

/301. (30 points) Regular Expressions and Context Free Grammars

- i. Given the following grammar: $S \rightarrow A B \mid \epsilon$ $A \rightarrow a A \mid \epsilon$ $B \rightarrow b B \mid \epsilon$
Identify the string (if any) that has *multiple rightmost derivations*:
- a a a
 - b b b
 - ϵ
 - None of the above
- ii. Identify the *regular grammar* (if any) among the following:
- $S \rightarrow (S) S \mid \epsilon$
 - $S \rightarrow a A \mid a$ $A \rightarrow a A \mid \epsilon$
 - $S \rightarrow a S a \mid a a \mid \epsilon$
 - All of the above
- iii. Identify the grammar (if any) that is *LL(1)* among the following:
- $T \rightarrow T * F \mid F$ $F \rightarrow \text{id} \mid (E)$
 - $A \rightarrow a B \mid a$ $B \rightarrow b B \mid b$
 - $S \rightarrow (S) S \mid \epsilon$
 - None of the above
- iv. Consider the regular expression $(x^* y)?$ x where $\Sigma = \{x,y\}$. Which of the following strings **cannot be** generated by the given regular expression.
- y
 - x x x x
 - x y y x x
 - All of the above
- v. Consider the regular expression $[5-7] \mid [23][0-8]$. Which one of the following strings **cannot** be generated by the given regular expression.
- 620
 - 59
 - 39
 - 20
- vi. Which one of the following regular expressions is equivalent to the given regular expression: $a . c$ where $\Sigma = \{a,b,c\}$.
- a c
 - a c | a c c
 - a a c | a b c | a c c
 - a b c | a a c

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2. (25 points) Top Down Parsing. Given the following grammar where STMT is the start symbol:

#1 $\text{STMT} \rightarrow \text{id } R ; \text{STMT}$

#3 $R \rightarrow \text{ASSIGN}$

#5 $\text{ASSIGN} \rightarrow := \text{num}$

#2 $\text{STMT} \rightarrow \epsilon$

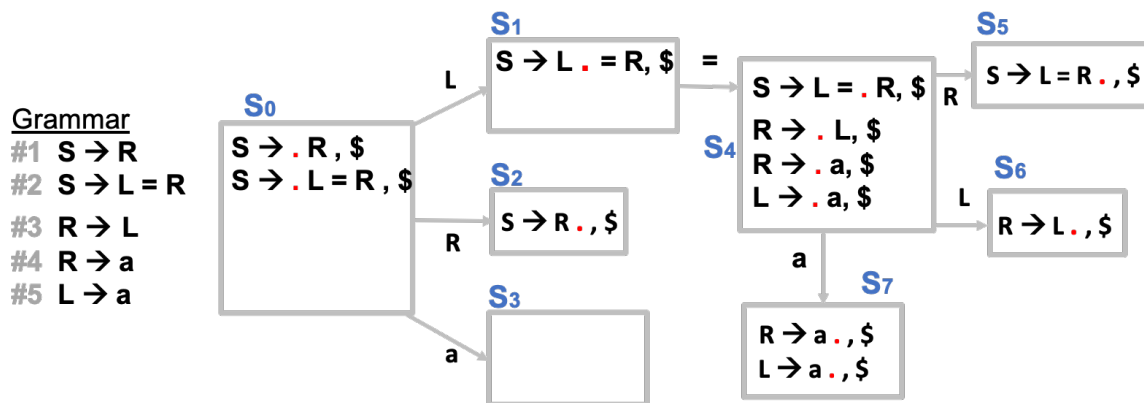
#4 $R \rightarrow \text{CALL}$

#6 $\text{CALL} \rightarrow (\text{id})$

- i. $\text{FIRST} (\text{STMT}) =$
- ii. $\text{FOLLOW} (\text{STMT}) =$
- iii. $\text{FIRST} (R) =$
- iv. $\text{FOLLOW} (R) =$
- v. $\text{TABLE} [R, (] =$
- vi. $\text{TABLE} [R, ;] =$
- vii. $\text{TABLE} [\text{STMT}, \$] =$
- viii. $\text{TABLE} [\text{ASSIGN}, :=] =$
- ix. $\text{TABLE} [\text{CALL}, \text{id}] =$
- x. $\text{TABLE} [\text{STMT}, \text{id}] =$

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3. (45 points) Bottom-Up Parsing: Given an incomplete SLR(1) state machine.



- i. Provide *items missing* from state **S₀** :
- ii. Provide *items missing* from state **S₁** :
- iii. Provide *items missing* from state **S₃** :
- iv. Provide action: **ACTION [S₀, a] =**
- v. Provide action: **ACTION [S₄, a] =**
- vi. Provide action: **ACTION [S₁, =] =**
- vii. Provide action: **ACTION [S₄, \$] =**
- viii. Provide action: **ACTION [S₂, \$] =**
- ix. Provide action: **ACTION [S₂, a] =**
- x. Provide action: **ACTION [S₆, \$] =**
- xi. Provide action: **ACTION [S₆, =] =**
- xii. Provide action: **ACTION [S₅, \$] =**
- xiii. Identify states, if any, that contain a *shift-reduce* conflict?
- xiv. Identify states, if any, that contains a *reduce-reduce* conflict?