Financial Mathematics

MATH 5870/6870¹ Fall 2021

Le Chen

lzc0090@auburn.edu

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Auburn University
Auburn AL

¹Based on Robert L. McDonald's *Derivatives Markets*. 3rd Ed. Pearson. 2013.



Chapter 1. Introduction to Derivatives

- § 1.1 What is a derivative?
- § 1.2 An overview of financial markets
- § 1.3 The use of derivatives
- § 1.4 Buying and short-selling financial assets
- § 1.5 Problems

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- The trade must be cleared (the obligations of each party are specified)
- 3. The trade must be settled (the buyer and the seller must deliver the cash or securities necessary to satisfy their obligations in the required period of time)
- 4. Ownership records are updated.

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- Market value or market cap: the sum of the market value of the claims that could be traded, without regard to whether they have traded.
- Notional value: Notional value measure the scale of a position, usually
 with reference to some underlying asset.
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Companies typically raise funds by

stock markets	bound markets	
Selling ownership claims	Obtaining a bank loan or issuing a bond	
Securities exchanges	Through dealers	
(NYSE, NASDAQ)		
	less frequent	

- Currencies were permitted to float in 1971 when the gold standard was
 officially abandoned. The modern market in financial derivatives began
 in 1972, when the Chicago Mercantile Exchange started trading futures
 contracts on seven currencies.
- 2. OPEC's 1973 reduction in the supply of oil was followed by high and variable oil prices.
- U.S. interest rates became more volatile following inflation and recessions in the 1970s.
- The market for natural gas has been deregulated gradually since 1978, resulting in a volatile market in recent years.
- 5. The deregulation of electricity began during the 1990s.

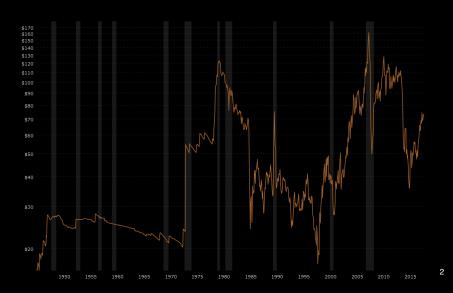
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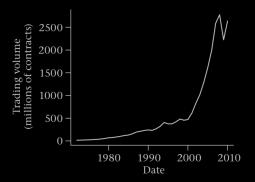
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History of the crude oil prices



²Image from https://www.macrotrends.net/

Price variability leads to the development of derivatives markets to efficiently share risk.



Millions of future contracts traded annually at the Chicago Board of Trade (CBT), Chicago Mercantile Exchange (CME), and the New York Mercantile Exchange (NYMEX), 1970-2011.

Examples of underlying assets on which futures contracts are traded:

Category	Description
Stock index	S&P 500 index, Euro Stoxx 50 index, Nikkei 225, Dow- Jones Industrials, Dax, NASDAQ, Russell 2000, S&P Sectors (healthcare, utilities, technology, etc.)
Interest rate	30-year U.S. Treasury bond, 10-year U.S. Treasury notes, Fed funds rate, Euro-Bund, Euro-Bobl, LIBOR, Euribor
Foreign exchange	Euro, Japanese yen, British pound, Swiss franc, Australian dollar, Canadian dollar, Korean won
Commodity	Oil, natural gas, gold, copper, aluminum, corn, wheat, lumber, hogs, cattle, milk
Other	Heating and cooling degree-days, credit, real estate

The role of financial markets

Insurance companies and individual communities/families have traditionally helped each other to share risks.

Markets make RISK-SHARING more efficient

The existence of risk-sharing mechanisms benefits everyone!

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Diversifiable risks	vanishes	lightening strike
Non-diversifiable risks	are reallocated to those	Stock market crash
	most willing to hold it	

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