

Machine Learning

Clustering

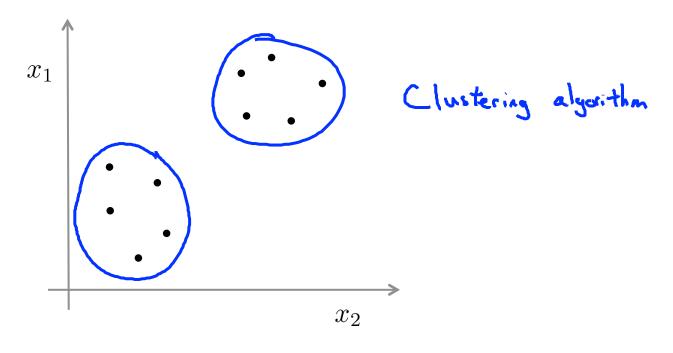
Unsupervised learning introduction

Supervised learning



Training set: $\{(x^{(1)}, y^{(1)}), (x^{(2)}, y^{(2)}), (x^{(3)}, y^{(3)}), \dots, (x^{(m)}, y^{(m)})\}$

Unsupervised learning



Training set: $\{x^{(1)}, x^{(2)}, x^{(3)}, \dots, x^{(m)}\}$

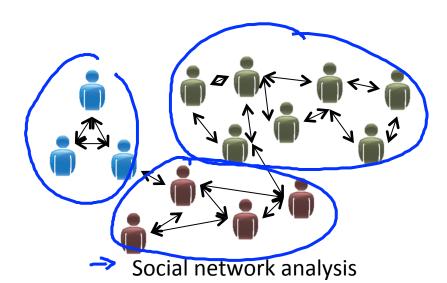
Applications of clustering

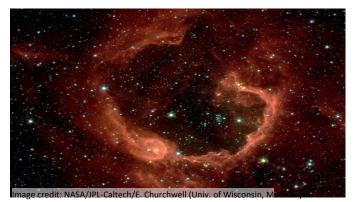


Market segmentation



Organize computing clusters





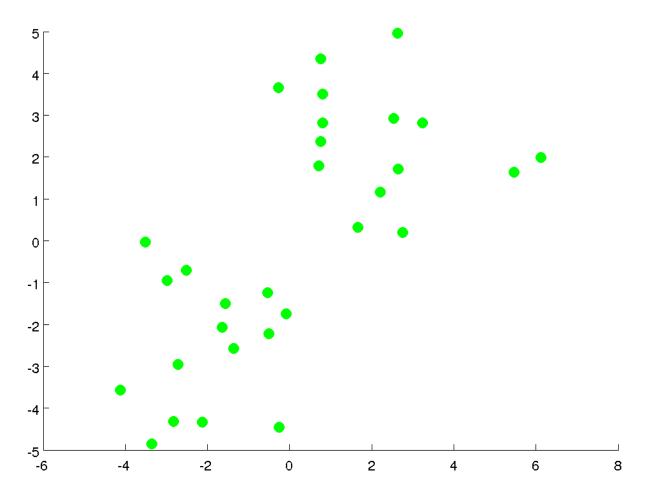
Astronomical data analysis

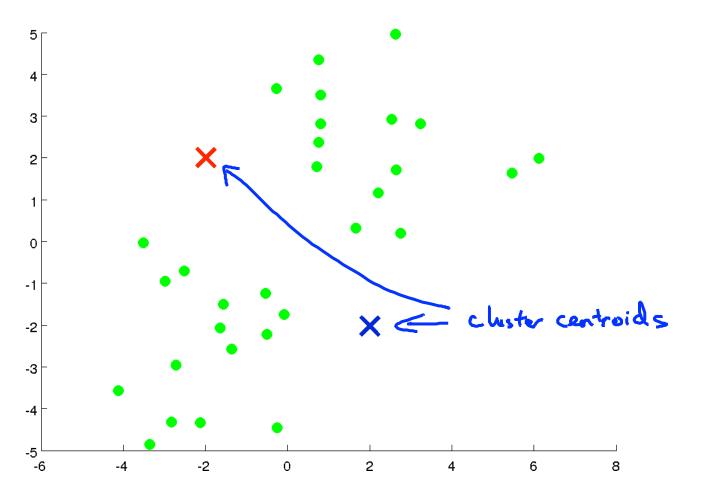


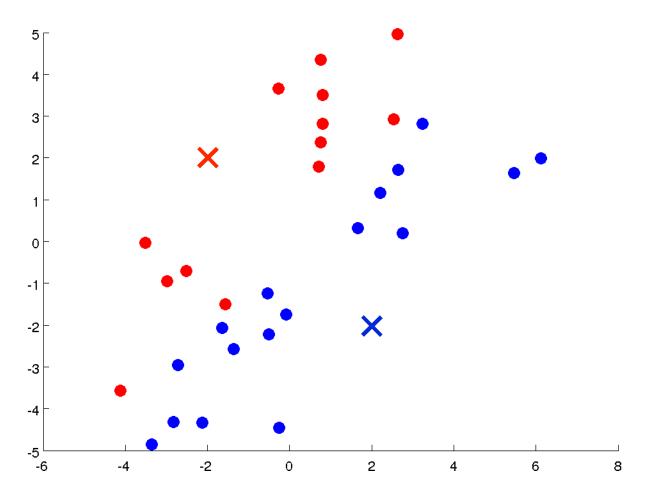
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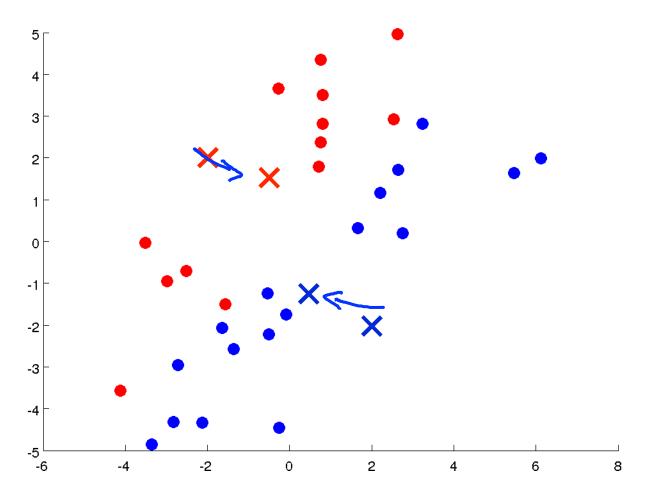
Clustering

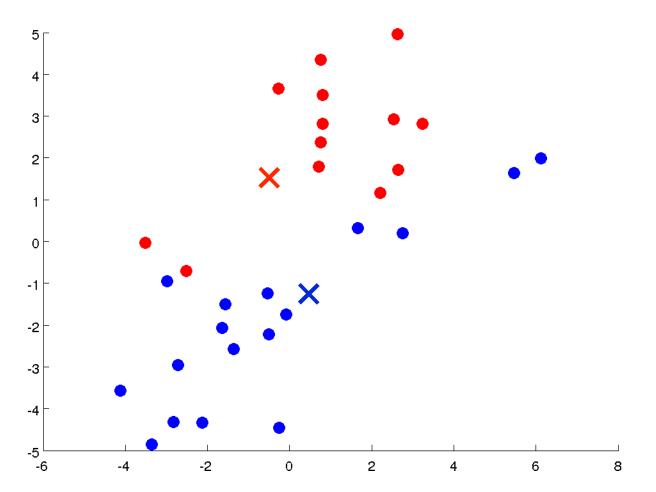
K-means algorithm

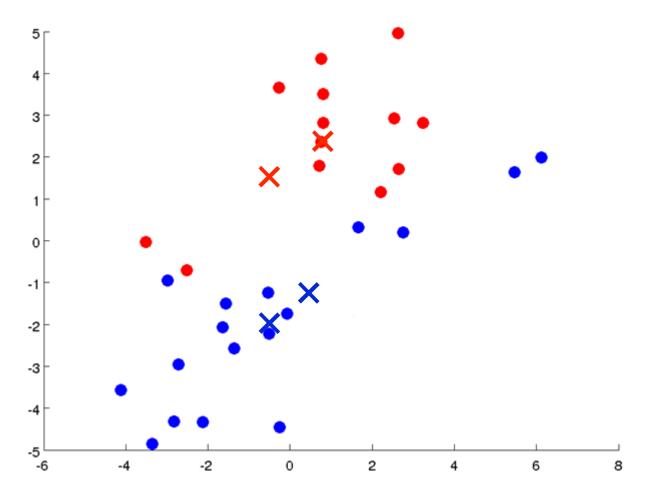


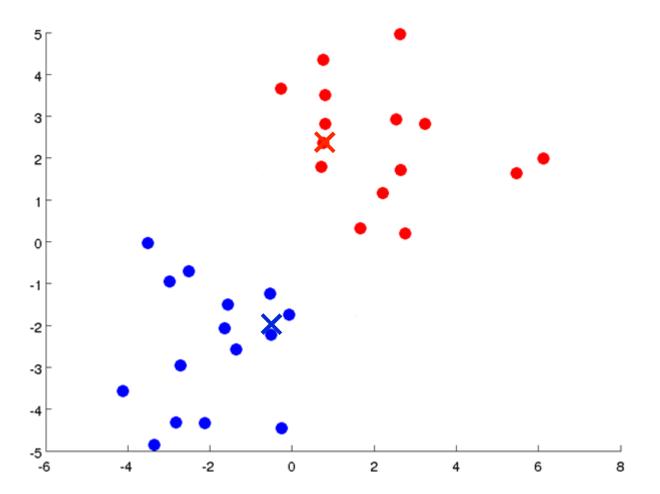


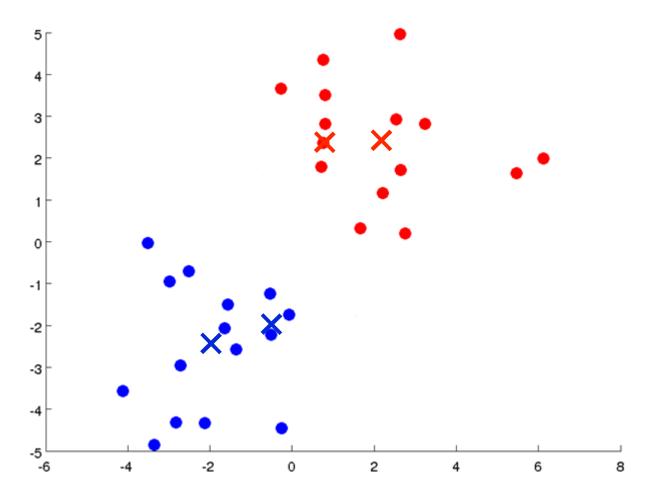


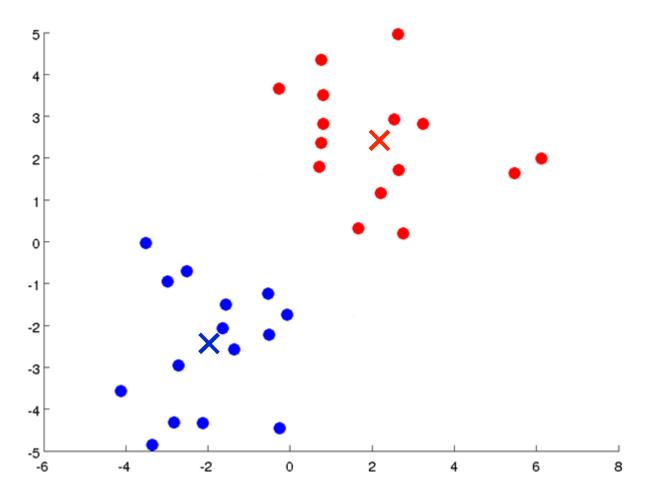












Input:

- K (number of clusters)
- Training set $\{x^{(1)}, x^{(2)}, \dots, x^{(m)}\}$

$$x^{(i)} \in \mathbb{R}^n$$
 (drop $x_0 = 1$ convention)

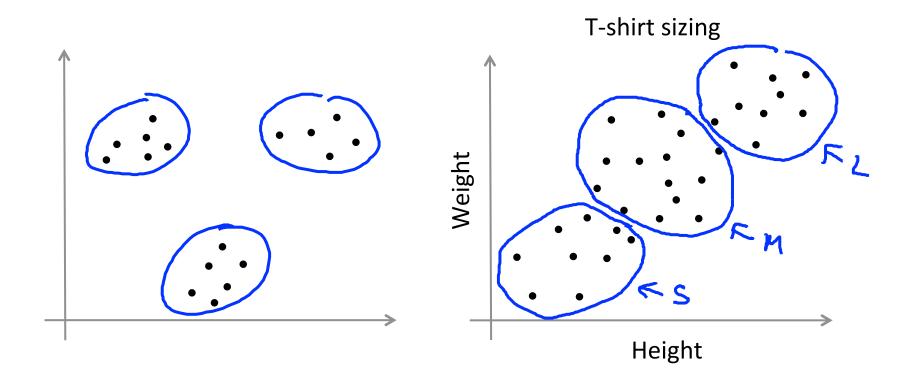


Randomly initialize K cluster centroids $\mu_1, \mu_2, \ldots, \mu_K \in \mathbb{R}^n$ Repeat { Repeat {

Cluster for i = 1 to mconsider the step of the st

K-means for non-separated clusters







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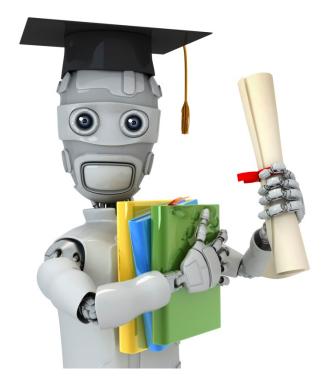
Clustering Optimization objective

K-means optimization objective

- $ightharpoonup c^{(i)}$ = index of cluster (1,2,...,K) to which example $x^{(i)}$ is currently assigned
- $\rightarrow \mu_k = \text{cluster centroid} \, \underline{k} \, (\mu_k \in \mathbb{R}^n)$
 - $\mu_{c^{(i)}}$ = cluster centroid of cluster to which example $x^{(i)}$ has been assigned $x^{(i)} \rightarrow 5$ $x^{(i)} = x^{(i)} = x^{(i)}$

Optimization objective:

```
Randomly initialize K cluster centroids \mu_1, \mu_2, \ldots, \mu_K \in \mathbb{R}^n Cluster essignment step (iii) containing K Repeat K
               c^{(i)} := \mathsf{index} (from 1 to K ) of cluster centroid
                        closest to x^{(i)}
         for k = 1 to K
                \mu_k := average (mean) of points assigned to cluster k
```



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Clustering Random initialization

Randomly initialize K cluster centroids $\mu_1, \mu_2, \dots, \mu_K \in \mathbb{R}^n$

```
Repeat {
        for i = 1 to m
           c^{(i)} := \text{index (from 1 to } K \text{ ) of cluster centroid}
                   closest to x^{(i)}
        for k = 1 to K
            \mu_k := average (mean) of points assigned to cluster k
```

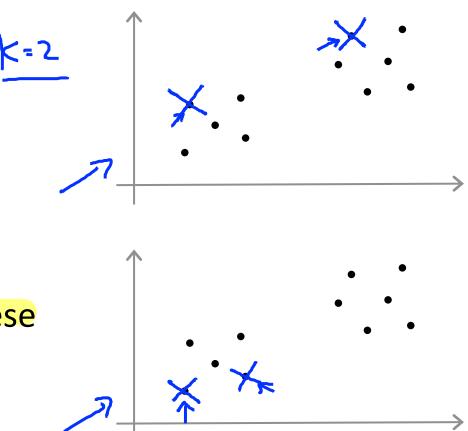
Random initialization

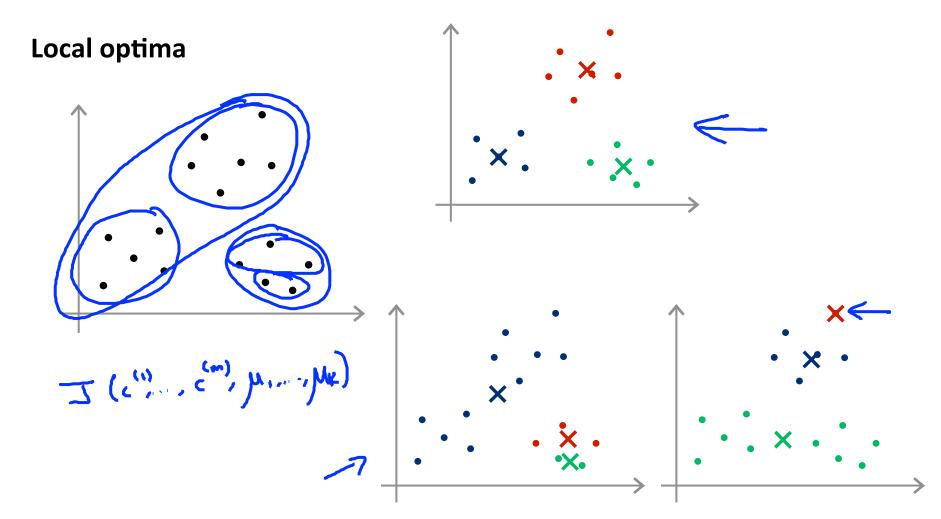
Should have K < m

Randomly pick \underline{K} training examples.

Set μ_1, \dots, μ_K equal to these K examples. $\mu_i = \chi^{(i)}$

$$\mu_{5} = \kappa_{(1)}$$



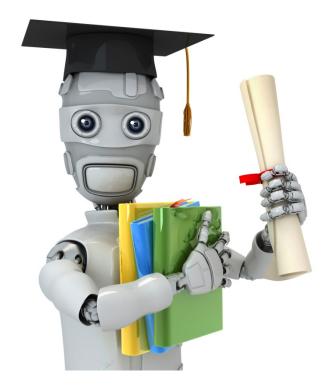


Random initialization

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For i = 1 to 100 {
```

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Randomly initialize K-means. Run K-means. Get c^{(1)},\dots,c^{(m)},\mu_1,\dots,\mu_K. Compute cost function (distortion) J(c^{(1)},\dots,c^{(m)},\mu_1,\dots,\mu_K) }
```

Pick clustering that gave lowest cost $J(c^{(1)},\ldots,c^{(m)},\mu_1,\ldots,\mu_K)$

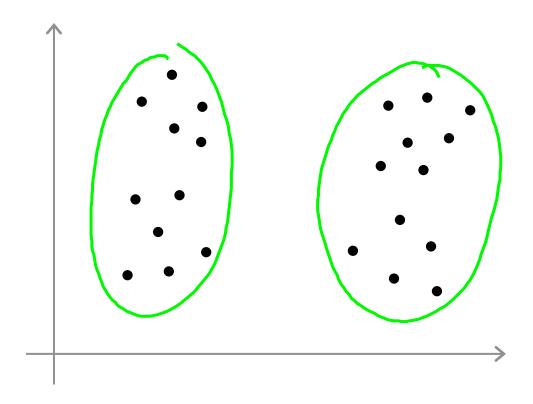


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Clustering

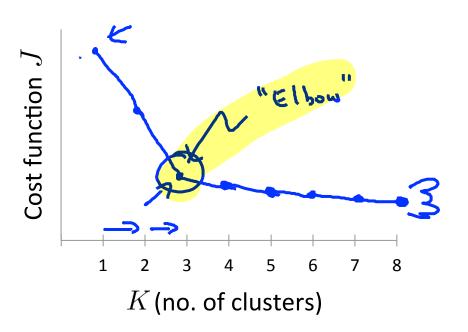
Choosing the number of clusters

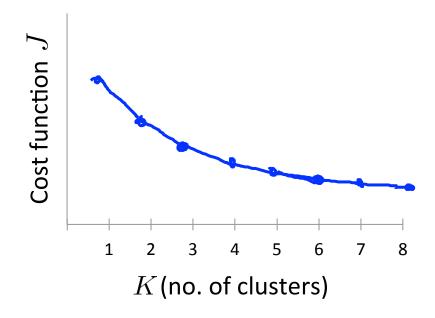
What is the right value of K?



Choosing the value of K

Elbow method:





Choosing the value of K

Sometimes, you're running K-means to get clusters to use for some later/downstream purpose. Evaluate K-means based on a metric for how well it performs for that later purpose.

