

Table 1. A contrast between QAA_v4 and QAA_v5

	$r_{rs}(\lambda) = R_{rs}(\lambda)/(0.52 + 1.7 R_{rs}(\lambda))$	
$u = b_b/(a+b_b)$	$r_{rs}(\lambda) = (g_0 + g_1 u(\lambda))u(\lambda)$ $u(\lambda) = \frac{-g_0 + \sqrt{(g_0)^2 + 4g_1 * r_{rs}(\lambda)}}{2g_1}; \quad g_0=0.089, g_1=0.125$	
	QAA_v5	QAA_v4
$\lambda_0 = 550; 555; 560$	$\chi = \log \left(\frac{r_{rs}(443) + r_{rs}(490)}{r_{rs}(\lambda_0) + 5 \frac{r_{rs}(667)}{r_{rs}(490)} r_{rs}(667)} \right),$ $a(\lambda_0) = a_w(\lambda_0) + 10^{-1.146 - 1.366\chi - 0.469\chi^2}$	$\chi = \log \left(\frac{r_{rs}(443) + r_{rs}(490)}{r_{rs}(\lambda_0) + 2 \frac{r_{rs}(640)}{r_{rs}(490)} r_{rs}(640)} \right),$ $a(\lambda_0) = a_w(\lambda_0) + 10^{h_0 + h_1\chi + h_2\chi^2}$
Exponent of $b_{bp}(\lambda)$	$\eta = 2.0 \left(1 - 1.2 \exp \left(-0.9 \frac{r_{rs}(443)}{r_{rs}(\lambda_0)} \right) \right)$	$\eta = 2.2 \left(1 - 1.2 \exp \left(-0.9 \frac{r_{rs}(443)}{r_{rs}(555)} \right) \right)$
$\zeta: a_{ph411}/a_{ph443}$	$\zeta = 0.74 + \frac{0.2}{0.8 + r_{rs}(443)/r_{rs}(\lambda_0)}$	$\zeta = 0.71 + \frac{0.06}{0.8 + r_{rs}(443)/r_{rs}(555)}$
$\xi: a_{dg411}/a_{dg443}$	$\xi = e^{S(443-411)},$ $S = 0.015 + \frac{0.002}{0.6 + r_{rs}(443)/r_{rs}(\lambda_0)}$	$\xi = e^{S(443-411)},$ $S = 0.015$
Upper limit for $R_{rs}(667)$	$R_{rs}(667) = 20.0(R_{rs}(\lambda_0))^{1.5}$	$R_{rs}(640) = 0.01R_{rs}(555) +$ $1.4R_{rs}(667) - 0.0005 \frac{R_{rs}(667)}{R_{rs}(490)}$
Lower limit for $R_{rs}(667)$	$R_{rs}(667) = 0.9(R_{rs}(\lambda_0))^{1.7}$	
If no $R_{rs}(667)$ measurements or measured $R_{rs}(667)$ out of the limits	$R_{rs}(667) = 1.27(R_{rs}(\lambda_0))^{1.47} +$ $0.00018 \left(\frac{R_{rs}(490)}{R_{rs}(\lambda_0)} \right)^{3.19}$	

Update of the Quasi-Analytical Algorithm (QAA_v6)

	$r_{rs}(\lambda) = R_{rs}(\lambda)/(0.52 + 1.7 R_{rs}(\lambda))$	
	$u(\lambda) = \frac{-g_0 + \sqrt{(g_0)^2 + 4g_0 * g_1 * r_{rs}(\lambda)}}{2g_1}$, where $g_0=0.089$ and $g_1=0.1245$	
	IF $R_{rs}(665) < 0.0015 \text{ sr}^{-1}$	(else)
2	$\chi = \log \left(\frac{r_{rs}(443) + r_{rs}(490)}{r_{rs}(560) + 5 \frac{r_{rs}(665)}{r_{rs}(490)} r_{rs}(665)} \right)$ $a(\lambda_0) = a(560) = a_w(\lambda_0) + 10^{h_0 + h_1 \chi + h_2 \chi^2}$ $h_0 = -1.146 \quad h_1 = -1.366 \quad h_2 = -0.469$	$a(\lambda_0) = a(665)$ $= a_w(665) + 0.39 \left(\frac{R_{rs}(665)}{R_{rs}(443) + R_{rs}(490)} \right)^{1.14}$
3	$b_{bp}(\lambda_0) = b_{bp}(560) = \frac{u(\lambda_0) \times a(\lambda_0)}{1 - u(\lambda_0)} - b_{bw}(560)$	$b_{bp}(\lambda_0) = b_{bp}(665) = \frac{u(\lambda_0) \times a(\lambda_0)}{1 - u(\lambda_0)} - b_{bw}(665)$
4	$\eta = 2.0 \left(1 - 1.2 \exp \left(-0.9 \frac{r_{rs}(443)}{r_{rs}(560)} \right) \right)$ longer wavelength	
5	$b_{bp}(\lambda) = b_{bp}(\lambda_0) \left(\frac{\lambda_0}{\lambda} \right)^\eta$	
6	$a(\lambda) = (1 - u(\lambda))(b_{bw}(\lambda) + b_{bp}(\lambda))/u(\lambda)$	
7 & 8	$\zeta = 0.74 + \frac{0.02}{0.8 + r_{rs}(443)/r_{rs}(560)}$ $\xi = e^{S(4425-4155)}, S = 0.015 + \frac{0.002}{0.6 + r_{rs}(443)/r_{rs}(560)}$	
9 & 10	$a_g(443) = \frac{a(416) - \zeta a(443)}{\xi - \zeta} - \frac{a_w(416) - \zeta a_w(443)}{\xi - \zeta}$ $a_{dg}(\lambda) = a_g(443) e^{-S(\lambda-443)}, a_{ph}(\lambda) = a(\lambda) - a_{dg}(\lambda) - a_w(443)$	

$\lambda)$: