Financial Mathematics

MATH 5870/6870¹ Fall 2021

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¹Based on Robert L. McDonald's *Derivatives Markets*. 3rd Ed. Pearson. 2013.

Chapter 2. An Introduction to Forwards and Options

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- § 2.1 Forward contracts
- § 2.2 Call options
- § 2.3 Put options
- § 2.4 Summary of forward and option positions
- § 2.5 Problems

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Six positions

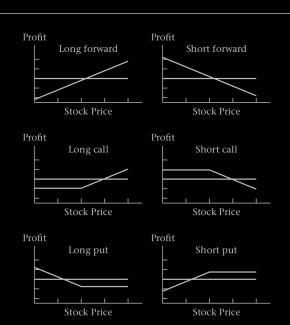
 $\{long, short\} \times \{forward, call, put\}$

$\begin{aligned} \text{Maximum possible profit and loss at maturity for} \\ & \{ \text{long, short} \} \times \{ \text{forward, call, put} \} \end{aligned}$

Position	Maximum Loss	Maximum Gain	
Long forward	Forward price	Unlimited	
Short forward	Unlimited	Forward price	
Long call	-FV(premium)	Unlimited	
Short call	Unlimited	FV(premium)	
Long put	-FV(premium)	Strike price — FV(premium)	
Short put	FV(premium) — Strike price	FV(premium)	

 $^{^{5}}FV(\cdot)$ denotes the function that returns the future value.

$\begin{aligned} & \text{Profit diagrams for} \\ & \{\text{long, short}\} \times \{\text{forward, call, put}\} \end{aligned}$



$\begin{aligned} & Summary \ of \ positions \ for \\ & \{long, short\} \times \{forward, call, put\} \end{aligned}$

Derivative	Position with Respect	Asset Price	
Position	to Underlying Asset	Contingency	Strategy
Long forward	Long (buy)	Always	Guaranteed purchase price
Short forward	Short (sell)	Always	Guaranteed sale price
Long call	Long (buy)	> Strike	Insures against high price
Short call	Short (sell)	> Strike	Sells insurance against high price
Long put	Short (sell)	< Strike	Insures against low price
Short put	Long (buy)	< Strike	Sells insurance against low price