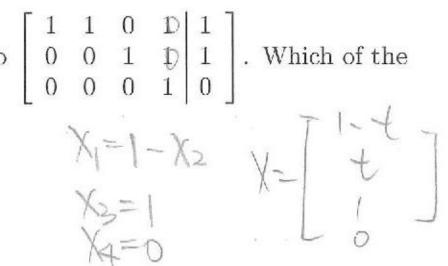
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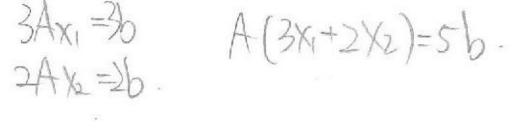
Part I - Multiple Choice. Clearly indicate your answer to each question by circling your choice. Each question is worth 2 marks.

For each question, choose the BEST option from the given options.

- 1. Suppose that the augmented matrix of a system of linear equations has been reduced to $\begin{bmatrix} 1 & 1 & 0 & D & 1 \\ 0 & 0 & 1 & D & 1 \\ 0 & 0 & 0 & 1 & 0 \end{bmatrix}$. Which of the following statements describes the set of solutions to the system?
 - (A) infinitely many solution with three parameters
 - (B) infinitely many solution with two parameters
 - (C) infinitely many solution with one parameter
 - (D) unique solution
 - (E) no solution



- 2. Let A be an $n \times n$ matrix and let \mathbf{x}_1 and \mathbf{x}_2 be two distinct solutions to the system $A\mathbf{x} = \mathbf{b}$. Which of the following statements are TRUE?
 - (i) A cannot be carried to I_n by elementary row operations $\sqrt{}$
 - (ii) $3\mathbf{x}_1 + 2\mathbf{x}_2$ is a solution to the system $A\mathbf{x} = 5\mathbf{b}$
- (iii) $3\mathbf{x}_1 + 2\mathbf{x}_2$ is a solution to the system $A\mathbf{x} = \mathbf{b}$
- (A) (ii) only
- (B) (iii) only
- (C) (i) and (iii) only
- (D)(i) and (ii) only
- (E) none of (i), (ii), or (iii)



3. Let A, B, and C be $n \times n$ matrices. Which of the following statements are TRUE?

(i)
$$(AB)^2 = A^2B^2$$

(ii)
$$(ABC)^T = A^T B^T C^T$$

(iii) If
$$A^2 = 0$$
, then $A = 0$.

- (A) (i) and (ii) only
- (B) none of (i), (ii), or (iii)
- (C) (ii) and (iii) only
- (**D**) (i), (ii), and (iii)
- (E) (iii) only

 $A \cdot A = 0$. $\begin{pmatrix} 1 & -1 \\ -1 \end{pmatrix} \begin{pmatrix} 1 & -1 \\ 1 & -1 \end{pmatrix}$ $= \begin{pmatrix} 0 & 0 \\ 0 & 0 \end{pmatrix}$.

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Part I - Multiple Choice. Clearly indicate your answer to each question by circling your choice. Each question is worth 2 marks.

For each question, choose the <u>BEST</u> option from the given options.



4. Which of the following matrices are symmetric?

(i)
$$A = [a_{ij}]$$
 where $a_{ij} = i^2 + j^2 \sqrt{A^{\top}} = [0]$

(ii)
$$A = [a_{ij}]$$
 where $a_{ij} = i^2 - j^2$

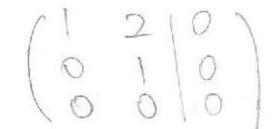
(iii)
$$A = [a_{ij}]$$
 where $a_{ij} = 2i + 2j$

- (A) (i) only
- (B) (ii) only
- (C) (iii) only
- (\mathbf{D}) (i) and (ii) only
- (E) (i) and (iii) only



5. Let A be an $m \times n$ matrix such that the system $A\mathbf{x} = \mathbf{b}$ has a unique solution. Which of the following statements are TRUE?

- (i) rank(A) = n
- (ii) the homogeneous system $A\mathbf{x} = \mathbf{0}$ has only the trivial solution $\sqrt{}$



- (iii) A is invertible
- (A) (i) and (ii) only
- (B) (i) and (iii) only
- (C) (ii) and (iii) only
- (D) (i) only
- (E) (ii) only

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Part II - Short Answer Questions. Write your solutions in the space provided below each question.

1. Find all solutions to homogeneous system of linear equations

$$2x_2 + 2x_3 + 2x_4 = 0$$
$$x_1 - x_3 - 3x_4 = 0$$
$$2x_1 + 3x_2 + x_3 + x_4 = 0$$
$$-2x_1 + x_2 + 3x_3 - 2x_4 = 0$$

[10 marks]

$$\begin{pmatrix}
0 & 2 & 2 & 2 & 0 \\
1 & 0 & -1 & -3 & 0 \\
2 & 3 & 1 & 1 & 0 \\
-2 & 1 & 3 & -2 & 0
\end{pmatrix}
\xrightarrow{R_1 \to R_2}
\begin{pmatrix}
1 & 0 & -1 & -3 & 0 \\
2 & 3 & 1 & 1 & 0 \\
-2 & 1 & 3 & -2 & 0
\end{pmatrix}
\xrightarrow{R_2 \to R_2}
\begin{pmatrix}
1 & 0 & -1 & -3 & 0 \\
-2 & 1 & 3 & -2 & 0
\end{pmatrix}
\xrightarrow{R_2 \to R_2}
\begin{pmatrix}
1 & 0 & -1 & -3 & 0 \\
0 & 2 & 2 & 2 & 0 \\
0 & 3 & 3 & 7 & 0 \\
0 & 1 & 1 & -8 & 0
\end{pmatrix}
\xrightarrow{R_2 \to R_2}
\begin{pmatrix}
1 & 0 & -1 & -3 & 0 \\
0 & 3 & 3 & 7 & 0 \\
0 & 1 & 1 & -8 & 0
\end{pmatrix}
\xrightarrow{R_2 \to R_2}
\xrightarrow{R_2 \to R_2}
\xrightarrow{R_2 \to R_2}
\begin{pmatrix}
1 & 0 & -1 & -3 & 0 \\
0 & 3 & 3 & 7 & 0 \\
0 & 1 & 1 & -8 & 0
\end{pmatrix}
\xrightarrow{R_1 \to 3R_2}
\xrightarrow{R_2 \to R_2}
\xrightarrow{R_2 \to R_2}
\begin{pmatrix}
1 & 0 & -1 & -3 & 0 \\
0 & 1 & 1 & 1 & 0 \\
0 & 0 & 0 & 1 & 0 \\
0 & 0 & 0 & 0 & 0
\end{pmatrix}
\xrightarrow{R_1 \to 3R_2}
\xrightarrow{R_2 \to R_2}
\xrightarrow{R_2 \to R_2}$$

$$\begin{pmatrix}
1 & 0 & -1 & -3 & 0 \\
0 & 1 & 1 & 1 & 0 \\
0 & 0 & 0 & 1 & 0 \\
0 & 0 & 0 & 0 & 0
\end{pmatrix}
\xrightarrow{R_1 \to 3R_2}
\xrightarrow{R_2 \to R_2}
\xrightarrow{R_2 \to R_2}$$

$$\begin{pmatrix}
1 & 0 & -1 & 0 & 0 \\
0 & 1 & 1 & 1 & 0 \\
0 & 0 & 0 & 0 & 0
\end{pmatrix}
\xrightarrow{R_1 \to 3R_2}
\xrightarrow{R_2 \to R_2}
\xrightarrow{R_1 \to 3R_2}
\xrightarrow{R_2 \to R_2}
\xrightarrow{R_1 \to 3R_2}
\xrightarrow{R_2 \to R_2}$$

$$\begin{pmatrix}
1 & 0 & -1 & 0 & 0 \\
0 & 1 & 1 & 1 & 0 \\
0 & 0 & 0 & 0 & 0
\end{pmatrix}
\xrightarrow{R_1 \to 3R_2}
\xrightarrow{R_2 \to R_2}
\xrightarrow{R_2 \to R_2}
\xrightarrow{R_1 \to 3R_2}
\xrightarrow{R_2 \to R_2}
\xrightarrow{R_2 \to R_2}$$

Condusion:
$$X = \begin{bmatrix} t \\ -t \\ t \end{bmatrix}$$
 tenk $\begin{pmatrix} X_1 = t \\ X_2 = t \\ X_3 = t \end{pmatrix}$

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2. Suppose a linear system of equations in the variables x_1, x_2, x_3 has augmented matrix

$$\left[\begin{array}{cc|cc|c} 1 & 1 & c & 1 \\ 1 & c & 1 & 1 \\ c & 1 & 1 & -2 \end{array}\right]$$

(a) For what values of c is the system (i) inconsistent, (ii) consistent with a unique solution, and (iii) consistent with infinitely

many solutions? [10 marks]

many solutions? [10 marks]
$$A = \begin{pmatrix} 1 & C & | & 1 \\ | & C & | & C \\ | & C & | &$$

$$\frac{R_{3}-CR_{1}}{0 \quad C-1 \quad I-C} = 0$$

$$0 \quad C-1 \quad I-C = 0$$

$$0 \quad I-C \quad I-C^{2} = 2-C$$

$$\begin{pmatrix}
1 & 1 & C & | & 1 \\
0 & C-1 & 1-C & | & 0 \\
0 & 0 & 2-C-C & -2-C
\end{pmatrix}$$

When 2-c-c=0 and -2-c=0

A is inconsistent.

$$C^{2}+C-2=0$$
 $-2-C+0$
 $(C+2)(C-1)=0$ $C^{2}+2$.
 $C^{2}+2$ $C^{2}+2$.

because it has grow of (o. olx)

Conclusion: (i) c=1 (ii) c+2 and c+1 (iii) c=-2

$$A = \begin{pmatrix} 1 & 1 & 0 & 1 \\ 0 & -1 & 1 & 0 \\ 0 & 1 & 1 & -2 \end{pmatrix} \xrightarrow{R_1 + R_2} R_3 + R_2.$$

$$\begin{pmatrix} 1 & 0 & 1 & 1 & 1 \\ 0 & -1 & 1 & 0 & 1 \\ 0 & 0 & 2 & 1 & -2 \end{pmatrix} \xrightarrow{\mathcal{R}} \begin{pmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & -1 & 0 \\ 0 & 0 & 1 & -1 \end{pmatrix}$$

$$rank(A) = n = 3$$

So when C=0, it's consistent with one solution.

hen 2-c-c=0 and -2-c=0

A is consistent with infinitely many golutions, becomes ronk(A) <n:

That means C= -2.

when 2-c-c2+0. A has unique golution because rank(A) = n (# of variables) C=+-2 and C=1

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3. (a) Define what it means for a matrix A to be in row-echelon form. [2 marks]

(1) The row of zeros is at the bottom of the matrix. (0000)

(2) The non-zero rows begin with the leading 1 (1)

(3) In the next row, entry of leading 1 should be on the right of the leading 1 of the row above it.

3. (b) Suppose $A = \begin{bmatrix} 1 & 0 & a & 1 \\ -1 & -1 & b & -2 \\ 3 & 1 & c & 0 \end{bmatrix}$, and the reduced row-echelon form of A is $\begin{bmatrix} 1 & 0 & 2 & 0 \\ 0 & 1 & -5 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$. Determine a, b, and c. [6 marks]

$$A = \frac{R_2 + R_1}{R_3 - 3R_1} \begin{pmatrix} 1 & 0 & \alpha & 1 \\ 0 & -1 & \alpha + b & -1 \\ 0 & 1 & C - 3\alpha & -3 \end{pmatrix} \xrightarrow{R_3 + R_2} \begin{pmatrix} 1 & 0 & \alpha & 1 \\ 0 & -1 & \alpha + b & -1 \\ 0 & 0 & 2\alpha + b + C & -4 \end{pmatrix} \xrightarrow{-R_2}$$

$$\begin{pmatrix}
1 & 0 & a & 1 \\
0 & 1 & -(a+b) & 1
\end{pmatrix}$$
Set $1 = 2$

$$1 - (a+b) = -5$$

$$1 - 2a + b + C = 0$$

$$1 - 2a + b + C = 0$$

$$1 - 2a + b + C = 0$$

$$900 = 2, b=3, c=1$$

which is exactly who we uset.

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4. (a) Let $A = \begin{bmatrix} 1 & -1 \\ 2 & 0 \end{bmatrix}$, and $X = \begin{bmatrix} x_1 & x_2 \\ x_3 & x_4 \end{bmatrix}$. Find the augmented matrix of the system $AX - XA = I_2$ in the variables x_1, x_2, x_3, x_4 . [4 marks]

$$= \begin{pmatrix} -2x_2 - x_3 & x_1 + x_2 - x_4 \\ 2x_1 - x_3 - 2x_4 & 2x_2 + x_5 \end{pmatrix}$$
which is equal $\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$ This means $\begin{cases} -2x_2 - x_3 = 1 \\ x_1 + x_2 - x_4 = 0 \\ 2x_1 - x_3 - 2x_4 = 0 \end{cases}$
So the augmented matrix is

So the augmented matrix is

$$\begin{pmatrix} 0 & -2 & -1 & 0 & -1 \\ 1 & 1 & 0 & -1 & 0 \\ 2 & 0 & -1 & -2 & 0 \\ 0 & 2 & 1 & 0 & 1 \end{pmatrix}$$

4. (b) A matrix B is said to be a square root of a matrix A if BB = A. Find two square roots of $A = \begin{bmatrix} 2 & 2 \\ 2 & 2 \end{bmatrix}$. [4 marks]

Call the two square root matrix C and D

$$C = (| | |) Check: CC = (| | |)(| | |) = (2 2 2) = A$$

$$D = (-1)$$
 check $D = (-1)(-1)(-1) = (-2) = A$.

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5. (a) Find the inverse of
$$A = \begin{bmatrix} 1 & -1 & 1 \\ 2 & -3 & 0 \\ -1 & 1 & -2 \end{bmatrix}$$
. [4 marks] $\left(A \mid I \right) \longrightarrow \left(I \mid A \mid A \right)$.

$$\begin{pmatrix} 1 & -1 & 1 & 1 & 0 & 0 \\ 2 & -3 & 0 & 0 & 1 & 0 \\ -1 & 1 & -2 & 0 & 0 & 1 \end{pmatrix} \xrightarrow{R_2 - 2R_1} \begin{pmatrix} 0 & -1 & 2 & | & 1 & 0 & 0 \\ 0 & -1 & 2 & | & -2 & 1 & 0 \end{pmatrix} \xrightarrow{R_1 - R_2}$$

$$\begin{pmatrix}
1 & 0 & 3 & | & 3 & -1 & 0 \\
0 & -1 & -2 & | & 2 & 1 & 0
\end{pmatrix}$$

$$\begin{pmatrix}
R_1 - 3R_3 \\
0 & -1 & 0 & | & 6 & -1 & 3 \\
R_2 + 2R_3 \\
0 & 0 & | & -1 & 0 & -1
\end{pmatrix}$$

$$-R_2$$

$$\begin{pmatrix}
1 & 0 & 0 & | & 6 & -1 & 3 \\
0 & 1 & 0 & | & 4 & -1 & 2 \\
0 & 0 & | & -1 & 0 & -1
\end{pmatrix}$$
So the $A^{1} = \begin{pmatrix} 6 & -1 & 3 \\
4 & -1 & 2 \\
-1 & 0 & -1
\end{pmatrix}$

5. (b) Given
$$\begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 3 & -1 & 2 \\ 1 & 0 & 4 \\ 2 & 1 & 0 \end{bmatrix} \begin{bmatrix} y_1 \\ y_2 \\ y_3 \end{bmatrix}$$
 and $\begin{bmatrix} z_1 \\ z_2 \\ z_3 \end{bmatrix} = \begin{bmatrix} 1 & -1 & 1 \\ 2 & -3 & 0 \\ -1 & 1 & -2 \end{bmatrix} \begin{bmatrix} y_1 \\ y_2 \\ y_3 \end{bmatrix}$. Express the variables x_1, x_2, x_3 in terms of z_1, z_2, z_3 and z_3 . Suggestion: Use part (a). [4 marks]

$$\begin{bmatrix} 2_1 \\ 2_2 \\ 2_3 \end{bmatrix} = A \cdot \begin{bmatrix} y_1 \\ y_2 \\ y_3 \end{bmatrix} \Rightarrow A' \cdot \begin{bmatrix} 2_1 \\ 2_2 \\ 2_3 \end{bmatrix} = A' \cdot A \cdot \begin{bmatrix} y_1 \\ y_2 \\ y_3 \end{bmatrix} \Rightarrow A' \cdot \begin{bmatrix} 2_1 \\ 2_2 \\ 2_3 \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \\ 2_3 \end{bmatrix} = \begin{bmatrix} 1$$

Recall A in S(a).

$$\begin{bmatrix} 3 \\ 1 \end{bmatrix} = \begin{bmatrix} 6 \\ 4 \\ -1 \\ 2 \end{bmatrix} \begin{bmatrix} 21 \\ 22 \\ 23 \end{bmatrix}$$

$$\begin{bmatrix} 1 \\ 21 \\ 22 \\ 23 \end{bmatrix}$$

$$\begin{bmatrix} 1 \\ 21 \\ 22 \\ 23 \end{bmatrix}$$

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$$\begin{bmatrix} 1 \\ 21 \\ 22 \\ 23 \end{bmatrix}$$

$$\begin{bmatrix} 1 \\ 21 \\ 22 \\ 23 \end{bmatrix}$$

$$\begin{bmatrix} 1 \\ 21 \\ 22 \\ 23 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} \chi_1 \\ \chi_2 \end{bmatrix} = \begin{bmatrix} 12 - 2 & 5 \\ 2 & -1 & -1 \end{bmatrix} \begin{bmatrix} 217 \\ 22 \\ 23 \end{bmatrix} \Rightarrow \begin{bmatrix} \chi_1 \\ \chi_2 \end{bmatrix} = \begin{bmatrix} 128, -282 + 583 \\ 281, -82 - 23 \end{bmatrix} \Rightarrow \begin{bmatrix} \chi_1 \\ \chi_2 \end{bmatrix} \begin{bmatrix} 128, -282 + 583 \\ 168, -382 + 88 \end{bmatrix} \begin{bmatrix} \chi_2 \\ \chi_3 \end{bmatrix} = \begin{bmatrix} 128, -282 + 583 \\ 168, -382 + 88 \end{bmatrix}$$

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6. (a) Show that if A is a
$$2 \times 2$$
 diagonal matrix of the form $\begin{bmatrix} a & 0 \\ 0 & a \end{bmatrix}$, then $AB = BA$ for any 2×2 matrix B. [2 marks]

6. (b) Let A be a 2×2 matrix with the property that AB = BA for all 2×2 matrices B. Show that A must be a diagonal

matrix of the form $\begin{vmatrix} a & 0 \\ 0 & a \end{vmatrix}$. [4 marks] Let B=[de] where b.c.d.e are random figure out that dg=ch real numbers holds for every choice of A=[fg] where f.g.h.i are constants. c and d.

$$AB=BA \Rightarrow |bf+dg=bf+ch| |ag=ch| |i-f=0 \Rightarrow |f=i|$$

$$|cf+eg=bg+ci| |cf+eg=bg+ci| |cf+eg=bg+ci| |cf+eg=bg+ci| |ch+ei=af+eh| |ch+ei=af$$

Pholds for every choice of c and d.

So g and h must be 0.

So
$$10=0$$
.

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$$(6 - 1 3)$$
 $(1 - 1)$ $(4 - 2)$ $(4 - 1)$ $(4 - 2)$

$$\begin{pmatrix} 1 & 0 & 2 & 1 \\ 3 & -1 & 3 & -2 \end{pmatrix}$$

$$cf - ci = bg - eg$$

 $c(f - i) = g(b - e)$

$$bh-eh=df-di$$

 $h(b-e)=d(f-i)$

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