#### Introduction

This kernel is an attempt to use every trick in the books to unleash the full power of Linear Regression, including a lot of preprocessing and a look at several Regularization algorithms.

At the time of writing, it achieves a score of about 0.121 on the public LB, just using regression, no RF, no xgboost, no ensembling etc. All comments/corrections are more than welcome.

```
In [1]:
        # Imports
        import pandas as pd
        import numpy as np
        from sklearn.model_selection import cross_val_score, train_test_split
        from sklearn.preprocessing import StandardScaler
        from sklearn.linear_model import LinearRegression, RidgeCV, LassoCV, ElasticNetCV
        from sklearn.metrics import mean_squared_error, make_scorer
        from scipy.stats import skew
        from IPython.display import display
        import matplotlib.pyplot as plt
        import seaborn as sns
        # Definitions
        pd.set option('display.float format', lambda x: '%.3f' % x)
        %matplotlib inline
        #njobs = 4
```

```
In [2]:
    # Get data
    train = pd.read_csv("../input/train.csv")
    print("train : " + str(train.shape))

train : (1460, 81)
```

```
In [3]:
    # Check for duplicates
    idsUnique = len(set(train.Id))
    idsTotal = train.shape[0]
    idsDupli = idsTotal - idsUnique
    print("There are " + str(idsDupli) + " duplicate IDs for " + str(idsTotal) + " to
    tal entries")

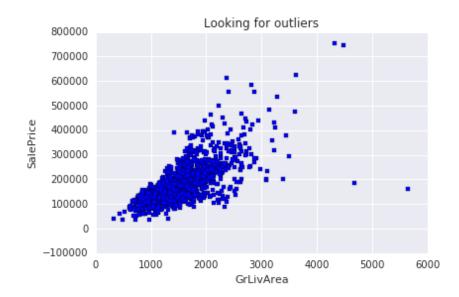
# Drop Id column
    train.drop("Id", axis = 1, inplace = True)
```

There are 0 duplicate IDs for 1460 total entries

# **Preprocessing**

```
In [4]:
    # Looking for outliers, as indicated in https://ww2.amstat.org/publications/jse/v
    19n3/decock.pdf
    plt.scatter(train.GrLivArea, train.SalePrice, c = "blue", marker = "s")
    plt.title("Looking for outliers")
    plt.xlabel("GrLivArea")
    plt.ylabel("SalePrice")
    plt.show()

train = train[train.GrLivArea < 4000]</pre>
```



There seems to be 2 extreme outliers on the bottom right, really large houses that sold for really cheap. More generally, the author of the dataset recommends removing 'any houses with more than 4000 square feet' from the dataset.

Reference: https://ww2.amstat.org/publications/jse/v19n3/decock.pdf

```
In [5]:
    # Log transform the target for official scoring
    train.SalePrice = np.log1p(train.SalePrice)
    y = train.SalePrice
```

Taking logs means that errors in predicting expensive houses and cheap houses will affect the result equally.

```
In [6]:
        # Handle missing values for features where median/mean or most common value does
        n't make sense
        # Alley: data description says NA means "no alley access"
        train.loc[:, "Alley"] = train.loc[:, "Alley"].fillna("None")
        # BedroomAbvGr : NA most likely means 0
        train.loc[:, "BedroomAbvGr"] = train.loc[:, "BedroomAbvGr"].fillna(0)
        # BsmtQual etc : data description says NA for basement features is "no basement"
        train.loc[:, "BsmtQual"] = train.loc[:, "BsmtQual"].fillna("No")
        train.loc[:, "BsmtCond"] = train.loc[:, "BsmtCond"].fillna("No")
        train.loc[:, "BsmtExposure"] = train.loc[:, "BsmtExposure"].fillna("No")
        train.loc[:, "BsmtFinType1"] = train.loc[:, "BsmtFinType1"].fillna("No")
        train.loc[:, "BsmtFinType2"] = train.loc[:, "BsmtFinType2"].fillna("No")
        train.loc[:, "BsmtFullBath"] = train.loc[:, "BsmtFullBath"].fillna(0)
        train.loc[:, "BsmtHalfBath"] = train.loc[:, "BsmtHalfBath"].fillna(0)
        train.loc[:, "BsmtUnfSF"] = train.loc[:, "BsmtUnfSF"].fillna(0)
        # CentralAir : NA most likely means No
        train.loc[:, "CentralAir"] = train.loc[:, "CentralAir"].fillna("N")
        # Condition : NA most likely means Normal
        train.loc[:, "Condition1"] = train.loc[:, "Condition1"].fillna("Norm")
        train.loc[:, "Condition2"] = train.loc[:, "Condition2"].fillna("Norm")
        # EnclosedPorch : NA most likely means no enclosed porch
        train.loc[:, "EnclosedPorch"] = train.loc[:, "EnclosedPorch"].fillna(0)
        # External stuff : NA most likely means average
        train.loc[:, "ExterCond"] = train.loc[:, "ExterCond"].fillna("TA")
        train.loc[:, "ExterQual"] = train.loc[:, "ExterQual"].fillna("TA")
```

```
# Fence : data description says NA means "no fence"
train.loc[:, "Fence"] = train.loc[:, "Fence"].fillna("No")
# FireplaceQu : data description says NA means "no fireplace"
train.loc[:, "FireplaceQu"] = train.loc[:, "FireplaceQu"].fillna("No")
train.loc[:, "Fireplaces"] = train.loc[:, "Fireplaces"].fillna(0)
# Functional : data description says NA means typical
train.loc[:, "Functional"] = train.loc[:, "Functional"].fillna("Typ")
# GarageType etc : data description says NA for garage features is "no garage"
train.loc[:, "GarageType"] = train.loc[:, "GarageType"].fillna("No")
train.loc[:, "GarageFinish"] = train.loc[:, "GarageFinish"].fillna("No")
train.loc[:, "GarageQual"] = train.loc[:, "GarageQual"].fillna("No")
train.loc[:, "GarageCond"] = train.loc[:, "GarageCond"].fillna("No")
train.loc[:, "GarageArea"] = train.loc[:, "GarageArea"].fillna(0)
train.loc[:, "GarageCars"] = train.loc[:, "GarageCars"].fillna(0)
# HalfBath : NA most likely means no half baths above grade
train.loc[:, "HalfBath"] = train.loc[:, "HalfBath"].fillna(0)
# HeatingQC : NA most likely means typical
train.loc[:, "HeatingQC"] = train.loc[:, "HeatingQC"].fillna("TA")
# KitchenAbvGr : NA most likely means 0
train.loc[:, "KitchenAbvGr"] = train.loc[:, "KitchenAbvGr"].fillna(0)
# KitchenQual : NA most likely means typical
train.loc[:, "KitchenQual"] = train.loc[:, "KitchenQual"].fillna("TA")
# LotFrontage : NA most likely means no lot frontage
train.loc[:, "LotFrontage"] = train.loc[:, "LotFrontage"].fillna(0)
# LotShape : NA most likely means regular
train.loc[:, "LotShape"] = train.loc[:, "LotShape"].fillna("Reg")
# MasVnrType : NA most likely means no veneer
train.loc[:, "MasVnrType"] = train.loc[:, "MasVnrType"].fillna("None")
train.loc[:, "MasVnrArea"] = train.loc[:, "MasVnrArea"].fillna(0)
# MiscFeature : data description says NA means "no misc feature"
train.loc[:, "MiscFeature"] = train.loc[:, "MiscFeature"].fillna("No")
train.loc[:, "MiscVal"] = train.loc[:, "MiscVal"].fillna(0)
# OpenPorchSF : NA most likely means no open porch
train.loc[:, "OpenPorchSF"] = train.loc[:, "OpenPorchSF"].fillna(0)
# PavedDrive : NA most likely means not paved
train.loc[:, "PavedDrive"] = train.loc[:, "PavedDrive"].fillna("N")
# PoolQC : data description says NA means "no pool"
train.loc[:, "PoolQC"] = train.loc[:, "PoolQC"].fillna("No")
train.loc[:, "PoolArea"] = train.loc[:, "PoolArea"].fillna(0)
# SaleCondition : NA most likely means normal sale
train.loc[:, "SaleCondition"] = train.loc[:, "SaleCondition"].fillna("Normal")
# ScreenPorch : NA most likely means no screen porch
train.loc[:, "ScreenPorch"] = train.loc[:, "ScreenPorch"].fillna(0)
```

```
# TotRmsAbvGrd : NA most likely means 0
train.loc[:, "TotRmsAbvGrd"] = train.loc[:, "TotRmsAbvGrd"].fillna(0)
# Utilities : NA most likely means all public utilities
train.loc[:, "Utilities"] = train.loc[:, "Utilities"].fillna("AllPub")
# WoodDeckSF : NA most likely means no wood deck
train.loc[:, "WoodDeckSF"] = train.loc[:, "WoodDeckSF"].fillna(0)
```

```
In [8]:
```

```
# Encode some categorical features as ordered numbers when there is information i
n the order
train = train.replace({"Alley" : {"Grvl" : 1, "Pave" : 2},
                       "BsmtCond" : {"No" : 0, "Po" : 1, "Fa" : 2, "TA" : 3, "Gd"
: 4, "Ex" : 5},
                       "BsmtExposure" : {"No" : 0, "Mn" : 1, "Av": 2, "Gd" : 3},
                       "BsmtFinType1" : {"No" : 0, "Unf" : 1, "LwQ": 2, "Rec" : 3
, "BLQ" : 4,
                                         "ALQ" : 5, "GLQ" : 6},
                       "BsmtFinType2" : {"No" : 0, "Unf" : 1, "LwQ": 2, "Rec" : 3
, "BLQ" : 4,
                                         "ALQ" : 5, "GLQ" : 6},
                       "BsmtQual" : {"No" : 0, "Po" : 1, "Fa" : 2, "TA": 3, "Gd"
: 4, "Ex" : 5},
                       "ExterCond" : {"Po" : 1, "Fa" : 2, "TA": 3, "Gd": 4, "Ex"
: 5},
                       "ExterQual" : {"Po" : 1, "Fa" : 2, "TA": 3, "Gd": 4, "Ex"
: 5},
                       "FireplaceQu" : {"No" : 0, "Po" : 1, "Fa" : 2, "TA" : 3,
"Gd": 4, "Ex": 5},
                       "Functional" : {"Sal" : 1, "Sev" : 2, "Maj2" : 3, "Maj1" :
4, "Mod": 5,
                                       "Min2": 6, "Min1": 7, "Typ": 8},
                       "GarageCond" : {"No" : 0, "Po" : 1, "Fa" : 2, "TA" : 3, "G
d": 4, "Ex": 5},
                       "GarageQual" : {"No" : 0, "Po" : 1, "Fa" : 2, "TA" : 3, "G
d": 4, "Ex": 5},
                       "HeatingQC" : {"Po" : 1, "Fa" : 2, "TA" : 3, "Gd" : 4, "E
x":5
                       "KitchenQual" : {"Po" : 1, "Fa" : 2, "TA" : 3, "Gd" : 4,
"Ex" : 5},
                       "LandSlope" : {"Sev" : 1, "Mod" : 2, "Gtl" : 3},
                       "LotShape" : {"IR3" : 1, "IR2" : 2, "IR1" : 3, "Reg" : 4},
                       "PavedDrive" : {"N" : 0, "P" : 1, "Y" : 2},
                       "PoolQC" : {"No" : 0, "Fa" : 1, "TA" : 2, "Gd" : 3, "Ex" :
4},
                       "Street" : {"Grvl" : 1, "Pave" : 2},
                       "Utilities" : {"ELO" : 1, "NoSeWa" : 2, "NoSewr" : 3, "All
Pub" : 4}}
                     )
```

Then we will create new features, in 3 ways:

- 1. Simplifications of existing features
- 2. Combinations of existing features
- 3. Polynomials on the top 10 existing features

```
In [9]:
        # Create new features
        # 1* Simplifications of existing features
        train["SimplOverallQual"] = train.OverallQual.replace({1 : 1, 2 : 1, 3 : 1, # bad
                                                               4 : 2, 5 : 2, 6 : 2, # ave
        rage
                                                               7:3,8:3,9:3,10:
        3 # good
                                                             })
        train["SimplOverallCond"] = train.OverallCond.replace({1 : 1, 2 : 1, 3 : 1, # bad
                                                               4: 2, 5: 2, 6: 2, # ave
        rage
                                                              7:3,8:3,9:3,10:
        3 # good
                                                             })
        train["SimplPoolQC"] = train.PoolQC.replace({1 : 1, 2 : 1, # average
                                                     3 : 2, 4 : 2 # good
                                                    })
        train["SimplGarageCond"] = train.GarageCond.replace({1 : 1, # bad
                                                            2 : 1, 3 : 1, # average
                                                            4 : 2, 5 : 2 # good
        train["SimplGarageQual"] = train.GarageQual.replace({1 : 1, # bad
                                                             2 : 1, 3 : 1, # average
                                                            4 : 2, 5 : 2 # good
        train["SimplFireplaceQu"] = train.FireplaceQu.replace({1 : 1, # bad
                                                               2 : 1, 3 : 1, # average
                                                              4 : 2, 5 : 2 # good
                                                             })
        train["SimplFireplaceQu"] = train.FireplaceQu.replace({1 : 1, # bad
                                                               2 : 1, 3 : 1, # average
                                                              4 : 2, 5 : 2 # good
        train["SimplFunctional"] = train.Functional.replace({1 : 1, 2 : 1, # bad
```

```
3 : 2, 4 : 2, # major
                                                    5:3,6:3,7:3, # minor
                                                    8 : 4 # typical
train["SimplKitchenQual"] = train.KitchenQual.replace({1 : 1, # bad
                                                      2 : 1, 3 : 1, # average
                                                      4 : 2, 5 : 2 # good
                                                     })
train["SimplHeatingQC"] = train.HeatingQC.replace({1 : 1, # bad
                                                  2 : 1, 3 : 1, # average
                                                  4 : 2, 5 : 2 # good
train["SimplBsmtFinType1"] = train.BsmtFinType1.replace({1 : 1, # unfinished
                                                        2 : 1, 3 : 1, # rec room
                                                        4:2,5:2,6:2# li
ving quarters
                                                       })
train["SimplBsmtFinType2"] = train.BsmtFinType2.replace({1 : 1, # unfinished
                                                        2 : 1, 3 : 1, # rec room
                                                        4:2,5:2,6:2#li
ving quarters
                                                       })
train["SimplBsmtCond"] = train.BsmtCond.replace({1 : 1, # bad
                                                2 : 1, 3 : 1, # average
                                                4 : 2, 5 : 2 # good
                                               })
train["SimplBsmtQual"] = train.BsmtQual.replace({1 : 1, # bad
                                                2 : 1, 3 : 1, # average
                                                4 : 2, 5 : 2 # good
                                               })
train["SimplExterCond"] = train.ExterCond.replace({1 : 1, # bad
                                                  2 : 1, 3 : 1, # average
                                                  4 : 2, 5 : 2 # good
                                                 })
train["SimplExterQual"] = train.ExterQual.replace({1 : 1, # bad
                                                  2 : 1, 3 : 1, # average
                                                  4 : 2, 5 : 2 # good
                                                 })
# 2* Combinations of existing features
# Overall quality of the house
train["OverallGrade"] = train["OverallQual"] * train["OverallCond"]
# Overall quality of the garage
```

```
train["GarageGrade"] = train["GarageQual"] * train["GarageCond"]
# Overall quality of the exterior
train["ExterGrade"] = train["ExterQual"] * train["ExterCond"]
# Overall kitchen score
train["KitchenScore"] = train["KitchenAbvGr"] * train["KitchenQual"]
# Overall fireplace score
train["FireplaceScore"] = train["Fireplaces"] * train["FireplaceQu"]
# Overall garage score
train["GarageScore"] = train["GarageArea"] * train["GarageQual"]
# Overall pool score
train["PoolScore"] = train["PoolArea"] * train["PoolQC"]
# Simplified overall quality of the house
train["SimplOverallGrade"] = train["SimplOverallQual"] * train["SimplOverallCond"
1
# Simplified overall quality of the exterior
train["SimplExterGrade"] = train["SimplExterQual"] * train["SimplExterCond"]
# Simplified overall pool score
train["SimplPoolScore"] = train["PoolArea"] * train["SimplPoolQC"]
# Simplified overall garage score
train["SimplGarageScore"] = train["GarageArea"] * train["SimplGarageQual"]
# Simplified overall fireplace score
train["SimplFireplaceScore"] = train["Fireplaces"] * train["SimplFireplaceQu"]
# Simplified overall kitchen score
train["SimplKitchenScore"] = train["KitchenAbvGr"] * train["SimplKitchenQual"]
# Total number of bathrooms
train["TotalBath"] = train["BsmtFullBath"] + (0.5 * train["BsmtHalfBath"]) + \
train["FullBath"] + (0.5 * train["HalfBath"])
# Total SF for house (incl. basement)
train["AllSF"] = train["GrLivArea"] + train["TotalBsmtSF"]
# Total SF for 1st + 2nd floors
train["AllFlrsSF"] = train["1stFlrSF"] + train["2ndFlrSF"]
# Total SF for porch
train["AllPorchSF"] = train["OpenPorchSF"] + train["EnclosedPorch"] + \
train["3SsnPorch"] + train["ScreenPorch"]
# Has masonry veneer or not
train["HasMasVnr"] = train.MasVnrType.replace({"BrkCmn" : 1, "BrkFace" : 1, "CBlo
ck": 1,
                                               "Stone" : 1, "None" : 0})
# House completed before sale or not
train["BoughtOffPlan"] = train.SaleCondition.replace({"Abnorm1" : 0, "Alloca" : 0
, "AdjLand" : 0,
                                                      "Family" : 0, "Normal" : 0,
"Partial" : 1})
```

```
In [10]:
    # Find most important features relative to target
    print("Find most important features relative to target")
    corr = train.corr()
    corr.sort_values(["SalePrice"], ascending = False, inplace = True)
    print(corr.SalePrice)
```

Find most important	features	relative	to	target
SalePrice	1.000			
OverallQual	0.819			
AllSF	0.817			
AllFlrsSF	0.729			
GrLivArea	0.719			
SimplOverallQual	0.708			
ExterQual	0.681			
GarageCars	0.680			
TotalBath	0.673			
KitchenQual	0.667			
GarageScore	0.657			
GarageArea	0.655			
TotalBsmtSF	0.642			
SimplExterQual	0.636			
SimplGarageScore	0.631			
BsmtQual	0.615			
1stFlrSF	0.614			
SimplKitchenQual	0.610			
OverallGrade	0.604			
SimplBsmtQual	0.594			
FullBath	0.591			
YearBuilt	0.589			
ExterGrade	0.587			
YearRemodAdd	0.569			
FireplaceQu	0.547			
GarageYrBlt	0.544			
TotRmsAbvGrd	0.533			
SimplOverallGrade	0.527			
SimplKitchenScore	0.523			
FireplaceScore	0.518			
SimplBsmtCond	0.204			
BedroomAbvGr	0.204			
AllPorchSF	0.199			
LotFrontage	0.174			
SimplFunctional	0.137			
Functional	0.136			
ScreenPorch	0.124			
SimplBsmtFinType2	0.105			
Street	0.058			
2 Caro Davado	0 056			

0.056

3SsnPorch

0.051
0.041
0.040
0.040
0.040
0.038
0.016
0.013
0.006
-0.015
-0.020
-0.028
-0.034
-0.037
-0.038
-0.040
-0.042
-0.148
-0.149
-0.286

Name: SalePrice, dtype: float64

```
In [11]:
         # Create new features
         # 3* Polynomials on the top 10 existing features
         train["OverallQual-s2"] = train["OverallQual"] ** 2
         train["OverallQual-s3"] = train["OverallQual"] ** 3
         train["OverallQual-Sq"] = np.sqrt(train["OverallQual"])
         train["AllSF-2"] = train["AllSF"] ** 2
         train["AllSF-3"] = train["AllSF"] ** 3
         train["AllSF-Sq"] = np.sqrt(train["AllSF"])
         train["AllFlrsSF-2"] = train["AllFlrsSF"] ** 2
         train["AllFlrsSF-3"] = train["AllFlrsSF"] ** 3
         train["AllFlrsSF-Sq"] = np.sqrt(train["AllFlrsSF"])
         train["GrLivArea-2"] = train["GrLivArea"] ** 2
         train["GrLivArea-3"] = train["GrLivArea"] ** 3
         train["GrLivArea-Sq"] = np.sqrt(train["GrLivArea"])
         train["SimplOverallQual-s2"] = train["SimplOverallQual"] ** 2
         train["SimplOverallQual-s3"] = train["SimplOverallQual"] ** 3
         train["SimplOverallQual-Sq"] = np.sqrt(train["SimplOverallQual"])
         train["ExterQual-2"] = train["ExterQual"] ** 2
         train["ExterQual-3"] = train["ExterQual"] ** 3
         train["ExterQual-Sq"] = np.sqrt(train["ExterQual"])
         train["GarageCars-2"] = train["GarageCars"] ** 2
         train["GarageCars-3"] = train["GarageCars"] ** 3
         train["GarageCars-Sq"] = np.sqrt(train["GarageCars"])
         train["TotalBath-2"] = train["TotalBath"] ** 2
         train["TotalBath-3"] = train["TotalBath"] ** 3
         train["TotalBath-Sq"] = np.sqrt(train["TotalBath"])
         train["KitchenQual-2"] = train["KitchenQual"] ** 2
         train["KitchenQual-3"] = train["KitchenQual"] ** 3
         train["KitchenQual-Sq"] = np.sqrt(train["KitchenQual"])
         train["GarageScore-2"] = train["GarageScore"] ** 2
         train["GarageScore-3"] = train["GarageScore"] ** 3
         train["GarageScore-Sq"] = np.sqrt(train["GarageScore"])
```

```
In [12]:
         # Differentiate numerical features (minus the target) and categorical features
         categorical_features = train.select_dtypes(include = ["object"]).columns
         numerical_features = train.select_dtypes(exclude = ["object"]).columns
         numerical_features = numerical_features.drop("SalePrice")
         print("Numerical features : " + str(len(numerical features)))
         print("Categorical features : " + str(len(categorical_features)))
         train num = train[numerical features]
         train cat = train[categorical features]
         Numerical features : 117
         Categorical features : 26
In [13]:
         # Handle remaining missing values for numerical features by using median as repla
         cement
         print("NAs for numerical features in train : " + str(train_num.isnull().values.su
         m()))
         train num = train_num.fillna(train_num.median())
         print("Remaining NAs for numerical features in train : " + str(train_num.isnull()
         .values.sum()))
         NAs for numerical features in train: 81
         Remaining NAs for numerical features in train: 0
In [14]:
         # Log transform of the skewed numerical features to lessen impact of outliers
         # Inspired by Alexandru Papiu's script : https://www.kagqle.com/apapiu/house-pric
         es-advanced-regression-techniques/regularized-linear-models
         # As a general rule of thumb, a skewness with an absolute value > 0.5 is consider
         ed at least moderately skewed
         skewness = train num.apply(lambda x: skew(x))
         skewness = skewness[abs(skewness) > 0.5]
         print(str(skewness.shape[0]) + " skewed numerical features to log transform")
         skewed_features = skewness.index
         train num[skewed features] = np.log1p(train num[skewed features])
         86 skewed numerical features to log transform
```

```
In [15]:
# Create dummy features for categorical values via one-hot encoding
print("NAs for categorical features in train : " + str(train_cat.isnull().values.
    sum()))
    train_cat = pd.get_dummies(train_cat)
    print("Remaining NAs for categorical features in train : " + str(train_cat.isnull
    ().values.sum()))
```

```
NAs for categorical features in train : 1
Remaining NAs for categorical features in train : 0
```

### Modeling

```
In [16]:
# Join categorical and numerical features
    train = pd.concat([train_num, train_cat], axis = 1)
    print("New number of features : " + str(train.shape[1]))

# Partition the dataset in train + validation sets

X_train, X_test, y_train, y_test = train_test_split(train, y, test_size = 0.3, ra
    ndom_state = 0)
    print("X_train : " + str(X_train.shape))
    print("X_test : " + str(X_test.shape))
    print("y_train : " + str(y_train.shape))
    print("y_test : " + str(y_test.shape))
```

```
New number of features : 319
X_train : (1019, 319)
X_test : (437, 319)
y_train : (1019,)
y_test : (437,)
```

```
In [17]:
    # Standardize numerical features
    stdSc = StandardScaler()
    X_train.loc[:, numerical_features] = stdSc.fit_transform(X_train.loc[:, numerical_features])
    X_test.loc[:, numerical_features] = stdSc.transform(X_test.loc[:, numerical_features])
```

```
/opt/conda/lib/python3.5/site-packages/pandas/core/indexing.py:465: SettingWithC
opyWarning:
A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: http://pandas.pydata.org/pandas-docs/stabl
e/indexing.html#indexing-view-versus-copy
    self.obj[item] = s
```

Standardization cannot be done before the partitioning, as we don't want to fit the StandardScaler on some observations that will later be used in the test set.

```
In [18]:
# Define error measure for official scoring : RMSE
scorer = make_scorer(mean_squared_error, greater_is_better = False)

def rmse_cv_train(model):
    rmse= np.sqrt(-cross_val_score(model, X_train, y_train, scoring = scorer, cv = 10))
    return(rmse)

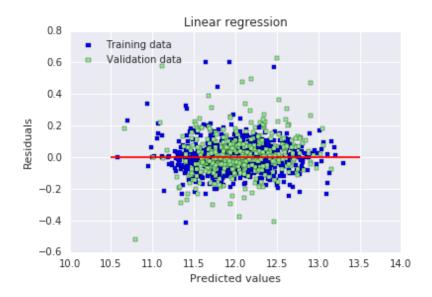
def rmse_cv_test(model):
    rmse= np.sqrt(-cross_val_score(model, X_test, y_test, scoring = scorer, cv = 10))
    return(rmse)
```

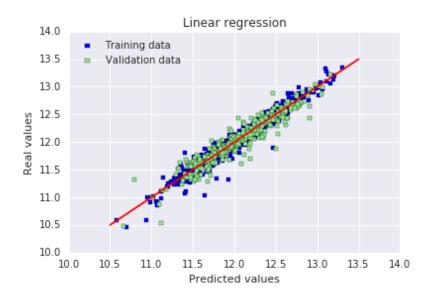
Note: I'm not getting nearly the same numbers in local CV compared to public LB, so I'm a tad worried that my CV process may have an issue somewhere. If you spot something, please let me know.

1\* Linear Regression without regularization

In [19]: # Linear Regression lr = LinearRegression() lr.fit(X\_train, y\_train) # Look at predictions on training and validation set print("RMSE on Training set :", rmse\_cv\_train(lr).mean()) print("RMSE on Test set :", rmse\_cv\_test(lr).mean()) y train pred = lr.predict(X train) y\_test\_pred = lr.predict(X\_test) # Plot residuals plt.scatter(y\_train\_pred, y\_train\_pred - y\_train, c = "blue", marker = "s", label = "Training data") plt.scatter(y\_test\_pred, y\_test\_pred - y\_test, c = "lightgreen", marker = "s", la bel = "Validation data") plt.title("Linear regression") plt.xlabel("Predicted values") plt.ylabel("Residuals") plt.legend(loc = "upper left") plt.hlines(y = 0, xmin = 10.5, xmax = 13.5, color = "red") plt.show() # Plot predictions plt.scatter(y\_train\_pred, y\_train, c = "blue", marker = "s", label = "Training da ta") plt.scatter(y test pred, y test, c = "lightgreen", marker = "s", label = "Validat ion data") plt.title("Linear regression") plt.xlabel("Predicted values") plt.ylabel("Real values") plt.legend(loc = "upper left") plt.plot([10.5, 13.5], [10.5, 13.5], c = "red") plt.show()

RMSE on Training set : 15758371373.7 RMSE on Test set : 0.395779797728





RMSE on Training set shows up weird here (not when I run it on my computer) for some reason. Errors seem randomly distributed and randomly scattered around the centerline, so there is that at least. It means our model was able to capture most of the explanatory information.

# 2\* Linear Regression with Ridge regularization (L2 penalty)

From the *Python Machine Learning* book by Sebastian Raschka: Regularization is a very useful method to handle collinearity, filter out noise from data, and eventually prevent overfitting. The concept behind regularization is to introduce additional information (bias) to penalize extreme parameter weights.

Ridge regression is an L2 penalized model where we simply add the squared sum of the weights to our cost function.

```
In [20]:
         # 2* Ridge
         ridge = RidgeCV(alphas = [0.01, 0.03, 0.06, 0.1, 0.3, 0.6, 1, 3, 6, 10, 30, 60])
         ridge.fit(X train, y train)
         alpha = ridge.alpha_
         print("Best alpha :", alpha)
         print("Try again for more precision with alphas centered around " + str(alpha))
         ridge = RidgeCV(alphas = [alpha * .6, alpha * .6, alpha * .7, alpha * .75, alpha
         * .8, alpha * .85,
                                   alpha * .9, alpha * .95, alpha, alpha * 1.05, alpha *
         1.1, alpha * 1.15,
                                   alpha * 1.25, alpha * 1.3, alpha * 1.35, alpha * 1.4],
                         cv = 10)
         ridge.fit(X train, y train)
         alpha = ridge.alpha
         print("Best alpha :", alpha)
         print("Ridge RMSE on Training set :", rmse_cv_train(ridge).mean())
         print("Ridge RMSE on Test set :", rmse_cv_test(ridge).mean())
         y_train_rdg = ridge.predict(X_train)
         y_test_rdg = ridge.predict(X_test)
         # Plot residuals
         plt.scatter(y_train_rdg, y_train_rdg - y_train, c = "blue", marker = "s", label =
         "Training data")
         plt.scatter(y_test_rdg, y_test_rdg - y_test, c = "lightgreen", marker = "s", labe
         1 = "Validation data")
         plt.title("Linear regression with Ridge regularization")
         plt.xlabel("Predicted values")
         plt.ylabel("Residuals")
         plt.legend(loc = "upper left")
         plt.hlines(y = 0, xmin = 10.5, xmax = 13.5, color = "red")
```

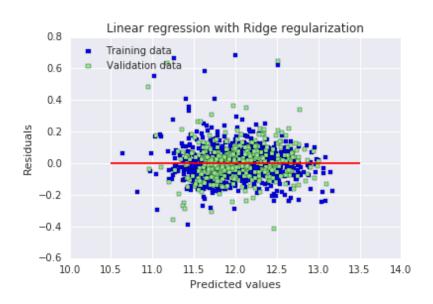
```
plt.show()
# Plot predictions
plt.scatter(y train rdg, y train, c = "blue", marker = "s", label = "Training dat
plt.scatter(y test rdg, y test, c = "lightgreen", marker = "s", label = "Validati
on data")
plt.title("Linear regression with Ridge regularization")
plt.xlabel("Predicted values")
plt.ylabel("Real values")
plt.legend(loc = "upper left")
plt.plot([10.5, 13.5], [10.5, 13.5], c = "red")
plt.show()
# Plot important coefficients
coefs = pd.Series(ridge.coef_, index = X_train.columns)
print("Ridge picked " + str(sum(coefs != 0)) + " features and eliminated the othe
r " + \
      str(sum(coefs == 0)) + " features")
imp_coefs = pd.concat([coefs.sort_values().head(10),
                     coefs.sort_values().tail(10)])
imp_coefs.plot(kind = "barh")
plt.title("Coefficients in the Ridge Model")
plt.show()
```

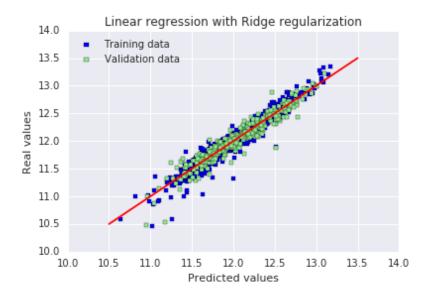
Best alpha: 30.0

Try again for more precision with alphas centered around 30.0

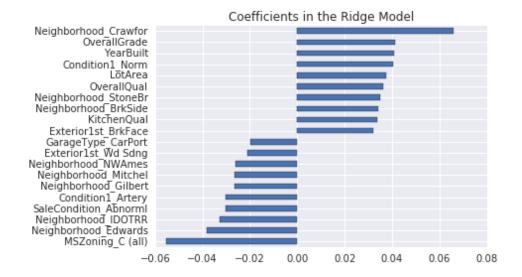
Best alpha : 24.0

Ridge RMSE on Training set : 0.115405723285 Ridge RMSE on Test set : 0.116427213778





Ridge picked 316 features and eliminated the other 3 features



We're getting a much better RMSE result now that we've added regularization. The very small difference between training and test results indicate that we eliminated most of the overfitting. Visually, the graphs seem to confirm that idea.

Ridge used almost all of the existing features.

### 3\* Linear Regression with Lasso regularization (L1 penalty)

LASSO stands for *Least Absolute Shrinkage and Selection Operator*. It is an alternative regularization method, where we simply replace the square of the weights by the sum of the absolute value of the weights. In contrast to L2 regularization, L1 regularization yields sparse feature vectors: most feature weights will be zero. Sparsity can be useful in practice if we have a high dimensional dataset with many features that are irrelevant.

We can suspect that it should be more efficient than Ridge here.

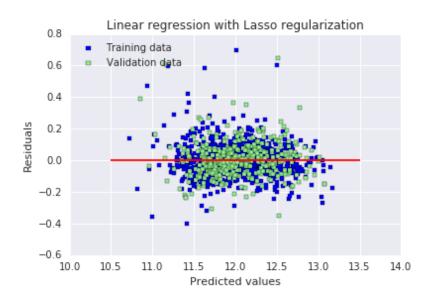
```
lasso = LassoCV(alphas = [alpha * .6, alpha * .65, alpha * .7, alpha * .75, alpha
* .8,
                          alpha * .85, alpha * .9, alpha * .95, alpha, alpha * 1.
05,
                          alpha * 1.1, alpha * 1.15, alpha * 1.25, alpha * 1.3, a
lpha * 1.35,
                          alpha * 1.4],
                max_iter = 50000, cv = 10)
lasso.fit(X_train, y_train)
alpha = lasso.alpha
print("Best alpha :", alpha)
print("Lasso RMSE on Training set :", rmse_cv_train(lasso).mean())
print("Lasso RMSE on Test set :", rmse cv test(lasso).mean())
y train las = lasso.predict(X train)
y_test_las = lasso.predict(X_test)
# Plot residuals
plt.scatter(y_train_las, y_train_las - y_train, c = "blue", marker = "s", label =
"Training data")
plt.scatter(y_test_las, y_test_las - y_test, c = "lightgreen", marker = "s", labe
1 = "Validation data")
plt.title("Linear regression with Lasso regularization")
plt.xlabel("Predicted values")
plt.ylabel("Residuals")
plt.legend(loc = "upper left")
plt.hlines(y = 0, xmin = 10.5, xmax = 13.5, color = "red")
plt.show()
# Plot predictions
plt.scatter(y_train_las, y_train, c = "blue", marker = "s", label = "Training dat
plt.scatter(y test las, y test, c = "lightgreen", marker = "s", label = "Validati
on data")
plt.title("Linear regression with Lasso regularization")
plt.xlabel("Predicted values")
plt.ylabel("Real values")
plt.legend(loc = "upper left")
plt.plot([10.5, 13.5], [10.5, 13.5], c = "red")
plt.show()
# Plot important coefficients
coefs = pd.Series(lasso.coef , index = X train.columns)
```

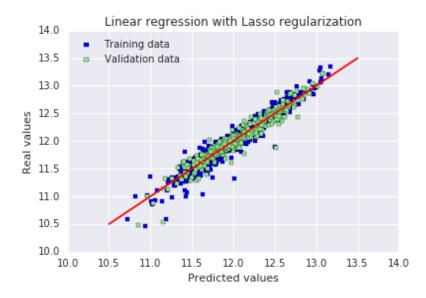
Best alpha: 0.0006

Try again for more precision with alphas centered around 0.0006

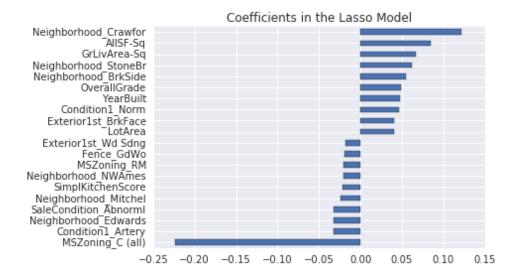
Best alpha: 0.0006

Lasso RMSE on Training set : 0.114111508375 Lasso RMSE on Test set : 0.115832132218





Lasso picked 110 features and eliminated the other 209 features



RMSE results are better both on training and test sets. The most interesting thing is that Lasso used only one third of the available features. Another interesting tidbit: it seems to give big weights to Neighborhood categories, both in positive and negative ways. Intuitively it makes sense, house prices change a whole lot from one neighborhood to another in the same city.

The "MSZoning\_C (all)" feature seems to have a disproportionate impact compared to the others. It is defined as *general zoning classification*: *commercial*. It seems a bit weird to me that having your house in a mostly commercial zone would be such a terrible thing.

# 4\* Linear Regression with ElasticNet regularization (L1 and L2 penalty)

ElasticNet is a compromise between Ridge and Lasso regression. It has a L1 penalty to generate sparsity and a L2 penalty to overcome some of the limitations of Lasso, such as the number of variables (Lasso can't select more features than it has observations, but it's not the case here anyway).

```
print("Best alpha :", alpha )
print("Try again for more precision with l1_ratio centered around " + str(ratio))
elasticNet = ElasticNetCV(11_ratio = [ratio * .85, ratio * .9, ratio * .95, ratio
, ratio * 1.05, ratio * 1.1, ratio * 1.15],
                          alphas = [0.0001, 0.0003, 0.0006, 0.001, 0.003, 0.006,
0.01, 0.03, 0.06, 0.1, 0.3, 0.6, 1, 3, 6],
                          max iter = 50000, cv = 10)
elasticNet.fit(X_train, y_train)
if (elasticNet.l1_ratio_ > 1):
    elasticNet.l1_ratio_ = 1
alpha = elasticNet.alpha_
ratio = elasticNet.l1 ratio
print("Best 11 ratio :", ratio)
print("Best alpha :", alpha )
print("Now try again for more precision on alpha, with 11 ratio fixed at " + str(
ratio) +
      " and alpha centered around " + str(alpha))
elasticNet = ElasticNetCV(l1_ratio = ratio,
                          alphas = [alpha * .6, alpha * .65, alpha * .7, alpha *
.75, alpha * .8, alpha * .85, alpha * .9,
                                    alpha * .95, alpha, alpha * 1.05, alpha * 1.1
, alpha * 1.15, alpha * 1.25, alpha * 1.3,
                                    alpha * 1.35, alpha * 1.4],
                          max iter = 50000, cv = 10)
elasticNet.fit(X_train, y_train)
if (elasticNet.l1_ratio_ > 1):
    elasticNet.l1_ratio_ = 1
alpha = elasticNet.alpha
ratio = elasticNet.l1_ratio_
print("Best l1_ratio :", ratio)
print("Best alpha :", alpha )
print("ElasticNet RMSE on Training set :", rmse_cv_train(elasticNet).mean())
print("ElasticNet RMSE on Test set :", rmse_cv_test(elasticNet).mean())
y_train_ela = elasticNet.predict(X_train)
y_test_ela = elasticNet.predict(X_test)
# Plot residuals
plt.scatter(y_train_ela, y_train_ela - y_train, c = "blue", marker = "s", label =
"Training data")
plt.scatter(y_test_ela, y_test_ela - y_test, c = "lightgreen", marker = "s", labe
```

```
1 = "Validation data")
plt.title("Linear regression with ElasticNet regularization")
plt.xlabel("Predicted values")
plt.ylabel("Residuals")
plt.legend(loc = "upper left")
plt.hlines(y = 0, xmin = 10.5, xmax = 13.5, color = "red")
plt.show()
# Plot predictions
plt.scatter(y_train, y_train_ela, c = "blue", marker = "s", label = "Training dat
plt.scatter(y_test, y_test_ela, c = "lightgreen", marker = "s", label = "Validati
on data")
plt.title("Linear regression with ElasticNet regularization")
plt.xlabel("Predicted values")
plt.ylabel("Real values")
plt.legend(loc = "upper left")
plt.plot([10.5, 13.5], [10.5, 13.5], c = "red")
plt.show()
# Plot important coefficients
coefs = pd.Series(elasticNet.coef_, index = X_train.columns)
print("ElasticNet picked " + str(sum(coefs != 0)) + " features and eliminated the
other " + str(sum(coefs == 0)) + " features")
imp coefs = pd.concat([coefs.sort values().head(10),
                     coefs.sort values().tail(10)])
imp_coefs.plot(kind = "barh")
plt.title("Coefficients in the ElasticNet Model")
plt.show()
```

/opt/conda/lib/python3.5/site-packages/sklearn/linear\_model/coordinate\_descent.p y:479: ConvergenceWarning: Objective did not converge. You might want to increas e the number of iterations. Fitting data with very small alpha may cause precisi on problems.

ConvergenceWarning)

Best l1\_ratio : 1.0
Best alpha : 0.0006

Try again for more precision with l1\_ratio centered around 1.0

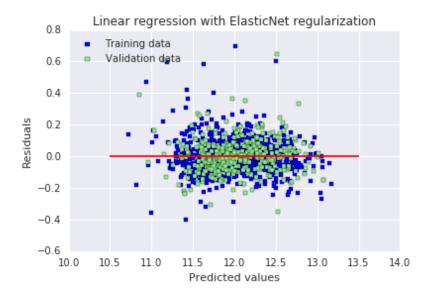
Best l1\_ratio : 1.0
Best alpha : 0.0006

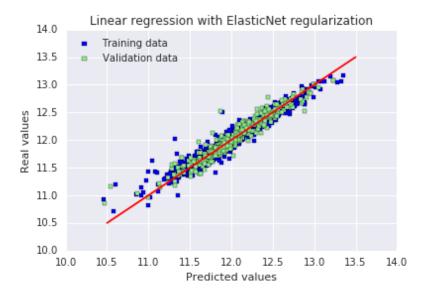
Now try again for more precision on alpha, with l1\_ratio fixed at 1.0 and alpha

centered around 0.0006
Best l1\_ratio : 1.0

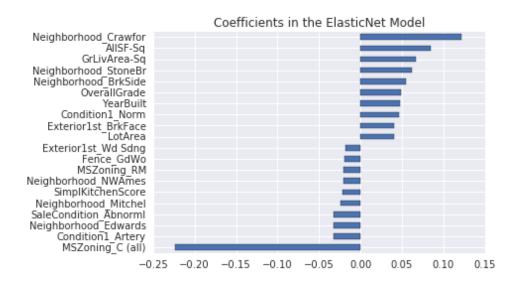
Best alpha: 0.0006

ElasticNet RMSE on Training set : 0.114111508375 ElasticNet RMSE on Test set : 0.115832132218





ElasticNet picked 110 features and eliminated the other 209 features



The optimal L1 ratio used by ElasticNet here is equal to 1, which means it is exactly equal to the Lasso regressor we used earlier (and had it been equal to 0, it would have been exactly equal to our Ridge regressor). The model didn't need any L2 regularization to overcome any potential L1 shortcoming.

Note: I tried to remove the "MSZoning\_C (all)" feature, it resulted in a slightly worse CV score, but slightly better public LB score.

# Conclusion

Putting time and effort into preparing the dataset and optimizing the regularization resulted in a decent score, better than some public scripts which use algorithms that historically perform better in Kaggle contests, like Random Forests. Being fairly new to the world of machine learning contests, I will appreciate any constructive pointer to improve, and I thank you for your time.