

6.10

μ_1 : 有装有线电视一周阅读时间

μ_2 : 没有装有线电视一周阅读时间

$(\bar{x} - \bar{y})$ 常態分配: $(\bar{x} - \bar{y}) \sim N(\mu_1 - \mu_2, \frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2})$

$$(1) \bar{x} - \bar{y} = 14.5 - 20.8 = -6.3 \text{ hr}$$

$$(2) (\bar{x} - \bar{y}) - 2\frac{\sigma}{2} \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}, (\bar{x} - \bar{y}) + 2\frac{\sigma}{2} \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}$$

$$1 - \alpha = 0.98, \frac{\alpha}{2} = 0.01, 2\frac{\sigma}{2} = Z_{0.01} = 2.327$$

$$\begin{aligned} & (\bar{x} - \bar{y}) \pm 2\frac{\sigma}{2} \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}} \\ & = (14.5 - 20.8) \pm 2.327 \sqrt{\frac{18.5^2}{250} + \frac{3.8^2}{150}} \\ & = (-6.3) \pm 0.84 \end{aligned}$$

6.11

μ_1 : 大公司每年平均休作天數

μ_2 : 小公司每年平均休作天數

$\mu_1 - \mu_2$ 區間估計

$$(\bar{x} - \bar{y}) \pm t_{\frac{\alpha}{2}}(n_1 + n_2 - 2) \sqrt{s_p^2 \left(\frac{1}{n_1} + \frac{1}{n_2} \right)}$$

$$1 - \alpha = 0.9, \frac{\alpha}{2} = 0.05, t_{\frac{\alpha}{2}}(n_1 + n_2 - 2) = t_{0.05}(25) = 1.708$$

$$\begin{aligned} s_p^2 &= \frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2} \\ &= \frac{(12 - 1)8^2 + (15 - 1)7^2}{12 + 15 - 2} \\ &= \frac{961}{25} \\ &= 38.44 \end{aligned}$$

$$\begin{aligned} & (\bar{x} - \bar{y}) \pm t_{\frac{\alpha}{2}}(n_1 + n_2 - 2) \sqrt{s_p^2 \left(\frac{1}{n_1} + \frac{1}{n_2} \right)} \\ & = (36 - 32) \pm 1.708 \sqrt{38.44 \left(\frac{1}{12} + \frac{1}{15} \right)} \\ & = 4 \pm 4.10 \end{aligned}$$

$\mu_1 - \mu_2 \in (-0.10, 8.10)$