# CALCULATING BOUNDS ON INFORMATION LEAKAGE USING MODEL-CKECINGG TOOLS

A Thesis presented to the Faculty of the Graduate School at the University of Missouri

 $\label{eq:continuous} \mbox{In Partial Fulfillment}$  of the Requirements for the Degree  $\mbox{Master of Science}$ 

by

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#### ACKNOWLEDGMENTS

This page is where you would acknowledge all those who helped you with your academic research. This is not necessarily where you would recognize loved ones who supported you during your studies. That would be more appropriately done in an optional Dedication page. I would like to thank Professor Smith Lorem ipsum dolor sit amet, consectetuer adipiscing elit. Vestibulum eu tellus. Nullam et odio eget sapien porttitor interdum. Donec vel ante. Maecenas in sem a nunc viverra hendrerit. Quisque ut massa quis pede blandit pharetra.

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### ABSTRACT

This is the abstract of your dissertation project. It should not exceed one page.

# Introduction

Introduce the reader to the current problem that you wish to solve, and why anyone should care about it.

# Theory background

### 2.1 Min-entropy

The introduction counts as chapter 1. This page shows how the bulk of your thesis will be organized: through chapters and sections. Here is a citation.[?]

### 2.2 Information leak

### 2.3 Two intuitive solutions

To count the number of outputs of a program, we come up with two approaches: Put the program in a double loop and count the number of outputs, or let the program iterate through all input values and record the outputs in an array. The first approach is time-consuming, while the second one is space-consuming.

#### 2.3.1 Double loop and counter

In algorithm 1, for each possible output value, we iterate through the input range to see if an input can result in this output. If we hit such an input, counter increases and the code breaks out of the inner loop to continue testing the next possible output value. After the double loop finishes, the value of OCounter is the number of outputs of program P.

Algorithm 1 Calculate the number of outputs using double loop.

```
S \leftarrow 0
O \leftarrow 0
SIn \leftarrow 0
OOut \leftarrow 0
OCounter \leftarrow 0
SMax \leftarrow 1 << bitLength - 1
OMax \leftarrow 1 << bitLength - 1
for O = 0 to OMax do
  for S = 0 to SMax do
     SIn \leftarrow S
     OOut \leftarrow P(SIn) // the program P takes SIn as input
     if OOut = O then
        OCounter \leftarrow OCounter + 1
        break
     end if
  end for
end for
```

In algorithm 1, we declared seven variables, and all of them require bitLength bits except for OCounter which is bitLength+1 bits. The total memory usage for variables is  $7 \times bitLength+1$  at O(bitLength). As with execution time, we assume program P takes time t(P) to execute, and the total execution time for the double loop when break is never reached is  $2^{bitLength} \times 2^{bitLength} \times t(P)$ . Thus the time complexity is  $(2^{O(bitLength)}) \times t(P)$ .

In order to get an estimation of how much time the double loop will take to execute, we implemented a piece of C code with an empty while loop which loops  $2^{32}$  times. On out experiment PC, this loop takes on average 10.30 seconds to complete. Were we to run a double loop in bit length of 32, the execution time would be  $2^{32} \times 10.30$  seconds, which is around 1403 years. Running the double loop directly would be infeasible.

#### 2.3.2 Single loop and array

In algorithm 2, we create an array with size equal to the maximum number of possible outputs (1 << bitLength), or  $2^{bitLength})$  and initialize it with zeros. While we iterate through the range of S, we set each OHit[P(SIn)] to 1. When a 0 turns to 1, we increase OCounter. After the loop, the value of OCounter is the number of outputs by program P.

Algorithm 2 Calculate the number of outputs using single loop and a table.

```
S \leftarrow 0
O \leftarrow 0
SIn \leftarrow 0
OOut \leftarrow 0
OCounter \leftarrow 0
SMax \leftarrow 1 << bitLength - 1
OMax \leftarrow 1 << bitLength - 1
OHit[OMax + 1] \leftarrow [0]
for S = 0 to SMax do
   SIn \leftarrow S
  OOut \leftarrow P(SIn) // the program P takes SIn as input
  if OHit[OOut] = 0 then
     OCounter \leftarrow OCounter + 1
     OHit[OOut] \leftarrow 1
  end if
end for
```

In algorithm 2 except for the array we have 7 variables using  $7 \times bitLength + 1$  memory. The array OHit[] is of size  $2^{bitLength} \times bitLength$  making a total of  $2^{bitLength} \times bitLength + 7 \times bitLength + 1$  at  $2^{O(bitLength)}$ . As with execution time, we assume program P takes time t(P) to execute, and the execution time for the single loop is  $2^{bitLength} \times t(P)$ . Thus the time complexity is  $(2^{O(bitLength)}) \times t(P)$ .

We set the bit length to 32. In array OHit[], each element is 32 bits and the number of elements is  $2^{32}$ . The total memory usage for this array is  $2^{32} \times 32$  bits, which is 16 gigabytes. To our knowledge, it is neither difficult nor expensive to build a PC with more than 16 gigabytes of memory, and we can get such a PC off-the-shelf from top gaming PC brands like Alienware. However, as this memory requirement grows exponentially, adding two to three bits to the bit length and the requirement will exceed the capacity of current PCs.

if this is
not hard
we need
reasons
not doing
this..

## Experiment with Getafix

We want to use model-checking tools to see if we can reduce the time requirement of algorithm ??. Specifically, we choose the reachability property and append algorithm 3 to the end of algorithm ??. The statement within the if statement has a label. Although the exact statement following that label is irrelevant, reaching this line means *OCounter* satisfies the constrains in the condition block.

(why and what other property are there)

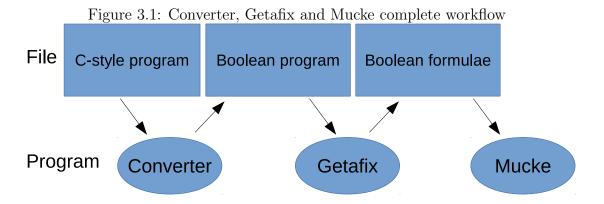
We experiment on several model-checking tools, including Interproc from [1], Berkeley Lazy Abstraction Software Verification Tool (Blast) from [2] and Getafix from [3]. We can not get correct reachability results from Interproc and Blast, so we shift our focus onto Getafix.

correct citations of web

page

Algorithm 3 Determine if *OCounter* meets certain constrains.

if value of *OCounter* meets certain constrains then reach: *OCounter* // a label followed by a statement end if



#### 3.1 Getafix

Getafix is a symbolic model checker for Boolean programs implemented in [3]. Getafix only supports reachability check. It translates sequential and concurrent Boolean programs into Boolean formulae and uses the model-checker Mucke to solve the reachability problem symbolically using Boolean Decision Diagrams [4].

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#### 3.2 The converter

Input for Getafix are boolean programs, meaning it only supports binary variables which can be either 0 or 1. We represent our problem in c-style code, thus we need to translate it into boolean form. We implemented a converter to automate this process, and figure 3.1 shows the complete workflow including the converter. The converter has three components, a parser, a built-in function generator and a piece of script which calls the first two components and assemble the output file. The converter has these properties:

1. The input to the converter is a c-style code file and a positive integer which

represent the bit length. The converter supports 32 bits and less. Also note that the converter represents a number with bit length of bitLength using bitLength + 1 bits. We do this so that writing a loop which iterate from 0 to 1 << bitLength - 1 is easier.

- 2. The output of the converter is a boolean program which follows the syntax of Getafix input file.
- 3. In the language that we defined for the input file, we support only one variable type: non-negative decimal integer. Again we support the length up to 32 bits.
- 4. Our converter does not support function definitions. The input file has two parts, variable declarations block and statements block. The parser will print these blocks into the main function of the output boolean program. Also we require all variable declarations to appear before statements in the input code. Getafix input syntax has this requirement, and we decide to keep it in our converter.
- 5. We implement support for the following symbolic operators in the language: plus +, minus -, and &, or |, xor ^, greater than >, equal ==, less than <, not equal !=, greater than or equal >=, less than or equal <=, left shift << and right shift >>.
- 6. We implement support for three control statements: if...else, while loop, goto and statements with labels. We currently do not support for loop, do...while loop, switch statements, break and continue, but these statements can be easily expressed using the supported ones.

Input to the parser is a c-style code file and a desired bit length. Output of the parser is its corresponding boolean program which follows the syntax of Getafix input file. First we define the syntax of the input code and second we create the parser using flex and bison. The parser scans the input code and builds a syntax tree. Then the parser prints the syntax tree as a boolean program. The parser has three points worth noting:

Table 3.1: Examples of input and output of the parser, with bit length of 4

Input	Output
ron CMorr 16.	decl SMax4,SMax3,SMax2,SMax1,SMax0;
var SMax = 16;	Smax4, SMax3, SMax2, SMax1, SMax1 := 1,0,0,0,0;
СТотого СТотого	STemp4,STemp3,STemp2,STemp1,STemp0 :=
STemp = STemp	minus(STemp4,STemp3,STemp2,STemp1,STemp0,0,0,1,0,1);

- 1. When printing the output code, the parser "stretches" each variable and literal into its binary form. Assume the desired bit length is bitLength. We split each variable into bitLength variables by copying the name of the variable bitLength times and append a counter value to each one. Also we convert a literal to its corresponding binary value and prepend it with zeros to reach the desired length. Table 3.1 contains an example of how the parser deals with a variable declaration.
- 2. In a boolean program, all operators operate on bit level, so we need to implement higher-level operators like plus, minus, greater than and left shift using operators that Getafix supports. In the parser, we print these high-level operators as function calls in the output boolean program, and the built-in function generator generates the body of the function. Table 3.1 contains an example of how the parser deals with a high-level operator.

3. In the boolean code syntax which Getafix defines, function call plus the semicolon is defined as a statement, and another rule allows the code to assign a
function call to an identifier, but function call itself is not an expression. This
means that a function call can not work as an expression as in many other
languages, and it leads to two problems: First, the decider expression in if...else
and while statements can not contain function calls. Second, parameters of a
function call or operands to an operator can not be a function call. We automated a solution in the parser to the first problem, which assigns the decider
expression to a temporary variable and use that variable as the decider, so we
can use the c-style if...else and while in the input code. For the second problem,
a possible solution would be to manage a set of internal temporary variables
and assign each function call to a variable, but we did not implement it.

Input to the built-in function generator is a desired bit length. Output is a set of high-level operators like plus and left shift implemented as functions. We do not track the necessary functions in the parser, as experiments with Getafix indicate that the uncalled functions affect little on the execution time. Listing 3.1 shows a sample function by the generator.

Listing 3.1: Greater than operator as a function in boolean program with bit length of 2.

```
bool isGT(left2 , left1 , left0 , right2 , right1 , right0)
begin
if (left2 != right2) then
    if (left2 = 1) then return 1; fi
else
```

Input to the third component, a piece of script, is a c-style code file and a desired bit length. Output of the script is a boolean program ready for Getafix to process. The script first passes the bit length to the built-in function generator and redirect its output to the output file. Then the script passes both the input to the parser and append its output to the output file. At this point the output is complete.

#### 3.3 Tests and results

Before we have the converter, we coded a test case manually and Getafix gave us the correct answer. Now with the converter we can run more complicated tests and see if Getafix is a good solution to the problem of calculating information leakage. We decide to run the ten test cases from paper [?]. In each test, O represents the output of its test, and S is the input.

#### 3.3.1 Sanity check

Listing 3.2 shows the code we use. In this test, O remains constant unless S is within a certain range. The program has 16 different outputs, ranging from 4 to 19.

Listing 3.2: Sanity check test program.

```
var base = 4;
if(S < 16){O = base+ S;}
else{O = base;}</pre>
```

Listing 3.3: Impliet flow test program.

# Monotonic programs

In this chapter we describe our discovery that if the test program P is monotonic, then we can execute the program wrapped in algorithm 1 and get a direct output count in a reasonable time.

### 4.1 Discovery by mistake

During the initial tests with the sanity check program of bit length 32, we code algorithm 1 in C using while instead of for, compile it and execute the program. The program terminates in less than a minute, and gives the correct output count. Later we time the execution of an empty loop from 0 to  $2^{32} - 1$  and the result is 10.30 seconds, so theoretically the double loop would take a much longer time to terminate, longer than our test result with sanity check.

# Summary and concluding remarks

Congratulations on completing your dissertation.

# Appendix A

# Title of first appendix

### A.1 Section title

Here is some additional information which would have detracted from the point being made in the main article.

#### A.1.1 Subsection title

This section even has subtitles

# **Bibliography**

- [1] Interproc, 2011.
- [2] MTC (models and theory of computation): BLAST project, 2008.
- [3] Salvatore La Torre, Madhusudan Parthasarathy, and Gennaro Parlato. Analyzing recursive programs using a fixed-point calculus. In *Proceedings of the 2009 ACM SIGPLAN Conference on Programming Language Design and Implementation*, PLDI '09, page 211222, New York, NY, USA, 2009. ACM.
- [4] Getafix boolean program checker, 2009.

#### **VITA**

This is a summary of your *professional* life, and should be written appropriately. This can be written in the following order: where your where born, what undergraduate university you graduated from, if you received a masters, and which institution you graduated from with your PhD (University of Missouri). You can describe when you began research with your current advisor.

In another paragraph, you could say if/when you were married, what the name of your kids are, and what your plans are for after graduation if you choose. Take a look at other vita's from other dissertations for examples.