```
# -*- coding: utf-8 -*-
"""a1.ipynb
```

Automatically generated by Colaboratory.

Original file is located at https://colab.research.google.com/drive/1Ez0ICGL6wIW22OxU\_UBJeJ\_8h427R\_Bo

# CSC413 Assignment 1: Word Embeddings

\*\*Deadline\*\*: February 5, 2021 by 10pm

\*\*Submission\*\*: Submit a PDF report containing your code, outputs, and your written solutions.

You may export the completed notebook, but if you do so

\*\*it is your responsibly to make sure that your code and answers do not get cut off\*\*.

\*\*Late Submission\*\*: Please see the syllabus for the late submission criteria.

\*\*Working with a partner\*\*: You may work with a partner for this assignment. If you decide to work with a partner, please create your group on Markus by February 5, 10pm, even if you intend to use grace tokens. Markus does not allow you to create groups past the deadline, even if you have grace tokens remaining.

Based on an assignment by George Dahl, Jing Yao Li, and Roger Grosse

In this assignment, we will make a neural network that can predict the next word in a sentence given the previous three. We will apply an idea called \*weight sharing\* to go beyond multi-layer perceptrons with only fully-connected layers.

We will also solve this problem problem twice: once in numpy, and once using PyTorch. When using numpy, you'll implement the backpropagation computation manually.

The prediction task is not very interesting on its own, but in learning to predict subsequent words given the previous three, our neural networks will learn about how to \*represent\* words. In the last part of the assignment, we'll explore the \*vector representations\* of words that our model produces, and analyze these representations.

You may modify the starter code, including changing the signatures of helper functions and adding/removing helper functions. However, please make sure that your TA can understand what you are doing and why.

.....

```
import pandas
import numpy as np
import matplotlib.pyplot as plt
import torch
import torch.nn as nn
import torch.optim as optim
"""## Question 1. Data
With any machine learning problem, the first thing that we would want to do
is to get an intuitive understanding of what our data looks like.
Download the file `raw_sentences.txt` from Quercus.
If you're using Google Colab, upload the file to Google Drive.
Then, mount Google Drive from your Google Colab notebook:
from google.colab import drive
drive.mount('/content/gdrive')
"""Find the path to 'raw sentences.txt':"""
file_path = '/content/gdrive/My Drive/CSC413/A/A1/raw sentences.txt' # TODO - UPDATE
ME!
"""You might find it helpful to know that you can run shell commands (like `ls`) by
using `!` in Google Colab, like this:
#!ls/content/gdrive/My\ Drive/
# !mkdir /content/gdrive/My\ Drive/CSC413
"""The following code reads the sentences in our file, split each sentence into
its individual words, and stores the sentences (list of words) in the
variable `sentences`.
.....
sentences = ∏
for line in open(file_path):
    words = line.split()
    sentence = [word.lower() for word in words]
    sentences.append(sentence)
```

```
"""There are 97,162 sentences in total, and these sentences are composed of 250 distinct words.
```

```
vocab = set([w for s in sentences for w in s])
print(len(sentences)) # 97162
print(len(vocab)) # 250
```

"""We'll separate our data into training, validation, and test. We'll use 10,000 sentences for test, 10,000 for validation, and the rest for training.

test, valid, train = sentences[:10000], sentences[10000:20000], sentences[20000:]

```
"""### Part (a) -- 2 pts
```

Display 10 sentences in the training set.

Explain how punctuations are treated in our word representation, and how words with apostrophes are represented.

(Note that for questions like this, you'll need to supply both your code \*\*and\*\* the output of your code to earn full credit.)

```
# Your code goes here
for i in range(10):
print(train[i])
```

"""Punctuations are treated as a single words in our word representation exceopt for apostrophes, it will combine with the rest of the word/letters after the apostrophes and it will be inside a double quotation mark in the display.

```
### Part (b) -- 2 pts
```

What are the 10 most common words in the vocabulary? How often does each of these words appear in the training sentences? Express the second quantity a percentage (i.e. number of occurrences of the word / total number of words in the training set).

These are good quantities to compute, because one of the first things that most machine learning model will learn is to predict the \*\*most common\*\* class. Getting a sense of the distribution of our data will help you understand our model's behaviour.

```
# Your code goes here
from collections import Counter
count = Counter([item for sublist in train for item in sublist])
common_word = sorted(count, key=count.get,reverse=True)
times = sorted(count.values(),reverse=True)
total = sum(count.values())
print("10 most common words in the vocabulary: ", common_word[:10])
print("total time each of these words appear in the training sentences: ",times[:10])
print("Precentage of these words appear in the training sentences: ", [x / total for x in
times[:10]])
"""### Part (c) -- 4 pts
Complete the helper functions 'convert words to indices' and
`generate_4grams`, so that the function `process_data` will take a
list of sentences (i.e. list of list of words), and generate an
$N \times 4$ numpy matrix containing indices of 4 words that appear
next to each other. You can use the constants 'vocab', 'vocab_itos',
and 'vocab stoi' in your code.
# A list of all the words in the data set. We will assign a unique
# identifier for each of these words.
vocab = sorted(list(set([w for s in train for w in s])))
# A mapping of j => word (string)
vocab_itos = dict(enumerate(vocab))
# A mapping of word => its j
vocab_stoi = {word:j for j, word in vocab_itos.items()}
def convert_words_to_indices(sents):
    .....
    This function takes a list of sentences (list of list of words)
    and returns a new list with the same structure, but where each word
    is replaced by its j in 'vocab_stoi'.
    Example:
    >>> convert_words_to_indices([['one', 'in', 'five', 'are', 'over', 'here'],
                                        ['other', 'one', 'since', 'yesterday'],
    [[148, 98, 70, 23, 154, 89], [151, 148, 181, 246], [248]]
```

You might find Python's `collections.Counter` class helpful.

```
.....
```

```
# Write your code here
    ans = []
    curr = 0
    for i in sents:
       ans.append(□)
       for j in range(len(i)):
         ans[curr].append(vocab_stoi[i[j]])
       curr += 1
    return ans
def generate_4grams(seqs):
    This function takes a list of sentences (list of lists) and returns
    a new list containing the 4-grams (four consequentively occuring words)
    that appear in the sentences. Note that a unique 4-gram can appear multiple
    times, one per each time that the 4-gram appears in the data parameter 'seqs'.
    Example:
    >>> generate_4grams([[148, 98, 70, 23, 154, 89], [151, 148, 181, 246], [248]])
    [[148, 98, 70, 23], [98, 70, 23, 154], [70, 23, 154, 89], [151, 148, 181, 246]]
     >>> generate_4grams([[1, 1, 1, 1, 1]])
     [[1, 1, 1, 1], [1, 1, 1, 1]]
    # Write your code here
    ans = []
    for i in seqs:
       for j in range(len(i)):
         if j \le len(i) - 4:
            ans.append([i[j], i[j+1], i[j+2], i[j+3]])
     return ans
def process_data(sents):
    This function takes a list of sentences (list of lists), and generates an
    numpy matrix with shape [N, 4] containing indices of words in 4-grams.
    indices = convert_words_to_indices(sents)
    fourgrams = generate_4grams(indices)
```

## return np.array(fourgrams)

```
train4grams = process_data(train)
valid4grams = process_data(valid)
test4grams = process_data(test)
```

"""## Question 2. MLP Math

Suppose we were to use a 2-layer multilayer perceptron to solve this prediction problem. Our model will look like this:

<img src="https://www.cs.toronto.edu/~lczhang/321/hw/p2\_model1.png" />

\begin{align\*}

\bf{x} &= \text{concatenation of the one-hot vector for words 1, 2 and 3} \\

 $\bf{m} &= \bf{W^{(1)}} \bf{x} + \bf{b^{(1)}} \$ 

 $\bf{h} &= \text{ReLU}(\bf{m}) \$ 

 $\bf{z} &= \bf{W^{(2)}} \bf{h} + \bf{b^{(2)}} \$ 

 $\bf{y} &= \text{textrm{softmax}(\bf{z}) }$ 

\end{align\*}

### Part (a) -- 2 pts

What is the shape of the input vector f(x)? What is the shape of the output vector f(y)? Let k represent the size of the hidden layer. What are the dimension of f(1) and f(2)?

### Part (b) -- 2 pts

Draw a computation graph for fy. Your graph should include the quantities  $fW^{(1)}$ ,  $f^{(2)}$ .

### Part (c) -- 3 pts

Derive the gradient descent update rule for  ${\ W}^{(2)}$ . You should begin by deriving the update rule for  $W^{(2)}_{ij}$ , and then vectorize your answer. Assume that we will use the softmax activation and cross-entropy loss.

Note: if you use the derivative of the softamx activation and the cross-entropy loss, you \*\*must\*\* derive them.

```
### Part (d) -- 4 pts
```

What would be the update rule for  $W^{(2)}_{ij}$ , if we use the square loss  $\mathcal{L}_{SE}(\bf{y}, \bf{t}) = \frac{1}{2}(\bf{y} - \bf{t})^2$ ?

Show that we will not get good gradient signal to update  $W^{(2)}_{ij}$  if we use this square loss.

```
### Part (e) -- 4 pts
```

In this question, we'll show a similar issue with using the sigmoid activation. Let's assume we have a deep neural network as follows:

```
\begin{align*}
h_1 &= \sigma(w_1 x + b_1) \\
h_2 &= \sigma(w_2 h_1 + b_2) \\
\dots
\end{align*}
```

where, for simplicity, \$x\$, \$w\_1\$, \$b\_1\$, \$h\_1\$, \$w\_2\$, \$b\_2\$, \$h\_2\$, etc., are all scalars. Show that

 $\begin{align*} $$ \|\frac x}\| \le \frac{1}{4} \|w_1\| \end{align*}$ 

In order to do so, you will need to first show that  $\simeq \simeq (z) (1 - \simeq z)$  (worth 1 point). Include a plot (or sketch) of the function  $\simeq (z)$  (worth 1 point).

### Part (f) -- 2 pts

Continue from the previous question, show that for a deeper neural network.

 $\label{lign*} $$ \left( \sum_{n=1}^{4^N} |w_1| w_2| \cdot w_N \right) \leq \left( \sum_{n=1}^{4^N} |w_1| w_2| \cdot w_N \right) \leq \left( \sum_{n=1}^{4^N} |w_1| w_2 \right)$ 

What would be a problem with this result?

### Part (g) -- 1 pts

Would we have the same issue as in part(f) we we replaced the sigmoid activation

with ReLU activations? Why or why not?

## Question 3. Weight Sharing - Math

From this point onward, we will change our architecture to introduce weight sharing. In particular, the input \$\bf{x}\$ consists of three one-hot vectors concatenated together. We can think of \$\bf{h}\$ as a representation of those three words (all together). However, \$\bf{W^{(1)}}\$ needs to learn about the first word separately from the second and third word, when some of the information could be shared. Consider the following architecture:

<img src="https://www.cs.toronto.edu/~lczhang/321/hw/p2\_model2.png" />

Here, we add an extra \*embedding\* layer to the neural network, where we compute the representation of \*\*each\*\* word before concatenating them together! We use the same weight \$\bf{W}^{(word)}\$ for each of the three words:

Note that there are no biases in the embedding layer.

```
### Part (a) -- 4 pts
```

Draw a computation graph for f(y). Your graph should include the quantities  $f(w)^{(w)}$ , f(w), f(u), f(u),

```
### Part (b) -- 2 pts
```

Using the computation graph from part (e), use the chain rule to write the quantity \$\frac{\partial{\bf y}}{\partial{\bf W}^{(word)}}\$ in terms of derivatives along the edges in the computation graph (e.g. \$\frac{\partial \bf{z}}{\partial {\bf \cdot}} \dots\$)

You don't need to compute the actual derivatives along the edges for this question. However, you will need to in Q4(a).

```
## Question 4. NumPy
```

In this question, we will implement the model from Question 3 using NumPy. Start by reviewing these helper functions, which are given to you:

.....

def make\_onehot(indicies, total=250):

.....

Convert indicies into one-hot vectors by

- 1. Creating an identity matrix of shape [total, total]
- 2. Indexing the appropriate columns of that identity matrix

.....

l = np.eye(total)
return [[indicies]

def softmax(x):

.....

Compute the softmax of vector x, or row-wise for a matrix x. We subtract x.max(axis=0) from each row for numerical stability.

.....

```
x = x.T
exps = np.exp(x - x.max(axis=0))
probs = exps / np.sum(exps, axis=0)
return probs.T
```

def get\_batch(data, range\_min, range\_max, onehot=True):

.....

Convert one batch of data in the form of 4-grams into input and output data and return the training data (xs, ts) where:

- 'xs' is an numpy array of one-hot vectors of shape [batch\_size, 3, 250]
- `ts` is either
  - a numpy array of shape [batch\_size, 250] if onehot is True,
  - a numpy array of shape [batch\_size] containing indicies otherwise

Preconditions:

```
- `data` is a numpy array of shape [N, 4] produced by a call
         to `process_data`
     - range_max > range_min
    xs = data[range_min:range_max, :3]
    xs = make_onehot(xs)
    ts = data[range_min:range_max, 3]
    if onehot:
         ts = make\_onehot(ts).reshape(-1, 250)
    return xs, ts
def estimate_accuracy(model, data, batch_size=5000, max_N=100000):
    Estimate the accuracy of the model on the data. To reduce
    computation time, use at most `max_N` elements of `data` to
    produce the estimate.
    correct = 0
    N = 0
    for i in range(0, data.shape[0], batch_size):
         xs, ts = get_batch(data, i, i + batch_size, onehot=False)
         z = model(xs)
         pred = np.argmax(z, axis=1)
         correct += np.sum(ts == pred)
         N += ts.shape[0]
         if N > max N:
             break
    return correct / N
"""### Part (a) -- 8 point
```

Your first task is to implement the model from Question 3 in NumPy. We will represent the model as a Python class. We set up the class methods and APIs to be similar to that of PyTorch, so that you have some intuition about what PyTorch is doing under the hood. Here's what you need to do:

- 1. in the `\_init\_` method, initialize the weights and biases to have the correct shapes. You may want to look back at your answers in the previous question. (0 points)
- 2. complete the 'forward' method to compute the predictions given a \*\*batch\*\* of inputs. This function will also store the intermediate values obtained in the computation; we will need these values for gradient descent. (3 points)
- 3. complete the 'backward' method to compute the gradients of the loss with respect to the

```
weights and biases. (4 points)
4. complete the 'update' method that uses the stored gradients to update the weights and
biases. (1 point)
class NumpyWordEmbModel(object):
    def init (self, vocab size=250, emb size=100, num hidden=100):
         Initialize the weights and biases to zero. Update this method
         so that weights and baises have the correct shape.
         self.vocab_size = vocab_size
         self.emb_size = emb_size
         self.num_hidden = num_hidden
         self.emb_weights = np.zeros((self.emb_size, self.vocab_size)) # W^{(word)}
         self.weights1 = np.zeros((self.num_hidden, 3 * self.emb_size))
                                                                          # W^{(1)}
         self.bias1 = np.zeros(self.num_hidden)
                                                              # b^{(1)}
         self.weights2 = np.zeros((self.vocab size, self.num hidden))
                                                                        # W^{(2)}
         self.bias2 = np.zeros(self.vocab_size)
                                                            # b^{(2)}
         self.cleanup()
    def initializeParams(self):
         Randomly initialize the weights and biases of this two-layer MLP.
         The randomization is necessary so that each weight is updated to
         a different value.
         You do not need to change this method.
         self.emb_weights = np.random.normal(0, 2/self.emb_size, self.emb_weights.shape)
         self.weights1 = np.random.normal(0, 2/self.emb_size, self.weights1.shape)
         self.bias1 = np.random.normal(0, 2/self.emb_size, self.bias1.shape)
         self.weights2 = np.random.normal(0, 2/self.num_hidden, self.weights2.shape)
         self.bias2 = np.random.normal(0, 2/self.num_hidden, self.bias2.shape)
    def forward(self, inputs):
         Compute the forward pass prediction for inputs.
         Note that for vectorization, 'inputs' will be a rank-3 numpy array
         with shape [N, 3, vocab_size], where N is the batch size.
         The returned value will contain the predictions for the N
         data points in the batch, so the return value shape should be
```

[N, something].

You should refer to the mathematical expressions we provided in Q3 when completing this method. However, because we are computing forward pass for a batch of data at a time, you may need to rearrange some computation (e.g. some matrix-vector multiplication will become matrix-matrix multiplications, and you'll need to be careful about arranging the dimensions of your matrices.)

For numerical stability reasons, we will return the \*\*logit z\*\* instead of the \*\*probability y\*\*. The loss function assumes that we return the logits from this function.

After writing this function, you might want to check that your code runs before continuing, e.g. try

```
xs, ts = get_batch(train4grams, 0, 8, onehot=True)
     m = NumpyWordEmbModel()
     m.forward(xs)
self.N = inputs.shape[0]
ipt = np.split(inputs,3,axis=1)
self.xa = ipt[0].reshape((self.N,inputs.shape[2])) # todo
self.xb = ipt[1].reshape((self.N,inputs.shape[2])) # todo
self.xc = ipt[2].reshape((self.N,inputs.shape[2])) # todo
self.va = self.xa @ (self.emb_weights).T # todo
self.vb = self.xb @ (self.emb_weights).T # todo
self.vc = self.xc @ (self.emb_weights).T # todo
self.v = np.concatenate([self.va,self.vb,self.vc],axis=1) # todo
self.m = self.v @ (self.weights1).T + self.bias1 # todo
self.h = np.maximum(self.m, 0) # todo
self.z = self.h @ (self.weights2).T + self.bias2 # todo
self.y = softmax(self.z)
return self.z
```

Calling `m(foo)` is equivalent to calling `m.forward(foo)`.

You do not need to change this method.

.....

return self.forward(inputs)

```
def backward(self, ts):
```

11111

Compute the backward pass, given the ground-truth, one-hot targets. Note that `ts` needs to be a numpy array with shape [N, vocab\_size]. Complete this method. You might want to refer to your answers to Q2 and Q3. But be careful: we are computing the backward pass for an entire batch of data at a time! Carefully track the dimensions of your quantities!

You may assume that the forward() method has already been called, so you can access values like self.N, self.y, etc..

This function needs to be called before calling the update() method.

```
z_bar = (self.y - ts) / self.N
self.w2_bar = z_bar.T @ self.h # todo, compute gradient for W^{(2)}
self.b2_bar = z_bar.T @ np.ones(self.N) # todo, compute gradient for b^{(2)}
h_bar = z_bar @ self.weights2 # todo
m_bar = (self.m > 0) * h_bar # todo
self.w1_bar = m_bar.T @ self.v # todo
self.b1_bar = m_bar.T @ np.ones(self.N) # todo
# ...
v_bar = m_bar @ self.weights1
v_bar0 = (v_bar[:,:self.num_hidden]).T @ self.xa
v_bar1 = (v_bar[:,self.num_hidden:self.num_hidden*2]).T @ self.xb
v_bar2 = (v_bar[:,self.num_hidden*2:]).T @ self.xc
self.emb_bar = v_bar0 + v_bar1 + v_bar2# todo, compute gradient for W^{(word)}
```

def update(self, alpha):

.....

Compute the gradient descent update for the parameters. Complete this method. Use `alpha` as the learning rate.

You can assume that the forward() and backward() methods have already been called, so you can access values like self.w1\_bar.

```
self.weights1 = self.weights1 - alpha * self.w1_bar
# todo... update the other weights/biases
self.bias1 = self.bias1 - alpha * self.b1_bar
self.weights2 = self.weights2 - alpha * self.w2_bar
self.bias2 = self.bias2 - alpha * self.b2_bar
```

```
self.emb_weights = self.emb_weights - alpha * self.emb_bar
```

```
def cleanup(self):
```

.....

Erase the values of the variables that we use in our computation.

```
You do not need to change this method.
```

.....

self.N = None

self.xa = None

self.xb = None

self.xc = None

self.va = None

self.vb = None

self.vc = None

self.v = None

self.m = None

self.h = None

self.z = None

self.y = None

self.z\_bar = None

self.w2\_bar = None

self.b2 bar = None

self.w1\_bar = None

self.b1\_bar = None

self.emb\_bar = None

## """### Part (b) -- 2 points

Complete the `run\_gradient\_descent` function. Train your numpy model to obtain a training accuracy of at least 25%. You do not need to train this model to convergence, but you do need to clearly show that your model reached at least 25% training accuracy.

def run\_gradient\_descent(model,

train\_data=train4grams, validation\_data=valid4grams, batch\_size=100, learning\_rate=0.1, max\_iters=5000):

.....

Use gradient descent to train the numpy model on the dataset train4grams.

....

```
n = 0
    while n < max iters:
         # shuffle the training data, and break early if we don't have
         # enough data to remaining in the batch
         np.random.shuffle(train_data)
         for i in range(0, train_data.shape[0], batch_size):
              if (i + batch_size) > train_data.shape[0]:
                  break
              # get the input and targets of a minibatch
              xs, ts = get_batch(train_data, i, i + batch_size, onehot=True)
              # erase any accumulated gradients
              model.cleanup()
              # forward pass: compute prediction
              # TODO: add your code here
             y = softmax(model.forward(xs))
              # backward pass: compute error
              model.backward(ts)
              model.update(learning_rate)
              # increment the iteration count
              n += 1
              # compute and plot the *validation* loss and accuracy
              if (n \% 100 == 0):
                  train_cost = -np.sum(ts * np.log(y)) / batch_size
                  train_acc = estimate_accuracy(model, train_data)
                  val_acc = estimate_accuracy(model, validation_data)
                  model.cleanup()
                  print("Iter %d. [Val Acc %.0f%%] [Train Acc %.0f%%, Loss %f]" % (
                         n, val_acc * 100, train_acc * 100, train_cost))
         if n >= max_iters:
              return
numpy_model= NumpyWordEmbModel()
numpy_model.initializeParams()
run_gradient_descent(numpy_model)
"""### Part (c) -- 2 pts
```

If we do not call `numpy\_model.initializeParams()`, your model weights will not change. Clearly explain (mathematically) why this is the case.

```
### Part (d) -- 2 pts
```

The `estimate\_accuracy` function takes the continuous predictions `z` and turns it into a discrete prediction `pred`. Show that for a given data point, `pred` is equal to 1 only if the predictive probability `y` is at least 0.5.

```
## Question 5. PyTorch
```

Now, we will build the same model in PyTorch.

m = self.fc\_layer1(v)
h = torch.relu(m)

return z

```
### Part (a) -- 2 pts
```

Since PyTorch uses automatic differentiation, we only need to write the \*forward pass\* of our model. Complete the `\_init\_` and `forward` methods below.

Hint: You might want to look up the `reshape` method in PyTorch.

```
class PyTorchWordEmb(nn.Module):
    def __init__(self, emb_size=100, num_hidden=300, vocab_size=250):
        super(PyTorchWordEmb, self).__init__()
        self.word_emb_layer = nn.Linear(vocab_size,
                                                         # num input W^(word)
                                          # num output W^(word)
                          emb size,
                                            bias=False)
        self.fc_layer1 = nn.Linear(3 * emb_size, # num input W^(1)
                                       num_hidden) # num output W^(1)
        self.fc_layer2 = nn.Linear(num_hidden, # num input W^(2)
                                      vocab_size) # num output W^(2)
        self.num_hidden = num_hidden
        self.emb_size = emb_size
    def forward(self, inp):
        vs = self.word_emb_layer(inp)
```

 $v = vs.reshape((-1,3*self.emb_size)) # TODO: what do you need to do here?$ 

 $z = self.fc_layer2(h) \# TODO:$  what do you need to do here?

```
"""### Part (b) -- 2 pts
```

The function `run\_pytorch\_gradient\_descent` is given to you. It is similar to the code that you wrote fro the PyTorch model, with a few differences:

- 1. We will use a slightly fancier optimizer called \*\*Adam\*\*. For this optimizer, a smaller learning rate usually works better, so the default learning rate is set to 0.001.
- 2. Since we get weight decay for free, you are welcome to use weight decay.

Use this function and train your PyTorch model to obtain a training accuracy of at least 37%. Plot the learning curve using the `plot\_learning\_curve` function provided to you, and include your plot in your PDF submission.

```
def estimate_accuracy_torch(model, data, batch_size=5000, max_N=100000):
    Estimate the accuracy of the model on the data. To reduce
    computation time, use at most 'max_N' elements of 'data' to
    produce the estimate.
    correct = 0
    N = 0
    for i in range(0, data.shape[0], batch_size):
         # get a batch of data
         xs, ts = get_batch(data, i, i + batch_size, onehot=False)
         # forward pass prediction
         z = model(torch.Tensor(xs))
         z = z.detach().numpy() # convert the PyTorch tensor => numpy array
         pred = np.argmax(z, axis=1)
         correct += np.sum(pred == ts)
         N += ts.shape[0]
         if N > max_N:
             break
    return correct / N
```

def run\_pytorch\_gradient\_descent(model,

```
train_data=train4grams,
validation_data=valid4grams,
batch_size=100,
learning_rate=0.001,
```

```
weight_decay=0,
max_iters=1000,
checkpoint_path=None):
```

....

Train the PyTorch model on the dataset `train\_data`, reporting the validation accuracy on `validation\_data`, for `max\_iters` iteration.

If you want to \*\*checkpoint\*\* your model weights (i.e. save the model weights to Google Drive), then the parameter `checkpoint\_path` should be a string path with `{}` to be replaced by the iteration count:

For example, calling

```
>>> run_pytorch_gradient_descent(model, ...,
checkpoint_path = '/content/gdrive/My Drive/CSC413/mlp/ckpt-{}.pk')
```

will save the model parameters in Google Drive every 500 iterations. You will have to make sure that the path exists (i.e. you'll need to create the folder CSC413, mlp, etc...). Your Google Drive will be populated with files:

- /content/gdrive/My Drive/CSC413/mlp/ckpt-500.pk
- /content/gdrive/My Drive/CSC413/mlp/ckpt-1000.pk

- ...

To load the weights at a later time, you can run:

>>> model.load\_state\_dict(torch.load('/content/gdrive/My Drive/CSC413/mlp/ckpt-500.pk'))

This function returns the training loss, and the training/validation accuracy, which we can use to plot the learning curve.

```
iters, losses = [], []
iters_sub, train_accs, val_accs = [], [] ,[]
```

n = 0 # the number of iterations while True:

```
for i in range(0, train_data.shape[0], batch_size):
              if (i + batch_size) > train_data.shape[0]:
                  break
              # get the input and targets of a minibatch
              xs, ts = get_batch(train_data, i, i + batch_size, onehot=False)
              # convert from numpy arrays to PyTorch tensors
              xs = torch.Tensor(xs)
              ts = torch.Tensor(ts).long()
              zs = model(xs)
              loss = criterion(zs, ts) # compute the total loss
              loss.backward()
                                         # compute updates for each parameter
              optimizer.step() # make the updates for each parameter
              optimizer.zero_grad() # a clean up step for PyTorch
              # save the current training information
              iters.append(n)
              losses.append(float(loss)/batch_size) # compute *average* loss
              if n \% 500 == 0:
                  iters sub.append(n)
                  train_cost = float(loss.detach().numpy())
                  train_acc = estimate_accuracy_torch(model, train_data)
                  train_accs.append(train_acc)
                  val_acc = estimate_accuracy_torch(model, validation_data)
                  val_accs.append(val_acc)
                  print("Iter %d. [Val Acc %.0f%%] [Train Acc %.0f%%, Loss %f]" % (
                          n, val_acc * 100, train_acc * 100, train_cost))
                  if (checkpoint_path is not None) and n > 0:
                       torch.save(model.state_dict(), checkpoint_path.format(n))
              # increment the iteration number
              n += 1
              if n > max_iters:
                  return iters, losses, iters_sub, train_accs, val_accs
def plot_learning_curve(iters, losses, iters_sub, train_accs, val_accs):
    Plot the learning curve.
```

```
.....
    plt.title("Learning Curve: Loss per Iteration")
    plt.plot(iters, losses, label="Train")
    plt.xlabel("Iterations")
    plt.ylabel("Loss")
    plt.show()
    plt.title("Learning Curve: Accuracy per Iteration")
    plt.plot(iters_sub, train_accs, label="Train")
    plt.plot(iters_sub, val_accs, label="Validation")
    plt.xlabel("Iterations")
    plt.ylabel("Accuracy")
    plt.legend(loc='best')
    plt.show()
pytorch_model = PyTorchWordEmb()
learning_curve_info
                                                                                            =
run pytorch gradient descent(pytorch model,max iters=8000,checkpoint path=
'/content/gdrive/My Drive/CSC413/A/A1/Q5/ckpt-{}.pk')
# you might want to save the `learning_curve_info` somewhere, so that you can plot
# the learning curve prior to exporting your PDF file
plot_learning_curve(*learning_curve_info)
"""### Part (c) -- 3 points
Write a function 'make_prediction' that takes as parameters
a PyTorchWordEmb model and sentence (a list of words), and produces
```

a prediction for the next word in the sentence.

Start by thinking about what you need to do, step by step, taking care of the difference between a numpy array and a PyTorch Tensor.

def make\_prediction\_torch(model, sentence):

Use the model to make a prediction for the next word in the sentence using the last 3 words (sentence[:-3]). You may assume that len(sentence) >= 3 and that 'model' is an instance of PyTorchWordEmb. You might find the function torch.argmax helpful.

This function should return the next word, represented as a string.

```
Example call:

>>> make_prediction_torch(pytorch_model, ['you', 'are', 'a'])

"""

global vocab_stoi, vocab_itos

# Write your code here
sentence = [word.lower() for word in sentence]
last = [sentence[-3:]]
index = convert_words_to_indices(last)
one_hot = make_onehot(index)
pred = torch.Tensor(one_hot)
y = model.forward(pred)
word_idx = torch.argmax(y)
return vocab_itos[word_idx.item()]

""""### Part (d) -- 4 points
```

Use your code to predict what the next word should be in each of the following sentences:

- "You are a"
- "few companies show"
- "There are no"
- "yesterday i was"
- "the game had"
- "yesterday the federal"

Do your predictions make sense? (If all of your predictions are the same, train your model for more iterations, or change the hyper parameters in your model. You may need to do this even if your training accuracy is >=37%)

One concern you might have is that our model may be "memorizing" information from the training set. Check if each of 3-grams (the 3 words appearing next to each other) appear in the training set. If so, what word occurs immediately following those three words?

# Write your code and answers here
print(make\_prediction\_torch(pytorch\_model, ['You', 'are', 'a']))
print(make\_prediction\_torch(pytorch\_model, ['few', 'companies', 'show']))
print(make\_prediction\_torch(pytorch\_model, ['There', 'are', 'no']))
print(make\_prediction\_torch(pytorch\_model, ['yesterday', 'i', 'was']))
print(make\_prediction\_torch(pytorch\_model, ['the', 'game', 'had']))
print(make\_prediction\_torch(pytorch\_model, ['yesterday', 'the', 'federal']))

```
"""### Part (3) -- 1 points
```

Report the test accuracy of your model. The test accuracy is the percentage of correct predictions across your test set.

.....

# Write your code here print("The test accuracy is", estimate\_accuracy\_torch(pytorch\_model,test4grams))

"""## Question 6. Visualizing Word Embeddings

While training the `PyTorchWordEmb`, we trained the `word\_emb\_layer`, which takes a one-hot

representation of a word in our vocabulary, and returns a low-dimensional vector representation of that word. In this question, we will explore these word embeddings.

```
### Part (a) -- 1 pts
```

The code below extracts the \*\*weights\*\* of the word embedding layer, and converts the PyTorch tensor into an numpy array.

Explain why each \*row\* of `word\_emb` contains the vector representing of a word. For example `word\_emb[vocab\_stoi["any"],:]` contains the vector representation of the word "any".

word\_emb\_weights = list(pytorch\_model.word\_emb\_layer.parameters())[0]
word\_emb = word\_emb\_weights.detach().numpy().T

# Write your explanation here

```
"""### Part (b) -- 1 pts
```

Once interesting thing about these word embeddings is that distances in these vector representations of words make some sense! To show this, we have provided code below that computes the cosine similarity of every pair of words in our vocabulary.

norms = np.linalg.norm(word\_emb, axis=1) word\_emb\_norm = (word\_emb.T / norms).T

similarities = np.matmul(word\_emb\_norm, word\_emb\_norm.T)

# Some example distances. The first one should be larger than the second

```
print(similarities[vocab_stoi['any'], vocab_stoi['many']])
print(similarities[vocab_stoi['any'], vocab_stoi['government']])
"""Compute the 5 closest words to the following words:
- "four"
- "go"
- "what"
- "should"
- "school"
- "your"
- "yesterday"
- "not"
.....
# Write your code here
def closest_words(w):
  similar = similarities[vocab stoi[w]]
  index = (np.argsort(similar))[::-1]
  print("5 closest words for", w,":")
  for i in range(5):
    print(vocab_itos[index[i]])
  return
following_words = ["four", "go", "what", "should", "school", "your", "yesterday", "not"]
for i in following_words:
  closest_words(i)
"""### Part (c) -- 2 pts
```

We can visualize the word embeddings by reducing the dimensionality of the word vectors to 2D. There are many dimensionality reduction techniques that we could use, and we will use an algorithm called t-SNE. (You don't need to know what this is for the assignment, but we may cover it later in the course.)

Nearby points in this 2-D space are meant to correspond to nearby points in the original, high-dimensional space.

The following code runs the t-SNE algorithm and plots the result. Look at the plot and find two clusters of related words. What do the words in each cluster have in common?

Note that there is randomness in the initialization of the t-SNE algorithm. If you re-run this code, you may get a different image.

Please make sure to submit your image in the PDF file for your TA to see.

```
import sklearn.manifold
tsne = sklearn.manifold.TSNE()
Y = tsne.fit_transform(word_emb)

plt.figure(figsize=(10, 10))
plt.xlim(Y[:,0].min(), Y[:, 0].max())
plt.ylim(Y[:,1].min(), Y[:, 1].max())
for i, w in enumerate(vocab):
        plt.text(Y[i, 0], Y[i, 1], w)
plt.show()
```

This question is to make sure that if you are working with a partner, that you and your partner contributed equally to the assignment.

Please have each team member write down the times that you worked on the assignment, and your contribution to the assignment.

# Example answer:

# I worked on the assignment on Jan 20 afternoon, Jan 26th 12pm-2pm, # and then Feb 4th in the evening. My partner and I had a meeting on # Jan 20th to read the entire assignment, and we did Question 1 together # while screensharing. I worked out the math for Q2, and checked my # partner's implementation in Q3. I also wrote the Q3 helper functions, # and Q4(b).

"""This assignment is finished individually by Hongyu Chen"""