# Assignment 1: ShiDong Xu 1006521890 Liang Chen 1005735126

## Part 1: Queries

- 1. Frugal doctors
  - a relation that lists all brand-name drug products' DIN and its price  $NamedDrugs(namedDIN, namedprice) := \Pi_{DIN,price}(Price \bowtie Product)$
  - a relation that lists all generic drug products' DIN, its price, and its corresponding brand-name drug DIN.

 $GenericDrugs(genericDIN, genericprice, parentDIN) := \Pi_{DIN,price,brand}(Price \bowtie Generic)$ 

- a relation that lists all brand-name drug DIN that has at least 1 generic product (Note: if only a brand-drug has a generic alternative, a doctor that prescribed the brand-name drug won't be selected whether or not this brand-name drug is more expensive that its generic alternatives )

$$ExpensiveNamed(DIN) := \Pi_{namedDIN} \bigg[ \sigma_{parentDIN=namedDIN}(NamedDrugs \times GenericDrugs) \bigg]$$

– a relation that lists all generic drugs' DINs that have at least 1 other alternative generic product with the same corresponding brand-named product that has a lower price.

ExpensiveGeneric(DIN) :=

$$\Pi_{G1.genericDIN} \begin{pmatrix} \sigma_{G1.genericDIN \neq G2.genericDIN} \\ \sigma_{G1.parentDIN = G2.parentDIN} \\ \sigma_{G1.genericprice} \end{pmatrix} (\rho_{G1}GenericDrugs) \times (\rho_{G2}GenericDrugs)$$

- a relation that contains DIN of all drugs that are NOT the cheapest option of its kind, which includes:
- a) brand-name drugs that have at least on generic alterative (no matter if the generic alternative is higher priced or not);
- b) generic drugs that have other generic alternatives of the same brand-name drug with lower price.

 $ExpensiveDrugs(DIN) := ExpensiveNamed \cup ExpensiveGeneric$ 

– a relation that contains doctors that have prescribed at least one drug that either prescribed a brand-name drug that has generic alternatives or some generic drugs that have lower-priced generic alternatives with the same brand-name (i.e. doctors that shouldn't be in the final answer).

$$RichDoctors(doctor) := \Pi_{doctor} \left[ \sigma_{drug=DIN}(ExpensiveDrugs \times Prescription) \right]$$

– a relation that contains doctors who have prescribed 2 or more drugs (since only doctors that have prescribed at least two different drugs want to be considered) TwoDrugDoctor(doctor) :=

$$\Pi_{D1.doctor} \left( \sigma_{D1.doctor = D2.doctor} \left[ (\rho_{D1} Prescription) \times (\rho_{D2} Prescription) \right] \right)$$

$$D1.drua \neq D2.drua$$

$$D1.drua \neq D2.drua$$

- a relation that contains only frugal doctors.

$$FrugalDoctor(doctor) := \Pi_{doctor}(TwoDrugDoctors - RichDoctors)$$

- 2. Price gougers
  - relation contains only the RxID of prescriptions of generic drugs  $GenericPre(RxID) := \Pi_{RxID} \left[ \sigma_{drug=DIN}(Generic \times Prescription) \right]$
  - find OCP of all pharmacists that filled at least 1 generic drug  $GenericPharm(OCP) := \Pi_{pharmacist}(GenericPre \bowtie Filled)$
  - find all pharmacists that have never filled a generic drug excluding ones that have never filled anything

$$NoGenericPharm(OCP) := \left[ \Pi_{OCP}(\rho_{F(RxID,date,OCP)}Filled) \right] - GenericPharm$$

- report OCP, name and date of registration  $PriceGougers(OCP, name, registered) := \Pi_{OCP, name, registered}(Pharmacist \bowtie NoGenericPharm)$
- 3. Potential doctor shopping
  - all prescriptions of brand-named drug products BrandPrescription(RxID, OHIP, DIN, doctor) :=

$$\Pi_{RxID,patient,DIN,doctor} \left[ \sigma_{DIN=drug}(Prescription \times Product) \right]$$

- all prescriptions of generic drug products
GenericPrescription(RxID, OHIP, DIN, doctor, brand) :=

$$\Pi_{RxID,patient,DIN,doctor,brand} \left[ \sigma_{DIN=drug}(Prescription \times Generic) \right]$$

- all patient who have been prescribed the same DIN by 2 different doctors

$$SameDIN(OHIP) := \Pi_{P1.patient} \left( \sigma_{P1.RxID \neq P2.RxID} \left[ (\rho_{P1}Prescription) \times (\rho_{P2}Prescription) \right] \right)$$

$$P1.drug \stackrel{\wedge}{=} P2.drug$$

$$P1.patient \stackrel{\wedge}{=} P2.patient$$

-all patient who have been prescribed 1 brand-named and 1 of its generic by 2 different doctors

BrandandGeneric(OHIP) :=

$$\Pi_{B.OHIP} \left( \sigma_{B.RxID \neq G.RxID} \left[ (\rho_B BrandPrescription) \times (\rho_G GenericPrescription) \right] \right)$$

$$B.DIN \neq G.DIN$$

$$B.DIN = G.OHIP$$

$$B.DIN = G.DIN$$

-all patient who have been prescribed 2 different generic products that have the same brand name equivalent

Generic and Generic (OHIP) :=

$$\Pi_{G1.OHIP} \left( \sigma_{G1.RxID \neq G2.RxID} \left[ (\rho_{G1}GenericPrescription) \times (\rho_{G2}GenericPrescription) \right] \right)$$

$$G1.DIN \neq G2.DIN$$

$$G1.OHIP = G2.OHIP$$

$$G1.brand = G2.brand$$

-Union all 3 different classes of patient for final result, and report all attributes by product with relation Patient

Potential Doctor Shopping(OHIP, name, phone) :=

$$\Pi_{OHIP,name,phone} \bigg[ (SameDIN \cup Brand and Generic \cup Generic and Generic) \bowtie Patient \bigg]$$

4. Safest ingredient

Cannot be expressed.

- 5. Drug shortage
  - A relation of all drugs and its manufacturer  $Drugs(DIN, manufacturer) := (\Pi_{DIN, manufacturer} Product) \cup (\Pi_{DIN, manufacturer} Generic)$
  - all unfilled prescriptions

$$unfilled Pre(\overline{RxID}, patient, DIN) :=$$

$$\left[ (\Pi_{RxID}Prescription) - (\Pi_{RxID}Filled) \right] \bowtie (\Pi_{RxID,patient,drug}Prescription)$$

– find all drug's DIN that has more than 2 unfilled prescriptions and at least 2 different patients

$$unfilledDrugs(DIN) :=$$

$$\Pi_{U1.DIN} \left( \sigma_{U1.patient \neq U2.patient} \left[ (\rho_{U1}unfilledPre) \times (\rho_{U2}unfilledPre) \times (\rho_{U3}unfilledPre) \right] \right) \\ U1.RxID \stackrel{\wedge}{\neq} U2.RxID \\ U3.RxID \stackrel{\wedge}{\neq} U2.RxID \\ U1.RxID \stackrel{\wedge}{\neq} U3.RxID \\ U1.DIN \stackrel{\wedge}{=} U2.DIN \\ U3.DIN \stackrel{\wedge}{=} U3.DIN \\ U3.D$$

- using the DIN, report DIN and manufacturer  $DrugShortage(DIN, manufacturer) := Drugs \bowtie unfilledDrugs$ 

- 6. Protecting drug patents
  - find all pairs of brand-named drugs, where the first drug DIN is strictly less than the second drug's DIN (i.e. no pseudo-duplicate pairs)

$$AllPairs(DIN1, name1, DIN2, name2) :=$$

$$\Pi_{P1.DIN,P1.name,P2.DIN,P2.name} \left( \sigma_{P1.DIN < P2.DIN} \left[ (\rho_{P1}Product) \times (\rho_{P2}Product) \right] \right)$$

– Intermediate table with every possible brand-named DIN paired with every possible active ingredient in brand-named drugs

$$Intermediate(DIN, name, ingredient) := (\Pi_{DIN, name} Product) \times (\Pi_{ingredient} Contains)$$

- find what each brand-named DIN lacks in ingredient, ie. every tuple indicates drug with DIN does NOT contain ingredient

$$NotContain(DIN, name, ingredient) := \\$$

$$Intermediate - \left[ (\Pi_{DIN,name}Product) \bowtie (\Pi_{DIN,ingredient}Contains) \right]$$

- new Contains table with names of the brand-names drugs

$$BrandContains(DIN, name, ingredient) := (\Pi_{DIN, name} Product) \bowtie (\Pi_{DIN, ingredient} Contains)$$

– find out all pairs of brand-named drugs that at least differs by 1 ingredient ,i.e. if a brand-name contains an ingredient that the other brand-name drug doesn't have, then this pair of brand-name drug is certainly no the pair of drugs with exactly the same ingredients

DifferentDrugs(DIN1, name1, DIN2, name2) :=

$$\Pi_{C.DIN,C.name,N.DIN,N.name} \left( \sigma \underset{C.ingredient=N.ingredient}{cc.oliv \neq N.DIN} \left[ (\rho_C BrandContains) \times (\rho_N NotContains) \right] \right)$$

- find out all pairs of brand-named drugs that have the exact same ingredient

ProtecDrugParent(DIN1, name1, DIN2, name2) := AllPairs - DifferentDrugs

- 7. Recent narcotics
  - find all brand-name narcotic

 $BrandNar(DIN, drugname) := \prod_{DIN.name} \sigma_{schedule='narcotic'} Product$ 

– find all generic narcotic

GenericNar(DIN, drugname) :=

$$ericNar(DIN, drugname) := \prod_{Generic.DIN, Generic.name} \left[ \sigma_{schedule='narcotic'} (Product \times Generic) \right]_{Product.DIN=Generic.brand}$$

- all narcotic drugs, including brand-name and generic

 $Nar(DIN, drugname) := BrandNar \cup GenericNar$ 

- all filled Prescription with DIN information included

FilledPre(RxID, fdate, OCP, DIN) :=

$$\Pi_{RxID,fdate,pharmacist,drug} \left[ (\rho_{F(RxID,fdate,pharmacist)}Filled) \bowtie Prescription \right]$$

- all filled prescription with a narcotic

FilledNar(RxID, fdate, OCP, DIN, drugname) :=

 $\Pi_{RxID,fdate,OCP,DIN,drugname}FilledPre \bowtie Nar$ 

- find the relation of all prescriptions with Narcotic that were not the most recent filled ones

EarlyNar(RxID, fdate, OCP, DIN, drugname) :=

$$\begin{array}{l} (yNar(RxID, fdate, OCP, DIN, drugname) := \\ \Pi & \begin{array}{l} E1.RxID \\ E1.fdate \\ E1.OCP \\ E1.DIN \\ E1.drugname \end{array} \begin{pmatrix} \sigma_{E1.RxID \neq E2.RxID} \left[ (\rho_{E1}FilledNar) \times (\rho_{E2}FilledNar) \right] \\ \left[ (\rho_{E1}FilledNar) \times$$

- find OCP, drugname, filled date information for the more recent filled narcotic prescription

PartialInfo(OCP, drugname, fdate) := $\Pi_{OCP,drugname,fdate}(FilledNar - EarlyNar)$ 

- find full pharmacists and drug information for the most recent filled narcotic prescrip-

RecentNarcotics(OCP, name, drugname, fdate) :=

 $\Pi_{OCP.name.drugname.fdate} PartialInfo \bowtie Pharmacist$ 

#### 8. Patients at risk

- find all instances where 2 or more drugs has been prescribed on the same day to the same patient by the same doctor

TwoDrug(DIN1, DIN2, doctor, date) :=

$$\Pi_{P1.drug,P2.drug,P1.doctor,P1.date} \begin{pmatrix} \sigma_{P1.drug \neq P2.drug} \\ \rho_{1.doctor} & \\ \rho_{2.doctor} \\ \rho_{2.doctor} \end{pmatrix} \left[ (\rho_{P1}Prescription) \times (\rho_{P2}Prescription) \right]$$

$$P1.patient = P2.patient$$

$$P1.date = P2.date$$

– get all interact-able ingredient for every brand named drug Interactable brand(DIN1, reactant) :=

$$\Pi_{DIN,ingredient2} \bigg[ Contains \bowtie (\rho_{I(ingredient,ingredient2)} Interaction) \bigg]$$

- get all interact-able ingredient for every generic drug Interactiable generic (DIN1, reactant) :=

$$\Pi_{DIN,ingredient2} \bigg[ Generic \bowtie (\rho_{C(brand,ingredient1,strength,unit)} Contains) \bowtie Interaction \bigg]$$

- get all interact-able ingredient for every drug, including generic and brand-named drugs

 $Interactable(DIN1, reactant) := Interactable brand \cup Interactiable generic$ 

- relation that contains all possible combination of drug1 DIN and its possible interactive ingredient

 $TwoDrug1(DIN1, reactant, DIN2, doctor, date) := Interactable \bowtie TwoDrug$ 

– relation that contain all active ingredient for both generic and brand-named drugs AllDrugs(DIN2, ingredient) :=

$$\left(\Pi_{DIN,ingredient}\left[Generic\bowtie(\rho_{(brand,ingredient,strength,unit)}Contains)\right]\right)\cup(\Pi_{DIN,ingredient}Contains)$$

- relation contains all the information from previous, and also the ingredient in drug2. TwoDrugFinal(DIN1, reactant, DIN2, ingredient2, doctor, date) :=

 $\Pi_{DIN1,reactant,DIN2,ingredient,doctor,date}(TwoDrug1 \bowtie AllDrugs)$ 

- report all by comparing reactant (from drug1) to ingredient (from drug 2)  $PatientAtRisk(doctor, date) := \Pi_{doctor, date} \sigma_{reactant=ingredient} TwoDrugFinal$
- 9. Many generics

Cannot be expressed.

### 10. Long-time customers

- find all OCP and name of all the most senior pharmacists. Seniors(sOCP) :=

$$\Pi_{OCP}Pharmacist - \Pi_{P1.OCP} \left( \sigma_{P1.OCP \neq P2.OCP} \left[ (\rho_{P1}Pharmacist) \times (\rho_{P2}Pharmacist) \right] \right)$$

- find all OCP and name of all the most junior pharmacists.

$$Juniors(jOCP) :=$$

$$\Pi_{OCP} P harmacist - \Pi_{P1.OCP} \left( \sigma_{P1.OCP \neq P2.OCP} \atop P1.registered \stackrel{\wedge}{<} P2.registered } \left[ (\rho_{P1} P harmacist) \times (\rho_{P2} P harmacist) \right] \right)$$

– find intermediate table that contains date of filled prescription, OHIP, patient name, and pharmacist's OCP.

Intermediate(date, OHIP, name, OCP) :=

$$\Pi_{date,patient,name,OCP} \bigg[ (\rho_{P(RxID,pdate,patient,drug,doctor,dosage,note)} Prescription) \bowtie Filled \bowtie Patient) \bigg]$$

$$(\rho_{Pat(patient,name,dob,phone,address)}Patient)$$

– find relation that contains all the dates where a patient had a prescription filled by a senior.

$$SeniorFilled(OHIP, name, sdate) := \Pi_{OHIP, name, date} \bigg[ \sigma_{sOCP = OCP}(Intermediate \times Seniors) \bigg]$$

- find relation that contains all the dates where a patient had a prescription filled by a junior.

$$JuniorFilled(OHIP, name, jdate) := \Pi_{OHIP, name, date} \bigg[ \sigma_{jOCP = OCP}(Intermediate \times Juniors) \bigg]$$

– find relation that only contains the earliest date where a patient had a prescription filled by a senior.

EarliestSenior(OHIP, name, sdate) :=

$$SeniorFilled$$
  $-$ 

$$\Pi_{P1.OHIP,P1.name,P1.sdate} \left[ \sigma_{P1.sdate > P2.sdate} \left[ (\rho_{P1}SeniorFilled) \times (\rho_{P2}SeniorFilled) \right] \right]$$

– find relation that only contains the earliest date where a patient had a prescription filled by a junior.

Earliest Junior(OHIP, name, jdate) :=

$$Junior Filled$$
  $-$ 

$$\Pi_{P1.OHIP,P1.name,P1.jdate} \left[ \sigma_{P1.jdate > P2.jdate} \left[ (\rho_{P1}JuniorFilled) \times (\rho_{P2}JuniorFilled) \right] \right]$$

- report all information.  $LongTimeCustomer(OHIP, name, jdate, sdate) := \Pi_{OHIP,name, jdate, sdate}(EarliestSenior \bowtie EarliestJunior)$ 

### 11. Lots of competition

- find all manufacturers who make at least 1 brand-name drugs.  $BrandManu(manufacturer, bDIN) := \Pi_{manufacturer, DIN} Product$
- make an intermediate table that describes for every brand-name drug every manufacturer makes, it also makes an equivalent generic drug. Intermediate(manufacturer, bDIN, gmanu) :=

$$\Pi_{B1.manufacturer.B1.bDIN,B2.manufacturer} \left( \sigma_{B1.manufacturer=B2.manufacturer} [(\rho_{B1}BrandManu) \times (\rho_{B1}BrandManu)] \right)$$

 $(\rho_{B2}BrandManu)]$ 

- relation that list all the brand-name product, its manufacturer, and all the manufacturer that makes the generic form of the brand-name product BrandAndGeneric(manufacture, bDIN, gmanu) :=

$$\Pi_{manufacturer,bDIN,gmanu} \bigg[ BrandManu \bowtie \rho_{G(DIN,bDIN,name,gmanu)} Generic \bigg]$$

- find all manufacturer that did NOT make a generic product for each of its brand-named product.

 $BadManu(manufacturer, bDIN) := \Pi_{manufacturer, bDIN}(Intermediate-BrandAndGeneric)$ 

- all manufacturer that make a generic product for every of its brand-named product, in other words, satisfy the first 2 rule in the question GoodBrandManu(manufacturer, bDIN) := BrandManu BadManu
- all manufacturer and its brand-named product that satisfy rule 1 and 2, and at least 1 different manufacturer makes a generic product of the brand-named drug BrandAndDiffGeneric(manufacture, bDIN) :=

$$\Pi_{manufacturer,bDIN} \left( \sigma_{manufacturer \neq bmanu} \left[ GoodBrandManu \bowtie (\rho_{G(DIN,bDIN,name,bmanu})Generic) \right] \right)$$

- isolate out the manufacturers that at least one of its brand-named product does not have a different manufacturer that makes a generic equivalent.
- $Monopolies(manufacturer) := \Pi_{manufacturer}(GoodBrandManu-BrandAndDiffGeneric)$

- Finally find all manufactures that satisfy all 3 rules in the question  $LotsCompetition(manufacturer) := (\Pi_{manufacturer}GoodBrandManu) - Monopolies$ 

### Part 2: Additional Integrity Constraints

1. Symmetry

 $Interaction - Interaction \bowtie (\rho_{I(ingredient2,ingredient1)} Interaction) = \emptyset$ 

- 2. Don't surpass those with seniority Cannot be expressed.
- 3. Brand-name first
  - find all prescriptions of brand-named drugs BrandPre(bRxID, bdate, bDIN, bdoctor) :=

$$\Pi_{RxID,date,drug,doctor} \left( Prescription \bowtie \left[ \Pi_{drug} \left( \rho_{P(drug,name,manufacturer,form,schedule,route)} Product \right) \right] \right)$$

– find all prescriptions of generic drugs

GenericPre(gRxID, gdate, gDIN, parentDIN, gdoctor) :=

$$\Pi_{RxID,date,drug,brand,doctor} \left( Prescription \bowtie \left[ \Pi_{drug,brand} \left( \rho_{G(drug,brand,name,manufacturer)} Generic \right) \right] \right)$$

– of all the prescriptions of generic drugs, only have the earliest prescription of generic drugs that have the same brand-name equivalent by the same doctor. If brand-named drug A has 2 generic drug B and C, and doctor X prescribed B before C, then table will only have Prescription for B for doctor X.

Earliest Generic With Same Brand (gRxID, gdate, gDIN, parent DIN, gdoctor) :=

$$GenericPre - \begin{bmatrix} \Pi & _{G1.gRxID}, & \sigma & _{G1.gdate} > _{G2.gdate} & (\rho_{G1}GenericPre \times \rho_{G2}GenericPre) ) \end{bmatrix} \\ G_{1.gdate} & \underset{G1.gDIN, \\ G1.parentDIN, \\ G1.gdoctor} \land \underset{G1.parentDIN}{\land} \\ G1.parentDIN = G2.parentDIN \end{bmatrix}$$

– find all earliest prescription of each brand-named drug by the same doctor. If doctor A prescribed the same brand-named drug multiple times, only the first time will be recorded, if doctor A prescribed several brand-name drugs, each drug's earliest prescription will be recorded, if doctor A only prescribed a brand-name drug once, this record will be stored

EarliestBrandPre(bRxID, bdate, bDIN, bdoctor) :=

$$BrandPre - \begin{bmatrix} \Pi_{B1.RxID,} \left( \sigma_{B1.bdoctor = B2.bdoctor} (\rho_{B1}BrandPre \times \rho_{B2}BrandPre) \right) \end{bmatrix} \\ B1.bdate, \\ B1.bDIN, \\ B1.bdoctor \\ B1.bdate > B2.bdate \end{bmatrix}$$

– find all the times when the same doctor prescribed a brand-named drug after prescribing an equivalent generic drug.

GenericFirst(DIN, gdoctor) :=

$$\Pi_{gDIN,gdoctor} \begin{bmatrix} \sigma_{gdoctor=bdoctor} & (EarliestBrandPre \times EarliestGenericWithSameBrand) \\ gdate \leq bdate \\ bDIN=parentDIN \end{bmatrix}$$

– find all the times when the same doctor prescribed a generic drug but never prescribed its equivalent brand-named drug

$$OnlyGeneric(DIN,gdoctor) := (\Pi_{parentDIN,gdoctor}EarliestGenericWithSameBrand) - \left[\Pi_{parentDIN,gdoctor}\left(\rho_{E(bRxID,bdate,parentDIN,gdoctor})EarliestBrandPre\right)\right]$$

- Integrity Constraint  $GenericFirst \cup OnlyGeneric = \emptyset$
- 4. Don't over-prescribe narcotics
  - Find all detailed prescriptions of brand-named narcotics. DetailedPre(drug, RxID, date, patient, doctor) :=

$$\prod_{\substack{drug, \\ RxID, \\ date, \\ patient, \\ doctor}} \left[ \sigma_{schedule='narcotic'} \left( Prescription \bowtie \left( \rho_{(drug,name,manufacturer,form,schedule,route)} Product \right) \right) \right]$$

- Integrity Constraint

$$\sigma \underset{D1.date=D2.date}{\underset{D1.date=D2.date}{\wedge}} \left[ (\rho_{D1}DetailedPre) \times (\rho_{D2}DetailedPre) \right] = \emptyset$$

$$\underset{D1.doctor=D2.doctor}{\overset{\wedge}{\longrightarrow}} D1.patient \underset{D1.RxID}{\overset{\wedge}{\longrightarrow}} D2.patient$$

$$D1.RxID \neq D2.RxID$$