Financial Mathematics

MATH 5870/6870¹ Fall 2021

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¹Based on Robert L. McDonald's *Derivatives Markets*. 3rd Ed. Pearson. 2013.

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Definition 18.1-1 A random variable X is said to have the *normal distribution* (or *normally distributed*) with mean μ and variance σ^2 , if the probability density function (pdf) is given by

$$f_X(x) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2}.$$

We write

$$X \sim N(\mu, \sigma^2).$$

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