#### Financial Mathematics

MATH 5870/6870<sup>1</sup> Fall 2021

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<sup>&</sup>lt;sup>1</sup>Based on Robert L. McDonald's *Derivatives Markets*. 3rd Ed. Pearson. 2013.

Chapter 9. Parity and other option relationships

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§ 9.1 Put-call parity

§ 9.2 Generalized parity and exchange options

§ 9.3 Comparing options with respect to style, maturity, and strike

§ 9.4 Problems

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### European versus American options

$$\textit{C}_{\mathrm{Amer}}(\textit{S},\textit{K},\textit{T}) \geq \textit{C}_{\mathrm{Eur}}(\textit{S},\textit{K},\textit{T})$$

$$P_{\mathrm{Amer}}(\boldsymbol{\mathcal{S}},\boldsymbol{\mathcal{K}},\boldsymbol{\mathcal{T}}) \geq P_{\mathrm{Eur}}(\boldsymbol{\mathcal{S}},\boldsymbol{\mathcal{K}},\boldsymbol{\mathcal{T}})$$

### Maximum and minimum option prices

$$S \geq \textit{C}_{\mathrm{Amer}}(\textit{S},\textit{K},\textit{T}) \geq \textit{C}_{\mathrm{Eur}}(\textit{S},\textit{K},\textit{T}) \geq \max\left(0,\mathrm{PV}_{0,\textit{T}}(\textit{F}_{0,\textit{T}}) - \mathrm{PV}_{0,\textit{T}}(\textit{K})\right)$$

$$K \ge P_{\mathrm{Amer}}(S, K, T) \ge P_{\mathrm{Eur}}(S, K, T) \ge \max(0, \mathrm{PV}(K) - \mathrm{PV}_{0, T}(F_{0, T}))$$

### Early exercise for American options

$$C_{\mathrm{Amer}} \geq C_{\mathrm{Eur}} > S_t - K$$

$$K - PV_{t,T}(K) > PV_{t,T}(Div)$$

See p. 277 for the proof of the first set of inequalities.

Unfinished...