Chen GU Assignment 3 CPSC 424

Building and running information

Development environment

Module loaded

Currently Loaded Modulefiles:

- 1) Base/yale_hpc
- 2) Langs/Intel/15
- 3) MPI/OpenMPI/1.8.6-intel15
- 4) Tools/TotalView/8.14.1-8
- 5) GPU/Cuda/8.0

env command

```
MKLR00T=/home/apps/fas/Langs/Intel/2015_update2/composer_xe_2015.2.164/mkl
MANPATH=/home/apps/fas/Tools/TotalView/toolworks/totalview.8.14.1-8/man:/u
sr/local/cluster/hpc/MPI/0penMPI/1.8.6-intel15/share/man:/home/apps/fas/La
ngs/Intel/2015_update2/composer_xe_2015.2.164/man/en_US:/home/apps/fas/Lan
gs/Intel/2015_update2/composer_xe_2015.2.164/debugger/gdb/intel64/share/ma
n/:/home/apps/fas/Langs/Intel/2015_update2/composer_xe_2015.2.164/debugger
/gdb/intel64_mic/share/man/:/usr/share/man:/opt/moab/share/man:
GDB_HOST=/home/apps/fas/Langs/Intel/2015_update2/composer_xe_2015.2.164/de
bugger/qdb/intel64 mic/bin/qdb-ia-mic
HOSTNAME=compute-45-4.local
PBS_VERSION=TORQUE-4.2.9
IPPROOT=/home/apps/fas/Langs/Intel/2015_update2/composer_xe_2015.2.164/ipp
INTEL_LICENSE_FILE=/home/apps/fas/Langs/Intel/2015_update2/composer_xe_201
5.2.164/licenses:/opt/intel/licenses:/home/apps/fas/Licenses/intel site.li
TERM=xterm-256color
SHELL=/bin/bash
HISTSIZE=1000
GDBSERVER_MIC=/home/apps/fas/Langs/Intel/2015_update2/composer_xe_2015.2.1
64/debugger/gdb/target/mic/bin/gdbserver
```

```
PBS JOBNAME=STDIN
LIBRARY_PATH=/usr/local/cluster/hpc/GPU/Cuda/8.0/lib64:/usr/local/cluster/
hpc/GPU/Cuda/8.0/lib:/usr/local/cluster/hpc/MPI/OpenMPI/1.8.6-intel15/lib:
/home/apps/fas/Langs/Intel/2015_update2/composer_xe_2015.2.164/ipp/../comp
iler/lib/intel64:/home/apps/fas/Langs/Intel/2015_update2/composer_xe_2015.
2.164/ipp/lib/intel64:/home/apps/fas/Langs/Intel/2015_update2/composer_xe_
2015.2.164/compiler/lib/intel64:/home/apps/fas/Langs/Intel/2015_update2/co
mposer_xe_2015.2.164/mkl/lib/intel64:/home/apps/fas/Langs/Intel/2015_updat
e2/composer_xe_2015.2.164/tbb/lib/intel64/gcc4.4
PERL5LIB=/opt/moab/lib/perl5
FPATH=/usr/local/cluster/hpc/MPI/OpenMPI/1.8.6-intel15/include:/home/apps/
fas/Langs/Intel/2015_update2/composer_xe_2015.2.164/mkl/include
PBS_ENVIRONMENT=PBS_INTERACTIVE
QTDIR=/usr/lib64/qt-3.3
QTINC=/usr/lib64/qt-3.3/include
INCLUDE_PATH=/usr/local/cluster/hpc/GPU/Cuda/8.0/include
MIC_LD_LIBRARY_PATH=/home/apps/fas/Langs/Intel/2015_update2/composer_xe_20
15.2.164/mpirt/lib/mic:/home/apps/fas/Langs/Intel/2015_update2/composer_xe
_2015.2.164/ipp/lib/mic:/home/apps/fas/Langs/Intel/2015_update2/composer_x
e 2015.2.164/compiler/lib/mic:/home/apps/fas/Langs/Intel/2015_update2/comp
oser_xe_2015.2.164/mkl/lib/mic:/opt/intel/mic/coi/device-linux-release/lib
:/opt/intel/mic/myo/lib:/home/apps/fas/Langs/Intel/2015_update2/composer_x
e_2015.2.164/tbb/lib/mic
PBS_0_WORKDIR=/lustre/home/client/fas/cpsc424/cg736/as/as6
ANT_HOME=/opt/rocks
LC_ALL=en_US
PBS_TASKNUM=1
USER=cq736
LD_LIBRARY_PATH=/usr/local/cluster/hpc/GPU/Cuda/8.0/lib64:/usr/local/clust
er/hpc/MPI/OpenMPI/1.8.6-intel15/lib:/home/apps/fas/Langs/Intel/2015_updat
e2/composer_xe_2015.2.164/mpirt/lib/intel64:/home/apps/fas/Langs/Intel/201
5_update2/composer_xe_2015.2.164/ipp/../compiler/lib/intel64:/home/apps/fa
s/Langs/Intel/2015_update2/composer_xe_2015.2.164/ipp/lib/intel64:/home/ap
ps/fas/Langs/Intel/2015_update2/composer_xe_2015.2.164/ipp/tools/intel64/p
erfsys:/opt/intel/mic/coi/host-linux-release/lib:/opt/intel/mic/myo/lib:/h
ome/apps/fas/Langs/Intel/2015_update2/composer_xe_2015.2.164/compiler/lib/
intel64:/home/apps/fas/Langs/Intel/2015_update2/composer_xe_2015.2.164/mkl
/lib/intel64:/home/apps/fas/Langs/Intel/2015_update2/composer_xe_2015.2.16
4/tbb/lib/intel64/gcc4.4:/home/apps/fas/Langs/Intel/2015_update2/composer_
xe_2015.2.164/debugger/ipt/intel64/lib
PBS_0_HOME=/home/fas/cpsc424/cg736
MIC_LIBRARY_PATH=/home/apps/fas/Langs/Intel/2015_update2/composer_xe_2015.
2.164/compiler/lib/mic:/home/apps/fas/Langs/Intel/2015_update2/composer_xe
_2015.2.164/mpirt/lib/mic:/home/apps/fas/Langs/Intel/2015_update2/composer
_xe_2015.2.164/tbb/lib/mic
ROCKS_ROOT=/opt/rocks
CPATH=/usr/local/cluster/hpc/GPU/Cuda/8.0/include:/usr/local/cluster/hpc/M
PI/OpenMPI/1.8.6-intel15/include:/home/apps/fas/Langs/Intel/2015_update2/c
omposer_xe_2015.2.164/ipp/include:/home/apps/fas/Langs/Intel/2015_update2/
```

```
composer xe 2015.2.164/mkl/include:/home/apps/fas/Langs/Intel/2015_update2
/composer xe 2015.2.164/tbb/include
PBS WALLTIME=14400
PBS_GPUFILE=/var/spool/torque/aux//5451302.rocks.omega.hpc.yale.internalgp
PBS MOMPORT=15003
PBS 0 QUEUE=cpsc424qpu
YHPC COMPILER=Intel
OMPI_MCA_orte_precondition_transports=f20cd2d28f432704-15e3f8c3bb8e89d6
NLSPATH=/home/apps/fas/Langs/Intel/2015_update2/composer_xe_2015.2.164/com
piler/lib/intel64/locale/%l_%t/%N:/home/apps/fas/Langs/Intel/2015_update2/
composer xe 2015.2.164/ipp/lib/intel64/locale/%l %t/%N:/home/apps/fas/Lang
s/Intel/2015_update2/composer_xe_2015.2.164/mkl/lib/intel64/locale/%l_%t/%
N:/home/apps/fas/Langs/Intel/2015_update2/composer_xe_2015.2.164/debugger/
gdb/intel64_mic/share/locale/%l_%t/%N:/home/apps/fas/Langs/Intel/2015_upda
te2/composer_xe_2015.2.164/debugger/gdb/intel64/share/locale/%l_%t/%N
MAIL=/var/spool/mail/cg736
PBS_0_LOGNAME=cg736
PATH=/usr/local/cluster/hpc/GPU/Cuda/8.0/samples/bin/x86_64/linux/release:
/usr/local/cluster/hpc/GPU/Cuda/8.0/bin:/home/apps/fas/Tools/TotalView/too
lworks/totalview.8.14.1-8/bin:/home/apps/fas/Tools/TotalView/toolworks/mem
oryscape.3.6.1-8/bin:/home/apps/fas/Tools/TotalView:/usr/local/cluster/hpc
/MPI/OpenMPI/1.8.6-intel15/bin:/home/apps/fas/Langs/Intel/2015_update2/com
poser_xe_2015.2.164/bin/intel64:/home/apps/fas/Langs/Intel/2015_update2/co
mposer_xe_2015.2.164/mpirt/bin/intel64:/home/apps/fas/Langs/Intel/2015_upd
ate2/composer_xe_2015.2.164/debugger/gdb/intel64_mic/bin:/home/apps/fas/La
ngs/Intel/2015_update2/composer_xe_2015.2.164/debugger/gdb/intel64/bin:/ho
me/apps/fas/Modules:/usr/lib64/qt-3.3/bin:/opt/moab/bin:/bin:/usr/bin:/usr
/local/sbin:/usr/sbin:/usr/java/latest/bin:/opt/rocks/bin:/opt/rocks
/sbin:/home/fas/hpcprog/ahs3/bin:/home/apps/bin:/home/fas/cpsc424/cg736/bi
YHPC COMPILER MINOR=164
PBS 0 LANG=en US.iso885915
PBS_J0BC00KIE=73291E674DD8783304A24E81A99DA7D9
TBBR00T=/home/apps/fas/Langs/Intel/2015_update2/composer_xe_2015.2.164/tbb
C_INCLUDE_PATH=/usr/local/cluster/hpc/GPU/Cuda/8.0/include:/usr/local/clus
ter/hpc/MPI/OpenMPI/1.8.6-intel15/include
F90=ifort
PWD=/home/fas/cpsc424/cg736
LMFILES =/home/apps/fas/Modules/Base/yale hpc:/home/apps/fas/Modules/Lang
s/Intel/15:/home/apps/fas/Modules/MPI/OpenMPI/1.8.6-intel15:/home/apps/fas
/Modules/Tools/TotalView/8.14.1-8:/home/apps/fas/Modules/GPU/Cuda/8.0
YHPC COMPILER MAJOR=2
JAVA_HOME=/usr/java/latest
GDB_CROSS=/home/apps/fas/Langs/Intel/2015_update2/composer_xe_2015.2.164/d
ebugger/gdb/intel64_mic/bin/gdb-mic
DOMAIN=omega
PBS NODENUM=0
LANG=C
```

```
MODULEPATH=/home/apps/fas/Modules
MOABHOMEDIR=/opt/moab
CUDADIR=/usr/local/cluster/hpc/GPU/Cuda/8.0
YHPC COMPILER RELEASE=2015
LOADEDMODULES=Base/yale_hpc:Langs/Intel/15:MPI/OpenMPI/1.8.6-intel15:Tools
/TotalView/8.14.1-8:GPU/Cuda/8.0
KDEDIRS=/usr
PBS NUM NODES=1
F77=ifort
PBS_0_SHELL=/bin/bash
LM_LICENSE_FILE=/home/apps/fas/Tools/TotalView/license.dat
PBS JOBID=5451302.rocks.omega.hpc.yale.internal
MPM_LAUNCHER=/home/apps/fas/Langs/Intel/2015_update2/composer_xe_2015.2.16
4/debugger/mpm/bin/start_mpm.sh
CXX=icpc
SSH_ASKPASS=/usr/libexec/openssh/gnome-ssh-askpass
HISTCONTROL=ignoredups
INTEL_PYTHONHOME=/home/apps/fas/Langs/Intel/2015_update2/composer_xe_2015.
2.164/debugger/python/intel64/
SHLVL=1
HOME=/home/fas/cpsc424/cg736
PBS 0 HOST=login-0-0.local
FC=ifort
PBS_VNODENUM=0
LOGNAME=cq736
QTLIB=/usr/lib64/qt-3.3/lib
CVS RSH=ssh
PBS QUEUE=cpsc424qpu
MODULESHOME=/usr/share/Modules
LESSOPEN=||/usr/bin/lesspipe.sh %s
PBS_MICFILE=/var/spool/torque/aux//5451302.rocks.omega.hpc.yale.internalmi
PBS 0 MAIL=/var/spool/mail/cg736
arch=intel64
INFOPATH=/home/apps/fas/Langs/Intel/2015_update2/composer_xe_2015.2.164/de
bugger/gdb/intel64/share/info/:/home/apps/fas/Langs/Intel/2015_update2/com
poser_xe_2015.2.164/debugger/gdb/intel64_mic/share/info/
CC=icc
PBS NP=5
PBS_NUM_PPN=1
PBS_0_SERVER=rocks.omega.hpc.yale.internal
INCLUDE=/home/apps/fas/Langs/Intel/2015_update2/composer_xe_2015.2.164/mkl
/include
MPI_PATH=/usr/local/cluster/hpc/MPI/OpenMPI/1.8.6-intel15
G_BROKEN_FILENAMES=1
PBS_NODEFILE=/var/spool/torque/aux//5451302.rocks.omega.hpc.yale.internal
PBS_0_PATH=/usr/local/cluster/hpc/GPU/Cuda/8.0/samples/bin/x86_64/linux/re
lease:/usr/local/cluster/hpc/GPU/Cuda/8.0/bin:/home/apps/fas/Tools/TotalVi
ew/toolworks/totalview.8.14.1-8/bin:/home/apps/fas/Tools/TotalView/toolwor
```

```
ks/memoryscape.3.6.1-8/bin:/home/apps/fas/Tools/TotalView:/usr/local/clust er/hpc/MPI/OpenMPI/1.8.6-intel15/bin:/home/apps/fas/Langs/Intel/2015_updat e2/composer_xe_2015.2.164/bin/intel64:/home/apps/fas/Langs/Intel/2015_upda te2/composer_xe_2015.2.164/mpirt/bin/intel64:/home/apps/fas/Langs/Intel/20 15_update2/composer_xe_2015.2.164/debugger/gdb/intel64_mic/bin:/home/apps/fas/Langs/Intel/2015_update2/composer_xe_2015.2.164/debugger/gdb/intel64/b in:/home/apps/fas/Modules:/usr/lib64/qt-3.3/bin:/opt/moab/bin:/usr/local/b in:/bin:/usr/bin:/usr/local/sbin:/usr/sbin:/usr/java/latest/bin:/opt/rocks/bin:/opt/rocks/sbin:/home/fas/hpcprog/ahs3/bin:/home/apps/bin:/home/fas/cpsc424/cg736/bin
BASH_FUNC_module()=() { eval `/usr/bin/modulecmd bash $*`}
_=/bin/env
```

How to run the code

The source code and scripts of different tasks are organized in sub directory task1, task2 and task3 respectively. For each task, I wrote a script which can run the code automatically.

To run the program, you can enter each sub directory and submit the job to running queue by typing:

```
qsub xxx.sh
```

Note: here xxx should be replaced by specific script name.

For task3, I do not provide a script. Since **NTB** is defined as macro, you have change the value of **NTB** and rebuild the program and rerun.

Output and evaluation

Throughout the assignment, I used M2090 for all the final timings.

Task 1

Part a

I ran my kernel and also my "kij" code using the matrix dimension described in the table below.

	Run1	Run2	Run3	Run4	Run5
n	1024	8192	1024	8192	8192
m	1024	8192	1024	8192	1024
р	1024	8192	8192	1024	8192

The following table shows the best timing for each case along with the corresponding block and grid dimension to achieve the best timing.

	Grid Dimension	Block Dimension	GPU TIME (ms)	CPU TIME (ms)
Run1	64 * 64	16 * 16	37.986271	884.213074
Run2	256 * 256	32 * 32	18498.746094	472161.750000
Run3	32 * 32	32 * 32	304.956665	7073.050781
Run4	256 * 256	32 * 32	2283.919189	59344.769531
Run5	32 * 256	32 * 32	2415.672852	66298.593750

Part b

	Grid Dimension	Block Dimension	Single Precision GPU TIME (ms)	Double Precision GPU TIME (ms)
m=p=n8192	256 * 256	32 * 32	18498.746094	28609.435547

We can see from the table above that GPU is efficient for single precision calculation. The time used in calculating double precision matrix multiplication increases by about 50%.

Part c

I wrote a script to increase the dimension by 1000 at a time and see if the timing is still larger than some number. Once the timing drops to near zero, I break the loop and report the largest size with reasonable timing. The largest size I found is n = p = m = 20684. The corresponding GPU TIME is **341605.875000 ms**.

Task 2

Part a

The following table shows the best timing for each case along with the corresponding block and grid dimension and tile size to achieve the best timing.

	Grid Dimension	Block Dimension	Tile Size	GPU TIME (ms)
Run1	32 * 32	32 * 32	32	14.724096
Run2	256 * 256	32 * 32	32	7456.747559
Run3	32 * 32	32 * 32	32	118.315903
Run4	256 * 256	32 * 32	32	951.742554
Run5	32 * 256	32 * 32	32	946.339355

Part b

	Grid Dimension	Block Dimension	Single Precision GPU TIME (ms)	Double Precision GPU TIME (ms)
m=p=n8192	256 * 256	32 * 32	7456.747559	12797.792969

With tiled calculation, both single and double precision calculation accelerate. However, single precision calculation is still much faster than double precision calculation (about 60%).

Part c

I reused the script I used in task 1. Again, the largest size I found is n = p = m = 20684. The corresponding GPU TIME is **164544.390625 ms**. The largest size is the same as that in task 1. But the corresponding GPU TIME decreases significantly (from **341605.875000** ms to **164544.390625 ms**)

Note

In task 2, I assume that the tiles and blocks are square and of the same size, but the matrix dimensions can be arbitrary. Below the is part of code that implement arbitrary matrix size.

```
/* if p is not an multiple of TW and it is the last tile,
  * the number of remaining element is in this tile is p % TW
  * Otherwise, it is a full tile with TW elements*/
int boarder = ((p%TW) !=0 && i == tile_num-1) ? p % TW : TW;
```

```
int indexa=ty*TW, indexb=tx;
for(; indexa<ty*TW+boarder; indexa++,indexb+=TW) {
  cvalue += atile[indexa] * btile[indexb];
}</pre>
```

Task 3

I implemented the multi-tiled strategy described in task 3. I use **NTB** to denote the number of adjacent tiles handled at one time. I started trials with **NTB** starting from 2 and incremented **NTB** at a time before **NTB** reaches 16. After that, I multiply **NTB** by 2 at a step. The following table shows the successful trials.

	Grid Dimension	Block Dimension	Tile Size	NTB	GPU TIME (ms)
n=p=m=8192	256 * 256	32 * 32	32	2	8068.263672
n=p=m=8192	256 * 256	32 * 32	32	3	8188.750488
n=p=m=8192	256 * 256	32 * 32	32	4	8025.918945
n=p=m=8192	256 * 256	32 * 32	32	5	7560.078125
n=p=m=8192	256 * 256	32 * 32	32	6	7890.470215
n=p=m=8192	256 * 256	32 * 32	32	7	7868.088867
n=p=m=8192	256 * 256	32 * 32	32	8	7410.684570
n=p=m=8192	256 * 256	32 * 32	32	9	7819.804688
n=p=m=8192	256 * 256	32 * 32	32	10	7373.133789
n=p=m=8192	256 * 256	32 * 32	32	11	7782.720215
n=p=m=8192	256 * 256	32 * 32	32	12	7753.938965
n=p=m=8192	256 * 256	32 * 32	32	13	7322.179199
n=p=m=8192	256 * 256	32 * 32	32	14	7746.424805
n=p=m=8192	256 * 256	32 * 32	32	15	7727.256348
n=p=m=8192	256 * 256	32 * 32	32	16	7274.133789

n=p=m=8192	256 * 256	32 * 32	32	32	7229.791504
n=p=m=8192	256 * 256	32 * 32	32	64	7210.930664
n=p=m=8192	256 * 256	32 * 32	32	128	7086.891602
n=p=m=8192	256 * 256	32 * 32	32	256	7068.958008

We can see when **NTB = 256**, it achieves the besting timing (7068.958008 ms).

The table below shows the comparison timing between tiled multiplication and multi-tiled multiplication. Multi-tiled calculation is slightly fasster than tile calculation when **NTB** is large. Overall, the timing of these 2 approaches is quite close. As described the assignment6.pdf, though the number of tiles loaded from global memory into shared memory would be reduced by ~25%. Unfortunately, multi-tiled approach does increase the usage of registers and shared memory, so the benefit of using multi-tiled calculation may not always be significant.

	Grid Dimension	Block Dimension	Tiled	Multi-Tiled (NTB=6)
n=p=m=8192	256 * 256	32 * 32	32	7456.747559

Note

In task 3, I assume that the matrix dimensions are multiples of the tile width. But my code can handle the case where the final block has fewer adjacent tiles than the other blocks. The following code does the job

```
int remaining_NTB = (Grid_Dim_X%NTB!=0&&blockIdx.x==gridDim.x-1)? Grid_Dim
_X%NTB : NTB;
...
while(row < n && col < m && kt < remaining_NTB){
    c[index] = cvalue[kt];
    kt++;
    index += TW;
}</pre>
```