

Financial Mathematics

MATH 5870/6870¹
Fall 2021

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¹Based on Robert L. McDonald's *Derivatives Markets*, 3rd Ed, Pearson, 2013.

Chapter 3. Insurance, Collars, and Other Strategies

Chapter 3. Insurance, Collars, and Other Strategies

§ 3.1 Basic insurance strategies

§ 3.2 Put-call parity

§ 3.3 Spreads and collars

§ 3.4 Speculating on volatility

§ 3.5 Problems

Chapter 3. Insurance, Collars, and Other Strategies

§ 3.1 Basic insurance strategies

§ 3.2 Put-call parity

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§ 3.4 Speculating on volatility

§ 3.5 Problems

Options can be

1. Used to insure long positions (floors)
2. Used to insure short positions (caps)
3. Written against asset positions (selling insurance)

Covered call writing

Covered put writing

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Four positions

positions w.r.t. asset	put option	call option
long	purchased (<i>floor</i>)	written
short	written	purchased (<i>cap</i>)

Buying insurance

floor = buying a *put* option

cap = buying a *call* option

Selling insurance

Covered *put* writing

Covered *call* writing

We will work under the following setup

S&S index

index price today	\$1,000
6-month interest rate	2%
premium for 1000-strike 6-month call	\$93.809
premium for 1000-strike 6-month put	\$74.201

Insuring a long position

– Floors

owning a home	owning a stock index
insuring the house	buying a put (floor)

Goal: to insure against a fall in the price of the underlying asset.

Example 3.1-1 Under the following scenario, compute the combined profit of insuring a long position via **buying a put** for the following S&R index.

index price today	\$1,000
6-month interest rate	2%
premium for 1000-strike 6-month put	\$74.201
index price at expiration	\$900

Solution.

$$\underbrace{\$900 - \$1,000 \times 1.02}_{\text{profit on S\&R index}} + \underbrace{\$1,000 - \$900 - \$74.201 \times 1.02}_{\text{profit on put}} = -\$95.68.$$



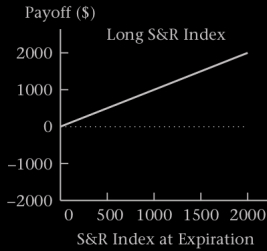
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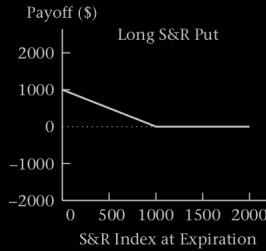
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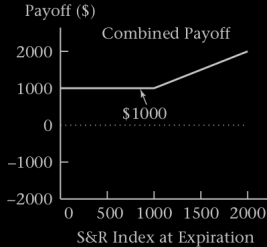




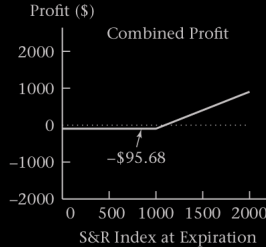
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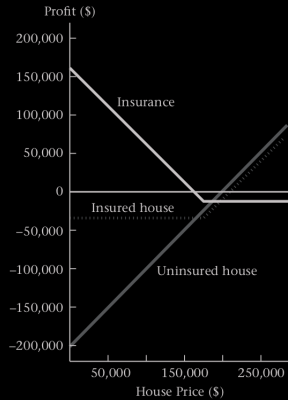
(b)



(c)



(d)



Insuring a short position

– Caps

If we have a short position in the S&R index, we experience a loss when the index rises.

We can insure a short position by purchasing a call option (cap) to protect against a higher price of repurchasing the index.

Example 3.1-2 Under the following scenario, compute the combined profit for insuring a short position via **buying a call** of the following S&R index.

index price today	\$1,000
6-month interest rate	2%
premium for 1000-strike 6-month call	\$93.809
index price at expiration	\$1,100

Solution.

$$\underbrace{\$1,000 \times 1.02}_{\text{future value of short S\&R index}} - \underbrace{\$93.809 \times 1.02}_{\text{FV of premium for call}} - \underbrace{\$1,000}_{\text{exercise the call option}} = -\$75.685.$$



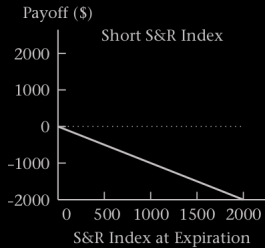
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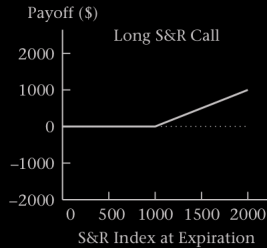
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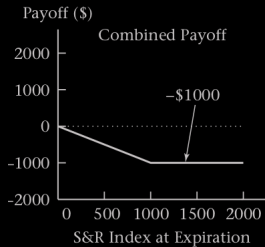




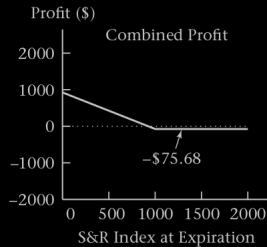
(a)



(b)



(c)



(d)

Selling insurance

For every insurance buyer there must be an insurance seller

Strategies used to sell insurance

- ▶ Covered writing (option overwriting or selling a covered call) is writing an option when there is a corresponding long position in the underlying asset.
- ▶ Naked writing is writing an option when the writer does not have a position in the asset.

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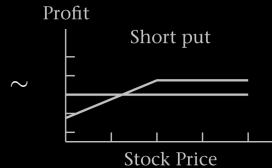
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Covered call writing

Long position of the asset + Sell a **call** option



Covered put writing

Short position of the asset + Sell a **put** option



Covered call writing

Example 3.1-3 Under the following scenario, compute the combined profit for writing a **covered call** for S&R index.

index price today	\$1,000
6-month interest rate	2%
premium for 1000-strike 6-month call	\$93.809
index price at expiration	\$1,100

Solution.

$$\underbrace{\$1,100 - \$1,000 \times 1.02}_{\text{profit on S\&R index}} + \underbrace{\$1,000 - \$1,100 + \$93.809 \times 1.02}_{\text{profit on written call}} = \$75.68.$$



Covered call writing

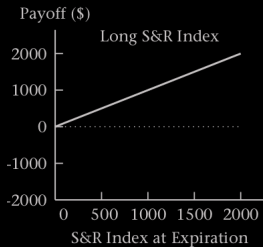
Example 3.1-3 Under the following scenario, compute the combined profit for writing a **covered call** for S&R index.

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index price at expiration	\$1,100

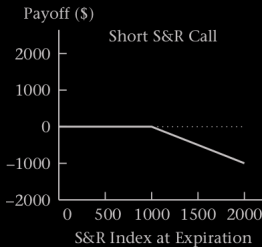
Solution.

$$\underbrace{\$1,100 - \$1,000 \times 1.02}_{\text{profit on S\&R index}} + \underbrace{\$1,000 - \$1,100 + \$93.809 \times 1.02}_{\text{profit on written call}} = \$75.68.$$

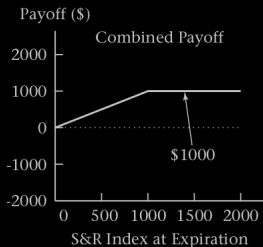




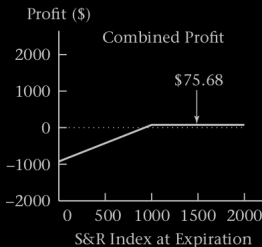
(a)



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Covered put writing

Example 3.1-4 Under the following scenario, compute the combined profit for writing a covered put for S&R index.

index price today	\$1,000
6-month interest rate	2%
premium for 1000-strike 6-month put	\$74.201
index price at expiration	\$900

Solution.

$$\underbrace{\$1,000 \times 1.02 - \$900}_{\text{profit on selling S\&R index}} + \underbrace{+\$900 - \$1,000 + \$74.201 \times 1.02}_{\text{profit on written put}} = \$95.685.$$



Covered put writing

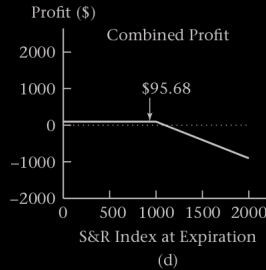
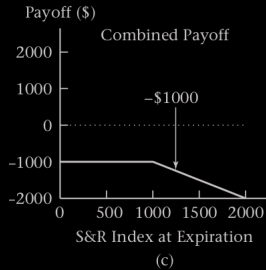
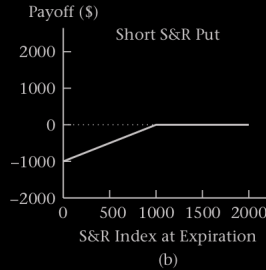
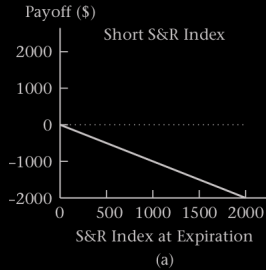
Example 3.1-4 Under the following scenario, compute the combined profit for writing a covered put for S&R index.

index price today	\$1,000
6-month interest rate	2%
premium for 1000-strike 6-month put	\$74.201
index price at expiration	\$900

Solution.

$$\underbrace{\$1,000 \times 1.02 - \$900}_{\text{profit on selling S\&R index}} + \underbrace{+\$900 - \$1,000 + \$74.201 \times 1.02}_{\text{profit on written put}} = \$95.685.$$





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It is possible to mimic a long forward position on an asset by
buying a call + selling a put,
with each option having the same strike price and expiration time.

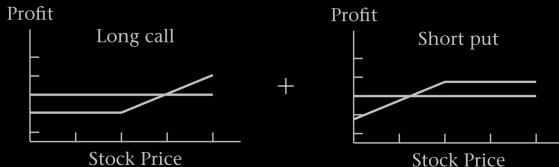
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A synthetic forward

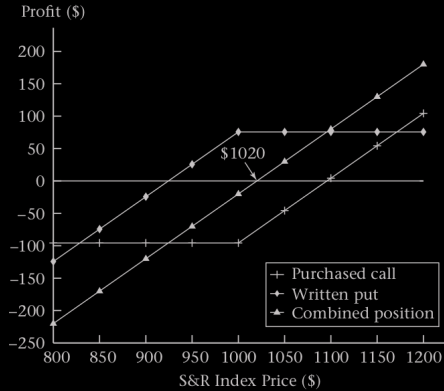
Example 3.2-1 Working with the S&R index. Suppose that

6-month interest rate	2%
premium for 1000-strike 6-month call	\$93.809
premium for 1000-strike 6-month put	\$74.201

Draw profit diagram for the combined position of a purchased call with a written put, namely,



Solution.



A synthetic long forward contract

We pay the net option premium

We pay the strike price

The actual forward

We pay zero premium

We pay the forward price

Basic Assumption

The net cost of buying the index using options
must equal
the net cost of buying the index using a forward contract.

NO ARBITRAGE!

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The Put-Call parity equation

$$\text{Call}(K, T) - \text{Put}(K, T) = \text{PV}(F_{0,T} - K)$$

- ▶ K : strike price
- ▶ T : expiration date
- ▶ $\text{Call}(K, T)$: the premium for call
- ▶ $\text{Put}(K, T)$: the premium for put
- ▶ $F_{0,T}$: the forward price at time T if one enters at time 0 into a long forward position
- ▶ $\text{PV}(\cdot)$: the present value function

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Example 3.2-2 Check Example 3.2-1 to see if the put-call parity equation is satisfied.

Solution. We need to check:

$$\$93.809 - \$74.201 \stackrel{?}{=} PV(\$1,000 \times 1.02 - \$1,000)$$

Clearly, LHS = \$19.61. On the other hand, the RHS is equal to

$$\begin{aligned} PV(\$1,000 \times 1.02 - \$1,000) &= PV(1,000 \times (1.02 - 1)) \\ &= PV(1,000 \times 0.02) \\ &= \frac{1,000 \times 0.02}{1.02} \\ &= \$19.61. \end{aligned}$$

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Hence, the put-call parity equation is satisfied. □

$$\text{Call}(K, T) - \text{Put}(K, T) = \text{PV}(F_{0,T} - K)$$



$$\text{PV}(F_{0,T}) + \text{Put}(K, T) = \text{Call}(K, T) + \text{PV}(K)$$

Buying the index and buying the put

generate the same payoff as

buying the call and buying a zero-coupon bond (i.e. lending) $\text{PV}(K)$

$$\text{Call}(K, T) - \text{Put}(K, T) = \text{PV}(F_{0,T} - K)$$



$$\text{PV}(F_{0,T}) - \text{Call}(K, T) = \text{PV}(K) - \text{Put}(K, T)$$

Writing a covered call

has the same profit as

lending $\text{PV}(K)$ and selling a put

$$\text{Call}(K, T) - \text{Put}(K, T) = \text{PV}(F_{0,T}) - \text{PV}(K)$$

Revisit four positions in Section 3.1

Position	Meaning	equivalent to
Inuring a long position (floors)		
Inuring a short position (caps)		
Covered call writing		
Covered put writing		

$$\text{Call}(K, T) - \text{Put}(K, T) = \text{PV}(F_{0,T}) - \text{PV}(K)$$

Revisit four positions in Section 3.1

Position	Meaning	equivalent to
Inuring a long position (floors)	Index + Put	
Inuring a short position (caps)		
Covered call writing		
Covered put writing		

$$\text{Call}(K, T) - \text{Put}(K, T) = \text{PV}(F_{0,T}) - \text{PV}(K)$$

Revisit four positions in Section 3.1

Position	Meaning	equivalent to
Inuring a long position (floors)	Index + Put	Bound + Call
Inuring a short position (caps)		
Covered call writing		
Covered put writing		

$$\text{Call}(K, T) - \text{Put}(K, T) = \text{PV}(F_{0,T}) - \text{PV}(K)$$

Revisit four positions in Section 3.1

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Inuring a long position (floors)	$\text{Index} + \text{Put}$	$\text{Bound} + \text{Call}$
Inuring a short position (caps)	$-\text{Index} + \text{Call}$	
Covered call writing		
Covered put writing		

$$\text{Call}(K, T) - \text{Put}(K, T) = \text{PV}(F_{0,T}) - \text{PV}(K)$$

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Revisit four positions in Section 3.1

Position	Meaning	equivalent to
Inuring a long position (floors)	Index + Put	Bound + Call
Inuring a short position (caps)	-Index + Call	-Bound + Put
Covered call writing	Index - Call	
Covered put writing		

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Revisit four positions in Section 3.1

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Inuring a long position (floors)	Index + Put	Bound + Call
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Covered call writing	Index - Call	Bound - Put
Covered put writing		

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Revisit four positions in Section 3.1

Position	Meaning	equivalent to
Inuring a long position (floors)	Index + Put	Bound + Call
Inuring a short position (caps)	-Index + Call	-Bound + Put
Covered call writing	Index - Call	Bound - Put
Covered put writing	-Index - Put	

$$\text{Call}(K, T) - \text{Put}(K, T) = \text{PV}(F_{0,T}) - \text{PV}(K)$$

Revisit four positions in Section 3.1

Position	Meaning	equivalent to
Inuring a long position (floors)	$\text{Index} + \text{Put}$	$\text{Bound} + \text{Call}$
Inuring a short position (caps)	$-\text{Index} + \text{Call}$	$-\text{Bound} + \text{Put}$
Covered call writing	$\text{Index} - \text{Call}$	$\text{Bound} - \text{Put}$
Covered put writing	$-\text{Index} - \text{Put}$	$-\text{Bound} - \text{Call}$

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§ 3.1 Basic insurance strategies

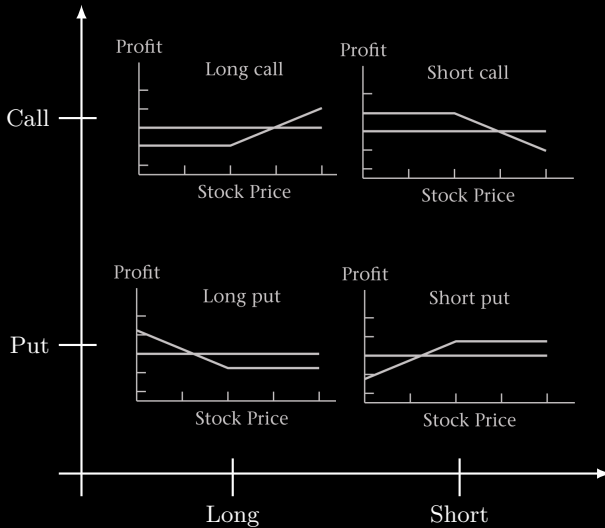
§ 3.2 Put-call parity

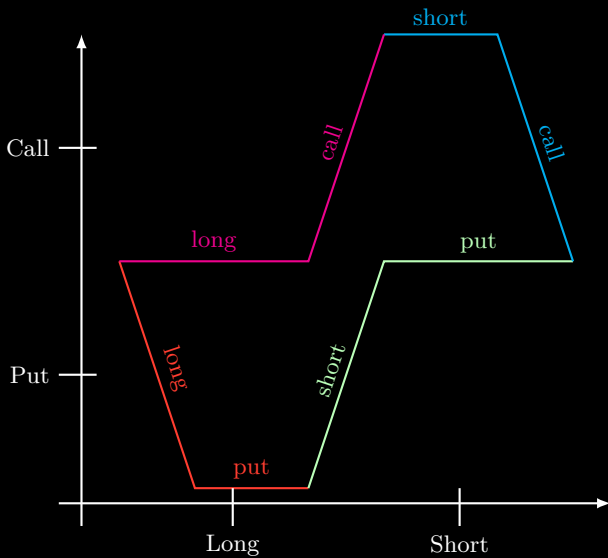
§ 3.3 Spreads and collars

§ 3.4 Speculating on volatility

§ 3.5 Problems

By combining two or more options, we find many well-known strategies.





An **option spread** is a position consisting of only calls or only puts, in which some options are purchased and some written.

- ▶ Bull and bear spreads

- ▶ Box spreads

- ▶ Ratio spreads

- ▶ Collars

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Example for this section

Black-Scholes option prices

Stock price = \$40

Volatility = 30%

Effective annual risk-free rate = 8.33%

Dividend yield = \$0

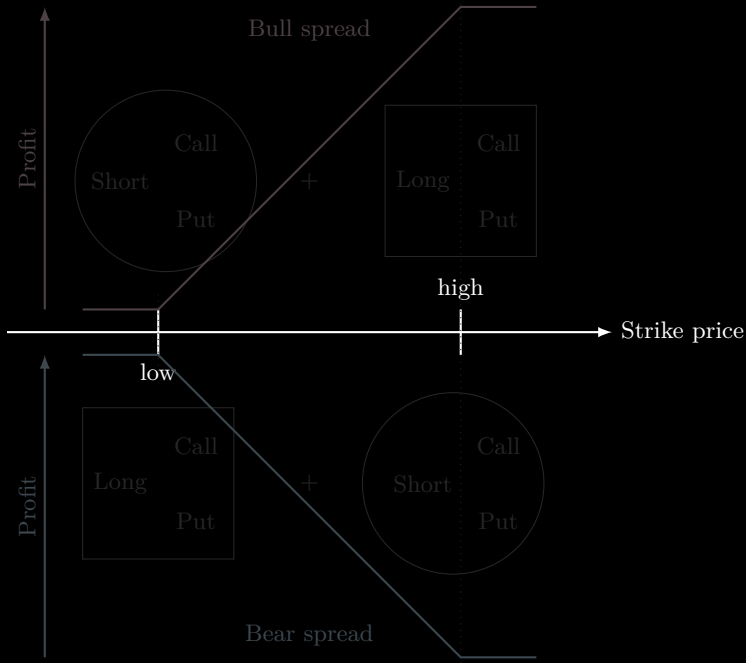
Expiration days = 91 days

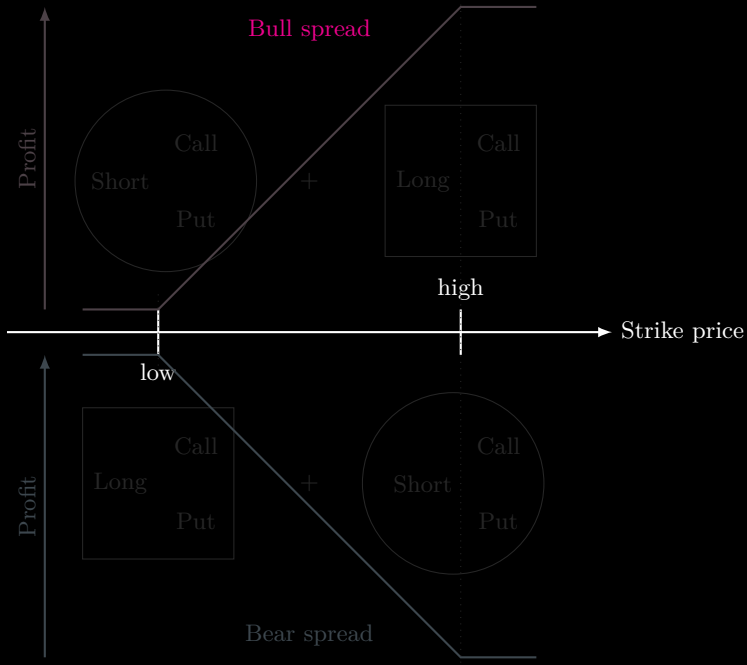
Strike	Call	Put
35	6.13	0.44
40	2.78	1.99
45	0.97	5.08

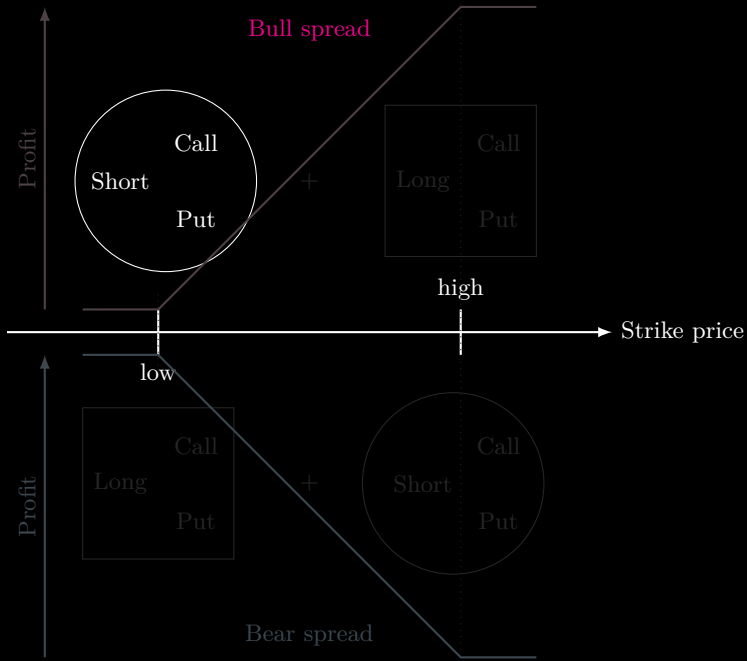
Bull and bear spreads

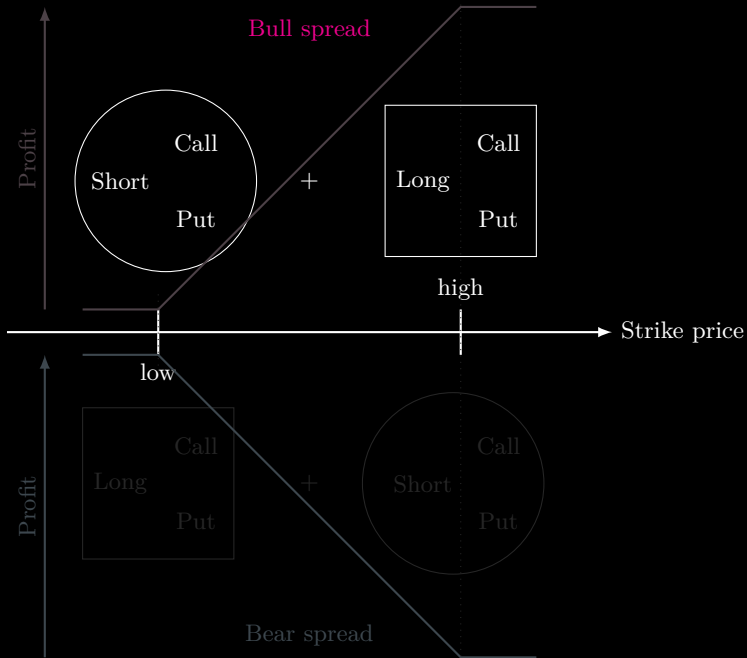
A position in which you buy a call and sell an otherwise identical call with a higher strike price is an example of a **bull spread**. Bull spreads can also be constructed using puts.

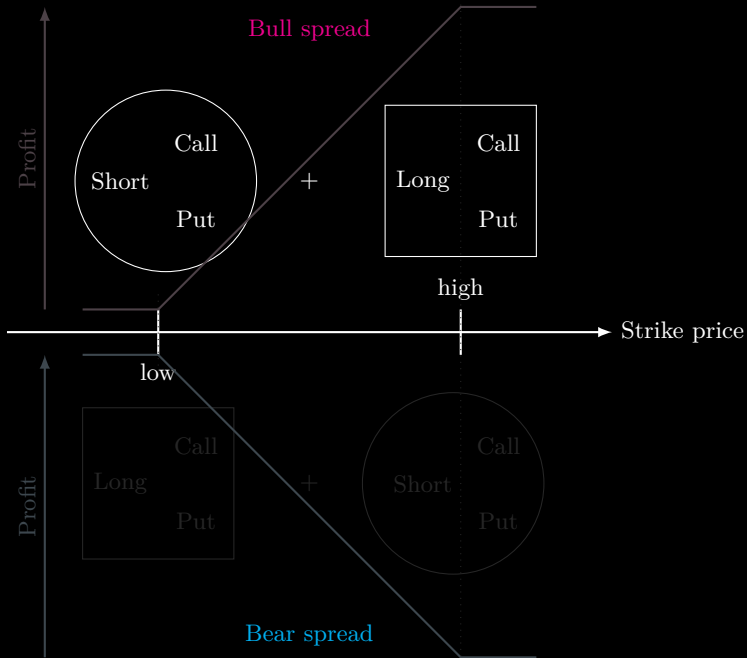
The opposite of a bull spread is a **bear spread**.

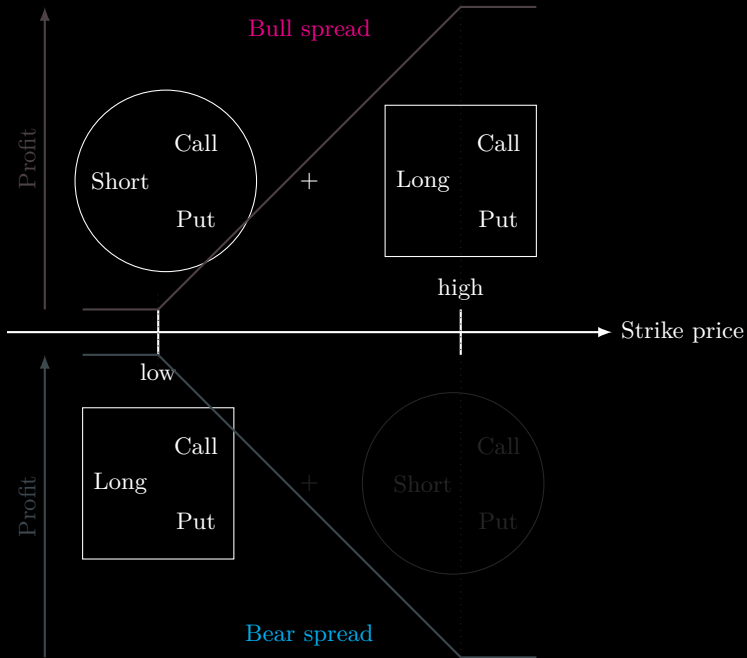


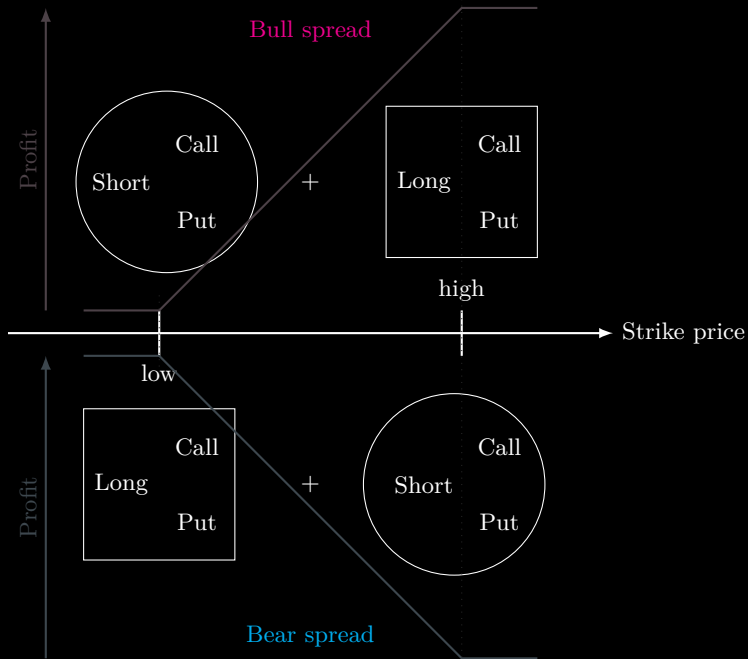


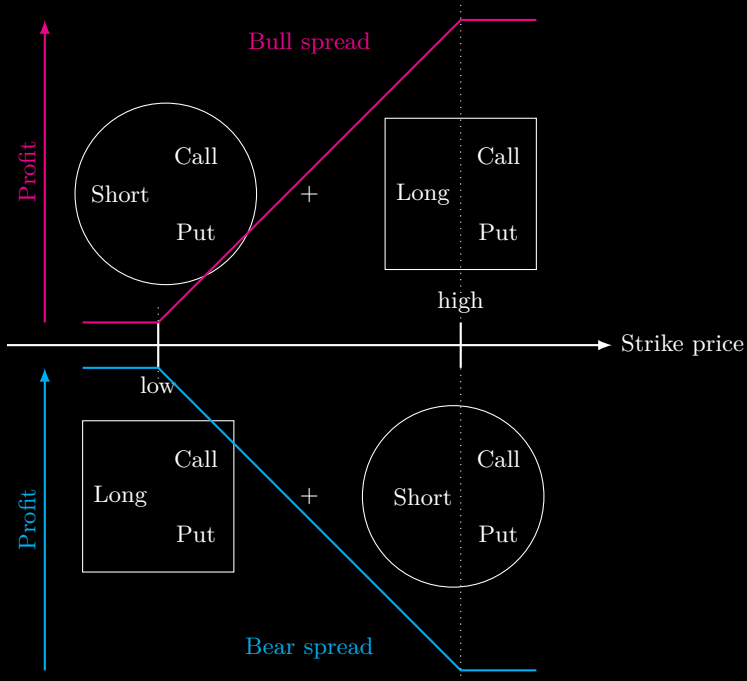












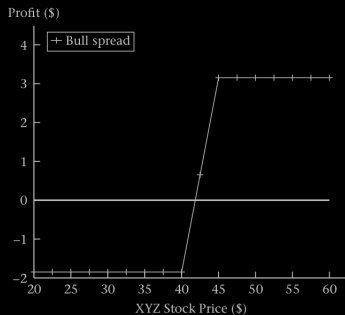
Example 3.3-1 Draw profit diagram for a 40-45 bull spread, namely, buying a 40-strike call and selling a 45-strike call.

Solution.



Example 3.3-1 Draw profit diagram for a 40-45 bull spread, namely, buying a 40-strike call and selling a 45-strike call.

Solution.



Box spreads

A **box spread** is accomplished by using options to create a **synthetic long forward** at one price and a **synthetic short forward** at a different price.

This strategy guarantees a cash flow in the future.

Hence, it is an option spread that is purely a means of borrowing or lending money. It is costly but has no stock price risk.

Example 3.3-2 Suppose we simultaneously enter into the following two transactions:

1. Buy a 40-strike call and sell a 40-strike put.
2. Sell a 45-strike call and buy a 45-strike put.

Explain why there is no free lunch. Draw the profit diagram.

Solution. Check book 74.



Example 3.3-2 Suppose we simultaneously enter into the following two transactions:

1. Buy a 40-strike call and sell a 40-strike put.
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Explain why there is no free lunch. Draw the profit diagram.

Solution. Check book 74.



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Solution. Check book 74.



Example 3.3-2 Suppose we simultaneously enter into the following two transactions:

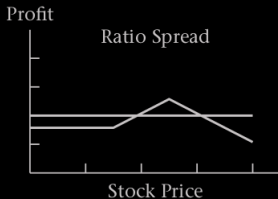
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 2. Sell a 45-strike call and buy a 45-strike put.
- Explain why there is no free lunch. Draw the profit diagram.

Solution. Check book 74.



Ratio spreads

A **ratio spread** is constructed by buying m options at one strike and selling n options at a different strike, with all options having the same type (call or put), same time to maturity, and same underlying asset.



Example 3.3-3 (Problem 3.15) Compute profit diagrams for the following ratio spreads:

- a Buy 950-strike call, sell two 1050-strike calls.
- b Buy two 950-strike calls, sell three 1050-strike calls.
- c Consider buying n 950-strike calls and selling m 1050-strike calls so that the premium of the position is zero. Considering your analysis in (a) and (b), what can you say about n/m ? What exact ratio gives you a zero premium?

Solution. Homework.



Example 3.3-3 (Problem 3.15) Compute profit diagrams for the following ratio spreads:

- a Buy 950-strike call, sell two 1050-strike calls.
- b Buy two 950-strike calls, sell three 1050-strike calls.
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Solution. Homework.



Collars

A **collar** is the purchase of a put option and the sale of a call option with a higher strike price, with both options having the same underlying asset and having the same expiration date.

If the position is reversed, i.e., sale of a put and purchase of a call, the collar is written.

The **collar width** is the difference between the call and put strikes.

Example 3.3-4 Draw the profit diagram for a purchased collar:

selling a 45-strike call + buying a 40-strike put.

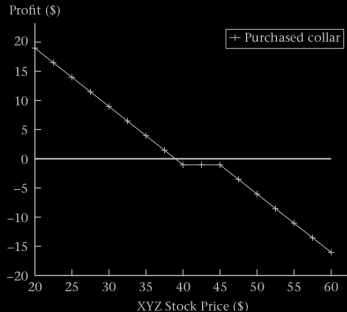
Solution.



Example 3.3-4 Draw the profit diagram for a purchased collar:

selling a 45-strike call + buying a 40-strike put.

Solution.



It is possible to find strike prices for the put and call such that the two premiums exactly offset one another. This position is called a **zero-cost collar**.

Example 3.3-5 Consider XYZ:

Strike	Call	Put
35	6.13	0.44
40	2.78	1.99
41.72	1.99	—
45	0.97	5.08

Show that the following gives a zero-cost collar

buying XYZ at \$40 + buying a 40-strike put + selling a 41.72-strike call

Draw the profit diagram.

Solution. Check book p. 77.



Example 3.3-5 Consider XYZ:

Strike	Call	Put
35	6.13	0.44
40	2.78	1.99
41.72	1.99	—
45	0.97	5.08

Show that the following gives a zero-cost collar

buying XYZ at \$40 + buying a 40-strike put + selling a 41.72-strike call

Draw the profit diagram.

Solution. Check book p. 77.



Chapter 3. Insurance, Collars, and Other Strategies

§ 3.1 Basic insurance strategies

§ 3.2 Put-call parity

§ 3.3 Spreads and collars

§ 3.4 Speculating on volatility

§ 3.5 Problems

Chapter 3. Insurance, Collars, and Other Strategies

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§ 3.5 Problems

Directional positions

- ▶ Bull spread
 - ▶ Bear spread
 - ▶ Collars
 - ▶ Box spreads
-

Nondirectional positions

- ▶ Straddles
- ▶ Strangle
- ▶ Butterfly spread

Investors who do not care whether the stock goes up or down,
but only how much it moves.

Investors are speculating on volatility.

Directional positions

- ▶ Bull spread
 - ▶ Bear spread
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-

Nondirectional positions

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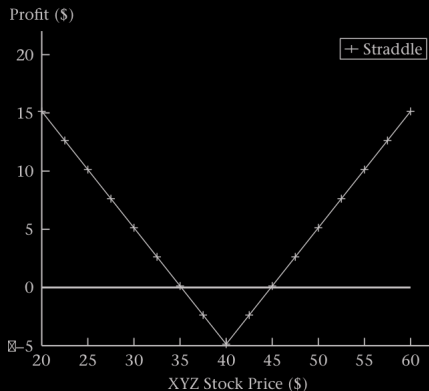
Investors who do not care whether the stock goes up or down,
but only how much it moves.

Investors are speculating on volatility.

Straddles

Straddle is the strategy of buying a call and a put with the same strike price and time to expiration.

A straddle is a bet that volatility will be high relative to the market's assessment



Strangle

Straddle is the strategy of buying an out-of-the-money call and put with the same time to expiration.

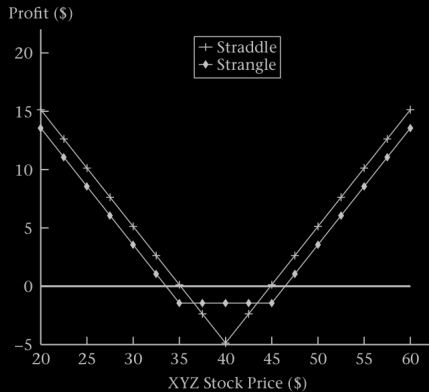
A strangle can be used to reduce the high premium cost, associated with a straddle.

Example 3.4-1 Draw profit diagram for 40-strike straddle and strangle composed of 35-strike put + 45-strike call.

Solution.

Example 3.4-1 Draw profit diagram for 40-strike straddle and strangle composed of 35-strike put + 45-strike call.

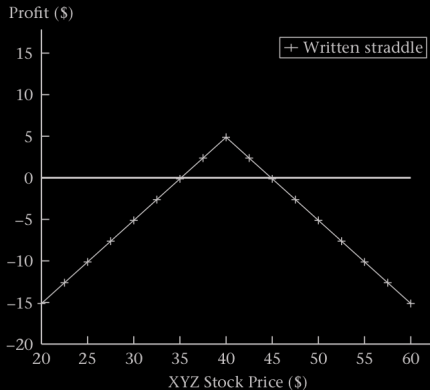
Solution.



Written straddles

Written straddle is the strategy of selling a call and put with the same strike price and time to maturity.

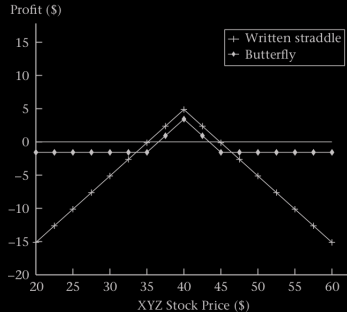
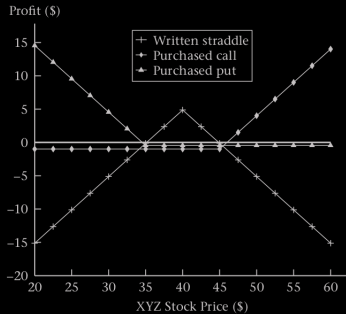
Unlike a purchased straddle, a written straddle is a bet that volatility will be low relative to the market's assessment



Butterfly spreads

Butterfly spreads = Insured wrien straddle
= Write a straddle + add a stragle

A butterfly spread insures against large losses on a straddle.



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§ 3.5 Problems

Problems: 3.3, 3.4, 3.5, 3.6, 3.7, 3.8, 3.9, 3.11, 3.13, 3.14, 3.15, 3.17, 3.18.

Due Date: TBA