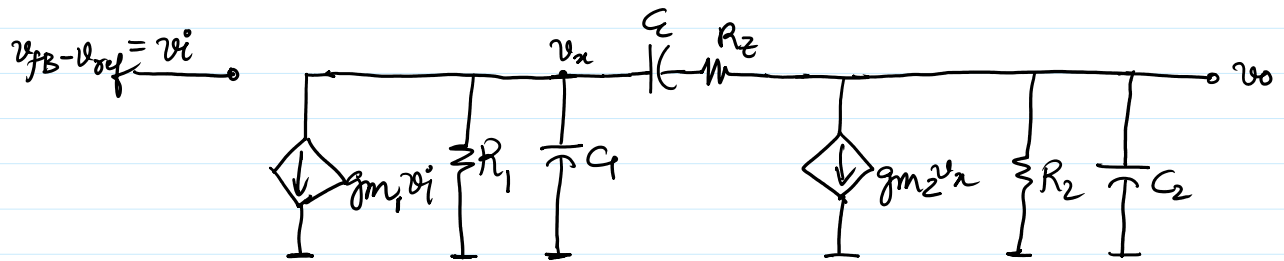


21/06/24

Stability Analysis



In the case of LDO [My LDO]

$$R_1 = r_{o1} \parallel r_{o3}, C_1 = C_{gpass}, R_2 = R_4 + R_2 \parallel r_{opass} \parallel R_L$$

$$\frac{v_o(s)}{v_i(s)} = \frac{g_{m1} R_1 g_{m2} R_2 (1 - s C_c / g_{m2})}{1 + s [R_1 (C_1 + C_c (1 + g_{m2} R_2)) + R_2 (C_2 + C_c)] + s^2 R_2 R_1 [C_1 C_2 + C_2 C_c + C_1 C_c]}$$

$$\omega_{p1} \text{ (dominant)} = \frac{1}{R_1 (C_1 + C_c (1 + g_{m2} R_2)) + R_2 (C_2 + C_c)} \approx \frac{1}{g_{m2} R_2 R_1 C_c}$$

$$\omega_{p2} \text{ (Non-dom)} = \frac{R_1 C_c g_{m2} R_2}{R_1 R_2 (C_1 C_2 + C_1 C_c + C_2 C_c)} \approx \frac{g_{m2} C_c}{C_1 C_2 + C_1 C_c + C_2 C_c}$$

$$\approx \frac{g_{m2}}{C_2} \text{ (bad approx for simplification)}$$

$$A_{DC} = g_{m1} R_1 g_{m2} R_2$$

$$\omega_{ugb} = A_{DC} \times \omega_{p1} = g_{m1} R_1 g_{m2} R_2 \times \frac{1}{g_{m2} R_2 R_1 C_c} = \frac{g_{m1}}{C_c}$$

$$A(s) \text{ [complete O.L.G]} = \frac{A_{DC} (1 - s/\omega_z)}{(1 + s/\omega_{p1}) (1 + s/\omega_{p2})}$$

for feedback factor = f

$$\text{Loop Gain (L.G)}(s) = A(s)f$$

$$\text{Closed L.G}(s) = \frac{1}{f} \frac{LG(s)}{1+LG(s)}$$

Calculating ϕ

* Assuming $z \geq 10 \cdot \omega_{ugb}$

$$\angle \frac{V_o}{V_{in}} = -\tan^{-1}\left(\frac{\omega}{\omega_z}\right) - \tan^{-1}\left(\frac{\omega}{\omega_{p1}}\right) - \tan^{-1}\left(\frac{\omega}{\omega_{p2}}\right)$$

Check the P.M at ω_{ugb} to evaluate the stability

After lot of simplification

$$\angle \frac{V_o}{V_{in}} = -\tan^{-1}\left(\frac{\omega_{ugb}}{\omega_z}\right) - \tan^{-1}(A_{DC}) - \tan^{-1}\left(\frac{\omega_{ugb}}{\omega_{p2}}\right)$$

Considering zero has been nullified by adding LHP zero $R_z = 1/g_{m2}$

$$\angle \frac{V_o}{V_{in}} = (\approx 0) - (\approx 90^\circ) - \tan^{-1}\left(\frac{\omega_{ugb}}{\omega_{p2}}\right)$$

$$P.M = 180^\circ - 90^\circ - \tan^{-1}\left(\frac{\omega_{ugb}}{\omega_{p2}}\right)$$

$$P.M = 90^\circ - \tan^{-1}\left(\frac{\omega_{ugb}}{\omega_{p2}}\right)$$

For P.M $\geq 60^\circ$

$$60^\circ = 90^\circ - \tan^{-1}\left(\frac{\omega_{ugb}}{\omega_{p2}}\right)$$

$$30^\circ = \tan^{-1}\left(\frac{\omega_{ugb}}{\omega_{p2}}\right) \Rightarrow \tan(30^\circ) = \frac{\omega_{ugb}}{\omega_{p2}}$$

$$0.577 \approx \frac{\omega_{ugb}}{\omega_{p2}} \Rightarrow \omega_{p2} = \frac{\omega_{ugb}}{0.577} \Rightarrow \omega_{p2} = 1.73 \omega_{ugb}$$

But ω_z will not be perfectly cancelled so, I'll keep a safe margin

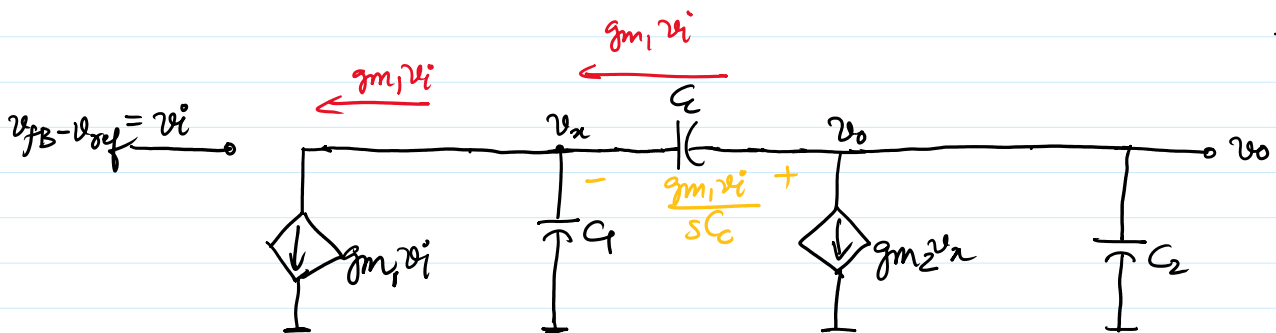
But ω_z will not be perfectly cancelled so, I'll keep a safe margin

$$\omega_{p2} \geq 2\omega_{uwb}$$

For this $\underline{C_c \geq 0.2C_L}$

Need of LHP zero to nullify RHP zero

- At higher freq curr flows through caps mostly



For large P.M $gm_2 \rightarrow \text{large}$

Then $v_x \rightarrow 0$ for $gm_2 \rightarrow \infty$

$$v_o = v_x + \frac{gm_1 v_i}{sC_c}$$

I ideally we donot want v_x [$v_x = 0$]

- LHP zero advances the signal
- RHP zero delays the signal [Make P.M Bad]

$$\Rightarrow \frac{gm_1}{sC_c} v_i - \frac{gm_1}{gm_2} v_i = \frac{gm_1}{sC_c} \left(1 - \frac{sC_c}{gm_2} \right)$$

$$v_x = -\frac{gm_1}{gm_2} v_i \quad \& \quad i_x = gm_1 v_i$$

So from this of RHP zero. If I add $1/gm_2$ Resistor we can nullify the effect