

Source This example is from (2.9.16) of [KS04]:

$$H_{p,q+1}^{1,p} \left(\begin{matrix} (1-a_i, 1)_{1,p} \\ (0, 1), (1-b_j, 1)_{1,q} \end{matrix} \right) = \frac{\prod_{i=1}^p \Gamma(a_i)}{\prod_{j=1}^q \Gamma(b_j)} {}_pF_q(a_1, \dots, a_p; b_1, \dots, b_q; -z)$$

Notes: ${}_pF_q$ is the generalized hypergeometric series (see [Erd+81] chapter 4).

$${}_pF_q(a_1, \dots, a_p; b_1, \dots, b_q; z) = \sum_{n=0}^{\infty} \frac{(a_1)_n \cdots (a_p)_n}{(b_1)_n \cdots (b_q)_n} \frac{z^n}{n!},$$

where $(a)_n$ denotes the Pochhammer symbol, which represents the rising factorial $\frac{\Gamma(a+n-1)}{\Gamma(a)} = a(a+1)(a+2)\cdots(a+n-1)$ for $n > 0$, and $(a)_0 = 1$.

References

- [Erd+81] Arthur Erdélyi, Wilhelm Magnus, Fritz Oberhettinger, and Francesco G. Tricomi. *Higher transcendental functions. Vol. I*. Based on notes left by Harry Bateman, Reprint of the 1953 original. Robert E. Krieger Publishing Co., Inc., Melbourne, Fla., 1981, pp. xviii+396. ISBN: 0-89874-069-X.
- [KS04] Anatoly A. Kilbas and Megumi Saigo. *H-transforms*. Vol. 9. Analytical Methods and Special Functions. Theory and applications. Chapman & Hall/CRC, Boca Raton, FL, 2004, pp. xii+389. ISBN: 0-415-29916-0. DOI: 10.1201/9780203487372. URL: <https://doi.org/10.1201/9780203487372>.