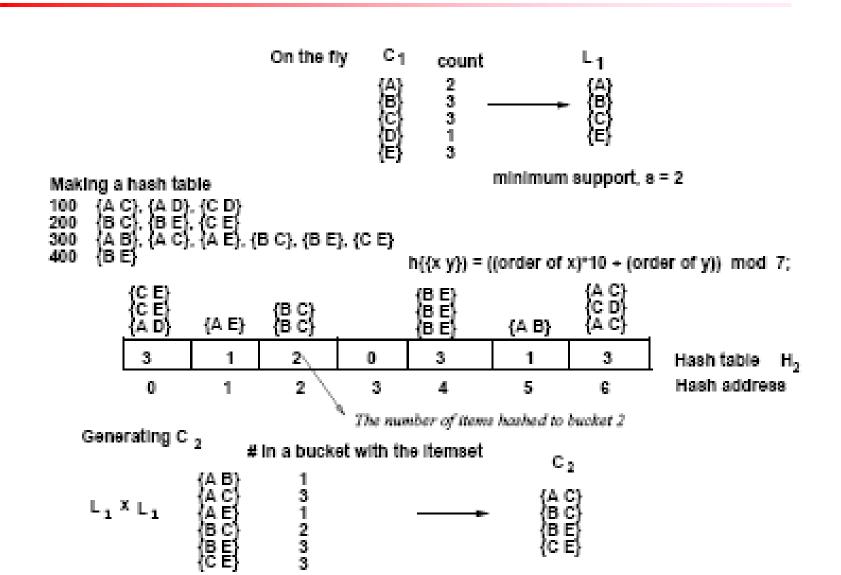
- A. Savasere, E. Omiecinski, and S. Navathe. An efficient algorithm for mining association in large databases. In VLDB'95.
- Partitioning technique
  - Partition the data into N small partitions
  - Phase 1: find local frequent itemsets on each data partition.
     Record all local frequent itemsets.
  - Phase 2: Integrate all local frequent itemsets, scan database, find global frequent itemsets.
- Correctness: Any itemset that is potentially frequent in DB must be frequent in at least one of the partitions

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## Partition: Scan Database Only Twice

- Each partition can be fit into memory
- Scan database only twice! Reduce I/O cost!
- Execution time scales linearly
- Good for very large-scale database
- Applicable to parallel/distributed computing systems
  - Each processor performs FIM on its local data
  - Central server aggregates local frequent itemsets, broadcast potential global itemsets
  - Each processor scans local data to count the frequency
  - Central server aggregates the counts, find the global itemsets

- J. Park, M. Chen, and P. Yu. An effective hash-based algorithm for mining association rules. In SIGMOD'95
- Hash-based technique
  - When scanning transactions to generate frequent k-itemsets,  $L_k$ , generate all (k+1)-itemsets for each transaction
  - Hash all (k+1)-itemsets into buckets, increase bucket count
  - If a (k+1)-itemset bucket count is below  $min\_sup$ , it must be removed from (k+1) candidate itemsets,  $C_{k+1}$
- Correctness: A k-itemset whose corresponding hashing bucket count is below the threshold cannot be frequent



#### Pros

- Reduce the number of candidates,  $C_k$ , especially for  $C_2$ . Size of  $C_2$  is usually huge, reduce  $C_2$  is crucial
- Execution time scales linearly when varying the size of data

Comparison of time (T15.I4.D100)

	Apriori	DHP
	number	number
$L_1$	820	820
$C_2$	335,790	338
$L_2$	207	207
$C_3$	618	618
$L_3$	201	201
$C_4$	184	184
$L_4$	98	98
$C_{5}$	30	30
$L_5$	23	23
$C_6$	1	1
$L_6$	1	1
total time	39.39	13.91

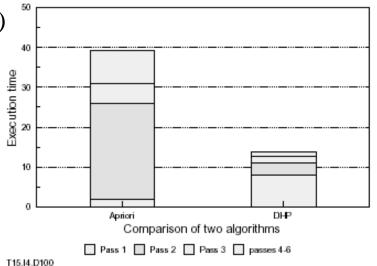
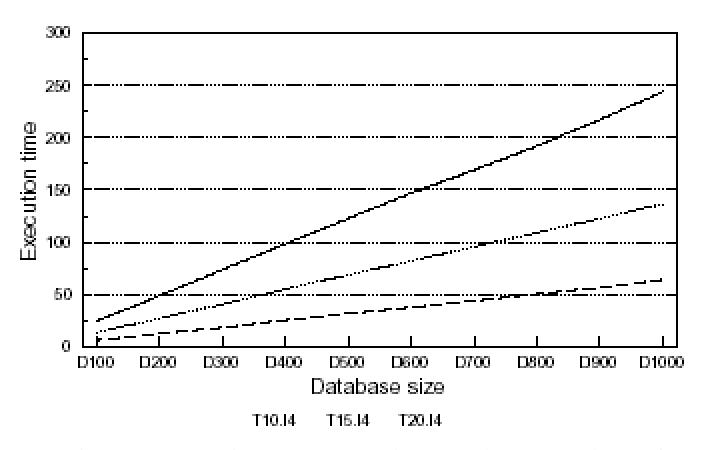


Figure 8: Execution time of Apriori and DHP

Comparison of time (T15.I4.D100)



Performance of DHP when increasing the size of database

#### Cons

- Consume more memory, for hash table
- The larger the hash table, the smaller C<sub>k</sub> and L<sub>k</sub>

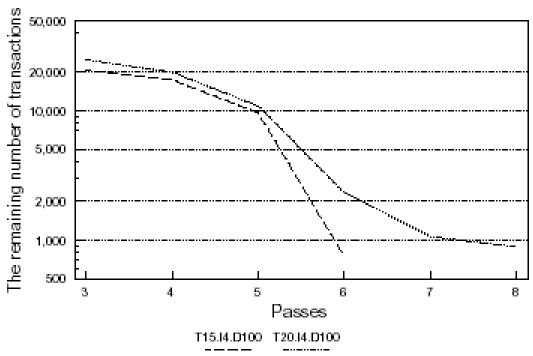
Results from varying hash table sizes (T10.I4.D100)

$H_2$	524,288	262,144	131,072	95,536	32,768
$L_1$	559	559	559	559	559
$ \{H_2 \geq s\} $	58	61	75	96	182
$C_2$	81	120	199	394	1355
$L_2$	45	45	45	45	45
$\alpha$	0.0314	0.0320	0.0345	0.0386	0.0545
size of $D_3$	498KB	$500 \mathrm{KB}$	507KB	539KB	603KB
$ D_3 $	19,732	19,741	19,755	20,501	21,607
total time	6.44	6.43	6.24	6.77	7.23

#### **Transaction Reduction**

- J. Park, M. Chen, and P. Yu. An effective hash-based algorithm for mining association rules. In SIGMOD'95
- Transaction reduction
  - When scanning transactions to generate frequent k-itemsets, L<sub>k</sub>, mark the transaction that contains no k-candidate
  - Remove all the marked transaction
  - The number of transactions drops dramatically

#### **Transaction Reduction**



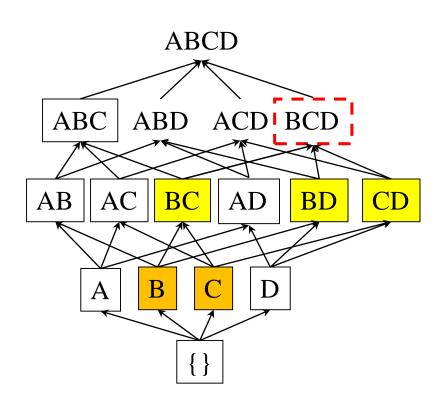
The number of original tx's: 100,000 s=0.75%

The remaining number of transaction in each pass

#### **DIC: Reduce Number of Scans**

- S. Brin, R. Motwani, J. Ullman, and S. Tsur. Dynamic itemset counting and implication rules for market basket data. In SIGMOD'97
- Sergey Brin, founder of Google!
- Partition database into blocks marked by starting points
- New candidate can be added at any starting point once all its subsets are determined frequent
- Reduce the number of database scans

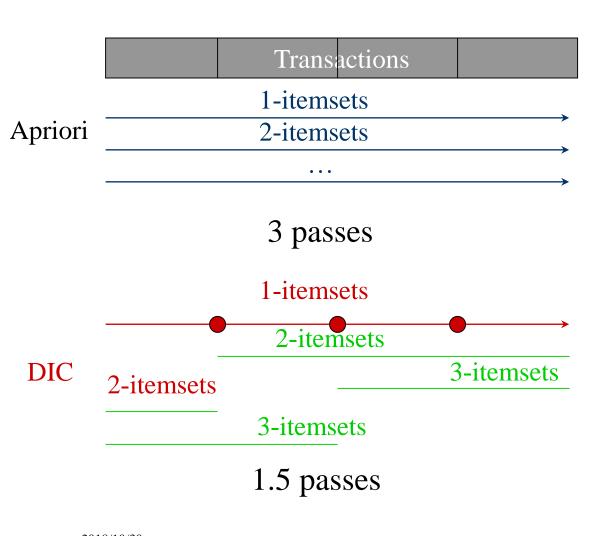
#### **DIC: Reduce Number of Scans**



Itemset lattice

- Once both B and C are determined frequent, new candidate BC is added, the counting of BC begins at the next starting point
- Once all length-2 subsets
   of BCD are determined
   frequent, new candidate
   BCD is added, the counting
   of BCD begins at the next
   starting point

#### **DIC: Reduce Number of Scans**



- Assume 40000 transactions, 4 partitions
- Begin counting 2-itemsets after the first 10000 have been read
- Begin counting 3-itemsets after the first 20000 have been read
- Scan database again, count 2 and 3-itemsets
- After 10000 transactions, finish counting 2-itemsets
- After 20000 transactions, finish counting 3-itemsets

#### **Exercise**

2. A database has 9 transactions. Let *min\_sup* = 20%. Please present all the frequent itemsets generated by DIC in the first iteration. (Note: partition the data into 3 blocks)

TID	List of items_IDs	
T100	l1,l2,l5	
T200	12,14	
T300	12,13	
T400	11,12,14	
T500	I1,I3	
T600	12,13	
T700	I1,I3	
T800	11,12,13,15	
T900	11,12,13	

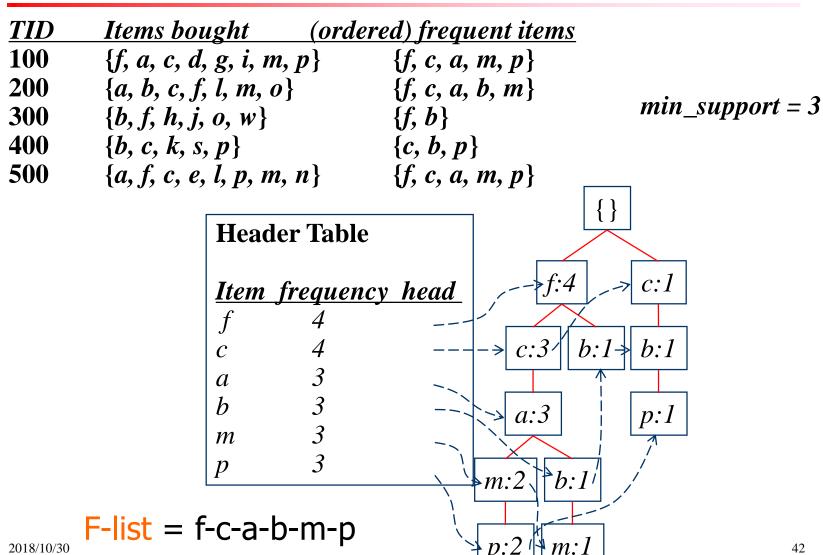
# **Bottleneck of Frequent-pattern Mining**

- Multiple database scans are costly
- Mining long patterns needs many passes of scanning and generates lots of candidates
  - To find frequent itemset  $i_1i_2...i_{100}$ 
    - # of scans: 100
    - # of Candidates:  $\binom{1}{100} + \binom{1}{100} + \dots + \binom{1}{1000} = 2^{100} 1 = 1.27*10^{30}!$
- Bottleneck: candidate-generation-and-test
- Can we avoid candidate generation?

# Construct FP-tree from a Transaction Database

- Scan DB once, find frequent 1-itemset (single item pattern)
- Sort frequent items in frequency descending order L
- Create the root of the tree, labeled with "null"
- Scan DB again, sort each transaction in L order, a branch is created for each transaction
  - Increment the count of each node along a common prefix by 1
  - Create nodes for the items following the prefix
- Build a header table, connect each item point in the tree

# Construct FP-tree from a Transaction **Database**



# Construct FP-tree from a Transaction Database

- 1. Scan the transaction database D once. Collect F, the set of frequent items, and their support counts. Sort F in support count descending order as L, the list of frequent items.
- 2. Create the root of an FP-tree, and label it as "null." For each transaction *Trans* in *D* do the following:
  - Select and sort the frequent items in *Trans* according to the order of *L*. Let the sorted frequent item list in the *Trans* be [p|P], where p is the first element and P is the remaining list.
  - Call insert\_tree ([p|P], T), which is performed as follows. If T has a child N such that N.item-name = p.item-name, then increment N's count by 1; else create a new node N, and let its count be 1, its parent link be linked to T, and its node-link to the nodes with the same item-name via the node-link structure.
  - If P is nonempty, call insert\_tree(P, N) recursively.

#### **Benefits of the FP-tree Structure**

#### Completeness

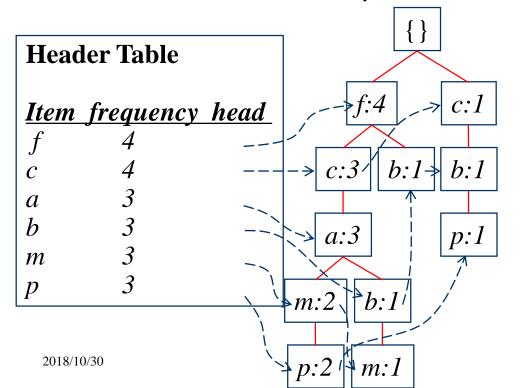
- Preserve complete information for frequent pattern mining
- Never break a long pattern of any transaction

#### Compactness

- Reduce irrelevant info—infrequent items are gone
- Items in frequency descending order: the more frequently occurring, the more likely to be shared
- Never be larger than the original database

#### **Construct Conditional Pattern Base**

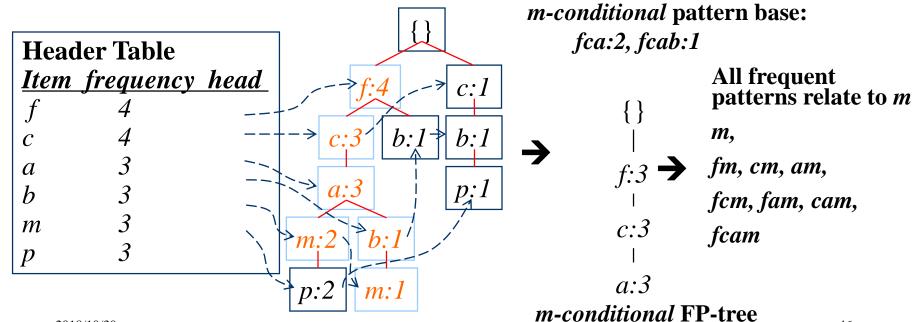
- Start at the frequent item header table in the FP-tree
- Traverse the FP-tree by following the link of each frequent item x
- Accumulate all of transformed prefix paths of item x into form x's conditional pattern base



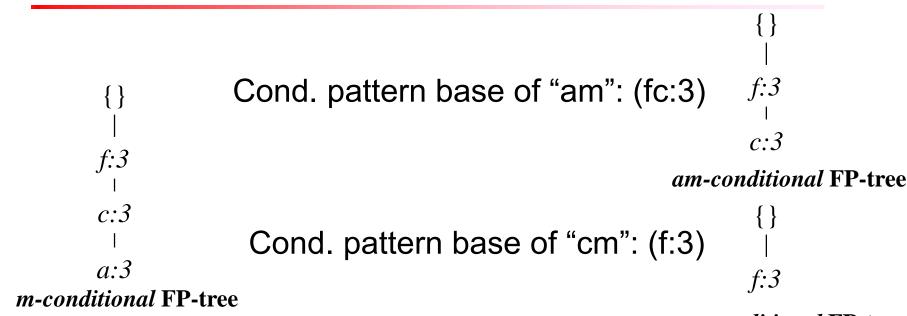
# conditional pattern bases item cond. pattern base c f:3 a fc:3 b fca:1, f:1, c:1 m fca:2, fcab:1 p fcam:2, cb:1

# From Conditional Pattern-bases to Conditional FP-trees

- For each pattern-base
  - Accumulate the count for each item in the base
  - Construct the FP-tree for the frequent items of the pattern base



#### **Recursion: Conditional FP-tree**



cm-conditional FP-tree

Cond. pattern base of "cam": (f:3) 
$$f:3$$

cam-conditional FP-tree

# Mining Frequent Patterns With FPtrees

procedure **FP\_growth**(*Tree,*  $\alpha$ )

- (1) if Tree contains a single path P then
- (2) **for each** combination (denoted as  $\beta$ ) of the nodes in the path *P*
- (3) generate pattern  $\beta \cup \alpha$  with support\_count = minimum support count of nodes in β;
- (4) **else for each**  $a_i$  in the header of *Tree* {
- (5) generate pattern  $\beta = a_i \cup \alpha$  with support\_count =  $a_i$ .support\_count;
- (6) construct  $\beta$ 's conditional pattern base and then  $\beta$ 's conditional FP\_tree  $Tree_{\beta}$ ;
- (7) if  $Tree_{\beta}$  then
- (8) call **FP\_growth**( $Tree_{\beta}$ , $\beta$ ); }

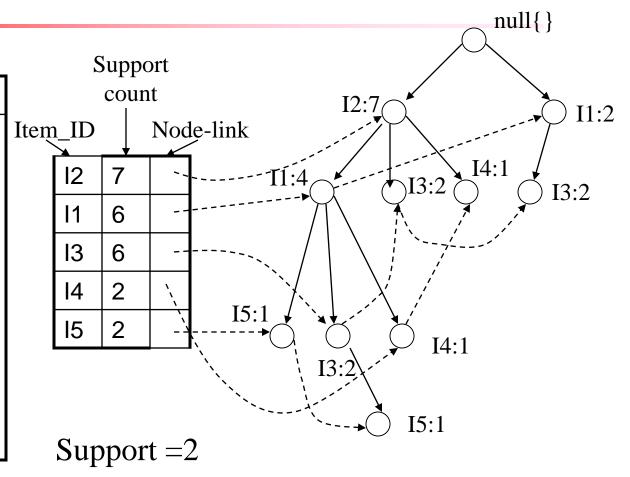
#### **Exercise**

3. A database has 9 transactions. Let *min\_sup* = 20%. Please construct the FP-tree for the database, the conditional FP-trees, and all the frequent itemsets.

TID	List of items_IDs		
T100	11,12,15		
T200	12,14		
T300	12,13		
T400	11,12,14		
T500	I1,I3		
T600	12,13		
T700	I1,I3		
T800	11,12,13,15		
T900	11,12,13		

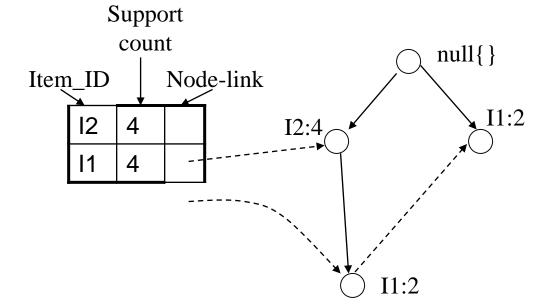
#### **Solution**

TID	List of items_IDs	
T100	11,12,15	
T200	12,14	
T300	12,13	
T400	11,12,14	
T500	I1,I3	
T600	12,13	
T700	I1,I3	
T800	11,12,13,15	
T900	11,12,13	

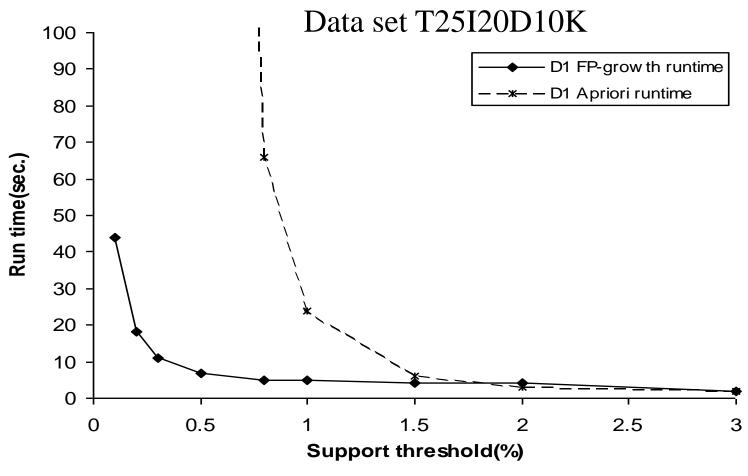


## **Solution**

item	conditional pattern base	conditional FP-tree	frequent patterns generated
15	{{I2,I1: 1}, {I2,I1,I3: 1}}	⟨I2: 2, I1: 2⟩	{12,15: 2}, {11,15: 2}, {12,11,15: 2}
I4	{{I2,I1: 1}, {I2: 1}}	⟨I2: 2⟩	{I2,I4: 2}
I3	{{I2,I1: 2}, {I2: 2}, {I1: 2}}	$\langle 12: 4, 11: 2 \rangle, \langle 11: 2 \rangle$	{12,I3: 4}, {11,I3: 4}, {12,I1,I3: 2}
I1	{{I2: 4}}	⟨I2: 4⟩	{I2,I1: 4}



# FP-Growth vs. Apriori: Scalability With the Support Threshold



# Why Is FP-Growth the Winner?

#### Divide-and-conquer:

- Decompose both the mining task and DB according to the frequent patterns obtained so far
- Focus searching on smaller databases

#### Other factors

- No candidate generation, no candidate test
- Compressed database: FP-tree structure
- Two scans of entire database
- Basic ops—counting local freq items and building sub FP-tree, no pattern search and matching

#### **Cons**

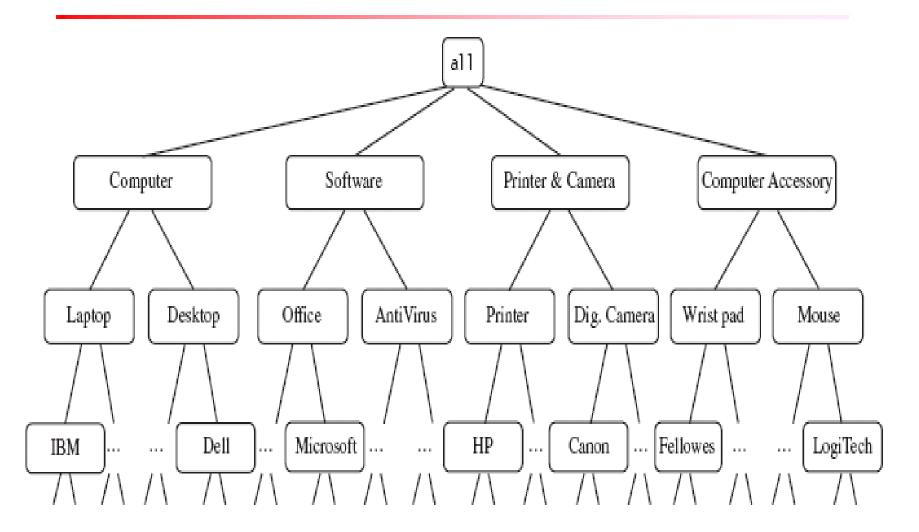
- Building FP-trees
  - A stack of FP-trees
- Redundant information
  - Transaction abcd appears in a-, ab-, abc-, ac-, c-FP-trees

# Mining Association Rules in Large Databases

- Basic concepts and a road map
- Mining single-dimensional Boolean association rules
- Mining multilevel association rules
- Mining multidimensional association rules
- Summary

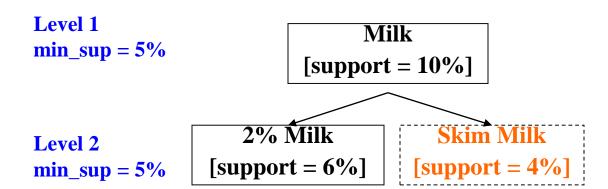
- Association rules at high concept levels may represent common sense knowledge
- Hard to find association rules at low concept level
  - Items at the lower level usually have lower support, less than min\_support threshold
- Mining association rules at multiple levels of abstraction
- Example: sales in AllElectronics store computer sector

# **Example**

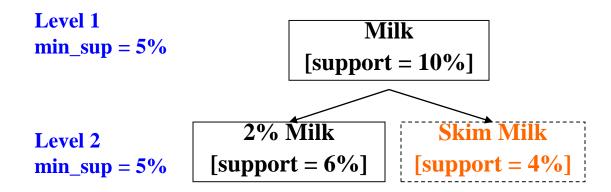


- Uniform support
  - Top-down, level-wise
  - Use uniform minimum support for each level
  - Perform Apriori at each level
  - Optimization: if an ancestor is infrequent, the search on the descendants can be avoided

#### uniform support



#### uniform support

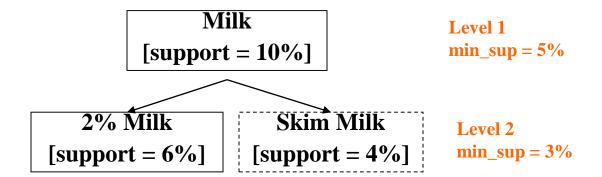


#### Drawbacks

- Miss interesting associations with too high threshold
- Generate too many uninteresting rules with too low threshold

- Reduced support
  - Top-down, level-wise
  - Each concept level has its own minimum support threshold
  - The lower level, the smaller threshold
  - Perform Apriori at each level

reduced support



#### Reduced support

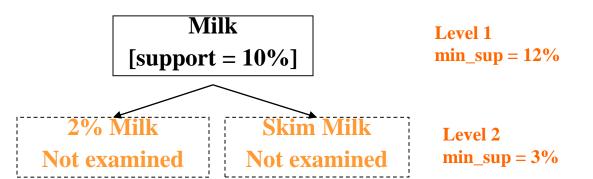
- Optimization -- level-cross filtering by single item
  - An item at the *i*th concept level is examined *iff* its parent concept at the (*i*-1)th level is frequent
  - If a concept is infrequent, its descendents are pruned from the database
  - Drawbacks

2018/10/30

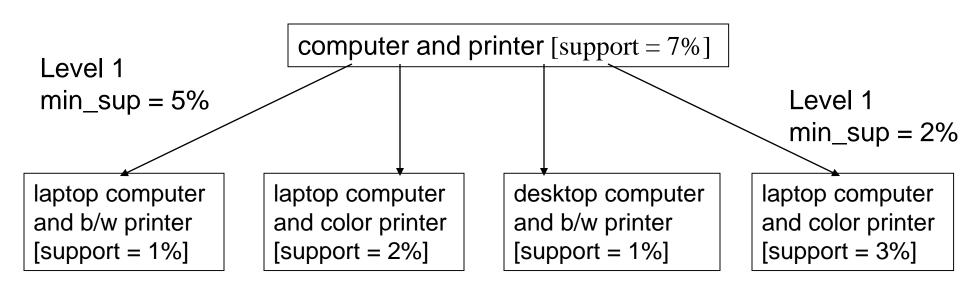
 Miss associations at low level items which are frequent based on a reduced min\_support, but whose ancestors do not satisfy min\_support

reduced support

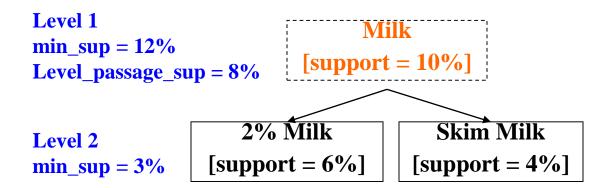
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- Reduced support
  - Optimization -- level-cross filtering by k-itemset
    - Only the children of frequent k-itemsets are examined
    - Drawback: many valuable patterns may be filtered out



- Reduced support
  - Optimization -- Controlled level-cross filtering by single item
    - next level min sup < level passage threshold < min sup</li>
    - Allow the children of items that do not satisfy the min\_sup to be examined if they satisfy the level passage threshold



# **Multi-level Association: Redundancy Filtering**

- Some rules may be redundant due to "ancestor" relationships between items
- Example
  - milk ⇒ wheat bread [support = 8%, confidence = 70%]
  - 2% milk ⇒ wheat bread [support = 2%, confidence = 72%]
- We say the first rule is an ancestor of the second rule
- A rule is redundant if its support is close to the "expected" value, based on the rule's ancestor

# Mining Association Rules in Large Databases

- Basic concepts and a road map
- Mining single-dimensional Boolean association rules
- Mining multilevel association rules
- Mining multidimensional association rules
- Summary

# Mining Multi-Dimensional Association

Single-dimensional rules:

```
buys(X, "milk") \Rightarrow buys(X, "bread")
```

- Multi-dimensional rules: ≥ 2 dimensions or predicates
  - Inter-dimension assoc. rules (no repeated predicates)

```
age(X,"19-25") \land occupation(X,"student") \Rightarrow buys(X, "coke")
```

hybrid-dimension assoc. rules (repeated predicates)

```
age(X,"19-25") \land buys(X, "popcorn") \Rightarrow buys(X, "coke")
```

- Categorical Attributes: finite number of possible values, no ordering among values
- Quantitative Attributes: numeric, implicit ordering among values — discretization, clustering approaches

## **Mining Quantitative Associations**

- Techniques can be used to categorize numerical attributes
  - Static discretization based on predefined concept hierarchies
  - Dynamic discretization based on data distribution
  - Clustering: Distance-based association
    - one dimensional clustering then association

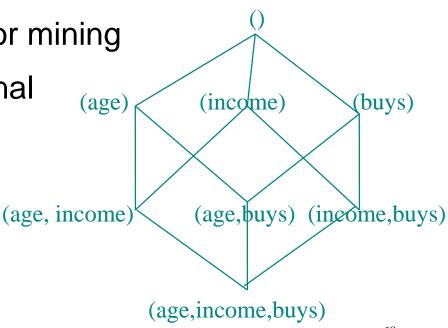
#### Static Discretization of Quantitative Attributes

- Discretized prior to mining using concept hierarchy
- Numeric values are replaced by ranges
- In relational database, finding all frequent k-predicate sets will require k or k+1 table scans

Data cube is well suited for mining

The cells of a n-dimensional cuboid correspond to the dimensions

Mining from data cubes can be much faster



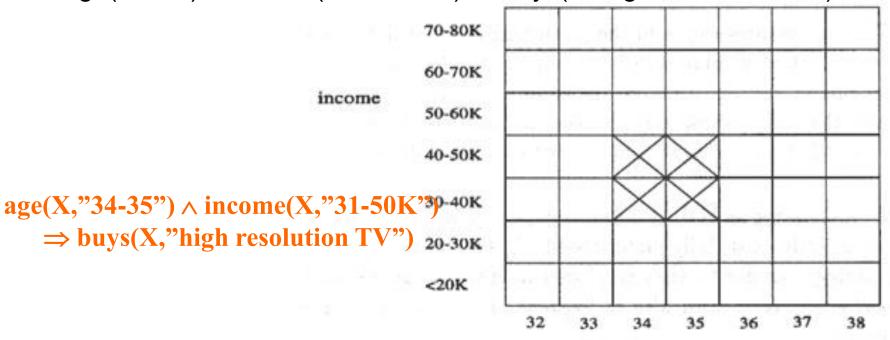
## **Quantitative Association Rules**

- Numeric attributes are dynamically discretized
  - Such that the confidence or compactness of the rules mined is maximized
- 2-D quantitative association rules:  $A_{quan1} \land A_{quan2} \Rightarrow A_{cat}$
- Association rule clustering system (ARCS)
  - Binning: 2-D grid, manageable size
  - Finding frequent predicate sets: scan the database, count the support for each grid cell
  - Clustering the rules: cluster adjacent cells to form a rule

## **Quantitative Association Rules**

#### Example

```
age(X,"34") \land income(X,"31-40K") \Rightarrow buys(X,"high resolution TV") age(X,"35") \land income(X,"31-40K") \Rightarrow buys(X,"high resolution TV") age(X,"34") \land income(X,"41-50K") \Rightarrow buys(X,"high resolution TV") age(X,"35") \land income(X,"41-50K") \Rightarrow buys(X,"high resolution TV")
```



# Mining Association Rules in Large Databases

- Basic concepts and a road map
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# **Summary**

- Frequent pattern mining—an important task in data mining
- Scalable frequent pattern mining methods
  - Apriori (Candidate generation & test)
  - Partition, DIC, DHP, etc.
  - Projection-based (FP-growth)
- Mining a variety of rules and interesting patterns