

Towards Measuring Plant Photosynthetic Heterogeneity

Oliver L Tessmer¹, Xi Yin¹, Jeffrey A Cruz^{2,3}, Linda J Savage², Xiaoming Liu¹, David M Kramer^{2,3}*, Jin Chen^{1,2}*

¹Department of Computer Science and Engineering, Michigan State University, East Lansing, MI 48824, USA

²Department of Energy Plant Research Laboratory, Michigan State University, East Lansing, MI 48824, USA

³Department of Biochemistry and Molecular Biology, Michigan State University, East Lansing, MI 48824, USA

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ABSTRACT

Motivation: Photosynthesis is one of the most important biological processes on earth. Plant photosynthetic heterogeneity refers to a plant comprising multiple regions, many of which have significantly different photosynthesis properties, probably because of vastly different leaf developmental stage and tolerance level to environmental changes. Measuring plant photosynthetic heterogeneity enables biologists to interpret the sophisticated photosynthesis phonemics data, which is particularly important for plant primary productivity estimation and modeling.

Results: Taking advantage of the rapid developing non-invasive plant phenotyping technologies, we develop a new plant photosynthetic heterogeneity measurement called PlantPH to effectively identify and integrate the plant morphological and physiological features.

The application of PlantPH on more than 1,000 Arabidopsis chloroplast plants, including dozens of ecotypes and hundreds of chloroplast mutant strains, has successfully identified a group of genes that affect photosynthesis under simulated natural environments.

Availability: Software is available at XXX.

Contact: jinchen@msu.edu, kramer8@cns.msu.edu

1 INTRODUCTION

By consuming water, light and CO_2 , plants produce sugars and release O_2 with photosynthesis (Kramer and Evans, 2011). The process involves the formation of high energy intermediates capable of generating reactive oxygen species. The photosynthetic apparatus, chloroplast and surrounding leaf tissue is inherently susceptible to oxidative damage, especially under stress conditions when the supply of light energy exceeds the capacity to utilize it (Durrant *et al.*, 1990; Asada, 1996). Plants have evolved a number of mechanisms, such as photosynthetic apparatus damage and repair (Melis, 1999), to dissipate excess light energy to minimize the potential for damage at the expense of photosynthetic efficiency (Adams III *et al.*, 2006; Rochaix, 2014). However, these mechanisms are sensitive to leaf development and thus may change from one leaf tissue to another, resulting in heterogeneous photosynthetic patterns (see examples in Figure 1 where the chlorophyll fluorescence images are false-color images and the light intensity of every pixel is proportional to photosynthetic efficiency (Toet and Walraven, 1996)). The heterogeneous patterns may also vary with the position, size and

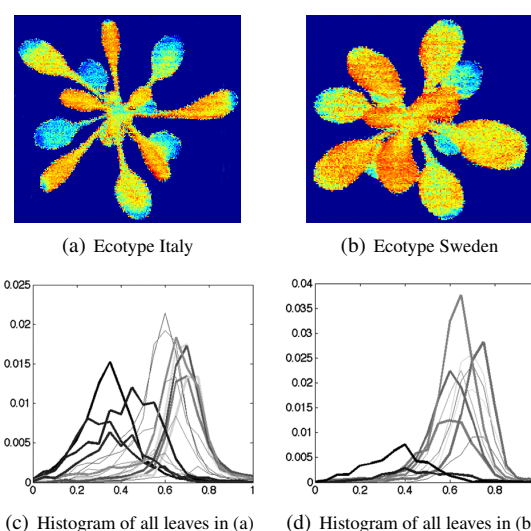


Fig. 1. We demonstrate the photosynthesis heterogeneity using two Arabidopsis ecotypes (Italy and Sweden). Both plants were grown under the same stress conditions, but the false-color images of photosystem II activity (a,b) and the distributions of the leaf-level photosynthesis (c,d) show that the Italy ecotype is more susceptible to environmental changes.

growth rate of leaves, since leaves at the same node are unique in age. By integrating plant morphological and physiological features, measuring plant photosynthetic heterogeneity aids interpretation of sophisticated photosynthesis phonemics data, which is particularly important for plant primary productivity estimation and modeling (Meng *et al.*, 2007).

Heterogeneity is a statistical concept relating to the uniformity in a substance (Hall, 2003). The granularity of plant photosynthetic heterogeneity studies can range from cells to tissues, leaves, and even to the whole plant level. While in-leaf variability in photosynthetic activity has been well-studied for the understanding of the effects of stomatal conductance (Cheeseman, 1991; Buckley *et al.*, 1997), recent works show that photosynthetic capacity may decline with vertical gradient and leaf age (Kitajima *et al.*, 2002; Chen *et al.*, 2008), suggesting that leaf-based photosynthetic heterogeneity is a key towards processing and understanding photosynthesis phenotype images.

Leaf heterogeneity in photosynthesis was first studied with computer simulation (Chen *et al.*, 2008). Due to the lack of high-throughput phenotyping technologies, the authors determined the

*to whom correspondence should be addressed

effects of biochemical variability via the Farquhar model (a mechanistic, biochemical model widely used to describe steady-state CO_2 assimilation in leaves), incorporating defined degrees of spatial variability of its parameters (Sharkey, 1985; Farquhar *et al.*, 2001). Recently, with the advent of advanced technologies of biomedical imaging, directly measuring heterogeneity has recently assumed new importance (Tiihonen *et al.*, 1996; Wieneke *et al.*, 1999; Wang *et al.*, 1999; Cruz *et al.*, 2015). The rapid development of lighting and imaging techniques enables real-time non-invasive monitoring of photosynthesis (Houle *et al.*, 2010; Cruz *et al.*, 2015), resulting in vast amount of chlorophyll fluorescence images of plants (Wituszynska *et al.*, 2013). These images can be used to quantify photosynthetic behavior in genetically diverse populations, enabling the measurement of variability of photosynthetic parameters at high resolution across leaves, leading to better understanding of the underlying mechanisms that control the photosynthetic properties (Rascher *et al.*, 2011; Fiorani and Schurr, 2013).

Measuring leaf-based photosynthetic variability in large-scale phenotyping experiments requires automatic identification of most of the visible leaves in all fluorescence images and an appropriate measurement for the variation of photosynthesis parameters across leaves that takes geometrical (leaf position and size), temporal (leaf growth rate) and physiological (leaf age) information into consideration. However, there is currently no existing infrastructure to analyze such an amount of phenotype information. In this paper, we present a new computational framework called *Plant Photosynthesis Heterogeneity* (PlantPH), and use the tool to analyze the leaf-level photosynthesis heterogeneity patterns of more than 100 Arabidopsis chloroplast mutant strains over dynamic lighting conditions, each with at least four replicates. The followed outlier detection process successfully identifies mutants with distinct heterogeneity patterns under specific subsets of the environmental conditions. Overall, PlantPH has the following three advantages:

1. It is the first computational framework to measure plant leaf-level heterogeneity of photosynthesis with leaf size, position and growth rate.
2. Its performance is significantly better than traditional heterogeneity tests that cannot fully use the spatial and temporal information in the fluorescence images.
3. It discovers multiple types of photosynthetic variabilities in a large scale experiment.

2 BACKGROUND

The inputs to plant heterogeneity test are leaf-level photosynthesis values obtained using leaf segmentation methods. The general method of assessing whether the leaves of a plant are photosynthetically homogeneous or heterogeneous is by means of the Cochran's Q-test (Conover, 1999) and the I^2 statistic (Higgins and Thompson, 2002; Higgins *et al.*, 2003).

2.1 Leaf Alignment and Tracking

The input to Plant heterogeneity test are leaf-level photosynthesis values. To obtain the values, a method is needed to identify every piece of leaf from a whole plant image, measure the fluorescence intensity of every pixel on a leaf, and finally convert the intensity values to biologically meaningful photosynthesis parameters.

In our previous studies, we have developed a new multi-leaf alignment and tracking algorithm (Yin *et al.*, 2014a) to meet the

requirements. Different from the naive procedure of aligning leaves iteratively using the Chamfer distance (Barrow *et al.*, 1977), our tool aims to find the best alignment of multiple leaves simultaneously in an input image. We formulate an optimization problem of an objective function with three terms: the average of chamfer distances of aligned leaves, the number of leaves, and the difference between the synthesized mask by the leaf candidates and the original image mask. The extension on leaf tracking (Yin *et al.*, 2014b) tracks multiple leaves from fluorescence plant videos by continuously applying template transformation to the current leaf candidates in order to fit to the previous frame. Experimental results show that the multi-leaf alignment and tracking tool performs substantially better than the baseline of the Chamfer matching algorithm in terms of both accuracy and efficiency.

However, there are two obstacles preventing us from directly using our leaf alignment algorithm in PlantPH. First, the tool only identifies one leaf if the leaf overlap rate is high (e.g. 59%). In addition, the leaf boundaries are not precisely identified by the multi-leaf alignment tool, since predefined leaf templates are used. Subsequently, the leftover of leaf alignment consists of partial leaves that are highly overlapped and leaf boundaries of the successfully recognized leaves (Fig. XX). The covered leaves are usually old leaves with diverse photosynthesis activities. Simply deleting them may result in inaccurate heterogeneity scores. The second obstacle is that the leaf alignment process is a time consuming process. Processing 100 images each containing 20 plants may take about 5 hours. It is not practical to apply leaf alignment on all the images (in our case 2 months would be needed to process all the 31,120 images).

2.2 Heterogeneity Test

Cochran's Q-test is the classical measure of heterogeneity (Conover, 1999). In the scenario of leaf-based photosynthetic heterogeneity, Q is calculated as the weighted sum of squared differences between the photosynthesis value of an individual leaf and the pooled photosynthesis value across all leaves with the weights being those used in the pooling method. The distribution of Q is a chi-square statistic with $k - 1$ degrees of freedom, where k is the number of leaves. Cochran's Q-test has been widely used in biomedical studies. For example, heterogeneity in the aggressiveness of tumor cell populations has been adopted as an essential feature in predicting treatment success (O'Sullivan *et al.*, 2003).

The I^2 statistic describes the percentage of variation across studies that is due to heterogeneity rather than chance (Higgins and Thompson, 2002; Higgins *et al.*, 2003). I^2 can be calculated as $I^2 = (Q - df)/Q$, where Q is Cochran's Q-test heterogeneity statistic and df is the degrees of freedom. A negative value indicates no observed heterogeneity, and larger values show increasing heterogeneity. I^2 is an intuitive and simple expression of the inconsistency. I^2 of leaf-based photosynthetic heterogeneity does not inherently depend upon the number of leaves, so that I^2 values of different plants become comparable. A confidence interval for I^2 can be constructed using either the iterative non-central chi-squared distribution method (Hedges and Pigott, 2001) or the test-based method (Higgins and Thompson, 2002).

However, due to the nature of plants, leaf-based photosynthetic heterogeneity often includes a small number of leaves. For example, there are fewer than ten rosette leaves on a 2-3 week old Arabidopsis thaliana (a model plant). Thus, the power of the traditional

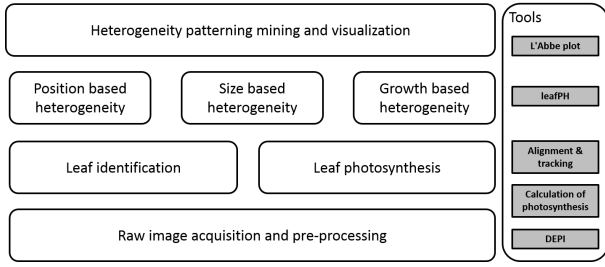


Fig. 2. Architecture of plant phenotype analysis where PlantPH serves as a key player for phenotype pattern mining.

Cochran's Q-test and I^2 statistic in such circumstances is low (Higgins *et al.*, 2003; Gavaghan *et al.*, 2000; Huedo-Medina *et al.*, 2006; Ioannidis *et al.*, 2007).

Furthermore, leaves with different locations, sizes or growth rates may have diverse photosynthetic performance, resulting in high level of heterogeneity (Van Lijsebettens *et al.*, 1991; Chen *et al.*, 2008). But none of these factors has yet been taken into the existing measurement of heterogeneity.

3 METHOD

In this article, we present a new leaf-based plant phenotype heterogeneity measurement, followed with a workflow to efficiently use the measurement on large-scale experiments (Fig. 2).

3.1 PlantPH Measurement

We introduce a new leaf-based heterogeneity measurement called *PlantPH* as follows. First, let $T = \{T_1, T_1, \dots, T_n\}$ be the set of effect estimates of a plant p with n leaves. The effect estimate T_i of leaf l_i in plant p is defined as the difference between the averaged photosynthetic values of the leaf and the whole plant. Mathematically, in each effect estimate T_i , let u_i and u_p be the averaged photosynthesis values of leaf l_i and the whole plant p , respectively. Under the assumption of normal distribution and homoscedasticity, the effect estimate T_i is the standardized mean difference (Hedges and Vevea, 1998), which can be estimated by:

$$T_i = \frac{c(l_i)(\mu(l_i) - \mu(p))}{S(l_i, p)} \quad (1)$$

where $c(l_i)$ is a correction factor for the positive bias suffered by the standardized mean difference with small sample sizes, which can be estimated by $c(l_i) = 1 - 3/(4(|l_i| - 1) - 1)$ (Hedges and Olkin, 1985). This adjustment will reduce the effect estimate of small leaves that only have a few pixels, and thus increase the robustness of the heterogeneity model (Huedo-Medina *et al.*, 2006). The pooled estimate of the within-group standard deviation $S(l_i, p)$ can be computed with (Hedges and Vevea, 1998):

$$S(l_i, p) = \sqrt{\frac{(|l_i| - 1)std^2(l_i) + (|p| - 1)std^2(p)}{|l_i| + |p| - 2}} \quad (2)$$

where $std^2(l_i)$ is the variance of leaf l_i , $std^2(p)$ is the variance of the averaged values of all leaves in plant p , and $|p|$ are the total number of pixels of leaf l_i and the whole plant p , respectively.

Then the Cochran's Q-test statistic for determining whether there is true leaf-based photosynthetic heterogeneity among the leaves is defined as:

$$Q = \sum_{i=1}^n w_i \left(T_i - \frac{\sum_{j=1}^n w_j T_j}{\sum_{j=1}^n w_j} \right)^2 \quad (3)$$

where n is the total number of leaves of the plant p , the right part of the equation is the weighted mean of effect estimates of all the leaves of the plant p , and $w_i = 1/(\tau^2 + \delta_i^2)$, where δ_i^2 is the sampling variance of the effect estimate T_i , and τ^2 is the between-study variance of all the effect estimates (Huedo-Medina *et al.*, 2006).

To estimate δ_i^2 , the sampling variance of each effect estimate T_i , we use the photosynthetic value of every pixel in the high-resolution fluorescence images, in which the total number of samples of a plant is much greater than 1000. According to (Huedo-Medina *et al.*, 2006), δ_i^2 is close to 0. Hence, by ignoring the computation of δ_i^2 and replacing it with 0, we have:

$$Q = \frac{1}{\tau^2} \sum_{i=1}^n \left(T_i - \frac{\sum_{j=1}^n T_j}{n} \right)^2 \quad (4)$$

Since both the between-study variance τ^2 and the Q statistic represent the true heterogeneity among the distributions of the leaf-level photosynthesis, we move τ^2 to the left of the equation and define a new measure called *PlantPH*:

$$PlantPH(f) = \sum_{i=1}^n \frac{(nT_i f(l_i) - \sum_{j=1}^n T_j f(l_j))^2}{n^3} \quad (5)$$

In Equation 5, *PlantPH*(f) is a measure for determining whether there is true heterogeneity among all leaves of a plant. It is independent to the total number of leaves, allowing for being comparable among different plants. We take plant leaf morphology into the plant heterogeneity test by defining $f(\cdot)$ as a function to measure the morphological properties (e.g., the area, position or growth rate) of a piece of leaf.

Specifically, in *PlantPH(area)* we have $f(l_i) = area(l_i)$, which measures the leaf surface area (Boyes *et al.*, 2001; Tessmer *et al.*, 2013), and in *PlantPH(growth)* we define $f(l_i) = growth_rate(l_i)$ by adopting a three-parameter nonlinear growth model to compute both the absolute growth rate (AGR) and the relative growth rate (RGR) (Richards, 1959; Hunt, 1982; Tessmer *et al.*, 2013). Moreover, in *PlantPH(position)*, we define $f(l_i) = position(l_i)$ to be 0 if l_i is at the center of the plant, and 1 otherwise, in order to measure whether the leaves with a similar developmental stage have heterogeneous photosynthetic values.

A P-value map was created in order to quickly assign a P-value to any plant based on only two parameters: the average intensity of fluorescence, and the range of fluorescence values. This map was developed according to the full set of arabidopsis data collected at the PLant REasearc Lab of MSU. First, the full set of plant images were divided into 100 bins (mean-bins) based on average intensity. Within each of these bins, the plants were divided into 100 bins (range-bins) based on the range of intensities within that mean-bin. Each of the resulting 10,000 bins corresponds to a p-value based on the range-bin so that p-values range from 0 to 1 within each mean-bin. This design takes full advantage of the large dataset in order to account for the tendency for high-intensity plants to have relatively large ranges. Plants with low p-values are considered "potentially heterogeneous" because they have a relatively large range for their average intensity. Applying computationally-intensive leaf segmentation to these plants is necessary to determine the meaning of their large ranges. In some cases they are still not considered heterogeneous, for example if the large range of intensity results from edge-of-leaf low intensity patterns.

3.2 PlantPH Workflow

As described in Section 2.1, it is impractical to directly call leaf alignment algorithms in PlantPH simply because of the high leaf overlap rate and computational efficiency. To meet the gap, we introduce an efficient workflow for leaf heterogeneity test (Fig. 2). First of all, an efficient statistical method is applied to screen the whole image dataset to identify all the candidate heterogeneous plant images. Second, on the candidate set, we apply a leaf alignment and tracking method and a spacial clustering method to identify leaves (Ester *et al.*, 1996; Kriegl *et al.*, 2011; Yin *et al.*, 2014b,a). In addition, a small region is added in the center of every plant image to represent the young leaves that are difficult to identify. Finally, we compute the leaf-based photosynthesis heterogeneity for every plant image using Eq. 5.

By manually browsing many plant images, we observe that i) heterogeneous plants are rare in the whole dataset, and ii) the distribution of all the photosynthesis values of a homogenous plant usually has a relatively narrower range than that of a heterogeneous plant. Therefore, we compute a p-value

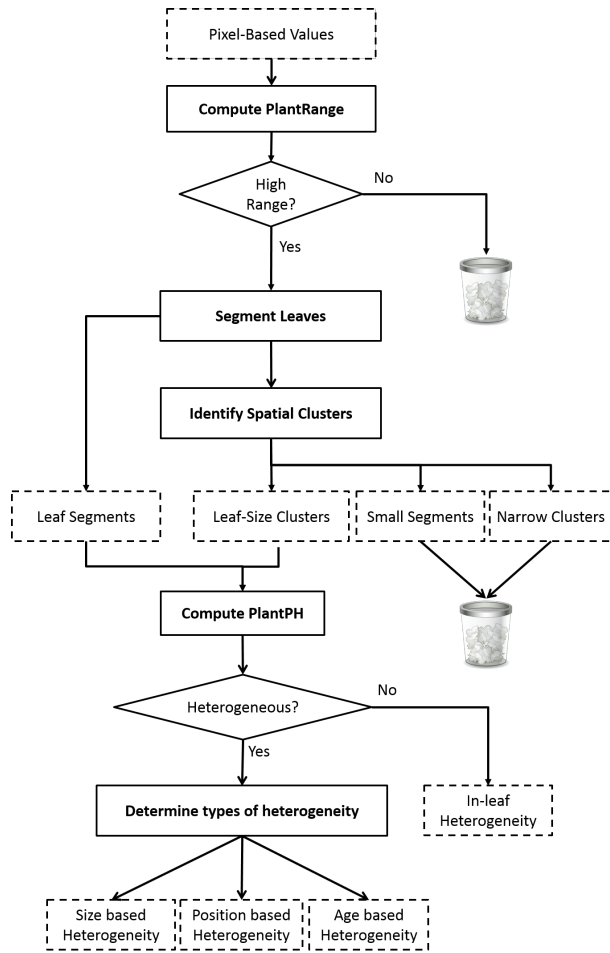


Fig. 3. Workflow of PlantPH, where the boxes with dashed lines are data and the boxes with solid lines are procedures.

for the range of photosynthetic values for every image:

$$p_value(PlantRange(p_{it})) = \quad (6)$$

where $PlantRange(p_{it})$ is defined as:

$$PlantRange(p_{it}) = \max(p_{it}) - \min(p_{it}) \quad (7)$$

where p_{it} is the image of plant i at time t , and functions \max and \min return the maximal and the minimum values of all the photosynthetic values of p_{it} after deleting top and bottom $k\%$ of the values (to exclude outliers).

We only select for the further process the plant images with relatively wide range of photosynthetic values using a p-value threshold. This process is efficient since it only needs the lowest and the highest values. Furthermore, it can remove about 85% of all the plant images, according to the results on the real data, allowing us to focus on a much smaller subset of all the images. Note that we use the range of values rather than standard deviation because the distribution of a heterogeneous plant consists of multiple distributions (Fig. 1).

Next, we process all the qualified plant images using a leaf alignment process introduced in Section 2.1. The outputs are identified leaves and the leftover images consisting of leaves that are partially covered by other leaves and leaf boundaries of the identified leaves (Fig. 4ab).

In the third step, in order to recognize the partially covered leaves, we employ a density based clustering algorithm called DBSCAN (Ester *et al.*, 1996; Kriegel *et al.*, 2011), which has been widely used for analysis of spatial information with physical constraints (Zaiane and Lee, 2002). Given all the non-segmented pixels, DBSCAN groups together pixels that are closely

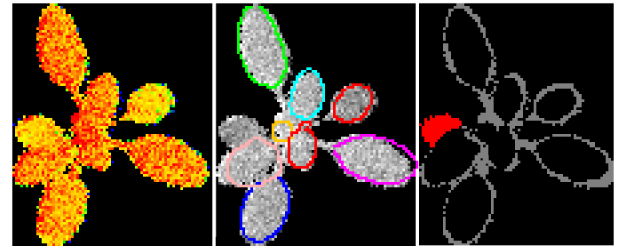


Fig. 4. An example of the PlantPH workflow, where (a) is a plant image, (b) is leaf alignment results, and (c) is spacial clustering results.

packed together into separated leaves, and discards leaf boundary pixels of the identified leaves with fine-tuning of the minimum thickness of the resulting clusters. Avoiding thin clusters is imperative to our application, since a leaf segmentation may result in a thin band of non-segmented pixels around the edge of a leaf. Considering these pixels as a separate leaf would not be appropriate – setting a minimum-thickness guarantees that any such pixels would not be clustered. Similarly, a leaf with very few pixels is statistically insignificant and often misleading even if the leaf is genuine. By setting a minimum number of pixels per cluster we discard very small clusters even if they meet the minimum thickness requirement (Fig. 4c).

In the fourth step, we apply *PlantPH* using all the leaves recognized by the leaf alignment method and all the clusters identified by the spatial clustering algorithm, resulting in heterogeneity matrix H .

Finally, we recognize the types of heterogeneity patterns in H with an outlier detection method, and visually explore them with the L'Abbe plot (Song, 1999).

4 RESULTS

We tested the performance of PlantPH on two datasets, i.e. a real dataset from a large-scale Arabidopsis phenotype screen experiment and a synthetic dataset that includes multiple types of heterogeneity patterns. We also compared PlantPH with two popular heterogeneity tests, where one is the traditional Cochran's Q-test and the I^2 statistic, and the other is a grid based heterogeneity test. Overall, the comparisons show that XXX.

4.1 Arabidopsis Experiment

4.1.1 Data Acquisition and Preprocessing In the photosynthesis phenotyping experiment, 567 Arabidopsis thaliana plants (wild types and genetic variations with single gene knockout) that include approximately 3,134 individual leaves, were grown side-by-side under three different light conditions (constant, sinusoid, fluctuate), for in total five days from 10 days old from seedling. Top-view fluorescence images were collected periodically (every 15 or 30 minutes) in order to observe the photosynthesis activity of all of the plants simultaneously. Each fluorescence image is a grey-scale image with a resolution of 1M pixels at 12-bit intensity. In total 31,120 fluorescence images were collected. Note that the averaged leaf cell size of Arabidopsis is about $6,000\mu m^2$ (Gegas *et al.*, 2014) and our image resolution is 3,600 pixels per squared inch. Therefore, each pixel in an image is sampled from about 1,000 leaf cells.

To accurately capture photosynthesis activities from the fluorescence images, data preprocessing step was employed to remove image background, identify plants in an image, and delete abnormalities (Xu *et al.*, 2015). From all of the processed images, biologists manually identified all the heterogenous plant images, which serve as the ground truth for performance test.

4.1.2 Performance Evaluation

4.2 PlantPH on synthetic data

4.2.1 Synthetic Data Generation A synthetic top-view fluorescence image was generated to test whether *PlantPH* is properly designed. The synthetic image contains a grid of synthetic plants, each with 9 circular leaves. Each synthetic plant is given a unique phenotype by gradually altering different factors along each dimension. Along the horizontal axis leaf-average fluorescence values are switched from low to high (one leaf at a time), and along the vertical axis in-leaf variation is gradually increased.

4.2.2 Performance Evaluation

5 DISCUSSION

A consensus view of the data is that the photosynthesis ability of a plant is not uniform across the whole area (Charles 2008, Meng 2007). The photosynthetic properties of plants can vary dramatically across cells, tissues, and organs (), reflecting differences in development, stress responses, regulation of processes such as stomatal conductance (), photodamage (), and storage of photosynthate () and contribute substantially to productivity ().

For example, we observed that the acclimation of photosynthesis in response to cold temperatures appears to be more rapid and robust in younger or emerging than older leaves, and ecotypes isolated from different latitudes show distinct heterogeneity patterns, implying that these responses are important for adaptation of photosynthesis to fluctuating temperatures. In other cases, exposure of plants to fluctuating light resulted in loss of photosynthetic capacity or increased photoinhibition in specific sets of leaves or leaf sectors. In many cases, older leaves are preferentially affected, suggesting that resources for maintenance or acclimation responses are preferentially directed to younger leaves. However, we have also identified mutant lines where younger leaves are preferentially affected, which presumably affect the development of photosynthetic robustness.

In order to systematically study the leaf level photosynthesis phenotypes, especially in a high-throughput screen manner, we developed a novel computational tool to automatically conduct statistical analysis on leaf based photosynthesis.

In the future, we will consider more plant-specific constraints including leaf shape similarity and symmetry.

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