

STAT4001

Data Mining and Stat Learning

Final group project

Academic Year 2019~2020

Group 13

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1. Introduction

This report is divided into two parts:

1. Home buyers were asked about their dream house, several factors were described. These factors are going to be analyzed by different methods, and be used to predict the final price of the houses.
2. On April 15, 1912, the sinking of the Titanic caused 1502 deaths out of 2224 passengers and crews. Some factors are going to be analyzed, to see whether some groups of people were more able to survival than the others. Several methods are used to predict the survival chance of different passengers.

2. Dream House

a. Data Description

i. Data Structure

```
> str(house)
'data.frame': 500 obs. of 15 variables:
 $ Id      : int  1 2 3 4 5 6 7 8 9 10 ...
 $ LotFrontage : int  65 80 68 60 84 85 75 NA 51 50 ...
 $ LotArea   : int  8450 9600 11250 9550 14260 14115 10084 10382 6120 7420 ...
 $ LotShape  : Factor w/ 4 levels "IR1","IR2","IR3",...: 4 4 1 1 1 1 4 1 4 4 ...
 $ OverallCond: int  5 8 5 5 5 5 6 5 6 ...
 $ MasVnrArea : int  196 0 162 0 350 0 186 240 0 0 ...
 $ TotalBsmtSF: int  856 1262 920 756 1145 796 1686 1107 952 991 ...
 $ X1stFlrSF  : int  856 1262 920 961 1145 796 1694 1107 1022 1077 ...
 $ X2ndFlrSF  : int  854 0 866 756 1053 566 0 983 752 0 ...
 $ GrLivArea  : int  1710 1262 1786 1717 2198 1362 1694 2090 1774 1077 ...
 $ TotRmsAbvGrd: int  8 6 6 7 9 5 7 7 8 5 ...
 $ GarageArea  : int  548 460 608 642 836 480 636 484 468 205 ...
 $ WoodDecksSF: int  0 298 0 0 192 40 255 235 90 0 ...
 $ OpenPorchSF : int  61 0 42 35 84 30 57 204 0 4 ...
 $ SalePrice   : int  208500 181500 223500 140000 250000 143000 307000 200000 129900 118000
```

Figure1

From the structure of “House.xlsx”, there are 500 observations and 15 variables. The “SalePrice” is the dependent variable and the others are independent variables. “Id” is omitted in the model fitting and prediction process.

ii. Variables Correlation

Before any model is fitted, it is better to generate a correlation matrix to understand the relationship of the variables. “LotShape”, a factor variable, is transformed into an integer variable so as to generate a correlation matrix.

However, there are NAs in several observations. In order to avoid bias, NAs are omitted in the correlation matrix computation. The correlation matrix is shown below.

	Id	LotFrontage	LotArea	LotShape	OverallCond	MasVnArea	TotalBsmtSF	X1stFlrSF	X2ndFlrSF	GrLivArea	TotRmsAbvGrd	GarageArea	WoodDeckSF	OpenPorchSF	SalePrice
Id	1.000000000	-0.03960341	0.019225620	0.02086340	0.071972032	-0.04647010	0.01489591	-0.0428554	0.009948307	-0.02910625	-0.01863534	-0.0258788	-0.0006792171	0.012831353	0.0023859221
LotFrontage	-0.039603459	1.0000000	0.377780072	-0.19484521	-0.13756649	0.17650945	0.36780439	0.40971294	0.109801417	0.04574465	0.36281455	0.3812756	0.1119367753	0.142384364	0.427655383
LotArea	0.0192256199	0.37778007	1.0000000	-0.12793624	-0.064787796	0.00328310	0.25692501	0.27375740	-0.003847152	0.19979832	0.14657921	0.1653141	0.088030601	0.009744772	0.295326480
LotShape	0.020863403	-0.19484521	-0.127936243	1.0000000	0.109103298	-0.12465004	-0.21365525	-0.19200884	-0.089595078	-0.21714805	-0.143953882	-0.2099072	-0.209957523	-0.09670773	-0.279053410
OverallCond	0.0719720318	-0.13756665	-0.064787796	0.10910330	1.0000000	-0.17094583	-0.23458147	-0.21113505	-0.003283083	-0.14957113	-0.11217097	-0.1994241	-0.0539569472	-0.092858436	-0.0024132
MasVnArea	0.017650945	0.003283100	-0.12465004	-0.170945826	1.0000000	0.35020178	0.32827133	0.173604532	0.38223293	0.31896337	0.3500395	0.1801592706	0.096806131	0.4710179	
TotalBsmtSF	0.0148959133	0.36780439	0.256925013	-0.21365525	-0.234581466	1.0000000	0.83054658	0.35020178	0.210550697	0.41993786	0.32591923	0.4885616	0.2664995893	0.159767277	0.670859686
X1stFlrSF	-0.0432855423	0.40971294	0.273757396	-0.19200884	-0.211135053	0.32827133	1.0000000	-0.25400001	0.50886574	0.40155650	0.4758677	0.279227058	0.122028118	0.652023012	
X2ndFlrSF	0.0099483065	0.10980142	-0.003847152	-0.08959508	0.003283083	0.17360453	-0.21055070	1.0000000	0.69592605	0.61558757	0.1870730	0.0655625535	0.223097678	0.319515343	
GrLivArea	-0.0291062517	0.40574465	0.199798319	-0.21714805	-0.149571134	0.38223293	0.41993786	0.5068834	1.0000000	0.84499944	0.5036839	0.2550982852	0.289380645	0.757808501	
TotRmsAbvGrd	-0.0186553363	0.36281455	0.146579207	-0.14395882	-0.112170968	0.31896337	0.32591923	0.40155650	0.615587572	0.84499944	1.0000000	0.3915961	0.1448610912	0.243564721	0.607749977
GarageArea	-0.0258787979	0.38127557	0.165314117	-0.20990716	-0.199424142	0.3500395	0.48856156	0.47586765	0.187073008	0.23000000	0.39159610	1.0000000	0.2796213107	0.211059501	0.699490531
WoodDeckSF	-0.0006792171	0.11199678	0.08803060	-0.20999575	0.053956947	0.18015926	0.26649957	0.25509829	0.14481099	0.2796213	1.000000000	0.116928642	0.3542982156	0.232630424	
OpenPorchSF	0.0128313534	0.14238436	0.009744772	-0.0967077	-0.02958436	0.09680613	0.15976728	0.12202812	0.223097678	0.28938064	0.24356472	0.2110595	0.169286420	0.000000000	0.323630424
SalePrice	0.0028592208	0.42765585	0.295326480	-0.27905341	-0.160381132	0.47101798	0.67085968	0.65202301	0.319515343	0.5780850	0.60774998	0.6994901	0.3542982156	0.323630424	1.000000000

Figure2

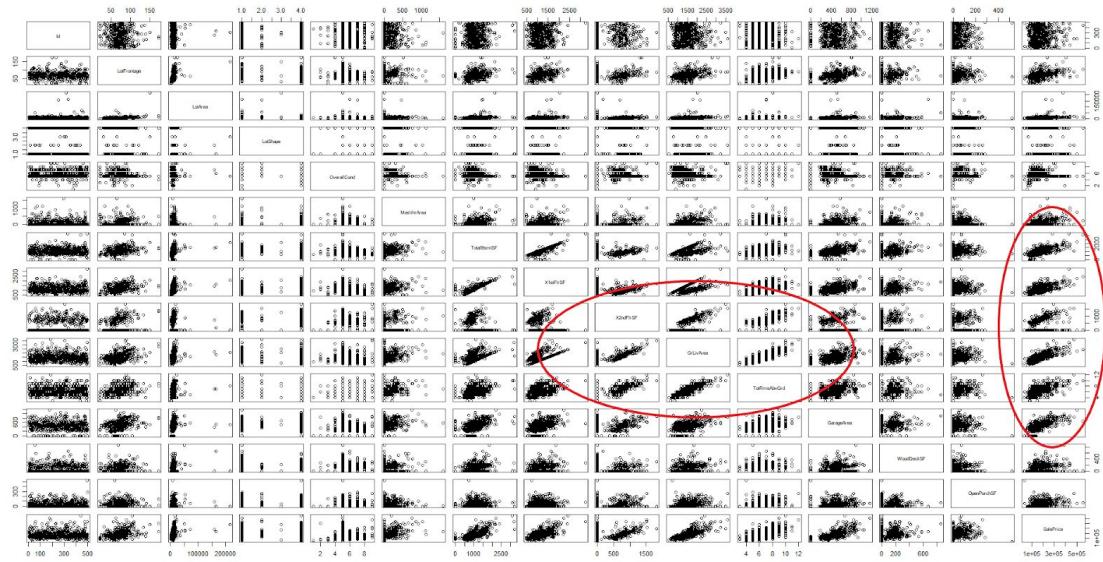


Figure3

After omitting the observations which contain missing value, A correlation matrix can be generated. From the general plot and the correlation matrix, the correlation coefficients between some variables and “SalePrice” are respectively higher. They are “GrLivArea”, “TotalBsmtSF”, “X1stFlrSF”, “TotRmsAbvGrd” and “GarageArea” etc. The correlation coefficients are over 0.6. We hypothesized that those variables will contribute more in model fitting and prediction.

However, the 2 figures also show that “X2ndFlrSF”, “GrLivArea” and “TotRmsAbvGrd” are also highly correlated. The phenomenon may affect the result of regression.

iii. Handling Missing Data

```
> summary(house)
   id      LotFrontage     LotArea    LotShape overallcond
Min. : 1.0  Min. : 21.00  Min. : 1526  IR1:171  Min. :1.000
1st Qu.:125.8 1st Qu.: 60.00  1st Qu.: 7590  IR2: 16  1st Qu.:5.000
Median :250.5  Median : 70.00  Median : 9375  IR3:  3  Median :5.000
Mean   :250.5  Mean   : 70.96  Mean   :11143  Reg:310  Mean   :5.552
3rd Qu.:375.2 3rd Qu.: 82.00  3rd Qu.:1604   3rd Qu.: 6.000
Max.  :500.0  Max.  :174.00  Max.  :215245  Max.  :9.000
NA's   :87

  MasVnrArea TotalBsmtSF xLstFltrSF x2ndFlrSF GrLivArea
Min. : 0.0  Min. : 0       Min. :483   Min. : 0.0  Min. :520
1st Qu.: 0.0  1st Qu.: 796  1st Qu.:884   1st Qu.: 0.0  1st Qu.:1148
Median : 0.0  Median :1016  Median :1096  Median : 0.0  Median :1463
Mean   :112.7  Mean   :1071  Mean   :1162   Mean   :344.5  Mean   :1516
3rd Qu.:180.0 3rd Qu.:1341 3rd Qu.:1392  3rd Qu.: 720.0 3rd Qu.:1767
Max.  :1600.0  Max.  :3206  Max.  :3228   Max.  :1818.0  Max.  :3608
NA's   :1

  TotRmsAbvGrd GarageArea woodDeckSF OpenPorchsF
Min. : 3.000  Min. : 0.0  Min. : 0.00  Min. : 0.00
1st Qu.: 5.000  1st Qu.: 31.0  1st Qu.: 0.00  1st Qu.: 0.00
Median : 6.000  Median : 470.5  Median : 0.00  Median : 27.50
Mean   : 6.486  Mean   : 622.8  Mean   : 94.93  Mean   : 46.89
3rd Qu.: 7.000  3rd Qu.: 576.0  3rd Qu.:168.00  3rd Qu.: 72.00
Max.  :12.000  Max.  :1166.0  Max.  :857.00  Max.  :523.00

  SalePrice
Min. :34900
1st Qu.:128425
Median :165550
Mean   :182517
3rd Qu.:216625
Max.  :555000
```

Figure5

After the simulation, the following model gives the lowest AIC.

```
Step: AIC=2442.01
LotFrontage ~ LotArea + LotShape + x2ndFlrSF + GrLivArea + TotRmsAbvGrd +
GarageArea + woodDeckSF
```

Figure6

Another linear model is fitted with the formula of the above model. The model gives 0.3412 R-squared. while the NAs are predicted by the model, the predicted values are rounded off since “LotFrontage” is integer. The NAs values of “LotFrontage” are substituted by the predicted value.

The same method is applied to the NA of “MasVnrArea”. A linear regression model is fitted with the formula: “MasVnrArea ~ .” The NA value of “MasVnrArea” is substituted by the predicted value.

From the summary of the dataset “House.xlsx”, there are 87 NAs in variable “LotFrontage” and 1 NA in “MasVnrArea. A linear regression model is fitted for “LotFrontage” against other variables without “Id”. However, the R-squared of the model is only 0.3451. To simplify the model, backward stepwise selection is applied.

b. Modeling

i. Linear Regression

Linear regression is using the least square method to minimize the residuals between a dependent variable (usually presented as y) and one or more independent variables (usually presented as x). The model is fitted using linear predictor functions whose unknown coefficients are estimated from the data through Linear regression.

```
numfolds = trainControl( method = "cv", number = 10)
cv_lin_reg = train(SalePrice ~ ., data = house_train,method = 'lm',trControl = numfolds)
```

Figure7

By using 10-folds cross-validation, we analyze the house training data set through linear regression.

```
> summary(cv_lin_reg)

Call:
lm(formula = .outcome ~ ., data = dat)

Residuals:
    Min      1Q  Median      3Q     Max 
-106510 -17523   -2107   17779  181331 

Coefficients:
            Estimate Std. Error t value Pr(>|t|)    
(Intercept) -5.773e+04  1.409e+04 -4.098 5.09e-05 ***
LotFrontage -1.239e+02  1.078e+02 -1.149 0.25115  
LotArea      2.689e-01  1.540e-01  1.747 0.08151 .  
LotShapeIR2  2.201e+04  9.696e+03  2.270 0.02379 *  
LotShapeIR3  9.215e+03  2.922e+04  0.315 0.75263  
LotShapeReg -7.385e+03  3.927e+03 -1.880 0.06080 .  
OverallCond  5.049e+03  1.595e+03  3.166 0.00167 ** 
MasVnrArea   4.487e+01  1.039e+01  4.318 2.01e-05 *** 
TotalBsmtSF  5.172e+01  7.423e+00  6.968 1.40e-11 *** 
X1stFlrSF    5.953e+01  2.917e+01  2.041 0.04198 *  
X2ndFlrSF    5.167e+01  2.833e+01  1.824 0.06893 .  
GrLivArea    2.169e+01  2.781e+01  0.780 0.43590  
TotRmsAbvGrd -1.093e+03  2.167e+03 -0.505 0.61415  
GarageArea    9.598e+01  1.079e+01  8.891 < 2e-16 *** 
WoodDeckSF   1.892e+01  1.559e+01  1.213 0.22576  
OpenPorchSF   6.590e+01  2.925e+01  2.253 0.02480 *  
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 35390 on 384 degrees of freedom
Multiple R-squared:  0.7975,    Adjusted R-squared:  0.7895 
F-statistic: 100.8 on 15 and 384 DF,  p-value: < 2.2e-16
```

Figure8

Some of the variables including "LotFrontage", "LotShapeIR3", "GrLivArea", "TotRmsAbvGrd" and "WoodDeckSF" are not statistical significantly by linear regression.

```
> RMSE  
[1] 103246.81 100708.90 100549.93 101034.30 103445.36 101063.15 97936.75 104606.54 104799.64 104268.73
```

Figure9

```
> lm(SalePrice ~ TotalBsmtSF + X1stFlrSF + X2ndFlrSF + GarageArea, data = house_train)  
Call:  
lm(formula = SalePrice ~ TotalBsmtSF + X1stFlrSF + X2ndFlrSF +  
    GarageArea, data = house_train)  
Coefficients:  
(Intercept) TotalBsmtSF X1stFlrSF X2ndFlrSF GarageArea  
-47191.12 58.65 80.01 79.64 101.70
```

Figure10

The RMSE of each round is shown above. Using Stepwise regression, the AIC is around 9000 on average. The best tune of the linear regression is four, including "TotalBsmtSF", "X1stFlrSF", "X2ndFlrSF" and "GarageArea" through modelling selection. Comparing the AIC and BIC of the lm1(before tuning) and lm2(after tuning), we can see that BIC decreased while AIC increased. One possible is the high cross-validation prediction error.

```
> AIC(lm1, lm2)  
      df      AIC  
lm1 17 9532.222  
lm2  6 9565.882  
> BIC(lm1, lm2)  
      df      BIC  
lm1 17 9600.077  
lm2  6 9589.830
```

Figure11

cross-validation

```
> print(cv_lin_reg)
Linear Regression

400 samples
 13 predictor

No pre-processing
Resampling: Cross-Validated (10 fold)
Summary of sample sizes: 360, 360, 360, 360, 360, 360, ...
Resampling results:

RMSE      Rsquared     MAE
37088.35  0.7864601  27035.66

Tuning parameter 'intercept' was held constant at a value of TRUE
```

Figure12

	RMSE <dbl>
RMSE of 1 st folds	29654.37
RMSE of 2 st folds	33912.28
RMSE of 3 st folds	35389.20
RMSE of 4 st folds	31047.64
RMSE of 5 st folds	42714.44
RMSE of 6 st folds	37140.67
RMSE of 7 st folds	36799.68
RMSE of 8 st folds	39586.24
RMSE of 9 st folds	41019.15
RMSE of 10 st folds	36069.85

Figure13

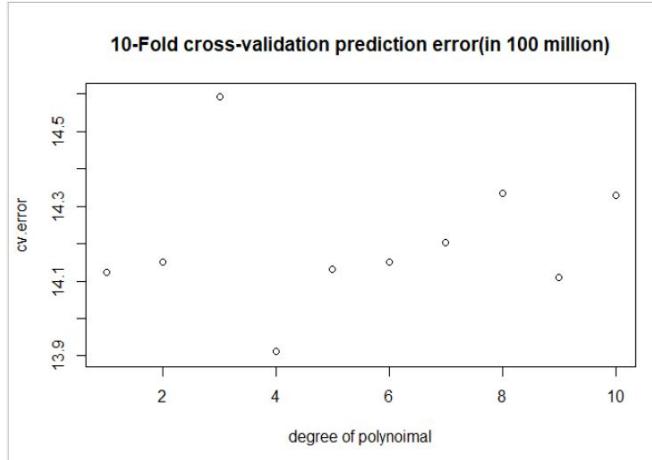


Figure14

A 10-folds cross-validation is applied to find out the best predictive model in 400 samples. Regarding the graph, the root-mean-square error (RMSE) is 37088.35. Also, the cross-validation prediction errors are extremely large, each value is more than 1 billion. The smallest one is around 1.39 billion (the fourth one), but still very large. It is believed that the complexity and diversity of data type contribute to the skyhigh prediction error.

```
> cv_error
[1,] 1426749555
[2,] 1456734986
[3,] 1431176949
[4,] 1435063782
[5,] 1468528152
[6,] 1443299772
[7,] 1431657332
[8,] 1438022963
[9,] 1450108186
[10,] 1438041432
```

Figure15

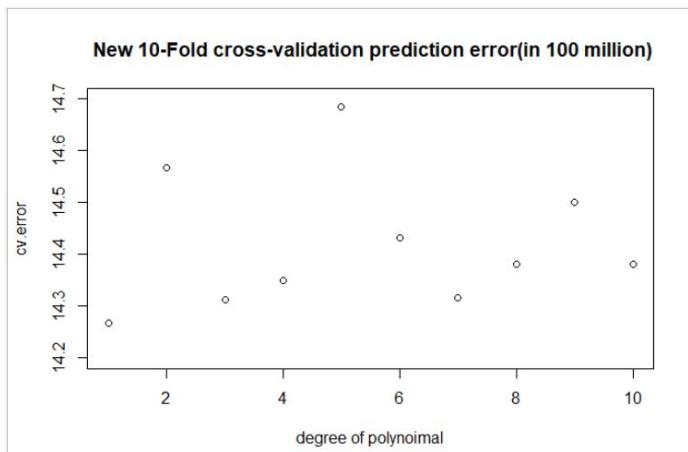


Figure16

Although the cross-validation prediction errors are still large, after the stepwise regression, they are closer to each other, meaning that the model still have rooms of improvement.

Interpretation

In view of the enormous value of cross-validation prediction error and Root-mean-squared Error, It is obvious that Linear Regression cannot predict the result in an accurate and precise way which makes sense as not all variable are collinear with Sale price.

iii. Ridge Regression

Introduction

Ridge regression is very similar to linear regression. The difference is that ridge regression implements a penalty lambda on MSE. The higher the lambda will give the weaker the contributes of all coefficients in the model. The selection of turning parameter lambda is the main focus in this section where

$$\text{Error} = \text{RSS} + \lambda \sum_{j=1}^p \beta_j^2$$

Grid of Lamda

The best RMSE of ridge regression model is 36 316.

```
> grid = 10^seq(12,-2,length=100)
> grid
[1] 1.000000e+12 7.220809e+11 5.214008e+11 3.764936e+11 2.718588e+11 1.963041e+11 1.417474e+11 1.023531e+11 7.390722e+10
[10] 5.336699e+10 3.853529e+10 2.782559e+10 2.009233e+10 1.450829e+10 1.047616e+10 7.564633e+09 5.462277e+09 3.944206e+09
[19] 2.848036e+09 2.056512e+09 1.484968e+09 1.072267e+09 7.742637e+08 5.590810e+08 4.037017e+08 2.915053e+08 2.104904e+08
[28] 1.519911e+08 1.097499e+08 7.924829e+07 5.722368e+07 4.132012e+07 2.983647e+07 2.154435e+07 1.555676e+07 1.123324e+07
[37] 8.111308e+06 5.857021e+06 4.229243e+06 3.053856e+06 2.205131e+06 1.592283e+06 1.149757e+06 8.302176e+05 5.994843e+05
[46] 4.328761e+05 3.125716e+05 2.257020e+05 1.629751e+05 1.176812e+05 8.497534e+04 6.135907e+04 4.430621e+04 3.199267e+04
[55] 1.668101e+04 1.204504e+04 8.697490e+03 6.280291e+03 4.534879e+03 3.274549e+03 2.364489e+03 1.707353e+03
[64] 1.232847e+03 8.902151e+02 6.428073e+02 4.641589e+02 3.351603e+02 2.420128e+02 1.747528e+02 1.261857e+02 9.111628e+01
[73] 6.579332e+01 4.750810e+01 3.430469e+01 2.477076e+01 1.788650e+01 1.291550e+01 9.326033e+00 6.734151e+00 4.862602e+00
[82] 3.511192e+00 2.535364e+00 1.830738e+00 1.321941e+00 9.545485e-01 6.892612e-01 4.977024e-01 3.593814e-01 2.595024e-01
[91] 1.873817e-01 1.353048e-01 9.770100e-02 7.054802e-02 5.094138e-02 3.678380e-02 2.656088e-02 1.917910e-02 1.384886e-02
[100] 1.000000e-02
```

Figure17

The grid of lambda is chosen as the above figure. 100 ridge regression models are fitted with the gird.

Cross-validation

```
> sqrt(cv.out$cvm)
[1] 77324.87 77037.34 76984.44 76949.92 76912.09 76870.64 76825.22 76775.47 76720.98 76661.32 76596.00 76524.52 76446.29 76360.73
[15] 76267.16 76164.87 76053.10 75931.02 75797.73 75652.27 75493.63 75320.72 75132.36 74927.32 74704.30 74461.93 74198.76 73913.30
[29] 73604.00 73269.24 72907.41 72516.86 72095.93 71643.00 71156.50 70634.92 70076.88 69481.14 68846.66 68172.64 67458.56 66704.23
[43] 65909.86 65076.09 64204.02 63295.29 62352.08 61377.13 60373.76 59345.84 58297.80 57234.54 56161.40 55084.04 54008.39 52940.48
[57] 51886.36 50851.84 49842.54 48863.83 47920.36 47016.30 46155.09 45339.45 44571.35 43852.00 43181.91 42560.91 41988.21 41462.51
[71] 40982.10 40544.90 40148.61 39790.74 39468.74 39180.02 38922.17 38692.80 38489.10 38308.91 38150.08 38010.63 37888.68 37782.51
[85] 37690.50 37611.25 37543.80 37486.44 37438.00 37397.62 37364.51 37337.85 37316.13 37300.02 37287.89 37279.58 37274.49 37271.94
> |
```

Figure18

The figure shows the RMSE of 100 different lambda in cross validation. A 10-folds cross-validation is applied to find out the best predictive model in 100 models. As shown below, there are 2 recommended lambda values which pointed out by 2 dotted lines. The left one is the lambda with the lowest MSE and the right one is the lambda with MSE above 1 sd of the lowest one. Therefore, the left lambda is chosen to be the best lambda. The value is around 7646.617 and the log value is around 8.942.

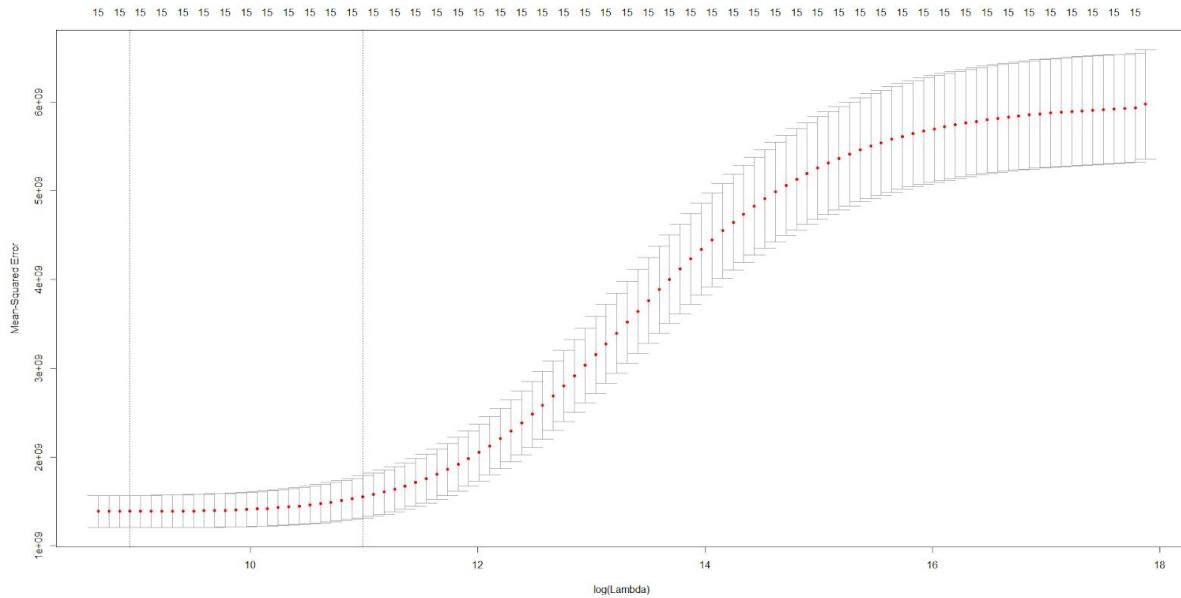


Figure19

Best Model

The best model is fitted with lamda 7646.617 and RMSE 36 316.

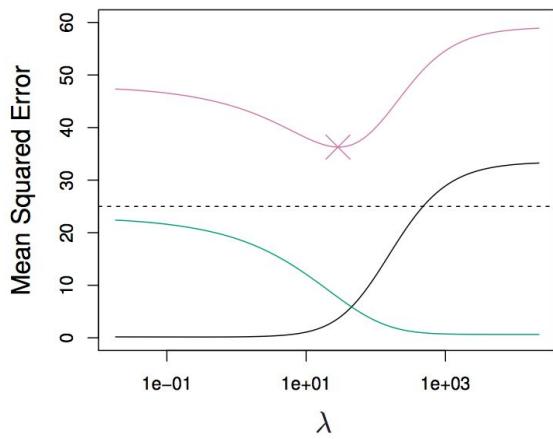


Figure20

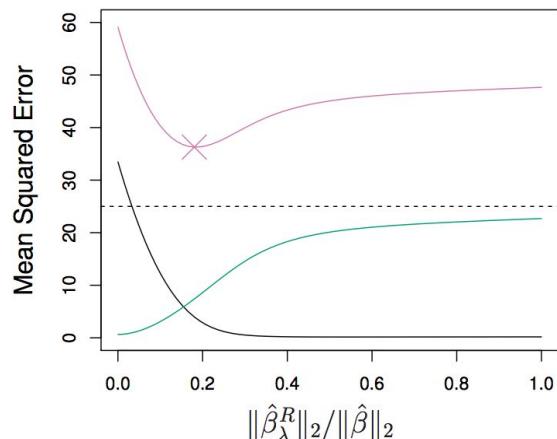


Figure21

Interpretation

In grid, lamda values are arranged in descending order. The 20th lamda value is 49770236 and the 50th lamda value is 11497.57. Therefore, the best lamda 7646.617 is respectively small. The ridge regression is not far from linear regression. The bias and MSE should be in optimum, the red cross in the above figure.

iv. Lasso Regression

Introduction

Lasso regression is very similar to ridge regression. Similarly, lasso regression implements a penalty lambda on MSE. The higher the lambda will give the weaker the contributes of all coefficients in the model. The selection of turning parameter lambda is also the main focus in this section where

$$\text{Error} = RSS + \lambda \sum_{j=1}^p |\beta_j|$$

Grid of Lamda

The best RMSE of ridge regression model is 35 603.

```
> grid = 10^seq(12,-2,length=100)
> grid
[1] 1.000000e+12 7.220809e+11 5.214008e+11 3.764936e+11 2.718588e+11 1.963041e+11 1.417474e+11 1.023531e+11 7.390722e+10
[10] 5.336699e+10 3.853529e+10 2.782559e+10 2.009233e+10 1.450829e+10 1.047616e+10 7.564633e+09 5.462277e+09 3.944206e+09
[19] 2.848036e+09 2.056512e+09 1.484968e+09 1.072267e+09 7.742637e+08 5.590810e+08 4.037017e+08 2.915053e+08 2.104904e+08
[28] 1.519911e+08 1.097499e+08 7.924829e+07 5.722368e+07 4.132012e+07 2.983647e+07 2.154435e+07 1.555676e+07 1.123324e+07
[37] 8.111308e+06 5.857021e+06 4.229243e+06 3.053856e+06 2.205131e+06 1.592283e+06 1.149757e+06 8.302176e+05 5.994843e+05
[46] 4.328761e+05 3.125716e+05 2.257020e+05 1.629751e+05 1.176812e+05 8.497534e+04 6.135907e+04 4.430621e+04 3.199267e+04
[55] 2.310130e+04 1.668101e+04 1.204504e+04 8.697490e+03 6.280291e+03 4.534879e+03 3.274549e+03 2.364489e+03 1.707353e+03
[64] 1.232847e+03 8.902151e+02 6.428073e+02 4.641589e+02 3.351603e+02 2.420128e+02 1.747528e+02 1.261857e+02 9.111628e+01
[73] 6.579332e+01 4.750810e+01 3.430469e+01 2.477076e+01 1.788650e+01 1.291550e+01 9.326033e+00 6.734151e+00 4.862602e+00
[82] 3.511192e+00 2.535364e+00 1.830738e+00 1.321941e+00 9.545485e-01 6.892612e-01 4.977024e-01 3.593814e-01 2.595024e-01
[91] 1.873817e-01 1.353048e-01 9.770100e-02 7.054802e-02 5.094138e-02 3.678380e-02 2.656088e-02 1.917910e-02 1.384886e-02
[100] 1.000000e-02
```

Figure22

The grid of lambda is the same as that of ridge regression model.

Original Model

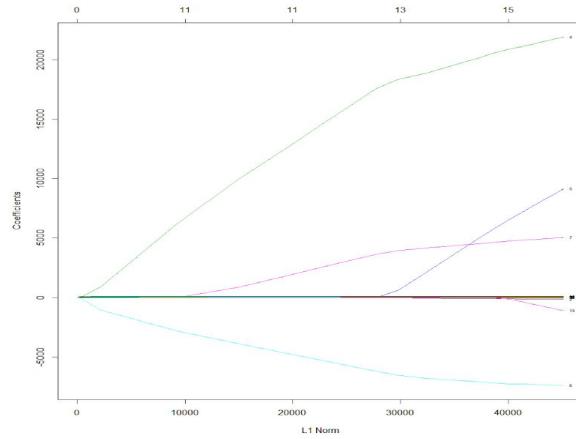


Figure23

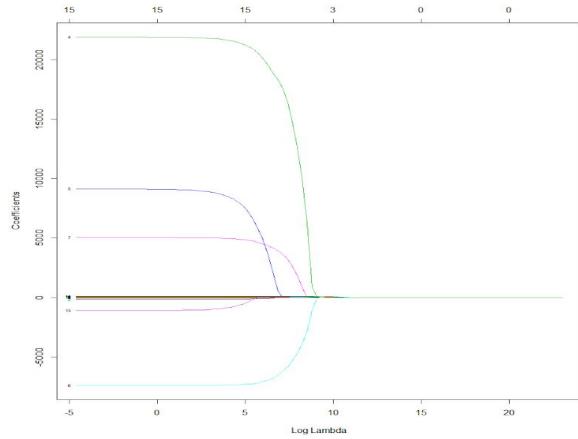


Figure24

Both figures show that the coefficient of lasso regression will decrease if the lambda increases. All coefficient will go to 0 if the log lambda is larger than 9. The figures also show that the 4th and 6th coefficient are firstly to be non-zero if lambda drops. They are corresponding to the coefficients of “LotShapeIR2” and “LotShapeReg”. Therefore, the simplest model of lasso should be “SalePrice” against “LotShapeIR2” and “LotShapeReg”.

Cross-validation

```
> sqrt(cv.out$cvm)
[1] 77033.87 73731.66 70407.47 67197.03 63645.82 60149.73 57018.44 54282.00 51900.65 49837.24 48056.91 46527.13 45217.77 44101.20
[15] 43155.01 42359.96 41680.95 41089.20 40573.19 40126.52 39735.46 39398.05 39136.43 38922.78 38725.77 38544.75 38362.39 38194.01
[29] 38033.08 37888.14 37764.61 37641.04 37522.81 37422.23 37342.56 37279.28 37229.34 37190.85 37164.26 37158.84 37170.32 37189.25
[43] 37211.59 37239.54 37275.58 37313.32 37348.82 37384.27 37419.01 37449.28 37471.46 37489.15 37507.25 37527.25 37548.00 37567.48
[57] 37586.86 37607.65 37627.23 37635.90 37639.93 37643.94 37647.32 37652.54 37657.81 37662.70 37667.63 37672.22 37676.38 37680.52
[71] 37684.21 37687.82 37691.13 37693.57 37695.98
```

Figure25

The figure shows the RMSE of 100 different lambda in cross validation. Similar to ridge regression, A 10-folds cross-validation is applied to find out the best predictive model in 100 models. As shown below, there are 2 recommended lambda values which pointed out by 2 dotted lines. Similarly, the left one is the lambda with the lowest MSE and the right one is the lambda with MSE above 1 sd of the lowest one. The left lamda is chosen to be the best lambda. The value is around 1536.384 and the log value is around 7.337.

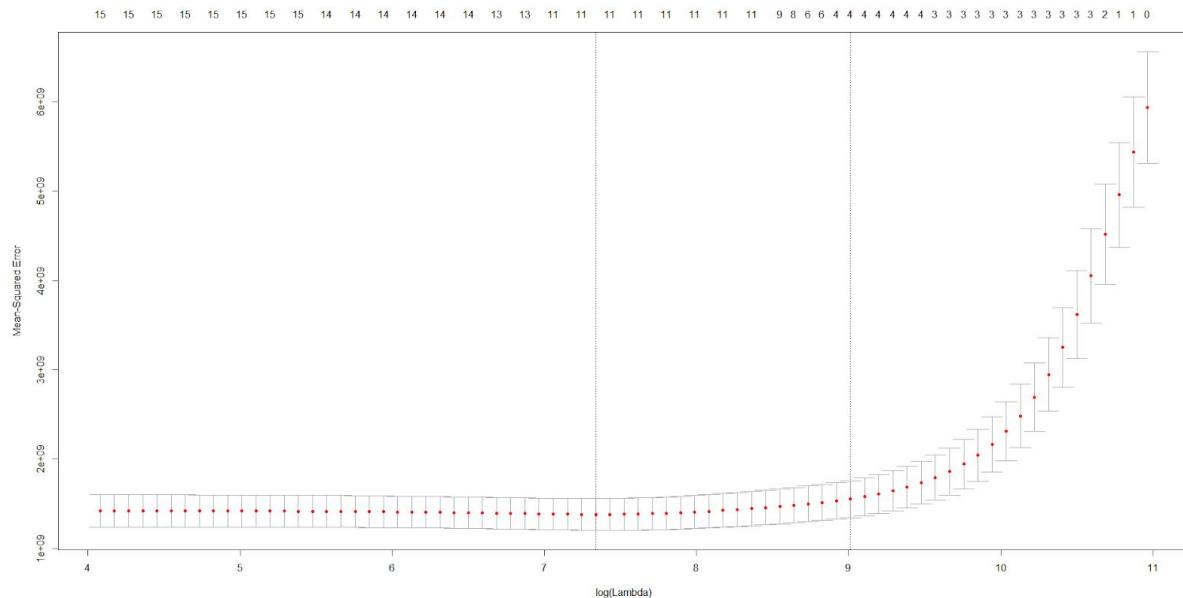


Figure26

Best Model

The best model is fitted with lamda 1536.384 and RMSE 35 603.

Interpretation

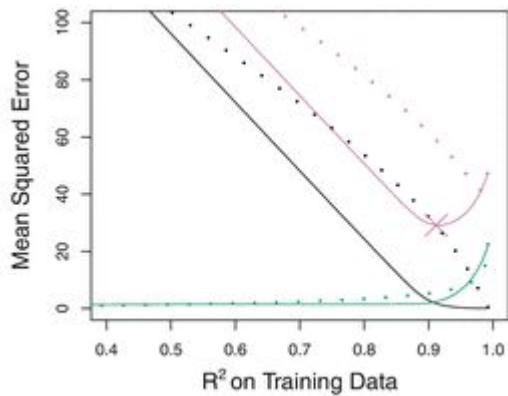


Figure27

As above mentioned, the RMSE from the best ridge regression is 36 316. Lasso regression performs better corresponding to RMSE. In conclusion, lasso gives less bias and variance than ridge in this case.

Remarks: Lasso(Solid), Ridge(Dash)

v. Regression Spline

introduction

Spline Regression is a non-parametric regression technique for testing non-linearity in the predictor variables and for modeling nonlinear functions. This regression technique divides the datasets into bins at intervals or points called knots and each bin has its separate fit.

Knots

Adding a greater number of knots can increase the flexibility of the Spline model. The choice of a knot placement depends on the distribution of each variable.

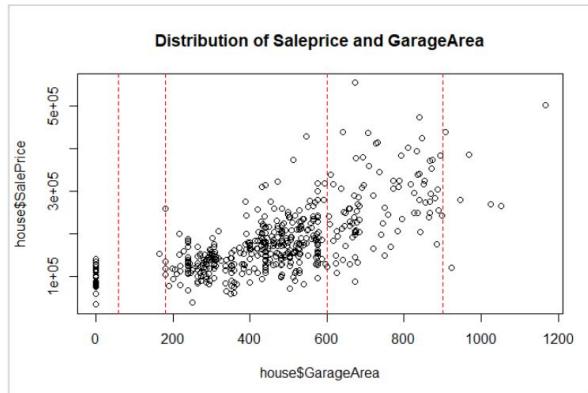
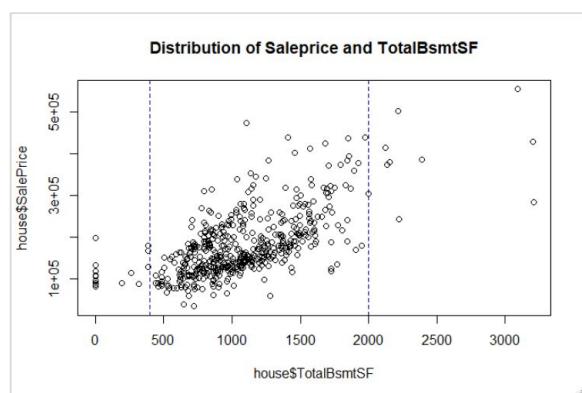


Figure28

Figure29

Regarding the graph shown above, the distribution is split into several parts respectively with respect to their density.

Result:

```
>spline_reg = lm(SalePrice ~bs(LotFrontage, knots=quantile(house$SalePrice, p=c(0.25,0.5,1))) + bs(LotArea, knots=quantile(house$SalePrice, p=c(0.2,0.4,1))) + bs(MasVnrArea, knots=quantile(house$SalePrice, p=c(0.05,0.25,0.75,1))) + bs(TotalBsmtSF, knots=quantile(house$SalePrice, p=c(0.15,0.7,1))) + bs(X1stFlrSF, knots=quantile(house$SalePrice, p=c(0.7,1))) + bs(X2ndFlrSF, knots=quantile(house$SalePrice, p=c(0.05,0.3,0.7,1))) + bs(GrLivArea, knots=quantile(house$SalePrice, p=c(0.1, 0.75,1))) + bs(TotRmsAbvGrd, knots=quantile(house$SalePrice, p=c(0.3,0.4,0.5,0.6,0.7,0.8,0.9,1))) + bs(GarageArea, knots=quantile(house$SalePrice, p=c(0.05,0.15,0.5,0.75,1))) + bs(WoodDeckSF, knots=quantile(house$SalePrice, p=c(0.05,0.5,1))) + bs(OpenPorchSF, knots=quantile(house$SalePrice, p=c(0.05,0.6,1)))
```

Residuals:

Min	1Q	Median	3Q	Max
-----	----	--------	----	-----

```

-144132 -17520    1485 17529 111400

Signif. codes: 0 ‘***’ 0.001 ‘**’ 0.01 ‘*’ 0.05 ‘.’ 0.1 ‘ ’ 1

Residual standard error: 32120 on 360 degrees of freedom

Multiple R-squared: 0.8436,      Adjusted R-squared: 0.8267

F-statistic: 49.79 on 39 and 360 DF, p-value: < 2.2e-16

```

We hypothesized that H null: the model is useless. Using the R output, the F-statistics shows that F-score is 49.79 and p-value is smaller than 2.2e-16 with 39 and 360 degree of the freedom. Therefore, the H null is rejected. The root-mean-square error (RMSE) is 122699.8. From R-squared value(0.8436 &0.8267), there is a strong relationship between House sale price and other variables. Therefore, 0.84 of the “SalePrice” can be explained and predicted by the regression spline.

Cross-Validation

10-folds cross validation is applied on the spline regression. The figure shows the RMSE of each fold of validation. The best performance of cross validation can give only 27492.74 which is relatively low. However, the code gives a warning message that some independent variables are out of the knots boundary so that the 6th entry are NaN because the knots are splitted by intuition.

RMSE <dbl>	
35988.70	(Intercept) 61290.1
	bs(LotFrontage, knots = quantile(house\$SalePrice, p = c(0.25, 0.5, 1)))1 -16442.5
	bs(LotFrontage, knots = quantile(house\$SalePrice, p = c(0.25, 0.5, 1)))2 10072.6
	bs(LotFrontage, knots = quantile(house\$SalePrice, p = c(0.25, 0.5, 1)))3 -14759.2
	bs(LotFrontage, knots = quantile(house\$SalePrice, p = c(0.25, 0.5, 1)))4 NA
	bs(LotFrontage, knots = quantile(house\$SalePrice, p = c(0.25, 0.5, 1)))5 NA
	bs(LotFrontage, knots = quantile(house\$SalePrice, p = c(0.25, 0.5, 1)))6 NA
41167.51	bs(LotArea, knots = quantile(house\$SalePrice, p = c(0.2, 0.4, 1)))1 112889.5
	bs(LotArea, knots = quantile(house\$SalePrice, p = c(0.2, 0.4, 1)))2 -322589.0
26519.90	bs(LotArea, knots = quantile(house\$SalePrice, p = c(0.2, 0.4, 1)))3 2108438.8
39574.96	bs(LotArea, knots = quantile(house\$SalePrice, p = c(0.2, 0.4, 1)))4 NA
	bs(LotArea, knots = quantile(house\$SalePrice, p = c(0.2, 0.4, 1)))5 118643.5
	bs(LotArea, knots = quantile(house\$SalePrice, p = c(0.2, 0.4, 1)))6 NA
	bs(MasVnrArea, knots = quantile(house\$SalePrice, p = c(0.05, 0.25, 0.75, 1)))1 45807.9
34883.77	bs(MasVnrArea, knots = quantile(house\$SalePrice, p = c(0.05, 0.25, 0.75, 1)))2 -111192.9
30605.46	bs(MasVnrArea, knots = quantile(house\$SalePrice, p = c(0.05, 0.25, 0.75, 1)))3 497335.7
36230.39	bs(MasVnrArea, knots = quantile(house\$SalePrice, p = c(0.05, 0.25, 0.75, 1)))4 41332.4
	bs(MasVnrArea, knots = quantile(house\$SalePrice, p = c(0.05, 0.25, 0.75, 1)))5 NA
	bs(MasVnrArea, knots = quantile(house\$SalePrice, p = c(0.05, 0.25, 0.75, 1)))6 NA
	bs(MasVnrArea, knots = quantile(house\$SalePrice, p = c(0.05, 0.25, 0.75, 1)))7 NA
NaN	
NaN	

vi. Regression tree

Original model

The original regression tree's summary and illustration is as follow,

```
Regression tree:
tree(formula = SalePrice ~ ., data = house[train, ], method = "class")
Variables actually used in tree construction:
[1] "GrLivArea"   "TotalBsmtSF" "GarageArea"   "OpenPorchSF" "WoodDecksSF"
Number of terminal nodes: 10
Residual mean deviance: 1.122e+09 = 2.694e+11 / 240
Distribution of residuals:
Min. 1st Qu. Median Mean 3rd Qu. Max.
-126200 -18640 2062 0 19060 98140
```

Figure30

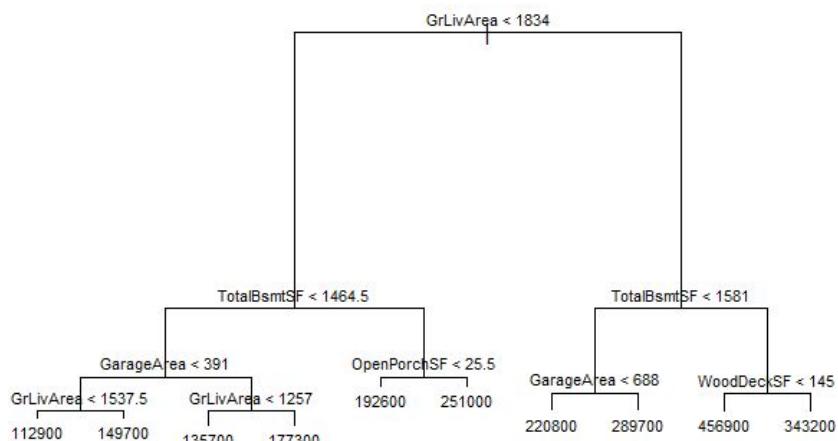
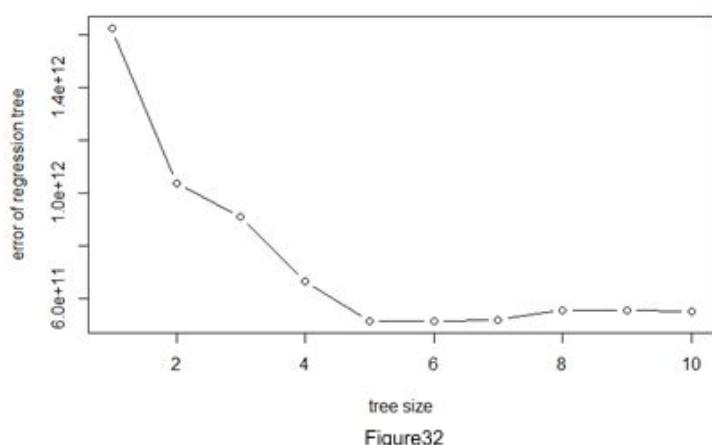


Figure31

And the root-mean-square error (RMSE) is 53338.69.

Cross-validation and tree pruning

The reason for pruning a tree is to prevent overfit problem. And the way to choose the optimal size of tree is to use the training data set to do cross validation, and then figure out which size of tree will produce the least error.



A 10 folds cross validation has been done and it is the following graphical presentation. As we can see, a tree size of 5 to 10 produces the least cross validation error. We try to prune the tree until it is a size of 5 regression tree. In this case, the regression tree will be prune until it is a size of 5 regression tree, i.e. a regression tree that only has 5 terminal notes.

However, a size of 5 regression tree seems not to be the best fit of the testing data, the error increased to 55918.44. Thus, with the same approach, we will test all tree size from 5 to 10 as they produce a similar amount of error. The following table represents the RMSE difference of different size of tree. It turns out to be a tree size of 10 still perform the best under this circumstance. As a result, a size of 10 tree is chosen to be our final model.

tree_result_RMSE <dbl>	
RMSE of tree size_5	55918.44
RMSE of tree size_6	57328.92
RMSE of tree size_7	55228.25
RMSE of tree size_8	54135.67
RMSE of tree size_9	53637.72
RMSE of tree size_10	53338.69

Figure33

The below graph shows the performance of different size of tree on predicting the actual price.

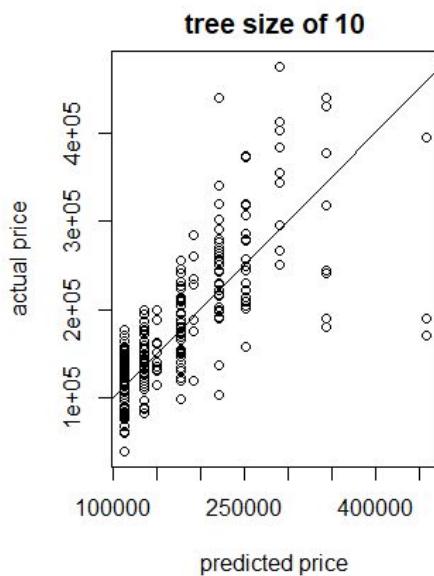


Figure34

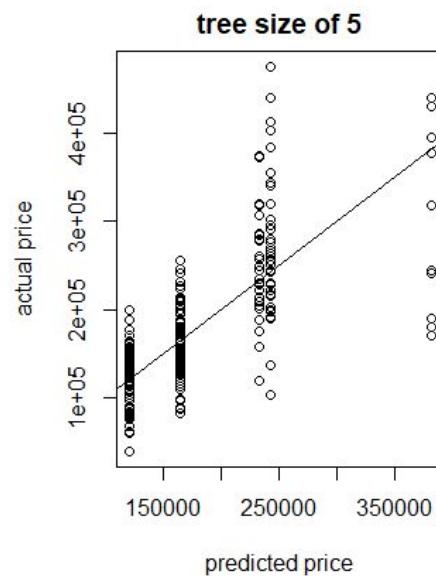


Figure35

Interpretation

We can think of it as a binary question. The first question is, is *GrlivArea* less than 1834? If yes, move to the next branch, is *TotalBsmtSF* less than 1464.5? If yes, move to the next branch. Keep this process until it reaches the terminal node(or sometimes called Leaf). The number that the leaf gives represents the predicted house price. As we can see, *TotalBsmtSF* and *GarageArea* both play an important role in the decision tree, they appeared pretty often and they are usually the parents tree of other sub trees, which means they are the factors that will usually be considered earlier.

Advantage of

using regression tree

Regression tree is easy to visualize and intuitive. Unlike other models, It can be easy to explain to other people or even layman.

vii. Gradient Boosting

Introduction

Gradient boosting is an ensemble model of weak learners. The most classic weak learner is decision tree. Gradient boosting ensembles a number of decision trees to make a strong learning of decision tree which can overcome overfitting. Therefore, similar to decision tree, interaction depth, number of trees and shrinkage, etc are the parameters to be discussed.

Simulation

```
> cv_gbm
Stochastic Gradient Boosting
400 samples
13 predictor
No pre-processing
Resampling: cross-validated (10 fold)
Summary of sample sizes: 360, 360, 360, 360, 360, 360, ...
Resampling results across tuning parameters:

shrinkage  n.trees   RMSE    Rsquared   MAE
0.001      0         76527.03  NaN        58306.51
0.001      50        74368.10  0.7113297  56464.46
0.001      100       72314.03  0.7193518  54705.72
0.001      150       70375.49  0.7222501  53041.86
0.001      200       68538.34  0.7254467  51492.49
0.001      250       66783.82  0.7298841  50007.86
0.001      300       65103.25  0.7327061  48570.30
0.001      350       63518.80  0.7371740  47241.30
0.001      400       62017.53  0.7403071  45970.28
0.001      450       60604.41  0.7431516  44752.60
0.001      500       59253.25  0.7458589  43597.29
0.001      550       57962.39  0.7477290  42486.35
0.001      600       56711.88  0.7502512  41455.51
```

The training dataset is 80% of the whole data so that there are 400 samples and 13 predictors(features) in the simulation. The grid of gbm is the following: interaction depth is a vector [1 3 5]; number of tree is a sequence from 0 to 2500 separated by 50 each; shrinkage is a vector of [0.01 0.001]; number of minobsinnode is 10.

Figure36

10-folds cross validation is applied during training. Finally, a gradient boosting model is trained with the formula “SalePrice” against all variables.

Features Importance

An important feature in gbm is the feature importance. The tables above rank the variables based on their relative influence. Relative influence indicates the relative importance of each variable in model training.

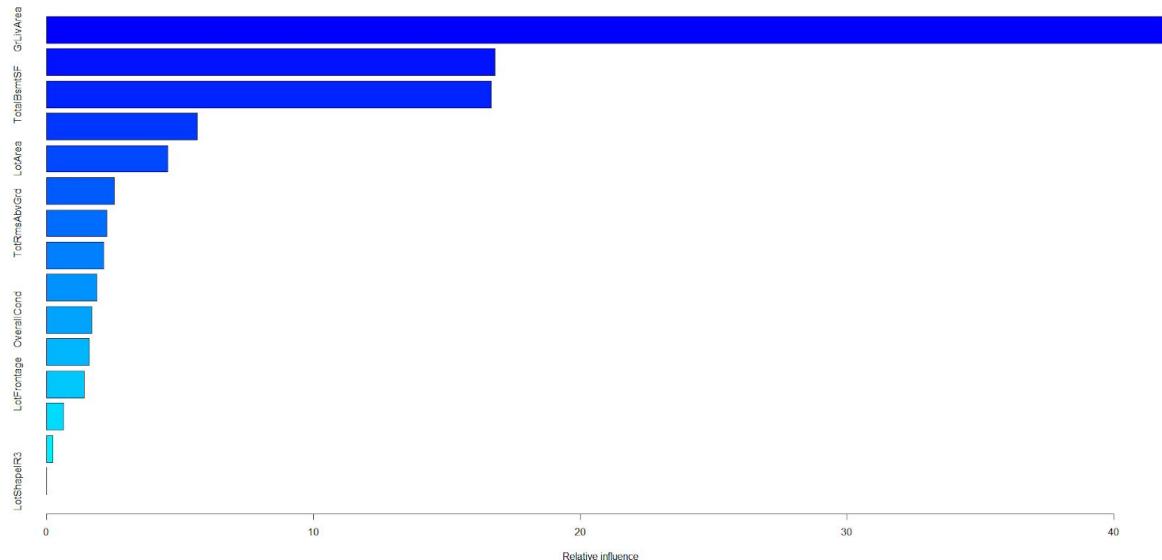


Figure37

var	rel.inf
GrLivArea	41.9818439
GarageArea	16.8188139
TotalBsmtSF	16.6566597
X1stFlrSF	5.6525017
LotArea	4.5336604
MasVnrArea	2.5416157
TotRmsAbvGrd	2.2544892
OpenPorchSF	2.1365754
WoodDeckSF	1.8750724
OverallCond	1.6842118
X2ndFlrSF	1.5909883
LotFrontage	1.4171835
LotShapeReg	0.6324724
LotShapeIR2	0.2239118
LotShapeIR3	0.0000000

Figure38

The figures show that the “GrLivArea” is the most important feature which gives almost 42 of relative influence. Both “GarageArea” and “TotalBsmtSF” are the second most important features which both give almost 17 of relative influence.

“LotShapeReg” and “LotShapeIR2” are the least important features which both give less than 1 of relative influence. “LotShapeIR3” is an unnecessary feature because it gives 0 relative influence in gbm modeling.

Summary of GBM

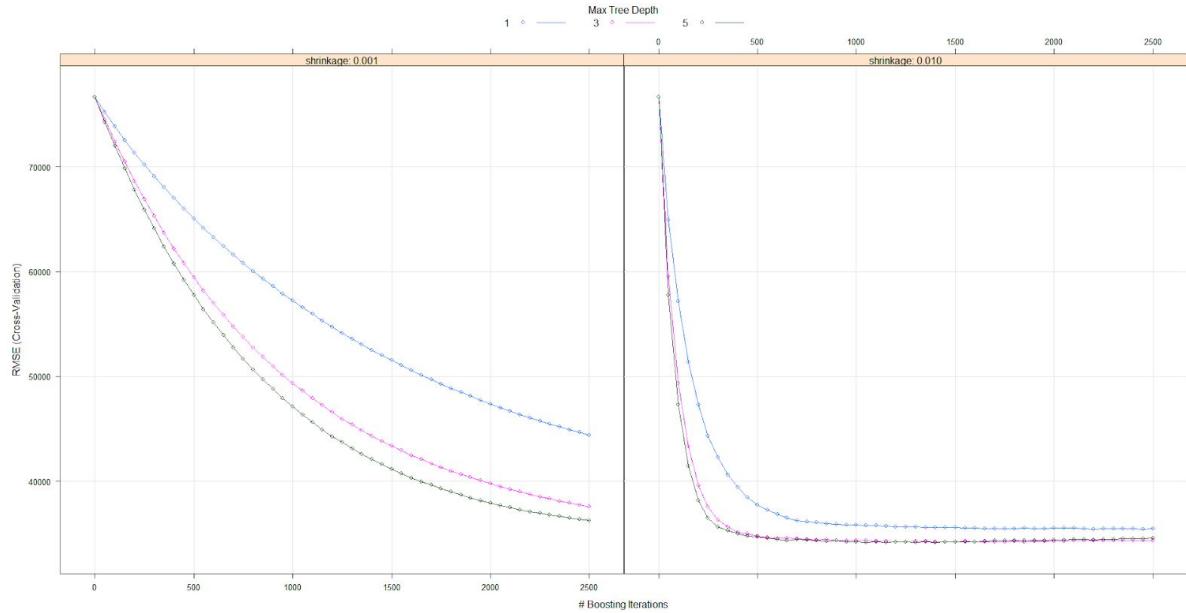


Figure38

The diagram shows the performance of gbm model with different parameters combinations. The figure shows that more iterations(number of trees) give a better model because it is a decreasing trend against RMSE. As shown, the RMSE of models with shrinkage 0.010 sharp drop while the RMSE of models with shrinkage 0.001 flat drop respectively. In general, gbm models with shrinkage 0.010 perform better than that with shrinkage 0.001. As the diagram is shown, 5 maximum tree depth(green line) perform better than 3(pink line) and 1 maximum tree depth(blue line). In conclusion, the best gbm model should be 500-1000 iterations, 0.010 shrinkage and 5 maximum tree depth.

Interpretation and Conclusion

The RMSE of gbm model is finally 35321.91. In some previous attempts, the RMSE can be less than 35000. However, it is hard to control the randomness of splitting when training the model. Nevertheless, gbm model is much better than regression tree as it ensembles 500 to 1000 trees to be a strong learner.

viii. Principal Component Regression

Introduction

Principal Component Regression (PCR) is a regression that performed on the component obtained by Principal Component Analysis (PCA). Where PCA is a machine learning technique for reducing the dimension of the variables.

Model

A 10 folds cross validation of PCR has been done and the result is as follows.

```
Data: X dimension: 400 15
      Y dimension: 400 1
Fit method: svdpc
Number of components considered: 15

VALIDATION: RMSEP
Cross-validated using 10 random segments.
          (Intercept) 1 comps 2 comps 3 comps 4 comps 5 comps 6 comps
CV          81021    42969   43066   41804   41770   40853   40971
adjCV       81021    42703   42822   41659   41591   40763   40980
          7 comps 8 comps 9 comps 10 comps 11 comps 12 comps 13 comps
CV          40771    40357   40476   40473   39337   38032   36935
adjCV       40810    40293   40377   40385   39178   38023   36810
          14 comps 15 comps
CV          37323    37697
adjCV       37187    37536

TRAINING: % variance explained
          1 comps 2 comps 3 comps 4 comps 5 comps 6 comps 7 comps
x           27.97    41.40   52.20   59.96   66.22   72.22   77.89
Saleprice_train 74.50    74.52   74.96   75.27   76.00   76.02   76.24
          8 comps 9 comps 10 comps 11 comps 12 comps 13 comps
x           83.19    87.81   92.29   95.86   97.70   99.03
Saleprice_train 77.23    77.40   77.43   79.24   80.07   81.40
          14 comps 15 comps
x           99.97    100.00
Saleprice_train 81.40    81.41
```

Figure39

As we can see, only 10 components can already explain 92.29% of the variance of dependent variables, and 13 components can even explain 99.03% of the variance of dependent variables. The RMSE of the testing data on the original model (a model that has all components) is 37707.86.

This picture shows that when the number of components is about 13, the MSEP is the lowest. Thus, we predict the data with only 13 components, and the RMSE is 37727.87, which is as

good as using all components in the model. However, can it be much better? The second figure represents the RMSE of each component on the test data. We can see that when we only take 11 components, the model performs the best, the RMSE is only 35368.06, which is much better than before.

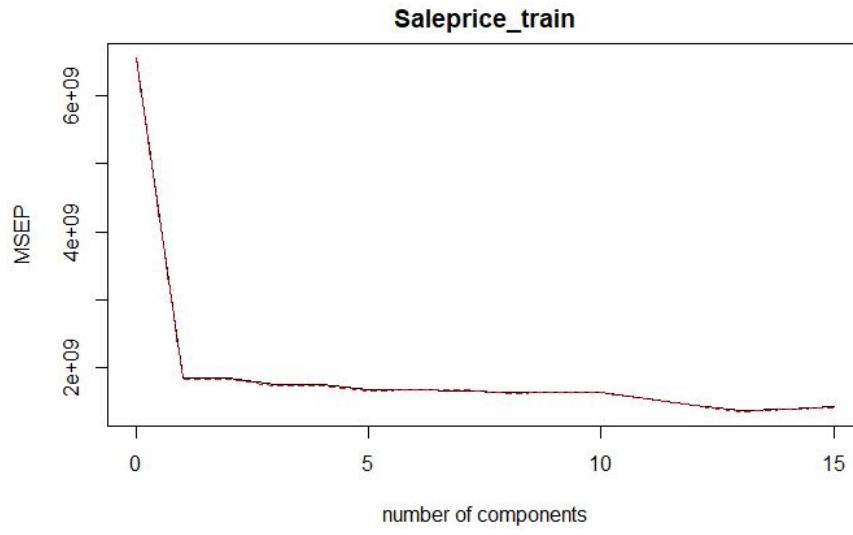


Figure40

RMSE_table <dbl>	
RMSE of 1 comp	41060.87
RMSE of 2 comp	40715.58
RMSE of 3 comp	39265.77
RMSE of 4 comp	39308.34
RMSE of 5 comp	40409.65
RMSE of 6 comp	40454.57
RMSE of 7 comp	41128.57
RMSE of 8 comp	39768.12
RMSE of 9 comp	39684.76
RMSE of 10 comp	39510.17

Figure41

RMSE_table <dbl>	
RMSE of 11 comp	35368.06
RMSE of 12 comp	38671.77
RMSE of 13 comp	37727.87
RMSE of 14 comp	37758.14
RMSE of 15 comp	37707.86

Figure42

interpretation

The reason why taking only 11 components rather than all components will perform better on the test data may due to the reduction of covariance in the dependent variables. Thus, the regression model becomes much efficient, yet the model is hard to be explained or understood. Since sometimes we cannot even explain the loading matrix from PCA, let alone to explain the regressed observed vector of outcomes from PCA. Nonetheless, it is a good way to reduce the noise from the model and the computation need for further machine learning processing.

ix. Partial Least Squares

Introduction

Similar to PCR, Partial Least Squares(PLS) has the similar concept to PCR. However, rather than finding the hyperplanes of variance between the dependent and independent variable, PLS project the dependent and independent to a new space in order to cancel out the covariance between the dependent variables.

Model

A 10 folds cross validation of PCR has been done and the result is as follows.

```
Data: X dimension: 400 15
      Y dimension: 400 1
Fit method: kernelpls
Number of components considered: 15

VALIDATION: RMSEP
Cross-validated using 10 random segments.
          (Intercept) 1 comps 2 comps 3 comps 4 comps 5 comps 6 comps
CV          81021   41129   38225   37557   37470   37223   37269
adjCV       81021   40958   38078   37432   37325   37101   37138
          7 comps 8 comps 9 comps 10 comps 11 comps 12 comps 13 comps
CV          37272   37285   37332   37500   37627   37657   37699
adjCV       37141   37153   37196   37350   37466   37497   37537
          14 comps 15 comps
CV          37698   37697
adjCV       37537   37536

TRAINING: % variance explained
          1 comps 2 comps 3 comps 4 comps 5 comps 6 comps 7 comps
X           27.91    34.41    42.24    48.16    56.87    64.09    70.1
SalePrice   76.38    80.03    80.86    81.25    81.35    81.39    81.4
          8 comps 9 comps 10 comps 11 comps 12 comps 13 comps 14 comps
X           73.84    78.16    82.8     83.89    88.56    89.82    95.03
SalePrice   81.40    81.40    81.4     81.41    81.41    81.41    81.41
          15 comps
X           100.00
SalePrice   81.41
```

Figure43

As we can see, only 10 components can already explain 82.8% of the variance of the dependent variables, and 13 components can explain 89.82% of the variance of the dependent variables.

The figure below shows when the number of components reaches 2, the MSEP drops dramatically, which also agrees with the RMSE table below. As we can see, when we only take 2 components, the RMSE is 36214.73, which is performing the best along taking other amounts of components to predict the test data. There is also a slight drop when we only use 4 components to predict the test data, the RMSE is also only 36232.74, which is the

second-lowest one. The RMSE of taking all components to predict the test data is 37707.86, we can see that taking 2 or 4 components can already dominate the performance.



Figure44

Interpretation and conclusion

Again, it is hard to explain the model as we cannot even explain the loading matrix. However, it is not surprising that PLS performs better than PCR, since PLS is known to be work better in terms of small size data. The only problem is using 2 components can only explain 34.41% of variance of the testing data and 4 components can only explain 48.16%, sometimes getting such a result may just be pure luck instead of removing the noise (or removing the covariance between the dependent variables) of the data.

	RMSE_pls <dbl>
RMSE of 1 comp	39426.15
RMSE of 2 comp	36214.73
RMSE of 3 comp	37056.94
RMSE of 4 comp	36232.67
RMSE of 5 comp	37369.65
RMSE of 6 comp	38003.36
RMSE of 7 comp	38024.38
RMSE of 8 comp	37802.67
RMSE of 9 comp	37740.96
RMSE of 10 comp	37741.92

Figure45

	RMSE_pls <dbl>
RMSE of 11 comp	37713.50
RMSE of 12 comp	37746.15
RMSE of 13 comp	37712.56
RMSE of 14 comp	37707.45
RMSE of 15 comp	37707.86

Figure46

Conclusion

Model	RMSE
Linear Regression	37088.35
Ridge Regression	36316
Lasso Regression	35603
Regression Spline	27492
Regression Tree	53338.69
Gradient Boosting	35321.91
Principal Component Regression	35368.06
Partial Least Squares	36214.73

As the table is shown, regression spline has the lowest RMSE in prediction because the knots are split into small pieces where fit the data very well. However, it is very time consuming since we have to define the knots manually. On the other hand, regression tree has the highest RMSE but it is easy to interpret and understand.

3. Titanic

a. Data Description

i. Data Structure

```
> str(Titanic)
'data.frame': 500 obs. of 9 variables:
 $ PassengerId: int 1 2 3 4 5 6 7 8 9 10 ...
 $ Survived    : int 0 1 1 1 0 0 0 0 1 1 ...
 $ Pclass      : int 3 1 3 1 3 3 1 3 3 2 ...
 $ Sex         : Factor w/ 2 levels "female","male": 2 1 1 1 2 2 2 2 1 1 ...
 $ Age         : num 22 38 26 35 35 NA 54 2 27 14 ...
 $ sibsp       : int 1 1 0 1 0 0 0 3 0 1 ...
 $ Parch       : int 0 0 0 0 0 0 1 2 0 ...
 $ Fare        : num 7.25 71.28 7.92 53.1 8.05 ...
 $ Embarked    : Factor w/ 4 levels "", "C", "Q", "S": 4 2 4 4 4 3 4 4 4 2 ...
```

Figure46

From the structure of “Titanic.xlsx”, there are 500 observations and 9 variables. The “Survived” is the dependent variable and the others are independent variables. “PassengerId” is omitted in the model fitting and prediction process.

ii. Variables Correlation

Similar to the “House” data, it is better to generate a correlation matrix to understand the relationship between the variables. “Sex” and “Embarked”, which are factor variables, are transformed into an integer variable so as to generate a correlation matrix.

NAs are also omitted in the correlation matrix computation so as to avoid bias. The correlation matrix is shown below.

	PassengerId	Survived	Pclass	Sex	Age	SibSp	Parch	Fare	Embarked
PassengerId	1.0000000000	0.07736386	-0.09640867	0.007219665	0.07517068	-0.10136540	-0.01836310	0.05128369	-0.0006638059
Survived	0.0773638602	1.00000000	-0.26925119	-0.560783075	-0.10967219	-0.02781408	0.10105374	0.20678764	-0.1520622644
Pclass	-0.0964086748	-0.26925119	1.00000000	0.126337925	-0.36619610	0.09719812	0.01337803	-0.58668333	0.2917918384
Sex	0.0072196650	-0.56078307	0.12633792	1.000000000	0.10567939	-0.07712978	-0.17046568	-0.18500424	0.1252571600
Age	0.0751706765	-0.10967219	-0.36619610	0.105679392	1.00000000	-0.35745600	-0.23982165	0.08832065	-0.0713452847
SibSp	-0.1013654039	-0.02781408	0.09719812	-0.077129781	-0.35745600	1.00000000	0.41312014	0.16636411	0.0521966716
Parch	-0.0183630954	0.10105374	0.01337805	-0.170465680	-0.23982165	0.41312014	1.00000000	0.25824915	0.0880073884
Fare	0.0512836865	0.20678764	-0.58668333	-0.185004235	0.08832065	0.16636411	0.25824915	1.00000000	-0.2869565340
Embarked	-0.0006638059	-0.15206226	0.29179184	0.125257160	-0.07134528	0.05219667	0.08800739	-0.28695653	1.0000000000

Figure47

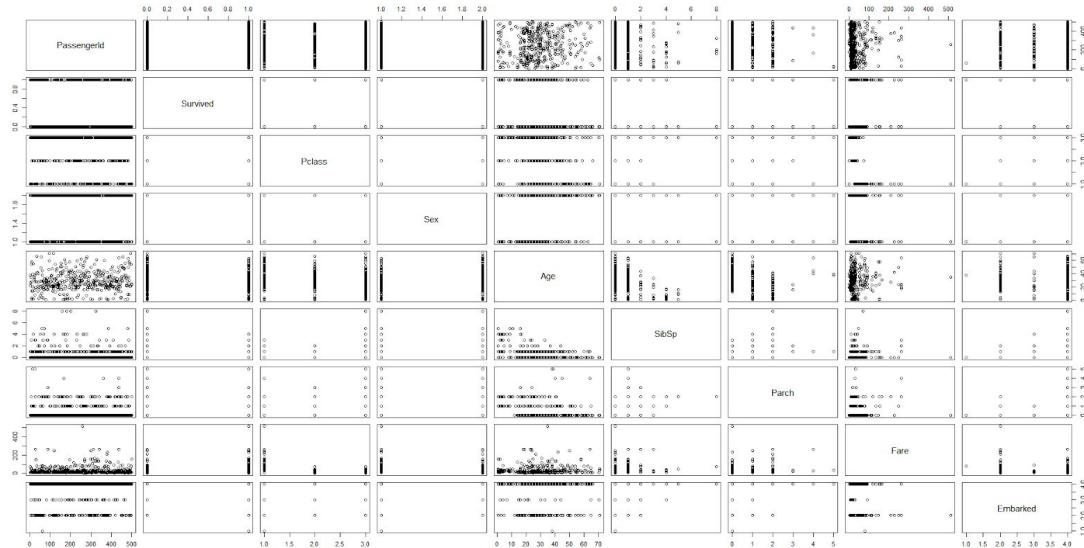


Figure48

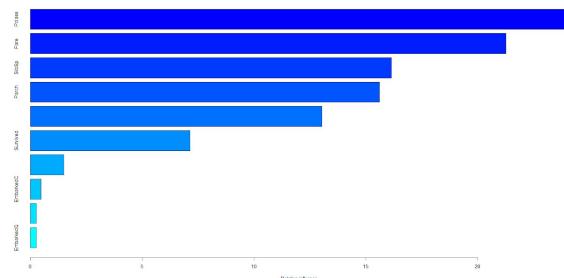
From the correlation matrix, “Survived” and “sex” is significantly correlated. We hypothesized that “sex” will contribute more in model fitting and prediction. “Pclass” and “Fare” are significantly correlated which may cause problems in model fitting. On the other hand, the general plot doesn’t show a significant correlation between variables.

iii. Handling Missing Data

```
> summary(Titanic)
  PassengerId   Survived      Pclass       Sex      Age     sibsp      Parch      Fare      Embarked
Min. : 1.0   Min. :0.000   Min. :1.000   female:185   Min. : 0.75   Min. :0.000   Min. :0.00   Min. : 0.000   : 1
1st Qu.:125.8 1st Qu.:0.000   1st Qu.:2.000   male :315    1st Qu.:20.12  1st Qu.:0.000   1st Qu.:0.00   1st Qu.: 7.925   C: 92
Median :250.5 Median :0.000   Median :3.000   Median :3.000   Median :28.00   Median :0.000   Median :0.00   Median :14.456   Q: 45
Mean   :250.5  Mean   :0.386   Mean   :2.326   Mean   :2.326   Mean   :39.20   Mean   :0.574   Mean   :0.38   Mean   :31.782   S:362
3rd Qu.:375.2 3rd Qu.:1.000   3rd Qu.:3.000   Median :3.000   3rd Qu.:37.75  3rd Qu.:1.000   3rd Qu.:0.00   3rd Qu.:30.071
Max.   :500.0  Max.   :1.000   Max.   :3.000   Max.   :3.000   Max.   :87.00   Max.   :8.000   Max.   :5.00   Max.   :512.329
NA's   :102
```

Figure49

From the summary of the dataset “Titanic.xlsx”, there are 102 NAs in variable “Age”. A gbm model is fitted for “Age” against other variables. 10-folds cross validation is also applied in the gbm model. Therefore, the missing “Age” can be predicted by the model.



Remarks: The gbm model provides feature importance. As the figure is shown, “Pclass” is the most important feature and “EmbarkedQ” is the least important feature for “Age” modeling.

Figure50

b. Modeling

i. KNN

K-Nearest Neighbor algorithm (KNN) is a non-parametric method used for classification. The decision rule of KNN is as follow,

$$N_K(x, x_i) y_i = 1 \text{ if } x_i \text{ is a neighbor of } x$$

$$N_K(x, x_i) y_i = 0 \text{ otherwise}$$

$$\text{The classifier: } C_K(x) = \frac{\sum_{i=1}^n N_K(x, x_i) y_i}{\sum_{i=1}^n N_K(x, x_i)}$$

$$C_K(x) > 0.5, \text{ predict } y = 1$$

$$C_K(x) < 0.5, \text{ predict } y = 0$$

There are 500 samples with 6 predictors classifies in 2 classes.

k	Accuracy	Kappa
1	0.752	0.47069169
2	0.740	0.43962619
3	0.732	0.42124631
4	0.698	0.33538732
5	0.726	0.40418203
6	0.728	0.41028532
7	0.738	0.41228525
8	0.730	0.41288011
9	0.738	0.43140387
10	0.736	0.41490399
11	0.742	0.42993000
12	0.724	0.39077151
13	0.730	0.39856725
14	0.716	0.36418153
15	0.712	0.36818472
16	0.702	0.33619645
17	0.708	0.34221197
18	0.692	0.30474041
19	0.690	0.29660555
20	0.692	0.30330613
21	0.686	0.29337846
22	0.678	0.29238873
23	0.672	0.29595448
24	0.672	0.25959368
25	0.650	0.21718437
26	0.660	0.24340876
27	0.656	0.23450768
28	0.626	0.16690427
29	0.598	0.09348391
30	0.618	0.10518172
31	0.626	0.14962893
32	0.638	0.17348579
33	0.654	0.20002220
34	0.636	0.15731662
35	0.646	0.18324781
36	0.656	0.2088109
37	0.64	0.14781043
38	0.622	0.12970643
39	0.638	0.15590957
40	0.650	0.18389046
41	0.646	0.17456350
42	0.646	0.17631510
43	0.636	0.15573451
44	0.644	0.17328980
45	0.64	0.17028170
46	0.624	0.14658260
47	0.642	0.16345758
48	0.646	0.17103784
49	0.648	0.17307222
50	0.650	0.17688892

Accuracy was used to select the optimal model using the largest value.
The final value used for the model was k = 1.

```

  learn      2   -none-   Mode
  k          1   -none-   numeric
  thedots    0   -none-   list
  xnames     18   -none-   character
  problemType 1   -none-   character
  typeValue   1   -none-   character
  obsLevels   2   -none-   character
  param       0   -none-   list

```

Figure51

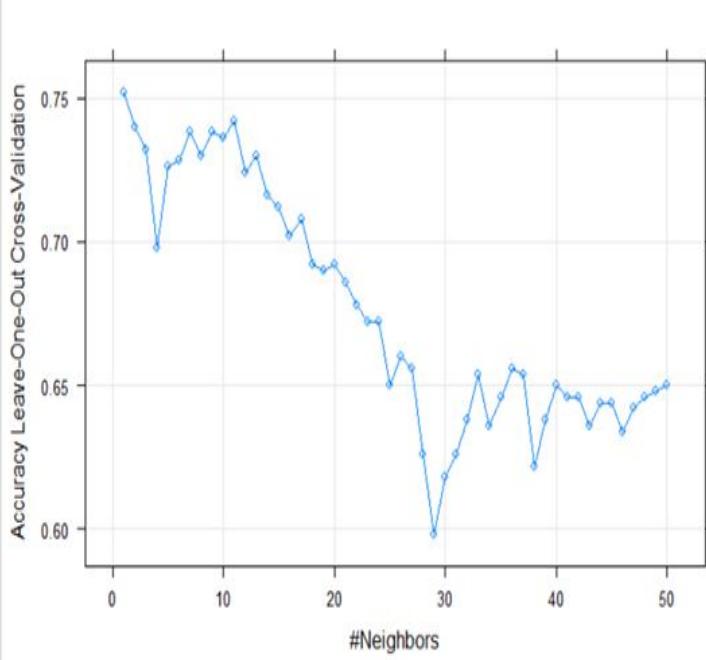


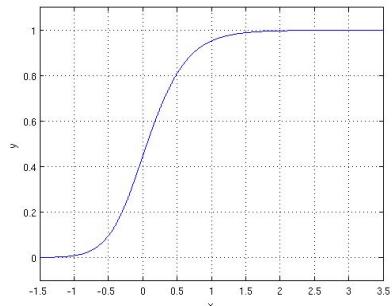
Figure52

From the result and graph, only “k” is a numeric variable. Accuracy was used to select the optimal model using the largest value. The final value used for the model was k = 10.

ii. Logistic Regression

introduction

Logistic regression is used to model the probability of a certain class or event, i.e. to predict the output with different categories. The reason for using it is because of the rate of convergence is high. Thus, the model (or the line) can fit the data better.



Model

The original model is as follow,

```
Call:
glm(formula = Survived ~ ., family = binomial, data = titanic_train[, 
])

Deviance Residuals:
    Min      1Q  Median      3Q     Max
-2.0783 -0.5989 -0.3407  0.5292  2.6027

Coefficients:
            Estimate Std. Error z value Pr(>|z|)
(Intercept) 4.544559  0.858007  5.297 1.18e-07 ***
Pclass2     -1.560551  0.537871 -2.901  0.00372 **
Pclass3     -2.795107  0.567045 -4.929 8.25e-07 ***
Sexmale     -3.037595  0.328714 -9.241 < 2e-16 ***
Age        -0.053449  0.013691 -3.904 9.46e-05 ***
SibSp       -0.546952  0.199712 -2.739  0.00617 **
Parch       0.168287  0.243458  0.691  0.48942
Fare        -0.001009  0.005304 -0.190  0.84914
EmbarkedQ   1.580764  0.629724  2.510  0.01206 *
EmbarkedS   0.348967  0.412109  0.847  0.39712
---
Signif. codes:  0 '****' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 481.14  on 359  degrees of freedom
Residual deviance: 296.07  on 350  degrees of freedom
AIC: 316.07

Number of Fisher Scoring iterations: 5
```

Figure53

And the prediction result is as follow,

original model	0	1
0	53	15
1	10	22

Accuracy = 0.75

The RMSE of each fold of cross validation is as follow,

	RMSE <dbl>
1 set of cross validation	0.3658122
2 set of cross validation	0.3538622
3 set of cross validation	0.3689574
4 set of cross validation	0.3486499
5 set of cross validation	0.3589968
6 set of cross validation	0.3604252
7 set of cross validation	0.3582554
8 set of cross validation	0.3512021
9 set of cross validation	0.3643373
10 set of cross validation	0.3553576

Figure54

Decision Rule Cut-Off

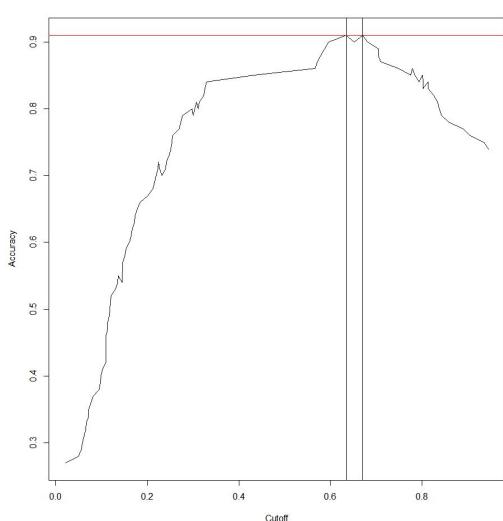
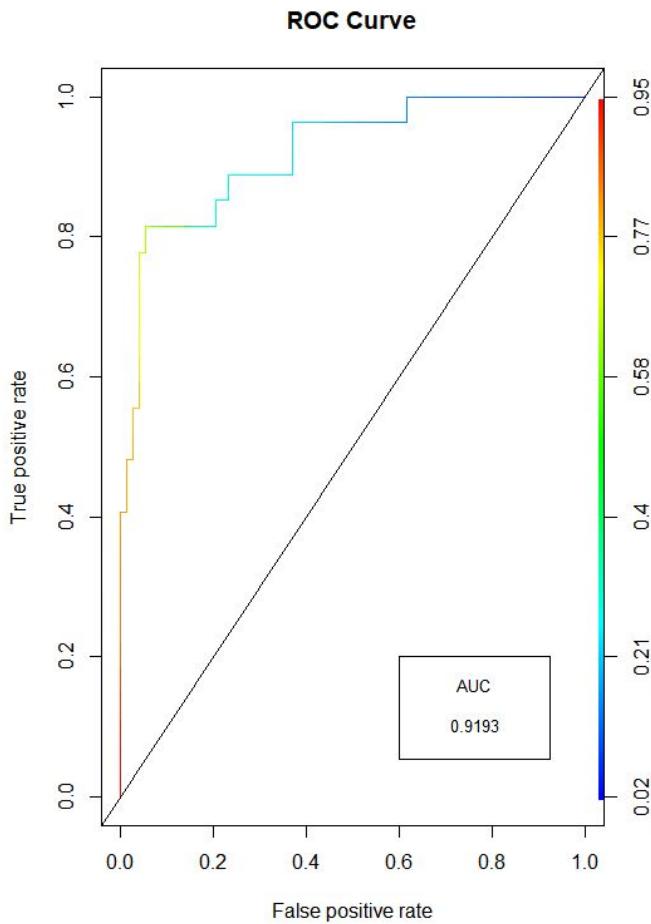


Figure55

However, when we change the cut-off of the model in a correct manner, then the model will become more accurate. In the other words, if we know where the dataset bias to, then we can receive a better model. The cut-off of the original model is 0.5. If the prediction probability is higher than 0.5, the model will classify it as 1 in survived, vice versa. However, the decision rule may not be the best. By using library “ROCR”, the prediction accuracy can be simulated through different cut-off. As the figure is shown, 0.5 cut-off is not the optimum accuracy of the model. In conclusion, the best cut-off is 0.67 which gives 0.91 accuracies.

Using the new cut-off, the prediction on test data get a 0.9 accuracy.

ROC



The ROC curve shows the trade-off between true positive rate(TPR) and false positive rate(FPR). The ROC is far from the 45-degree diagonal so that the accuracy of the model performs well. On the other hand, AUC is 0.9193. AUC is equivalent to the probability that a randomly chosen TPR is ranked higher than that of FPR. Therefore, the AUC measure mentions that the TPR rate is higher than FPR rate in our model.

Figure56

Model Selection

Rather than changing the cut-off, we can also drop some useless parameters out. As we can see, some variables are not significant, which means there is room for us to drop some variables that is less useless to prevent overfitting and let the model become much more general. The AIC and the optimized model is as follow,

```

Step: AIC=328.13
Survived ~ Pclass + Sex + Age + SibSp

      Df Deviance    AIC
<none>     316.13 328.13
- SibSp     1   323.96 333.96
- Age       1   331.14 341.14
- Pclass    2   344.06 352.06
- Sex       1   438.35 448.35

```

Figure57

```

Call:
glm(formula = Survived ~ Pclass + Sex + Age + SibSp, family = binomial,
     data = tin4log_train)

Deviance Residuals:
    Min      1Q  Median      3Q      Max
-2.3608 -0.5668 -0.3918  0.6307  2.4724

Coefficients:
            Estimate Std. Error z value Pr(>|z|)
(Intercept) 4.40918   0.65943   6.686 2.29e-11 ***
Pclass2     -1.27154   0.41837  -3.039 0.002371 **
Pclass3     -2.21180   0.39592  -5.586 2.32e-08 ***
Sexmale     -3.04678   0.29783 -10.230 < 2e-16 ***
Age        -0.04797   0.01261  -3.804 0.000143 ***
SibSp      -0.48668   0.17429  -2.792 0.005231 **
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 535.00 on 399 degrees of freedom
Residual deviance: 341.28 on 394 degrees of freedom
AIC: 353.28

Number of Fisher Scoring iterations: 5

```

Figure58

And the 10 folds RMSE ,accuracy and ROC are as follow,

	RMSE <dbl>
1 set of cross validation	0.3574021
2 set of cross validation	0.3571269
3 set of cross validation	0.3611478
4 set of cross validation	0.3621071
5 set of cross validation	0.3600803
6 set of cross validation	0.3602852
7 set of cross validation	0.3564025
8 set of cross validation	0.3587751
9 set of cross validation	0.3614368
10 set of cross validation	0.3630320

Figure59

improved model	0	1
0	55	16
1	8	21

Accuracy = 0.76

ROC

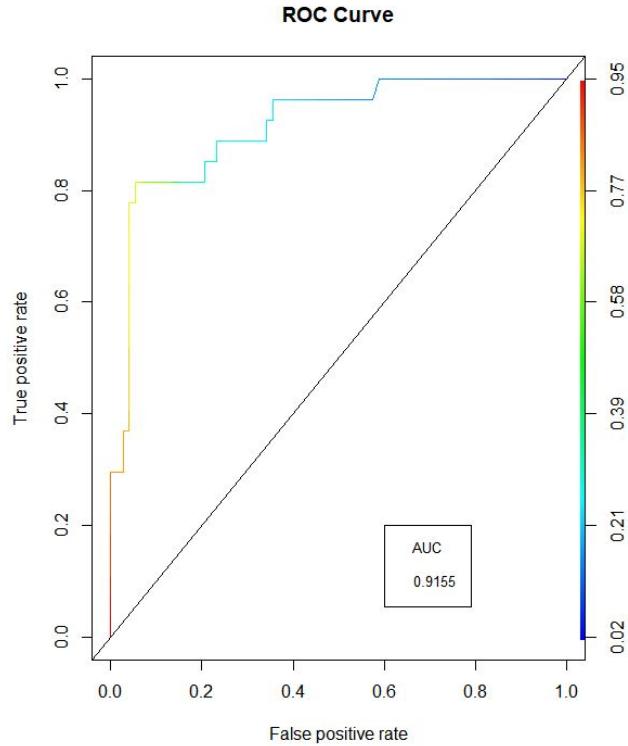


Figure60

As we can see, after the model selection process, the model becomes more accurate and simpler. However, when we take a look at ROC of the second model (figure 60), we can see that the AUC is slightly lesser, which may indicate we may drop too many variables, more investigation may be needed.

Interpretation

The coefficient in the summary of the logistic model indicates the contribution of the number to the model, and since they have a high convergence rate, it is more likely to converge to the favorable result in classification and the result is surprisingly good, about 90% of the result is correctly estimated.

iii. Classification tree

introduction

Classification tree is a type of decision tree. The only difference between classification tree and regression tree is, classification tree is used to predict categorical variable, whereas decision tree is used to predict continuous variables.

Model

The summary and the plot of the classification tree is as follow,

```
Classification tree:
tree(formula = Survived ~ ., data = titanic_train)
variables actually used in tree construction:
[1] "Sex"      "Pclass"    "Embarked" "Age"       "Fare"
Number of terminal nodes:  9
Residual mean deviance:  0.7797 = 304.8 / 391
Misclassification error rate: 0.1775 = 71 / 400
```

Figure61

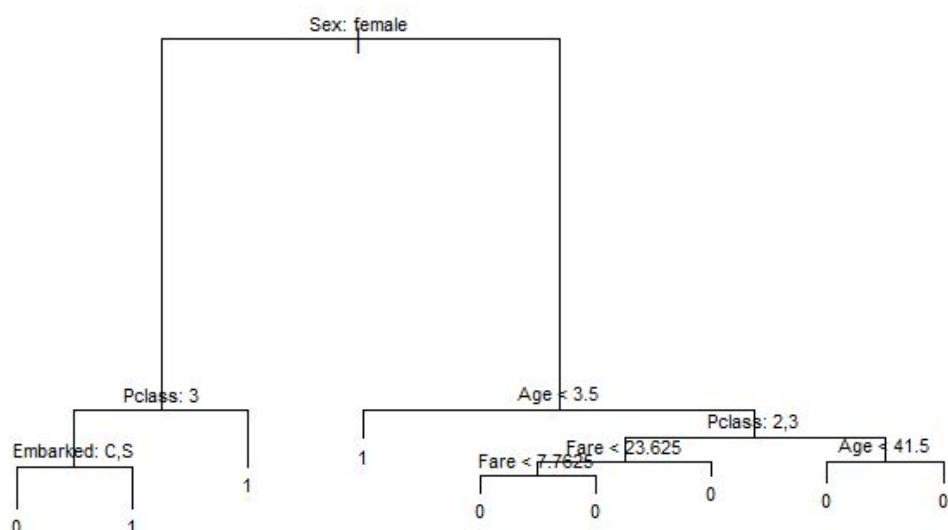


Figure62

And the prediction result is as follow,

Original tree	0	1
0	57	16
1	6	21

Accuracy = 0.78

A classification rate of 0.78 is actually a very outstanding result in terms of only 400 rows of training data and before any tuning of parameters. It is time to see the effect on tree pruning, i.e. get rid of some useless sub trees.

Pruning and model selection

The following graph shows the misclassification error on 10 cv points. As we can see, the misclassification error reaches the lowest on both sizes of 2, 3, 5 trees. Since it is hard to determine which is the best tree, and the following table shows the accuracy of each size of tree.

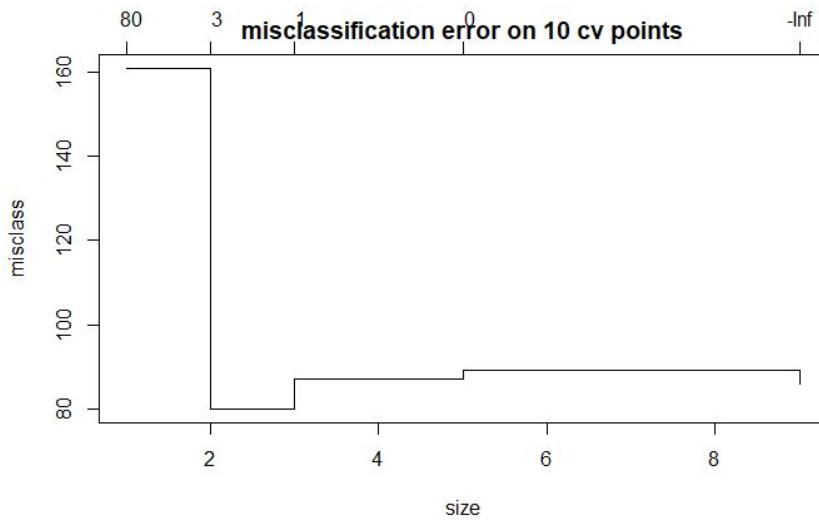


Figure63

tree size	accuracy
2	0.76
3	0.77
5	0.81

Thus, a model with tree size of 5 will be chosen.

Special fact

When we looking at the plot of different sizes of tree, we figure out that *sex* may be the major reason for the survival result.

The graphs below are the tree model of different size.

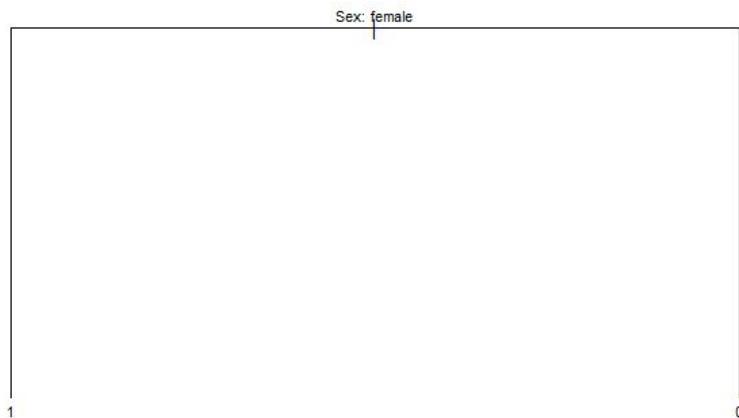


Figure64

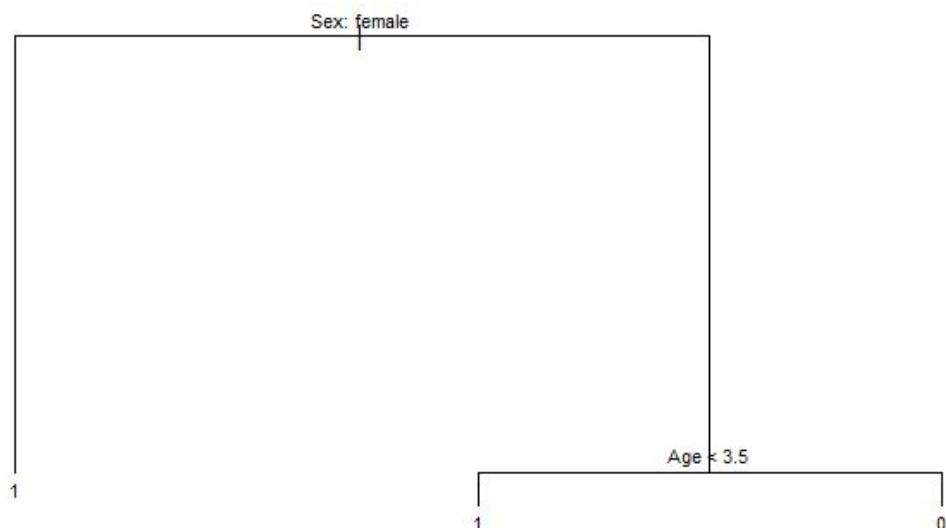


Figure65

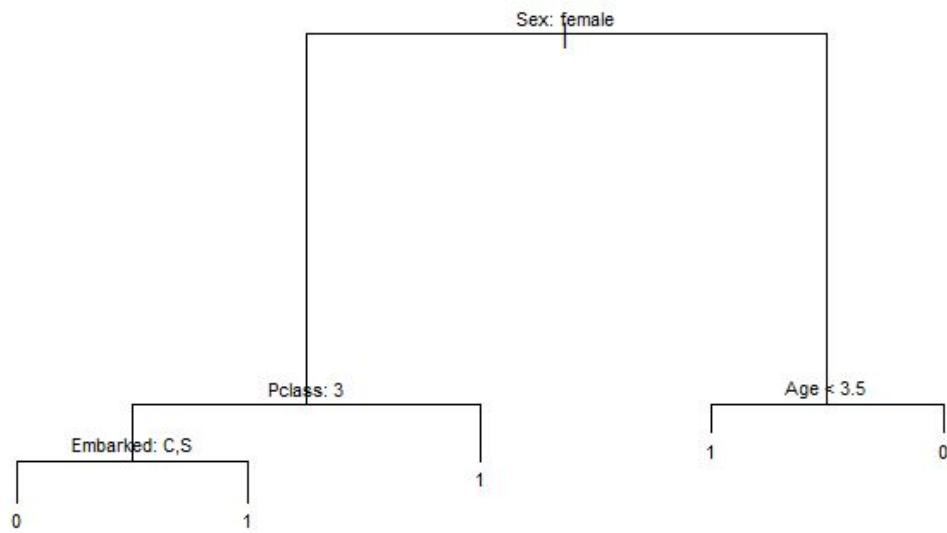


Figure66

We can see that the major factor that the tree consider will always be the *sex*, and more precisely, *Female*. Even a binary tree only classify whether the survivor is Male or female already receive a 0.76 accuracy. We can see how important female is in this dataset.

Conclusion

Classification tree is obviously a strong tool. It performs pretty well even dealing with a small amount of data and receive a 0.81 accuracy, which is pretty impressive. Although it may due to that fact that female is the major factor that affects the survivor, we still cannot deny its power. Furthermore, classification tree is easy to understand and easy to interpret. Tree pruning can even reduce the complexity of the model, making it being more understandable whilst reducing the problem of overfitting.

iv. Random forest

Introduction

Random Forest can be considered as a set of decision tree, in other words, it is an ensemble learning method. When we are talking about decision tree, we know that tree pruning can actually increase the accuracy. One reason for this effect occurs is because the overfitting problem has been reduced, as the tree may be too fit to the training data set, i.e. there may be some pattern only occurs in the training dataset. Thus, in order to deal with this problem, rather than pruning tree, training multiples tree and gather all advantage of them may also be a good idea, and that is what we call random forest.

Model

A 10-folds cross validation has been done and the result is as follow,

```
Random Forest

400 samples
 7 predictor
 2 classes: '0', '1'

No pre-processing
Resampling: Cross-Validated (10 fold, repeated 3 times)
Summary of sample sizes: 361, 360, 360, 360, 359, 361, ...
Resampling results across tuning parameters:

  mtry  Accuracy   Kappa
  1     0.7833927  0.5000134
  2     0.8125453  0.5845067
  3     0.8275281  0.6242803
  4     0.8283615  0.6279940
  5     0.8166114  0.6062560
  7     0.8092120  0.5936528
  9     0.8076053  0.5911707
 10    0.8026673  0.5816914

Accuracy was used to select the optimal model using the largest value.
The final value used for the model was mtry = 4.
```

Figure67

As we can see, when $mtry = 3, 4$ the model performs the best. This means when 3, 4 and 5 variables randomly sampled as candidates at each split, the models under this condition perform the best. Although the algorithm advise us to select the model with $mtry = 4$, but since when $mtry = 3, 4$, the performances are so similar. Thus both parameters will be tested.

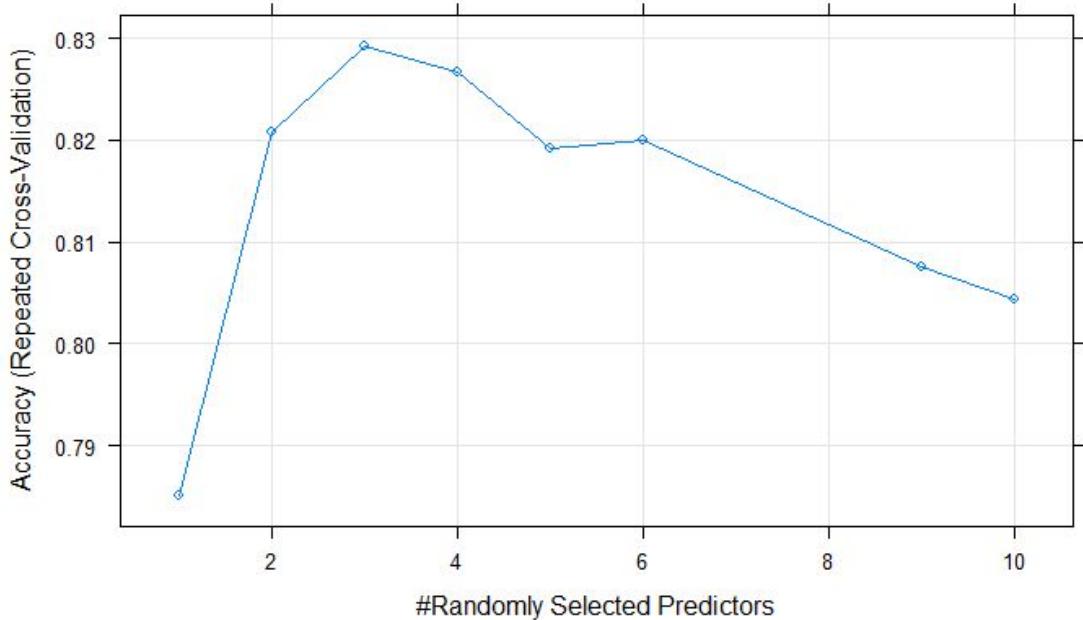


Figure68

Result

Surprisingly, when $\text{mtry} = 3$ and $\text{mtry} = 4$, they both obtain the same result. The confusion matrix is as follow, the accuracy of testing data also agrees with the cross validation result of the training data.

mtry = 3, 4	0	1
0	57	12
1	6	25

$$\text{Accuracy} = 0.82$$

Interpretation

Different from decision tree, since random forest is an assembly of decision tree, so it is hard to interpret the result obtained from random forest. However, if we can think of random forest is a set of tree, then the concept will be easy for layman to understand.

Comparison with a single classification tree

Not surprisingly, random forest does have better performance compare to classification tree. Although the difference may not be so obvious, it may due to the small size of the dataset. We expect the difference will be larger when the size of the dataset increase.

v. Linear Discriminant Analysis

Introduction

Linear discriminant analysis (LDA) is a supervised dimension reduction statistical method. It projects labeled data into a lower dimension plane, and figure out its characteristic or linear combination, in order to form a linear classifier. It assumes independent variables follows normal distribution, thus when the independent variables are not following normal distribution, the performance may not be too favorable.

Model

The LDA model after 10-folds cross validation is as follow,

```
Call:  
lda(x, grouping = y)  
  
Prior probabilities of groups:  
 0   1  
0.61 0.39  
  
Group means:  
    Pclass2  Pclass3  Sexmale      Age     SibSp     Parch     Fare  
0 0.1844262 0.6516393 0.8524590 30.68852 0.5737705 0.3196721 22.86294  
1 0.2500000 0.4102564 0.2564103 27.93750 0.4743590 0.4038462 38.85823  
  EmbarkedC EmbarkedQ EmbarkedS  
0 0.1557377 0.05737705 0.7868852  
1 0.2307692 0.14743590 0.6153846  
  
Coefficients of linear discriminants:  
          LD1  
Pclass2 -0.805448729  
Pclass3 -1.490543754  
Sexmale -2.247040620  
Age     -0.028066952  
SibSp   -0.225666906  
Parch   0.084089834  
Fare    -0.001140404  
EmbarkedC -0.395744912  
EmbarkedQ  0.354568125  
EmbarkedS -0.393287193
```

Figure69

Accuracy = 0.78

Fortunately, we do not have to tune the parameter by our self, as the function will help us to tune the parameter, by fitting different folds of data into the normal distribution, then it will automatically receive the optimal mean of each component.

Cross-Validation

Accuracy of the 1 folds	0.8138889
Accuracy of the 2 folds	0.8277778
Accuracy of the 3 folds	0.8194444
Accuracy of the 4 folds	0.8083333
Accuracy of the 5 folds	0.8194444
Accuracy of the 6 folds	0.8138889
Accuracy of the 7 folds	0.8166667
Accuracy of the 8 folds	0.8138889
Accuracy of the 9 folds	0.8222222
Accuracy of the 10 folds	0.8027778

10-folds cross-validation is applied to the LDA model. Since LDA is not able to compute RMSE, accuracy of each fold validation is applied. As the figure shown, the accuracy of each fold validation is all over 0.8. The figure shows that LDA model performs stably around 0.8 to 0.82.

Figure70

Interpretation

The group means in the model means the mean of the respective components such as Age is 30 if getting 0, and 27.9 if getting 1. It follows the ‘voting rules’, if the data is close to 0, for example, Age is close to 30.688, Fare is close to 22.86, and so on, then the answer is 0; else if the data close to 1, then the answer is 1.

Problem

LDA is a very powerful algorithm and it is not normal that it only has accuracy for 0.78. Thus, an investigation has been done and the result is as follows. As we can see, at least 3 variables are not following normal distribution, as a result, it is letting the accuracy not as favorable as we think.

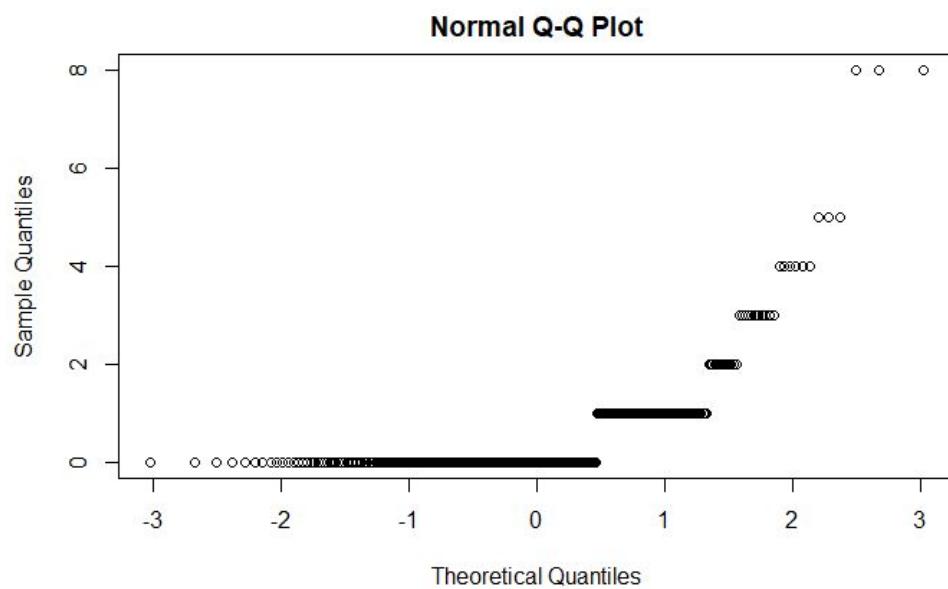


Figure71

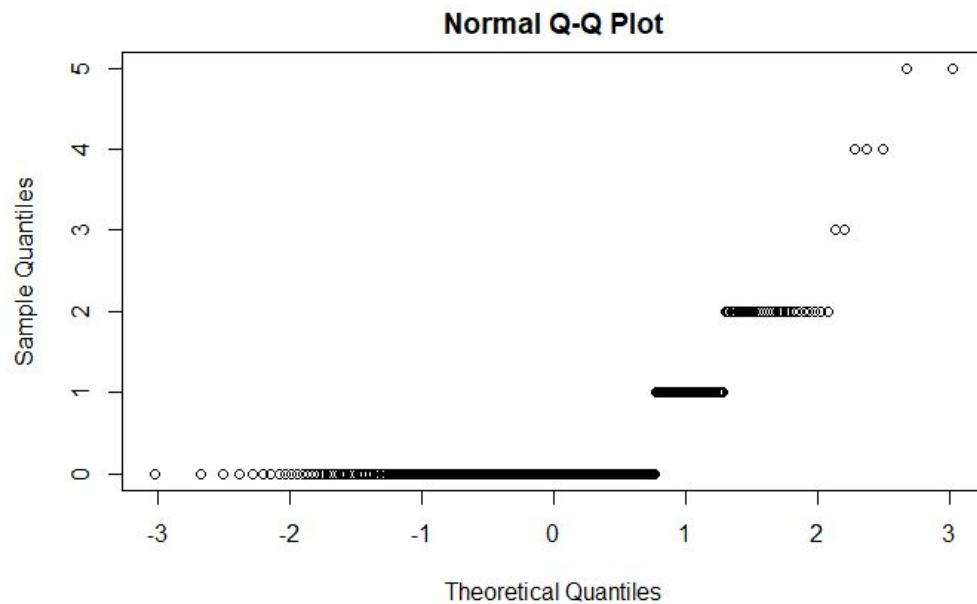


Figure72

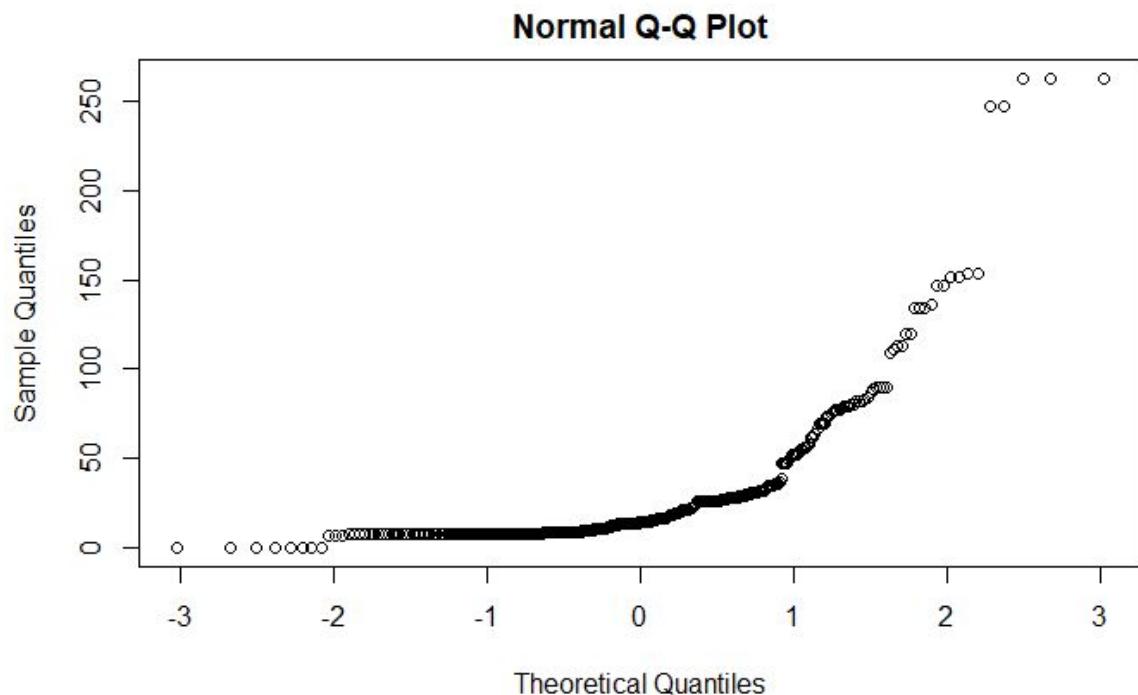


Figure73

Conclusion

Although LDA is very powerful in other datasets. However, as the amount of data is not enough to follow the law of large numbers, so some variables are not following normal distribution, and it leads to such a non-favourable result. Nevertheless, it still receives an accuracy of 0.78, which is still better than some naive statistical method such as linear regression and shows how powerful it can be in other datasets.

vi. Gradient Boosting

Introduction

Gradient boosting is strong learning through ensembling a number of decision trees. Therefore, similar to decision tree, interaction depth, number of trees and shrinkage, etc are the parameters to be discussed. In classification case, the metric will be accuracy.

Simulation

Stochastic Gradient Boosting					
400 samples					
7 predictors					
2 classes: '0', '1'					
No pre-processing					
Resampling: Cross-validated (10 fold)					
Summary of sample sizes: 360, 360, 360, 360, 360, 360, 360, ...					
Resampling results across tuning parameters:					
shrinkage	interaction.depth	n.trees	Accuracy	Kappa	
0.001	1	0	0.5850109	0.0000000	
0.001	1	50	0.5850109	0.0000000	
0.001	1	100	0.5850109	0.0000000	
0.001	1	150	0.5850109	0.0000000	
0.001	1	200	0.5850109	0.0000000	
0.001	1	250	0.5850109	0.0000000	
0.001	1	300	0.7773499	0.3337927	
0.001	1	350	0.7898499	0.5635830	
0.001	1	400	0.7898499	0.5635830	
0.001	1	450	0.7898499	0.5635830	
0.001	1	500	0.7898499	0.5635830	
0.001	1	550	0.7898499	0.5635830	
0.001	1	600	0.7898499	0.5635830	
0.001	1	650	0.7898499	0.5635830	
0.001	1	700	0.7898499	0.5635830	
0.001	1	750	0.7898499	0.5635830	
0.001	1	800	0.7898499	0.5635830	
0.001	1	850	0.7898499	0.5635830	
0.001	1	900	0.7898499	0.5635830	
0.001	1	950	0.7898499	0.5635830	
0.001	1	1000	0.7898499	0.5635830	
0.001	1	1050	0.7898499	0.5635830	
0.001	1	1100	0.7898499	0.5635830	
0.001	1	1150	0.7898499	0.5635830	

Figure74

The training dataset is 80% of the whole data so that there are 400 samples and 7 predictors(features) in the simulation where “PassengerId” is omitted. The grid of gbm is the following: interaction depth is a vector [1 3 5]; number of tree is a sequence from 0 to 2500 separated by 50 each; shrinkage is a vector of [0.01 0.001]; number of minobsinnode is 10.

10-folds cross validation is applied during training. Finally, a gradient boosting model is trained with the formula “Survived” against all variables.

Feature Importance

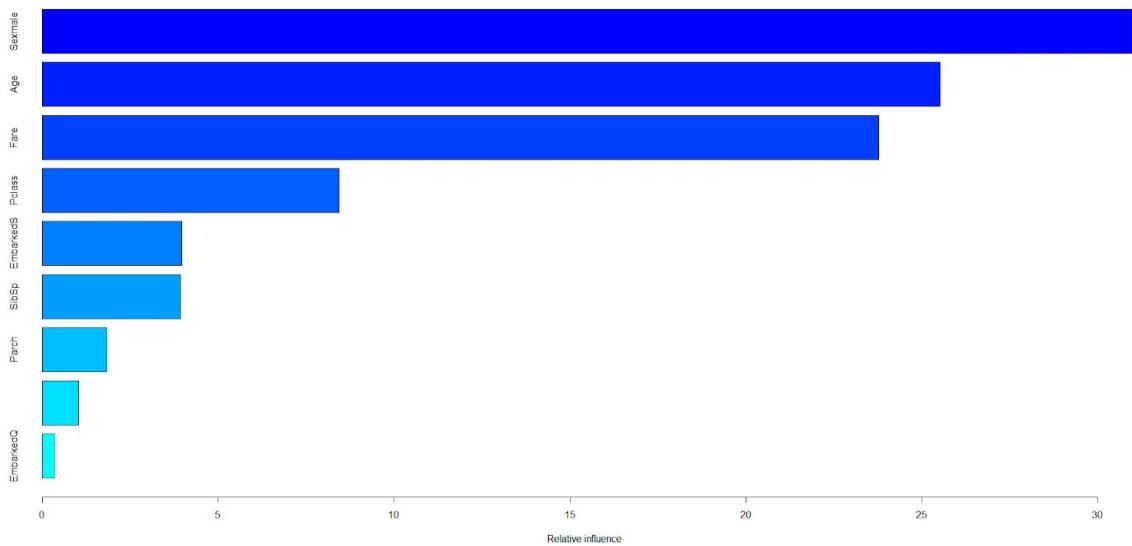


Figure75

```
var      rel.inf
Sexmale 31.1531575
      Age 25.5245054
      Fare 23.7782815
      Pclass 8.4299316
EmbarkedS 3.9605719
      SibSp 3.9340772
      Parch 1.8402215
EmbarkedC 1.0253790
EmbarkedQ 0.3538745
```

Figure76

The figures show that the “sex” is the most important feature which gives around 31 of relative influence. “Age” and “Fare” are the second and third most important features which give almost 25 and 23 of relative influence.

Dummy variable “Embarked” are the least important features which give the lowest relative influence. However, “Embarked” is still necessary for modeling because the relative influence is non-zero.

Summary of GBM

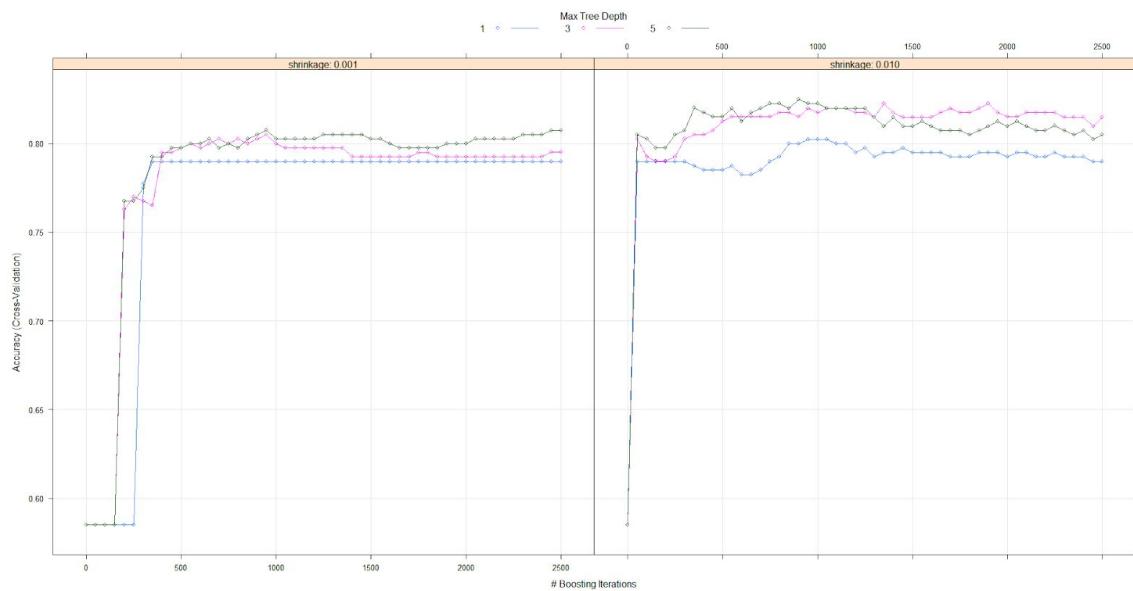


Figure77

The diagram shows the performance of gbm model with different parameter combinations. The figure shows that 500 to 1500 iterations(number of trees) gives better model because it is a sharp increasing trend and becomes flat. As shown, the accuracy of models with shrinkage 0.010 is generally higher than models with shrinkage 0.001. As the diagram is shown, 5(green line) or 3(pink line) maximum tree depth perform better than 1 maximum tree depth(blue line). In conclusion, the best gbm model should be 500-1500 iterations, 0.010 shrinkage, and 5 or 3 maximum tree depth.

Confusion Matrix & Interpretation

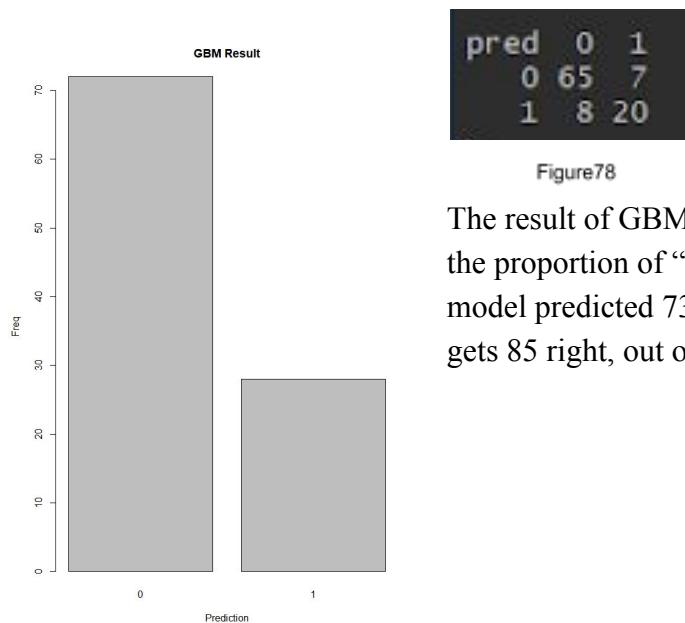


Figure78

The result of GBM is good. From the histogram, the proportion of “0” is much greater than “1”. The model predicted 73 “0” and 27 “1”. The prediction gets 85 right, out of 100 entries.

Figure79

Receiver Operating Characteristic Curve(ROC Curve)

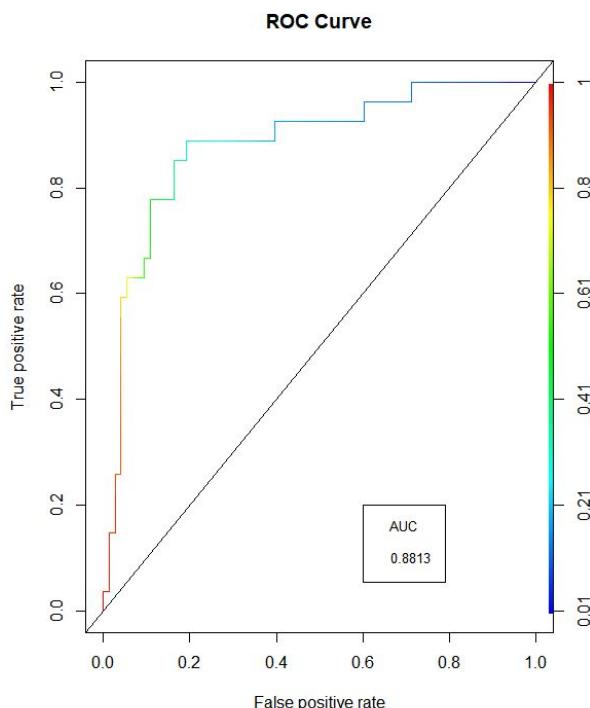


Figure80

The ROC curve shows the trade-off between true positive rate(TPR) and false positive rate(FPR). The ROC is far from the 45-degree diagonal so that the accuracy of the model performs well. On the other hand, AUC is 0.8813. Therefore, the AUC measure mentions that the TPR rate is higher than FPR rate in our model.

Decision Rule Cut-Off

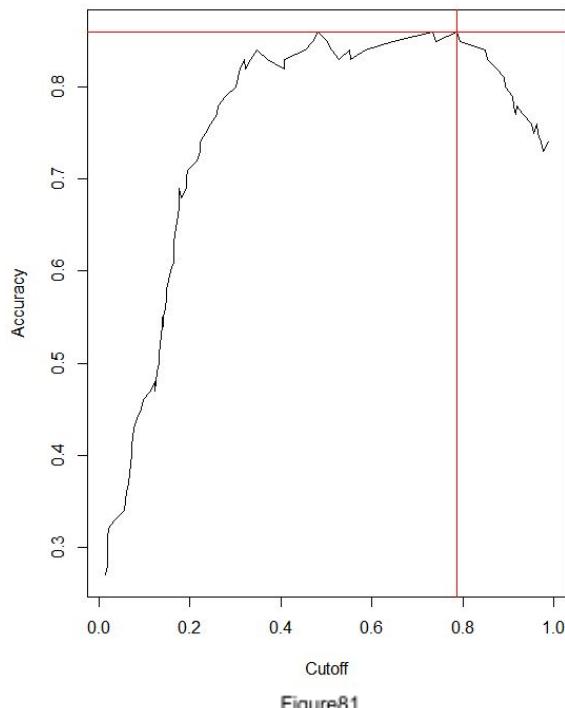


Figure81

The cut-off of the original model is 0.5. If the prediction probability is higher than 0.5, the model will classify it as 1 in survived, vice versa. However, the decision rule may not be the best. By using library “ROCR”, the prediction accuracy can be simulated through different cut-off. As the figure is shown, 0.5 cut-off is not the optimum accuracy of the model. In conclusion, the best cut-off is 0.79 which gives 0.86 accuracies.

Using the new cut-off, the prediction on test data gets a 0.84 accuracy.

vii. Support Vector Machine

Introduction

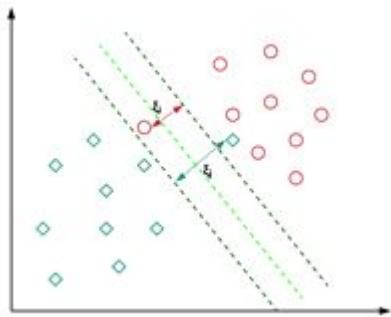


Figure82

Support-vector-machine is a supervised learning model for classification. As shown above, support-vector-machine builds a linear hyperplane(green dash line) to classify squares and circles. 2 black dash lines are the margin of the hyperplane.

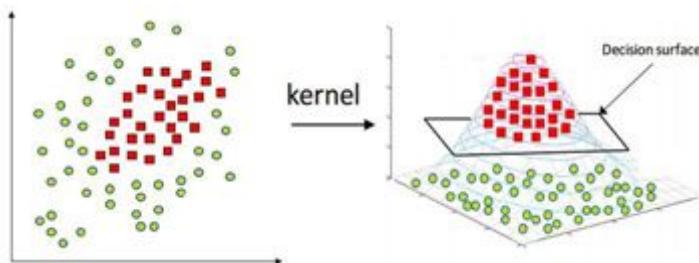


Figure83

Normally, data don't separate clearly. In "Titanic" case, the radial kernel is applied to solve the problem. If the data points are overlapping, the radial kernel will increase the dimensions. As the figure is shown, some hyperplanes fit after a new dimension is defined. The new dimension is defined to be:

$$f(x_1, x_2) = e^{-\frac{\|x_1 - x_2\|}{\sigma}}$$

SVM Model and Cross Validation

```
call:  
best.tune(method = svm, train.x = survived ~ ., data = titanic_train, ranges = list(cost = c(0.01, 0.1, 1, 10, 100, 1000, 10000)))  
  
Parameters:  
  SVM-Type: C-classification  
  SVM-Kernel: radial  
  cost: 1  
  
Number of Support Vectors: 214
```

Figure84

```
Parameter tuning of 'svm':  
- sampling method: 10-fold cross validation  
- best parameters:  
  cost  
    1  
- best performance: 0.2025  
- Detailed performance results:  
  cost   error dispersion  
1 1e-02 0.4150 0.06032320  
2 1e-01 0.2325 0.05779514  
3 1e+00 0.2025 0.06061032  
4 1e+01 0.2175 0.07642171  
5 1e+02 0.2175 0.06566963  
6 1e+03 0.2250 0.05773503  
7 1e+04 0.2450 0.05502525
```

Figure85

10-folds cross validation is applied in tuning the SVM model. As shown from the above figure, 0.01 to 10000 cost parameters are input in cross validation. The second figure shows the result that the 3rd row, cost=1, gives the least error and small dispersion. Therefore, 1 cost parameter is the best within 7 choices. On the other hand, the first figure also shows the radial is the best kernel method.

Confusion Matrix & Interpretation

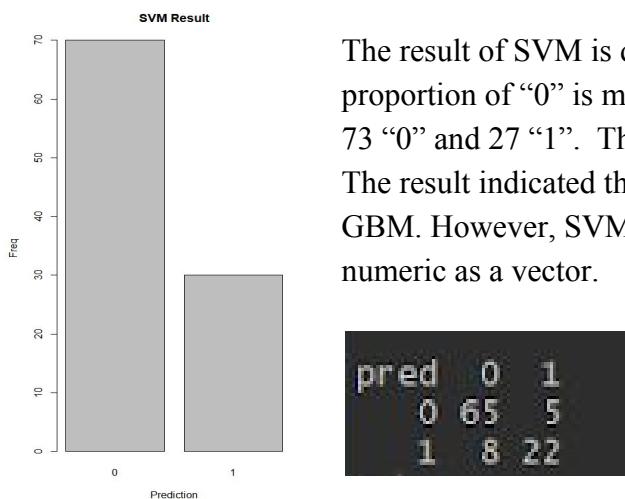


Figure86

pred	0	1
0	65	5
1	8	22

Figure87

The result of SVM is quite good. From the histogram, the proportion of "0" is much greater than "1". The model predicted 73 "0" and 27 "1". The prediction gets 87 right, out of 100 entries. The result indicated that SVM is a strong learner as strong as GBM. However, SVM can't handle NA and the variables must be numeric as a vector.

Conclusion

Model	Accuracy
KNN	0.752
Logistic Regression	0.90
Classification Tree	0.78
Random Forest	0.82
Linear Discriminat Analysis	0.78
Gradient Boosting	0.85
Support Vector Machine	0.87

As the table shown, logistic regression has the highest accuracy in prediction because it performs well in binary classification. However, it is very weak in non-binary classification problem. On the other hand, KNN has the lowest accuracy because it only performs well only in low dimension.

Contribution

CHENG Wing Ryan	25%
Hung Fan Hin	25%
Lee Ka Hin	25%
Li Tak Leong	25%