## F# Tutorial

# Pipe-Forward Operator

February 20, 2018

# 1 Syntax, variables, functions

## Key concepts:

- 1. Having a good text editor helps you code much easier.
- 2. (a) Once defined, a variable in F# cannot change value (unless "mutable" is used)
  - (b) If you need an updated value, create a new one.
- 3. Different datatypes (e.g. integer and decimal-numbers) do not combine easily.
- 4. Defining and using functions in F# is slightly different from math notation/ other languages.
  - (a) F# automatically detects the type of the variables (e.g. integer, double, etc.) for a function.
  - (b) The variable types for a function will be enforced.

## 1.1 Setting Up

#### 1.1.1 Comments

You can use double-slash //, triple-slash ///, or star-bracket (\* ..... \*) to make comments.

```
// These words are ignored.
/// These words are ignored.
(* These words are ignored. *)
let x = 1
let y = x + 5
```

## 1.1.2 F# Interactive

If you are using Visual Studio, you can run the code above by highlighting/selecting the code using your mouse, and press ALT + ENTER, or right-click and select Execute in Interactive.

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#### 1.1.3 Intellisense

If you are using Visual Studio or Visual Studio Code, you can put your mouse on top of the variable name x or y, and see that it is an int or integer.

This feature will help you identify what is each variable/function, and make coding easier for you.



## 1.2 Data Type

## 1.2.1 Common data types and printing

Some of the common types in F# are:

Keyword	Description	Print in output:
int	Integer	%i
double or float	Decimal numbers	%f
string	Words/Sentences	%s
bool	True/False	%b
-	Other objects	%A or %O

```
let name = "John"
let age = 21
let height = 170.5

printfn "My name is: %s" name

printfn "Name: %s. Age: %i. Height: %f." name age height

printfn "His height is: %.2f" height
// %.2f for showing two decimals.
```

## Output:

```
1 // Output:
2 // My name is: John
3 // Name: John. Age: 21. Height: 170.500000
4 // His height is: 170.50
```

For example, in the second example, inside the string-format, there are %s, %i, %f. And so, we expect a string, integer, and decimal (in that order) after the string-format specification in order to completely print the result to the output console.

## 1.2.2 Equality and simple if-else

The let ... = ... combination is used to assigned a value to a variable. Other than this situation, the equal sign = is used for equality testing. =, <> are used for equality/inequality testing.

In Java/C++, ==, != are used for comparison, and in Javascript, ===, !== are used.

### 1.2.3 Immutability

In F#, variables are by default immutable/unchangable. Once defined, the value of a variable cannot be changed. You can make a variable changable/mutable using the keyword mutable and symbol <-, but this is <u>highly discouraged</u>. (If you use VisualStudio, then the color of the variable name will change color, warning you of potential mutable values)

If you try to update an immutable/unchangable value using <-, you will get an error.

```
// Uncomment the code below to see an error:
let immutableValue = 100
immutableValue <- 300

This value is not mutable. Consider using the mutable keyword, e.g. 'let mutable immutableValue = expression'.</pre>
```

## Benefit of immutable/unchangable values

Imagine the code below, with a mutable value x, and after thousands of lines of code later, you used x's value again:

```
let mutable x = 100

2 //
3 // Thousands of lines of code later.....
4 // You have many lines of code in between.....
5 // It is hard to keep track.....
6 // Have you changed/updated x's value?
7 // Did you accidentally call any function that modify x?
8 // Can you guarantee x's value stay unchanged?
9 //
10 //
11 let y = x + 1
12 // What is the value of y?
13 //
14 // That depends on what happens between y's definition
15 // and x's definition.
```

On the other hand, if x is immutable/unchangable:

```
let x = 100
//
//
// Thousands of lines of code later.....
// You have many lines of code in between....
// But because x is immutable/unchangable....
// We can be sure that x stays constant....
// And we can safely conclude that....
/// let y = x + 1
// y = 101
```

Conclusion: Use immutable/unchangable value whenever possible. AVOID mutable/changable value whenever possible.

## 1.2.4 (+) Operator on the same type of variable

Integers, double, and string support the (+) operation:

```
let number1 = 40
let number2 = 55
let addTwoNumbers = number1 + number2

// Remark: "float" and "double" mean the same thing in F#.
let sqrtTwoApprox = 1.414
let piApprox = 3.1415926
let addTwoDecimals = sqrtTwoApprox + piApprox

let sentenceStart = "My school is "
let schoolName = "National University of Singapore"
let combinedSentence = sentenceStart + schoolName
```

However, you cannot add an integer with a decimal in F# directly using (+), and you cannot add/concatenate a string with a number directly using (+). If you use VisualStudio, then you may see an error similar to the one below.

Furthermore, some functions, like the square root sqrt and math exponent (\*\*) only accepts decimal numbers:

```
let sqrtRootOfNine = sqrt 9.0
let twoToPowerOfFive = 2.0 ** 5.0
```

And it will cause error if you use them with integer input instead.

### 1.3 Functions

#### 1.3.1 One variable functions

You can define functions using let followed by the inputs of your function.

```
let f x = x + 5

let result1 = f 10
let result2 = f 20
```

## Output:

```
1 // val result1 : int = 15
2 // val result2 : int = 25
```

Notice the following:

- 1. To apply the function f, you do not need to use the math notation f(x). You can apply the arguments by separating with a space.
- 2. If you hover your mouse on top of the function f, you will see that f is a function that accepts only integer x as the argument.



- (a) This is because in the function, x will be added (+) to the integer 5. We have seen before that we cannot use the symbol (+) to combine an integer with a decimal number directly. Hence, x has to be of type int.
- (b) As a consequence, if you try to input a decimal number to the function f, then it will fail:

3. As mentioned, F# automatically inferred that x is an integer. This is different from other languages (e.g. Java, C++) that needs you to specify the type of the variable (is it an integer? double? etc.)

So, you can spend less time on the tiny details (e.g. what is the variable type), and focus more on the correctness of your program.

Similarly, the following function accepts decimals/double only.

```
let DiscountFunc originalPrice = originalPrice * 0.8

let discountedPrice = DiscountFunc 399.99
printfn "New price: %.2f" discountedPrice
// Output: "New price: 319.99"

let anotherDiscount = DiscountFunc discountedPrice
printfn "New price: %.2f" anotherDiscount
// Output: "New price: 255.99"
```

Remark: The %.2f for printing 2 decimals.

This function does not accept integer values:

#### INPUT ERROR PICTURE HERE!

We need to convert integer to decimal (using double or float) before using the function.

```
let convertedPrice = double 100
let decimalResult = DiscountFunc convertedPrice
printfn "New price: %.2f" decimalResult
// Output: "New price: 80.00"
```

Similarly, the following function accepts strings only.

```
// Define a function for string.
let AddGreeting name =
    "Hello " + name

let greeting1 = AddGreeting "John"
let greeting2 = AddGreeting "Mary"
```

Output:

```
1 // val greeting1 : string = "Hello John"
2 // val greeting2 : string = "Hello Mary"
```

And it will cause error if you try to input an integer value to this function:

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Exercise: Write a function that calculates the area of a circle of radius r.

```
let CircleArea r =
//
//
// ... INSERT YOUR CODE HERE ...
// Hint: Use "System.Math.PI"
```

#### 1.3.2 Two variable functions

You can define a function that takes in two variables:

```
let g x y = 3 * x + y

let result3 = g 3 1
let result4 = g 10 2

// val result3 : int = 10
```

```
1 // val result3 : int = 10
2 // val result4 : int = 32
```

Notice the following:

- 1. To apply the function g, you do not need to use the math notation g(x, y) with brackets and commas. This is different from other programming languages (e.g. Java, C++). You can apply the arguments by separating with a space.
- 2. If you hover your mouse on top of g, as seen in this picture:

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You will see that the variables x, y need to be integers.

- (a) This is because in the function, x will be multiplied with 3, and then later added with y. As seen before, the addition and multiplication symbol (+), (\*) only combined numbers of the same type (integers with integers, double with double)
- (b) As a consequence, if you input decimals into the function, it will fail:

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3. Again, you can spend less time typing out the details (i.e. what are the types of x, y? Integer? Double?) and focus more on making your program/algorithm works, and make yourself more productive (compared to other programming languages)

Similarly, the following function accepts two decimal numbers:

```
let CalculateNewBalance interestRate principal =
    principal * (1.0 + interestRate)

let balance1 = CalculateNewBalance 0.05 100000.00

printfn "New Balance: %f" balance1
// Output: "New Balance: 105000.00"

let balance2 = CalculateNewBalance 0.03 5000.00

printfn "New Balance: %f" balance2
// Output: "New Balance: 5150.00"
```

And it will cause error if you try to change one of the input into integer.

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#### 1.3.3 Multivariable functions

```
let h x y z = 3 * x + 4 * y + 5 * z

// 3*3 + 4*4 + 5*5 = 50

let result5 = h 3 4 5

// 3*1 + 4*1 + 5*1 = 12

let result6 = h 1 1 1
```

Output:

```
1 // val result5 : int = 50
2 // val result6 : int = 12
```

## 1.3.4 Default integers for +, \*

If you use (+), (\*) with no other information available in your function (e.g. an appearance of a decimal, string, etc.), then F# will assume the function variables as integers.

```
let AddThree x y z = x + y + z
let addThreeResult = AddThree 5 6 7
```

If you hover your mouse on top of AddThree, the you see that all the inputs are inferred to be integers.

If you want this function to work for decimals, then you will need to annotate/manually add in the type for one of the variables:

```
let AddThreeCustom (x:double) y z = x + y + z
```

Here, we are explicitly saying that x is a double. And since y, z interacts with x using (+), we can infer that y, z are also doubles (and we do not need to explicitly label them as decimal/doubles)

## 1.4 Scoping

## 1.4.1 Indenting

You can use a let inside a let, i.e. you can define a variable inside a variable. For example:

```
let AddFriend person1 =
let endOfSentence = " and Mary are friends"
person1 + endOfSentence

let combinedSentence1 = AddFriend "Jack"
```

Output:

```
1 // combinedSentence1 : string = "Jack and Mary are friends"
```

Notice that the two lines immediately after the AddFriend function has some spaces in front of each line. This means that those two lines are accessible only inside the AddFriend function.

So, you cannot access the endOfSentence variable outside of the function. The following code will not work:

```
let AddFriend person1 =
    let endOfSentence = " and Mary are friends"
    person1 + endOfSentence

// ERROR: "endOfSentence" is not accessible outside of "
    AddFriend"

let x = endOfSentence
"ERROR: endOfSentence is not accessible outside of
    AddFriend"
```

#### 1.4.2 Reuse variable name

By carefully using indenting/spacing, you can repeatedly use the same variable name, as long as the spacing/indenting is such that the variables do not cause conflict with each other.

```
let DrinkFunction person =
let endOfSentence = "likes to drink coffee."

person + endOfSentence

let EatFunction person =
let endOfSentence = "prefers eating chocolate."

person + endOfSentence

printfn "%s" (DrinkFunction "Jack")
// Output:
```

```
// "Jack likes to drink coffee."
printfn "%s" (EatFunction "Jill")
// Output:
// "Jill prefers eating chocolate."
```

The endOfSentence inside these two functions will not cause conflict with each other.

## 1.4.3 From top to bottom

F# code are read from top to bottom. For example, look at the following code:

```
let a = 5

let f1 b =
    a + b

let f2 b =
    a + a + b

printfn "%i" (f1 10)
printfn "%i" (f2 10)
```

Notice that there are no spacing/indenting before  $let\ a=5$  and the definition of f1, f2. These variables and functions are equally indented, and so the value of a is accessible from f1, f2

However, the following code below will not be accepted, because a is defined later/down lower in the code, but it is incorrectly used before it is defined (i.e. above it).

```
// ERROR: "a" is not yet defined.
let f1 b =
    a + b
"ERROR!"
// ERROR: "a" is not yet defined.
let f2 b =
    a + a + b
"ERROR!"
// ERROR: "a" is defined too late! It is used above.
let a = 5
```

## 1.4.4 Warning: No TAB

In Python, you use TAB to indent the file. The TAB button will insert a special character.

However, in F#, you use blank spaces to do indenting. You should configure/adjust your IDE (e.g. VisualStudio, VisualStudioCode, etc.) so that it insert multiple blank spaces instead of a special character.

For example, the code below is indented using 4 spaces for the second and third line.

# These are 4 blank spaces! Not the special character "TAB"

If you did not configure your IDE correctly, or if you copy-and-paste the special TAB character from another source (e.g. Notepad), then you may see the following error:

```
plet AddFriend person1 =
    let endOfSentence = " and Mary are friends"
    person1 + endOfSentence
    TABs are not allowed in F# code unless the #indent "off" option is used
```

# 1.5 Reset F# Interactive

Remember to reset your F# Interactive once in a while, so that you don't have too many previous variables (especially if you re-use the same variable names)

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In Visual Studio, you can Right-click the interactive window, and select "Reset Interactive Session", or use the shortcut key CTRL + ALT + R

# 2 Pipe-forward

## **Key Concept:**

- 1. Coding in F# is similar to building LEGO.
  - Source: Scott Wlaschin
- 2. The output of one function is the input of the next function.

### 2.1 Introduction

F# has an operator, called the pipe-forward operator.

The definition of pipe-forward is:

```
let inline (|>) x f = f x
```

(The inline keyword is used to handle some special cases.) You do not need to worry about the definition. This operator is already implemented in F# by default.

## 2.2 Simple demonstration

Let us take a look at an example:

```
let Add5Func x = x + 5

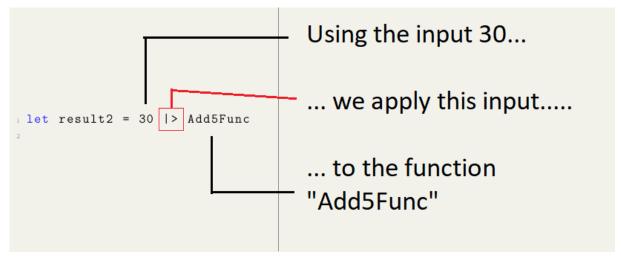
let result1 = Add5Func 30
4 // val result1 : int = 35
```

Notice that the variable/input 30 is located after the function Add5Func.

However, with the new symbol |>, we can specify the variable/input first, and then the function that we want to apply it to.

```
let result2 = 30 |> Add5Func
// val result2 : int = 35
```

How this code should be interpreted is the following:



## 2.3 Why is this useful?

The reason why the symbol |> is useful is because it helps us to compose functions. Let's say that you are given these functions:

```
let GetGrade score =
    if score >= 90 then "A"
    else if score >= 70 then "B"
    else if score >= 50 then "C"
    else "D"

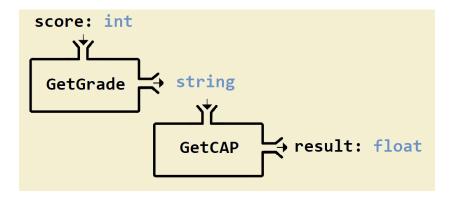
// For Singaporean University. (Maximum CAP 5.0)
let GetCAP grade =
    if grade = "A" then 5.0
    else if grade = "B" then 4.0
    else if grade = "C" then 3.0
    else 2.0
```

Remark: In American universities, they use a maximum score/GPA of 4.0. In Singapore we use CAP 5.0.

We can take a look at the signatures of the functions:

```
1 GetGrade: int -> string
2 GetCAP: string -> float
```

So, we can use the result of the first function GetGrade as the input of a second function GetCAP.



```
let GetCAPfromScore1 score =
let intermediateResult = GetGrade score
let finalResult = GetCAP intermediateResult
// return
finalResult

let cap1 = GetCAPfromScore1 95
let cap2 = GetCAPfromScore1 85
```

## Output:

```
1 // val cap1 : float = 5.0
2 // val cap2 : float = 4.0
```

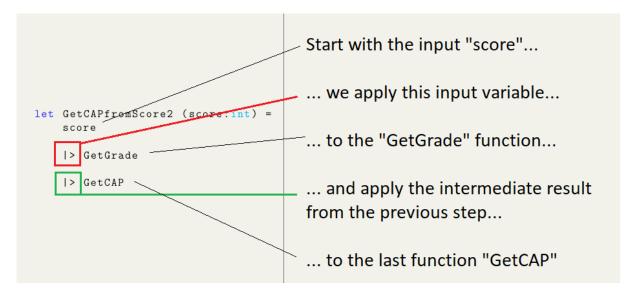
Notice that in the code above, we named out the intermediate steps/variables, i.e. intermediateResult and finalResult, even though it makes the code longer.

However, if we use the pipe-forward operator |>, we can simplify it as:

```
// GetGrade: int -> string
// GetCAP: string -> float
let GetCAPfromScore2 score =
score
|> GetGrade
|> GetCAP

let cap3 = GetCAPfromScore2 95
// val cap3 : float = 5.0
```

How this code should be interpreted:



Remark: The code will not compile if we put the functions in the wrong order:

Because score is an int, but the function GetCAP only accepts string as input. Similarly, the intermediate result from GetCAP is float, but the function GetGrade only accepts int

## 2.4 More Examples

Let us consider another hypothetical example.

Imagine that you want to buy or sell a company's stock, based on the company's performance relative to the financial analyst's estimate.

1. F# has a built-in function, List.average to find the average of a list of numbers:

```
let average1 = List.average [1.0; 2.0; 3.0; 4.0; 5.0]
let average2 = List.average [80.0; 85.0; 90.0; 95.0;
100.0]
```

2. You are provided another function, **GetPerformance**, that determines the condition of the company.

Assume that the actual profit of the company is \$ 6.0 billion for that year, then we say that the company is:

- OUTPERFORM: If actual profit exceed the analystEstimate by 5%
- UNDERPERFORM: If actual profit misses the analystEstimate by 5%
- NEUTRAL: If actual profit is within 5% of the analystEstimate

```
let GetPerformance analystAverageEstimate =
let actualProfit = 6.0
if actualProfit > analystAverageEstimate * 1.05
then "OUTPERFORM"
else if actualProfit < analystAverageEstimate * 0.95
then "UNDERPERFORM"
else
"NEUTRAL"</pre>
```

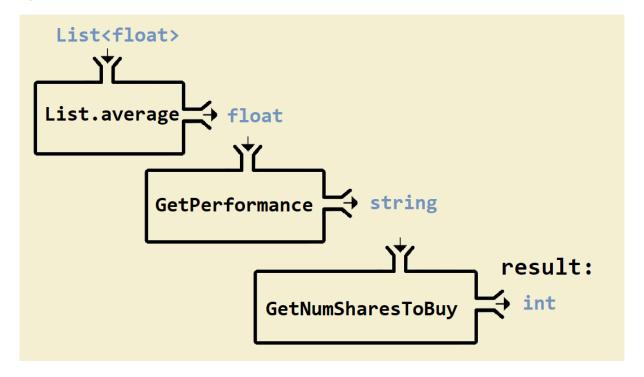
- 3. You are also provided another function, GetNumSharesToBuy, that determines how much additional shares to buy/sell depending on the company's condition:
  - OUTPERFORM: Buy additional 1000 shares.
  - UNDERPERFORM: Sell 1000 shares.
  - NEUTRAL: Hold the same portfolio.

```
1 let GetNumSharesToBuy performance =
2    if performance = "OUTPERFORM" then
3         1000    // buy 1000 shares
4    else if performance = "UNDERPERFORM" then
5         -1000    // sell 1000 shares
6    else
7         0     // hold.
```

So, the function signatures are:

```
List.average:
List<double> -> double
GetPerformance: double -> string
GetNumSharesToBuy: string -> int
```

In this carefully crafted example, notice that the result of the one function can act as the input to the other function.



So, we can combine them into a big function:

```
// Assume the profit is already known to be $6.0 billion,
    and written in "GetPerformance"

let GetNumSharesFromEstimate1 individualEstimates =
    let intermediateResult1 =
        List.average individualEstimates

let intermediateResult2 =
        GetPerformance intermediateResult1

let finalResult = GetNumSharesToBuy intermediateResult2
    // output
    finalResult
```

Notice that the code above uses a lot of temporary variables intermediateResult1, etc. which makes the code unnecessarily longer.

## Usage example:

1. In this example, the actual profit (6.0 billion) exceeds all the financial analyst's prediction, which means this is good news.

```
let numShares1 = GetNumSharesFromEstimate1 [4.0; 5.0; 3.0;
        2.0; 2.5]
printfn "Number of shares to buy(+) or sell(-): %i"
        numShares1
// Output:
// "Number of shares to buy(+) or sell(-): 1000"
```

2. In this example, the actual profit (6.0 billion) misses all the financial analyst's prediction, which means this is bad news.

```
let numShares2 = GetNumSharesFromEstimate1 [8.0; 7.0;
     10.0; 12.0; 10.5]
printfn "Number of shares to buy(+) or sell(-): %i"
     numShares2
// Output:
// "Number of shares to buy(+) or sell(-): -1000"
```

The following is the original code:

```
// Assume the profit is already known to be $6.0 billion,
    and written in "GetPerformance"

let GetNumSharesFromEstimate1 individualEstimates =
    let intermediateResult1 =
        List.average individualEstimates

let intermediateResult2 =
        GetPerformance intermediateResult1

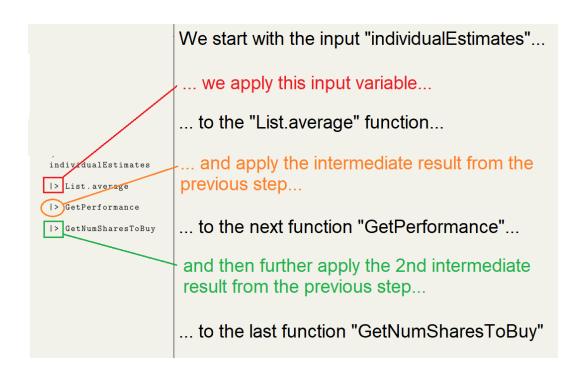
let finalResult = GetNumSharesToBuy intermediateResult2
    // output
    finalResult
```

And the following is the simplified version with the pipe-forward operator |>

```
let GetNumSharesFromEstimate2 individualEstimates =
individualEstimates

| List.average
| GetPerformance
| GetNumSharesToBuy
```

How this code should be interpreted:



### 2.5 Benefits

The benefits of using the pipe-forward operator |>:

- 1. You can remove unnecessary clutter/words on our computer screen. You do not need explicitly write out intermediate result, and we can focus more on the internal logic/calculations (and reserve the naming for variables/results that are truely important).
- 2. It is easier to follow instructions than to reason mathematically. Consider the following two statements:

$$y = h\left(g\left(f\left(x\right)\right)\right)$$

```
Start with variable x.

Step 1: Use function f.

Step 2: Use function g.

Step 3: Use function h.
```

Most common languages\* are written from left-to-right, and top-to-bottom. So, the conventional mathematical notation  $h\left(g\left(f\left(x\right)\right)\right)$  is not very natural to most languages. Whereas in the second case, it gives us a simple step-by-step instructions on how to get our final result.

This makes it easier to non-programmers to understand your code (e.g. if you work with a manager or a trader); it makes it easier for you to understand your own code (e.g. if you re-visit some code that you have written 1 year ago).

Once you get used to this syntax, you may find other traditional programming language, e.g. Java/ C++ to be a bit verbose/too long.

<sup>\*</sup>Exception: Hebrew and Arabic.

#### 2.6 Intellisense

In actual code development, we will do things step by step (instead of collecting everything together and chain everything using |>).

1. We will first start off like this:

```
let myFunction1 (individualEstimates: List<float>) =
individualEstimates
|> List.average
```

If you are using VisualStudio or VisualStudioCode, hover your mouse over myFunction1 to see the type signature:

```
List<float> -> float
```

2. Next, let's add one more line:

```
let myFunction2 individualEstimates =
individualEstimates

| > List.average
| > GetPerformance
```

We know that until the List.average step, we have an intermediate result of type float. So, we want the next function, GetPerformance, to take in float as an input.

Hover your mouse over myFunction2 to see the type signature:

```
List<float> -> string
```

3. Finally, let's add one more line:

```
let myFunction3 individualEstimates =
individualEstimates
| List.average
| GetPerformance
| GetNumSharesToBuy
```

The new function, GetNumSharesToBuy, should ideally accept string as its input (which it does). And if we hover your mouse over myFunction3 to see the type signature:

```
List<float> -> int
```

## 2.7 Exercise

Scenario: Assume that you are in a trading firm, and you want to manage your employees based on their performance.

You are given the following functions:

1. The F# build-in function, List.sum that finds the sum of a list of doubles/decimals.

```
1 let sum1 = List.sum [1.0; 2.0; 3.0; 4.0; 5.0]  // sum
    from 1 to 5
2 let sum2 = List.sum [1.0 .. 100.0]  // sum
    from 1 to 100
```

- 2. Another function, GetStatus, that determines how well is the trader
  - TOP TRADER: Profit exceeds \$ 10.0 million.
  - HUGE LOSSES: Loses \$3.0 million.
  - NORMAL TRADER: Remaining cases

- 3. Another function, GetBonus, that determines how many months of bonus is given to the trader.
  - TOP TRADER: 24 months bonus (i.e. 2 years bonus)
  - HUGE LOSSES: 6 months bonus (i.e. half year bonus)
  - NORMAL TRADER: 0 months bonus (i.e. no bonus)

Again, the output of one function is the input of the next function:

```
List.sum : List<double > -> double

GetStatus: double -> string

GetBonus: string -> int

let GetBonusFromTrades1 listOfTrades =

let intermediateResult1 = List.sum listOfTrades

let intermediateResult2 = GetStatus intermediateResult1

let finalResult = GetBonus intermediateResult2

// output

finalResult
```

Try to re-implement the function above using the pipe-forward operator |>.

```
let GetBonusFromTrades2 (listOfTrades: List < double >) =

let GetBonusFromTrades2 (listOfTrades: List < double >) =

// implement the function above.
```

Examples of use cases:

1. This trader helped the company earned some money.

```
let bonus1 =
    GetBonusFromTrades2 [1.0; -2.0; 0.5; 0.3; 0.4; 0.2]
printfn "He received a bonus of %i months" bonus1
```

2. This trader made one huge profitable deal, with other tiny losses.

```
let bonus2 =
GetBonusFromTrades2 [-2.0; -1.0; -0.5; 30.0; -1.0]
printfn "She received a bonus of %i months" bonus2
```

## 2.8 Function with same input and output type

The mathematical term is called *endomorphism*.

In all the above examples, we have chosen functions that have different input and output types, so that it is obvious which function comes after which one.

Sometimes, you may face with functions that have the same input and output type. For example:

```
let Square x = x * x
let Cube x = x * x * x
let Add5 x = x + 5

// Square: int -> int
// Cube : int -> int
// Add5 : int -> int
```

All of these functions are int -> int, and so you may compose them in different orders, or you may apply the same function multiple times, which may cause the function to completely change.

## 1. Example 1

$$f_1(x) = (x^2 + 5)^3$$

Output:

```
1 // val demo1 : int = 216
2 // val demo2 : int = 729
```

## 2. Example 2

$$f_2(x) = (x^2)^3 + 5$$

## Output:

```
1 // val demo3 : int = 6
2 // val demo4 : int = 69
```

### 3. Exercise:

Try to implement the following function using pipe-forward:

$$f_3(x) = [(x+5)^2 + 5]^3$$

```
//let Square x = x * x
//let Cube x = x * x * x
//let Add5 x = x + 5
let f3 x =

// IMPLEMENT YOUR FUNCTION ABOVE
// Testing:
// Testing:
// [ (1+5)^2 + 5 ]^3 = 68921
let demo5 = f3 1
// [ (2+5)^2 + 5 ]^3 = 157464
let demo6 = f3 2
```

# 3 List in F#

Key Concept:

- 1. Introduce basic List functions
  - (a) List.filter
  - (b) List.map
- 2. Code in F# are very easy to understand (thanks for pipe-forward operator |> and the F# language design)
- 3. Anonymous functions / lambda function also helps.
  - You are defining a function at the exact location where it is most useful. So it boosts productivity.
  - fun is a keyword in F#!

## 3.1 Creating a list

You can create a list of integers/ float / string using the following notations:

```
let list1 = [1 .. 100]
let list2 = [50 .. 80]
let list3 = [1 .. 2 .. 100]

let list4 = [1.0 .. 100.0]
let list5 = [0.0 .. 0.05 .. 1.0]

let list6 = [1; 20; 50; 100; 55; 5; 10]
let list7 = [1.0; 6.0; 5.0; 10.0; 3.0; 2.0]

let list8 = ["ABC"; "DEF"; "GHI"; "JKL"; "MNO"]
```

The ; is used to separate different elements, and [a .. b], [a .. diff .. b] is used to specify any increasing/decreasing pattern.

If you hover your mouse on top of those variables (using VisualStudio or VisualStudioCode), you will see the types are int list, float list, etc. An alternate notation would be List<int>, List<double>, etc.

Warning: You cannot create a list with different types, e.g. the example below tries to create a list with a string, an integer, and a decimal/float.

```
let listError = ["ABC"; 123; 400.0]
// ERROR! Cannot define different type in the same list!
```

### 3.2 List.filter

Here is a simple function that returns true/false, depending on whether x is divisible by 2:

```
let IsItEven x = (x % 2 = 0)

let trueOrFalse1 = IsItEven 10
let trueOrFalse2 = IsItEven 3
```

Remark: x % 2 means the remainder after we divide x by 2.

We can use this function together with List.filter:

```
let result1 = List.filter IsItEven [1 .. 100]
// Output:
// [2; 4; 6; .....; 98; 100]
```

The List.filter function filters a list, and only select the elements which satisfy some requirement; the requirement is specified through a function IsItEven.

Alternatively, because the definition of IsItEven is quite easy, we can even implement it immediately after List.filter, at the point where we need it the most.

```
let result2 = List.filter (fun x -> x % 2 = 0) [1 .. 100]
// Output:
// [2; 4; 6; ....; 98; 100]
```

The notation (fun x  $\rightarrow$  x % 2 = 0) is used to define anonymous/lambda function, i.e. functions that are easy to define, that we do not need to give it a name, e.g. IsItEven.

Benefits:

- We define this function using the fun keyword at exactly where it is used.
- If we define too many custom functions, e.g. IsItEven, then it will be hard to keep track when we have 1000+ functions, and we will lose productivity.

Remark: The code (fun  $x \rightarrow x \% 2 = 0$ ) represents a "thing", and that "thing" is a function, just like IsItEven is a function.

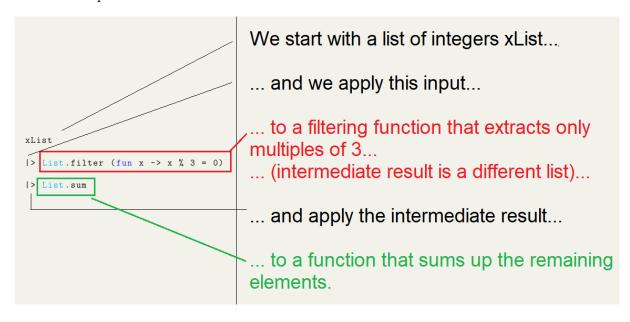
Side note: fun is a keyword in the F#! Programming in F# is very fun!

## List.filter and Pipe-Forward |>

Let us look at the following function:

```
let SumMultiplesOfThree xList =
    xList
    |> List.filter (fun x -> x % 3 = 0)
    |> List.sum
```

How to interpret this function:



So, F# is able to express all of these calculations with just 3 lines of code, which is quite elegant, maybe similar to Python code (in style), compared to other more traditional languages (Java/C++) which we need to write longer.

Using this function:

```
// 3 + 6 + 9 + ... + 99 = 1683
let result3 = SumMultiplesOfThree [1 .. 100]

// 3 + 6 + 9 + ... + 198 = 6633
let result4 = SumMultiplesOfThree [1 .. 200]
```

### Output:

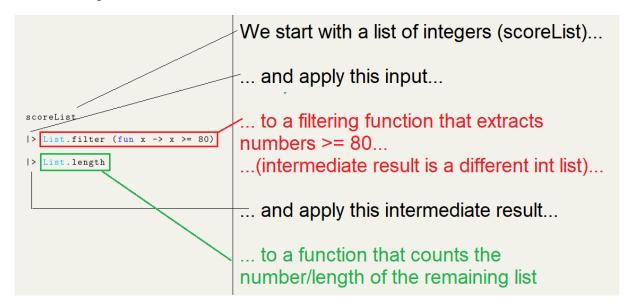
```
1 // val result3 : int = 1683
2 // val result4 : int = 6633
```

## Another example

Let's say you want to find out how many students in your class got at least 80 points in an exam.

```
let CountGreaterThan80 scoreList =
scoreList
| > List.filter (fun x -> x >= 80)
| > List.length
```

How to interpret this function:



Using this function:

```
let result5 =
    CountGreaterThan80 [60; 65; 70; 75; 80; 85; 90; 95]
printfn "%i students scored 80 or above." result5
```

### Output:

```
1 // "4 students scored 80 or above."
```

## Another example

This function adds up all multiples of 3, e.g.  $3, 6, 9, \ldots$ , but ignore all multiples of 5, e.g.  $5, 10, \underline{15}, 20, 25, \underline{30}, \ldots$ 

```
let SumMultiplesOf3ButNot5 xList =
    xList
    |> List.filter (fun x -> (x % 3 = 0) && (x % 5 <> 0))
    |> List.sum

let result6 = SumMultiplesOf3ButNot5 [1 .. 100]
```

### Output:

```
1 // val result6 : int = 1368
```

#### Remark:

- (x % 3 = 0): is x divisible by 3?
- (x % 5 <> 0): is x NOT a multiple of 5?

## Exercise (Euler Project Question 1)

Implement a function that sums up all multiples of 3 or 5 in a list.

```
let SumMultiplesOf3Or5 xList =

// Hint: || means OR, && means AND

// From 1 to 10, the multiples of 3 or 5 are 3, 5, 6, 9, 10

// 3 + 5 + 6 + 9 + 10 = 33

let result7 = SumMultiplesOf3Or5 [1 .. 10]

let result8 = SumMultiplesOf3Or5 [1 .. 999]
```

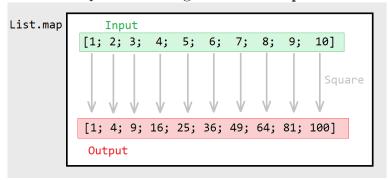
Remark: After you have completed this question, you can create an account an submit your solution here for personal achievement/accomplishment.

https://projecteuler.net/problem=1

## 3.3 List.map

```
let Square x = x * x
let result9 = List.map Square [1 .. 10]
```

The List.map function transform each individual element of a list using some transformation. The transformation is specified through a function Square.



Alternatively, we can use the fun keyword to define the Square function

```
let result10 = List.map (fun x \rightarrow x * x) [1 .. 100]
```

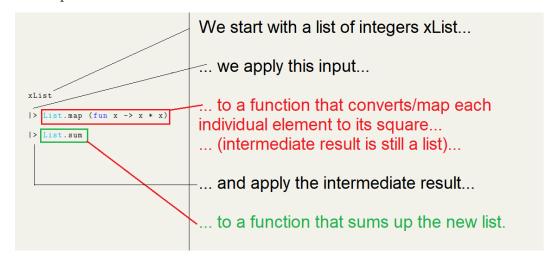
## List.map and Pipe-Forward |>

Let us look at an example:

```
let SumOfSquares xList =
    xList
    |> List.map (fun x -> x * x)
    |> List.sum

// 1^2 + 2^2 + 3^2 + 4^2 + ... + 10^2 = 385
let result11 = SumOfSquares [1 .. 10]
```

How to interpret the code:



#### Exercise

There are two supermarkets in town. One of them want to round the prices of each <u>individual</u> goods to the nearest dollar (might round-up or round-down). The other want to round DOWN the prices of each individual goods to the nearest dollar.

The functions System.Math.Floor, System.Math.Round\* are used round the prices:

```
let originalPrice1 = 1.35
let originalPrice2 = 3.99

let newPrice1 = originalPrice1 |> System.Math.Floor
let newPrice2 = originalPrice2 |> System.Math.Floor

// Temporary ignore decimal numbers like 1.50, 2.50.
let newPrice3 = originalPrice1 |> System.Math.Round
let newPrice4 = originalPrice2 |> System.Math.Round
```

#### Output:

```
val newPrice1 : float = 1.0
val newPrice2 : float = 3.0

val newPrice3 : float = 1.0
val newPrice4 : float = 4.0
```

\*Remark: We will temporary ignore decimals like 1.50, 2.50, because F# uses "Banker's Rounding" when tie-breaking is required. (Google it for more info)

1. Write a function that accepts a list of prices of the original products, and computes the final price of everything after each item are individually rounded-down.

```
// Round the prices to closest integer (ignore 1.50, 2.50,
    etc.)
let TotalPriceAfterRoundDown priceList =

// Implement your function here.
```

2. Write a function that accepts a list of prices of the original products, and computes the final price of everything after each item are individually rounded to the nearest integer (ignore 1.50, 2.50, etc.).

```
1 let TotalPriceAfterRound priceList =
2
3
4
5     // Implement your function here.
```

## **Application: Sample Variance**

We will try to implement the sample variance function (VAR.S in Excel 2010 or later, or see https://www.miniwebtool.com/sample-variance-calculator/).

Sample Variance = 
$$\frac{1}{N-1} \sum_{i=1}^{N} (x_i - \overline{x})^2$$

Remark: It is divided by N-1, not N, because of statistics reasons (Bessel's correction).

#### Remark:

- 1. We use the double function to convert an integer to decimal (you can also use it to process string to decimals, if the string is well defined)
- 2. At the last step, we divide by (N 1.0) and not (N 1) because we are working with decimals.
- 3. The compiler knows xList is a float list or List<float>, because at some point it interacted with \*\* 2.0.

```
let result12 = SampleVariance [1.0 .. 7.0]
// val result12 : double = 4.666666667
```

## Exercise (Euler Project Question 6)

Given a list of integers  $x_1, x_2, \ldots, x_n$ , write a function that calculates the following:

$$\left(\sum_{i=1}^{n} x_i\right)^2 - \left(\sum_{i=1}^{n} x_i^2\right)$$

If you want, you can use the following hint:

```
let ProjectEulerProblem6 xList =
    // if xList = [a;b;c], calculate a^2 + b^2 + c^2
    let sumOfSquares =

// if xList = [a;b;c], calculate a + b + c
let sum =

// return
(sum * sum) - sumOfSquares
```

To use the function:

```
let result13 = ProjectEulerProblem6 [1 .. 100]
printfn "Answer for ProjectEuler Problem6 is: %i" result13
```

Remark: After you have completed this question, you can create an account an submit your solution here for personal achievement/accomplishment.

https://projecteuler.net/problem=6

## Exercise (Euler Project Question 7)

You are given the following function that determines whether a positive integer x is a prime number or not. You can just directly use it. You do not need to implement it yourself.

```
let IsPrime x =
    let squareRoot = x |> double |> sqrt |> int
    if x = 1 then false
    else if x = 2 then true
    else if x % 2 = 0 then false
    else
        [3 .. 2 .. squareRoot]
        |> List.forall (fun i -> x%i <> 0)
// val IsPrime: x:int -> bool
```

Reminder: You can directly use the IsPrime function in the previous page. You do not need to re-implement it again.

https://projecteuler.net/problem=7

As mentioned in the URL, we want to find the 10001th prime number. We will start with a random guess of 500000.

1. Use the IsPrime function and the List.length function to determine how many prime numbers are between 2 and 500000.

```
1 let numberOfPrimesWithinRange =
2     [2 .. 500000]
3    |> .....
4
5
6     // Calculate how many primes are between 2 and 500000
7     // Use "IsPrime", and later "List.length"
```

Hopefully, you will get an answer of 41538.

This means that there are 41538 prime numbers between 2 and 500000, and so the 10001th prime number that we are looking for is also in this range (we could have chosen a smaller range, but 2 to 500000 is good enough).

2. The List.item function can be used to extract an item at an index/location. However, be careful that index/locations are 0-based. e.g.

So, to find the 10001th element of a list, you need to use (List.item 10000).

3. Use IsPrime function and (List.item 10000) to find the 10001th prime number (which is between 2 to 500000).

```
1 let find10001thPrime =
2    [2 .. 500000]
3    |> ......
4
5
6    // Use "IsPrime", and later "List.item 10000"
```

Remark: After you have completed this question, you can create an account an submit your solution online for personal achievement/accomplishment.

## Exercise (Euler Project Question 10)

Reminder: Use the IsPrime function defined earlier. Do not re-implement IsPrime again. Problem: Write a function that takes in a list of integers, and calculates the sum of all the prime numbers in that list.

```
let Problem10_Version1 (xList: List<int>) =

2
3
4
5
6
7 // test:
8 let result1 = Problem10_Version1 [1 .. 9]
9 // 2 + 3 + 5 + 7 = 17.

10
11 let result2 = Problem10_Version1 [1 .. 99]
12 // 2 + 3 + 5 + 7 + 11 + ... + 83 + 89 + 97 = 1060.
```

However, if you try the following, you may potentially encounter an error:

```
let result3 = Problem10_Version1 [2 .. 2000000]
// ERROR!
// System.OverflowException: Arithmetic operation resulted
in an overflow.
```

...because there are too many numbers to sum up, and the int cannot handle large sums. A workaround is to use the System.Numerics.BigInteger (Java also has such Big-Integer standard library). We convert each individual prime number into a BigInteger before sum them all up.

```
open System.Numerics

let SumAllPrimes xList =
    xList
    |> List.filter (IsPrime)
    |> List.map (BigInteger)
    |> List.sum

// Remark: The code below can take 10 seconds, as this is not the most optimal algorithm.

let result17 = SumAllPrimes [2 .. 2000000]

printfn "The sum of all primes from 2 to 2000000 is: %A"
    result17
```

Remark: After you have completed this question, you can create an account an submit your solution here for personal achievement/accomplishment.

https://projecteuler.net/problem=10

## Optional Exercise (Try at home) (Euler Project Question 3)

https://projecteuler.net/problem=3

Given an integer Z, write a function that finds the largest prime factor of Z. e.g. The prime factors of 13195 are 5, 7, 13, 29, and so the largest for 13195 is 29.

### Problem Analysis

To find the largest prime factor for Z, we will first try to find all factors of Z (not necessarily prime factors) between 1 and  $\sqrt{Z}$ .

Let  $S_1 = \{a_1, \dots, a_n\}$  be all the factors of Z (not necessarily prime factors) between 1 and  $\sqrt{Z}$ . This set will always contain at least one element:  $a_1 = 1$ .

Let  $S_2 = \left\{ \frac{Z}{a_1}, \dots, \frac{Z}{a_n} \right\}$ . These are all the factors of Z between  $\sqrt{Z}$  and Z. This set

will always contain at least one element:  $\frac{Z}{\hat{z}} = Z$ .

And so,  $S_1 \cup S_2 = \left\{a_1, \dots, a_n, \frac{Z}{a_1}, \dots, \frac{Z}{a_n}\right\}$  are all the factor of Z (not necessarily prime factors). And we just need to find that out of this set  $S_1 \cup S_2$ , which number is the largest prime number.

- 1. Example:  $3 \times 7 = 21$ . The largest prime factor is  $7 > \sqrt{21} \approx 4.58$ .
- 2. Example:  $6 \times 11 = 66$ . The largest prime factor is  $11 > \sqrt{66} \approx 8.12$ .

#### Hints:

1. The function IsPrimeBigInteger is implemented for you. This is a slightly modified version of the IsPrime function that takes in a BigInteger as an input (as compared to an int). No need to re-implement this function.

```
let IsPrimeBigInteger x =
let squareRoot = x |> double |> sqrt |> BigInteger
if x = BigInteger(1) then false
else if x = BigInteger(2) then true
else if x % BigInteger(2) = BigInteger(0) then false
else
[BigInteger(3) .. BigInteger(2) .. squareRoot]
|> List.forall (fun i -> x%i <> BigInteger(0))
```

2. To determine whether x is divisible by y, when x, y are both BigIntegers, do the following:

```
x % y = BigInteger(0)
```

We cannot do x % y = 0, because we cannot <u>directly</u> compare a BigInteger with an integer.

```
open System. Numerics
 let FindLargestPrimeFactor (Z: BigInteger) =
      let approxSqrt = Z |> double |> sqrt |> BigInteger
      // Find factors of Z between [2 .. sqrt(Z)]
      // Not necessarily prime factors.
      let list1 =
          [BigInteger(2) .. approxSqrt]
          |> .....
          // Complete the logic above
      // Produce another list such that:
      // For each element "a" in list1, it gives "Z / a"
      let list2 =
          list1
          |> .....
18
19
          // Complete the logic above
20
21
      // List.append combines the two lists.
      let combinedList =
          List.append list1 list2
25
      // Choose only prime numbers from the combinedList, and
     find the maximum using List.max
      combinedList
27
      |> .....
      // Complete the logic above
1 let number1 = BigInteger(21)
2 let result18 = FindLargestPrimeFactor number1
3 // Expect result: 7
5 let number2 = BigInteger(66)
6 let result19 = FindLargestPrimeFactor number2
```

Remark: After you have completed this question, you can create an account an submit your solution online for personal achievement/accomplishment.

let number3 = BigInteger.Parse("600851475143")
let result20 = FindLargestPrimeFactor number3

7 // Expect result: 11

# 4 Tuples, Records, Discriminated Union

Key concept:

- 1. Tuple is a good data-structure for many things:
  - (a) To represents terms that goes together, e.g. 2-D coordinates, Year-Month, etc.
  - (b) For pattern matching, especially for pairwise operation or grouping operation.
  - (c) For testing out ideas quickly. (and use other data-structures after you have done testing)
- 2. You can directly extract the content of a tuple, and use underscore "\_" to ignore any part of the tuple that you don't need.

## 4.1 Tuples

A 2D-coordinate may look like this:

```
let point1 = (1.0, 2.0)
let point2 = (3.0, 4.0)
```

Hover your mouse on top of these two objects. Notice that the signature is float \* float. So these points have two coordinates, each of them are float or double

Output:

```
_1 // The first point is distance 2.236068 away from origin _2 // The second point is distance 5.000000 away from origin
```

Notice that we have an extraction process let (x,y) = point that helps us extract the contents of point (and save the contents into the variables x,y). In fact, we can directly do the extraction process in the function definition:

```
let DistanceFromOrigin2 (x,y) =
    sqrt (x ** 2.0 + y ** 2.0)
```

### Tuples of Different Type

We can mix tuples of different type (compared to list, which cannot contain elements of different types).

```
let mixedTuple1 = (1.0, "HELLO")
let mixedTuple2 = (1, "Hello", true)
```

If you hover your mouse on top of these, you will see that:

- The first tuple has signature float \* string
- The second tuple has signature int \* string \* bool

As before, we can extract the contents of the tuple using let.

```
let (extractedDecimal, extractedString) = mixedTuple1
printfn "The extracted decimal is: %f" extractedDecimal
printfn "The extracted string is: %s" extractedString

let (extractedInteger, extractedString2, extractedBool) =
    mixedTuple2
printfn "The extracted integer is: %i" extractedInteger
printfn "The extracted string is: %s" extractedString2
printfn "The extracted boolean is: %b" extractedBool
```

#### Output:

```
1 // The extracted decimal is: 1.000000
2 // The extracted string is: HELLO
3
4 // The extracted integer is: 1
5 // The extracted string is: Hello
6 // The extracted boolean is: true
```

If you only want to extract part of a tuple, you can use the underline "\_" to ignore any part of the tuple that you don't need.

```
let personalInfo = ("John", 21, 170.0)

let (extractedName,_,_) = personalInfo

printfn "The extracted name is: %s" extractedName
// The extracted name is: John
```

## Example

You are given data about the number of student in each class. The data is saved in a List<string \* int>. e.g. in the first list, Class A has 50 students, Class B has 40 students, etc.

```
let studentList =
    [("A",50); ("B", 40); ("C", 45); ("D", 48)]
let studentList2 =
    [("A", 40); ("B", 30); ("C", 20); ("D", 25); ("E", 29);
    ("F", 50)]
```

The following function helps to find the total number of students in those school:

#### Output:

```
1 // val totalStudent1 : int = 183
```

Of course, we can directly do the extraction process in the function definition:

## Output:

```
1 // val totalStudent2 : int = 194
```

#### Exercise

You are given data about how each student score in a class. e.g. In this class, Ali scored 85.0 points, Baba scored 95.0 points, etc.

```
let classScore1 =
    [("Ali", 85.0); ("Baba", 95.0); ("Charlie", 87.0); ("Dan", 92.0); ("Emily", 96.0); ("Fiona", 92.0)]
```

Write a function that accepts a list of names with their scores, and return the class average.

```
let ClassAverage (scores: List<string * double>) =

let ClassAverage (scores: List<string * double>) =

// Implement your function here.
// Hint: List.map and List.average
```

## Example

A country currently wants to implement a new tax system:

• COMMON: 5% tax

• IMPORTS: 10% tax

• ALCOHOL: 20% tax

A supermarket wants currently saves the data in a List<string \* double \* string>, where the first string is the product, the double is the original price before tax, and the last string is the product code. e.g.

```
let productList1 =
    [("Bread", 2.40, "COMMON");
    ("Beer", 10.20, "ALCOHOL");
    ("Swiss Chocolate", 8.20, "IMPORTS");
    ("Rice", 20.50, "COMMON");
    ("Red Wine", 30.00, "ALCOHOL");
    ("Australian Beef", 18.50, "IMPORTS")]
```

The following code will help calculate the total price after tax:

```
1 let TotalAfterTax (productList: List<string * double *</pre>
    string> ) =
     productList
      |> List.map (fun tuple ->
          let (_,priceBeforeTax,productType) = tuple
          // Data Extraction above!
          if productType = "COMMON" then
              1.05 * priceBeforeTax
          else if productType = "ALCOHOL" then
              1.20 * priceBeforeTax
10
          else
              1.10 * priceBeforeTax
      |> List.sum
let totalPrice = TotalAfterTax productList1
printfn "The final price after tax is: %.2f" totalPrice
```

Output:

```
The final price after tax is: 101.66
```

Again, we can move the extraction process into the function definition:

Notice that the values are extracted immediately after the fun keyword.

#### Exercise

A clothing store is planning to do a discount sale:

• CLEARANCE: 50% off.

• SHIRT: 30% off.

• JEANS: 20% off.

You are given a List<string \* double> that represents an item's product code and their original price. e.g. the customer below bought a clearance item, two shirts and two jeans.

```
let listOfClothes =
[ ("CLEARANCE", 70.0); ("SHIRT", 20.0); ("SHIRT", 40.0)
; ("JEANS", 55.0); ("JEANS", 79.9)]
```

Write a function that takes a list of items and their original price, and return the total price after discount.

```
let TotalAfterDiscount (priceList: List<string * double>) =

2
3
4
5
6
7
8
9
10
11
12  // Implement your function here.
```

The expected final price after discount is \$184.92

#### 4.2 List.allPairs

```
let allPairs1 = List.allPairs [1;2;3] ["A";"B"]
```

Output:

```
1 // val allPairs1 : (int * string) list =
2 // [(1, "A"); (1, "B");
3 // (2, "A"); (2, "B");
4 // (3, "A"); (3, "B")]
```

### Example

Given two lists  $S_1$  and  $S_2$ , we want to find the sum of all products  $a \times b$ , where  $a \in S_1, b \in S_2$ .

```
let SumOfAllPairProducts list1 list2 =
    List.allPairs list1 list2
    |> List.map (fun (x,y) -> x * y)
    |> List.sum

let list1 = [1;2;3]
    let list2 = [5;6]

let result2 = SumOfAllPairProducts list1 list2
    // val result2 : int = 66
```

We can also verify mathematically:

$$\sum_{x \in S_1} \sum_{y \in S_2} x \cdot y = \sum_{x \in S_1} \left[ x \cdot \left( \sum_{y \in S_2} y \right) \right] = \left( \sum_{y \in S_2} y \right) \cdot \left( \sum_{x \in S_1} x \right)$$

$$(1 + 2 + 3) \cdot (5 + 6) = 6 \times 11 = 66$$

### Exercise (Euler Project Question 9)

https://projecteuler.net/problem=9

Find the only Pythagorean triplet a, b, c that satisfy:

$$a < b < c$$
,  $a + b + c = 1000$ ,  $a^2 + b^2 = c^2$ 

### Hints:

For  $1 \le a \le 1000, 1 \le b \le 1000$ , let c = 1000 - a - b. Then select (a, b) such that:

$$c > 0 \qquad a^2 + b^2 = c^2$$

Once you have figured out the value of a, b, then you can calculate c = 1000 - a - b, and calculate  $a \times b \times c$ , and submit your answer online for personal achievement/accomplishment.

## Exercise (Euler Project Question 4)

https://projecteuler.net/problem=4

A palindromic number reads the same from left-to-right or right-to-left.

The largest palindromic number made from the product of two 2-digit numbers is  $9009 = 91 \times 99$ .

Find the largest palindrome made from the product of two 3-digit numbers.

You can use the following IsPalindrome function that is already implemented for you. You do not need to re-implement it.

Find the largest palindrome number which is a product of two 3-digit numbers  $a \times b$ , where  $100 \le a \le 999$ , and  $100 \le b \le 999$ 

```
let findProductPalindrome =
    List.allPairs [100 .. 999] [100 .. 999]
    // |> List.map (fun (a,b) -> .....)
    // |> .......

failwith "NOT YET IMPLEMENTED!"
```

Again, you can submit your answer online for personal achievement/accomplishment.

## 4.3 Discriminated Union and Matching

Using string to represent a data could potentially backfire, when we encounter a case that we have not noticed.

For example, we have seen the following example, where we determine how many shares to buy given the stock's performance.

However, we may have a scenario where another programmer may accidentally created a typo:

```
let numSharesToBuy1 = GetNumSharesToBuy "Outperform"

// Output:
// val numSharesToBuy1 : int = 0

// ERROR! We should buy more of this stock!
// But the typo prevents us from buying more stock.
```

On the other hand, we could also have another scenario where a new method is not yet implemented.

```
let numSharesToBuy2 =
    GetNumSharesToBuy "REALLY BAD PERFORMANCE"

// Output:
// val numSharesToBuy2 : int = 0

// ERROR! We should sell everything we have!
// But we have not included the "REALLY BAD PERFORMANCE" case.
```

The solution is to use discriminated union:

```
type StockPerformance =

UUTPERFORM
UNDERPERFORM
NEUTRAL
```

Here, StockPerformance is a special type/class that has only 3 elements. So, we can

redefine the function (and prevent and typo error)

```
let GetNumSharesToBuy2 performance =
     if performance = OUTPERFORM then
                  // buy 1000 shares
      else if performance = UNDERPERFORM then
          -1000 // sell 1000 shares
     else
          0
                  // hold.
9 let numSharesToBuy3 = GetNumSharesToBuy2 OUTPERFORM
let numSharesToBuy4 = GetNumSharesToBuy2 UNDERPERFORM
11 let numSharesToBuy5 = GetNumSharesToBuy2 NEUTRAL
_{13} // val numSharesToBuy3 : int = 1000
_{14} // val numSharesToBuy4 : int = -1000
15 // val numSharesToBuy5 : int = 0
17 // And we do not need to worry about typo error:
18 let numSharesError = GetNumSharesToBuy2 outperform
19 // ERROR! "outperform" is not defined!
20 // Do you mean "OUTPERFORM"?
21 "ERROR!
```

### Pattern Matching

On the other hand, we can replace the if/else using pattern matching (a little bit similar to the switch statement from Java/C++).

```
let GetNumSharesToBuy3 performance =
match performance with
l OUTPERFORM -> 1000
l UNDERPERFORM -> -1000
l NEUTRAL -> 0

let numSharesToBuy6 = GetNumSharesToBuy3 OUTPERFORM
let numSharesToBuy7 = GetNumSharesToBuy3 UNDERPERFORM
let numSharesToBuy8 = GetNumSharesToBuy3 NEUTRAL
```

The benefit of using pattern matching is that Intellisense will suggest to you that you may miss out specific case if you did not complete all discriminated union case. For example, if you update the StockPerformance by adding one more line:

```
type StockPerformance =

UUTPERFORM
UNDERPERFORM
NEUTRAL
REALLYBAD
```

Notice that we have added an extra line: REALLYBAD. As a result, the code with pattern match below will have a warning:

```
let GetNumSharesToBuy3 performance =

match performance with

OUTPERFORM ->

UNDERPERFORM -

NEUTRAL -> 0

was performance: StockPerformance

Incomplete pattern matches on this expression. For example, the value 'REALLYBAD' may indicate a case not covered by the pattern(s).
```

# 4.4 Record Type

# 5 Fold, Scan, State

Key concept:

- 1. The fold and scan functions are used to keep track of states.
  - It can be considered as eliminating a lot of intermediate steps, where the number of intermediate steps may change based on the length of the list.
  - It is somewhat similar to using a mutable state, but less things to keep track of.

## 5.1 Example of folding

Let us look at an example:

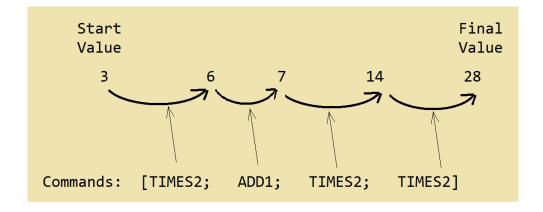
Here, Commands is a discriminated union (i.e. an abstract data type) that only has two different possible values. So, it is a little bit safer than using a list of strings (because strings can take on a lot of values)

```
let ChangingFunction prevResult currentCommand =
    match currentCommand with
    | TIMES2 -> prevResult * 2
    | ADD1 -> prevResult + 1

let startingValue = 3
```

Here, ChangingFunction tells us how to modify a value based on the Commands accepted.

```
let result1 =
List.fold ChangingFunction startValue listOfCommands1
// val result1 : int = 28
```



Here, we have a startValue of 3, and we go through the listOfCommands1 and evolve the startValue based on the ChangingFunction.

An equivalent implementation would be the following:

Or if we use mutable, then:

```
let result1_version3 =
let mutable valueSoFar = startValue
for command in listOfCommands1 do
let updatedValue =
ChangingFunction valueSoFar command
valueSoFar <- updatedValue
// return
valueSoFar</pre>
```

This is most similar to codes that you may write in Java/C++

Warning: If you use VisualStudio /VisualStudioCode, you may see that valueSoFar is highlighted yellow in your editor, as a warning that there is a mutable value in our program. As mentioned before, F# discourages the usage of mutable values.

# A Appendix

# A.1 Optional Topics

#### A.1.1 inline functions

On some occasion, if you need to use the same function on different type which supports (\*), then you can use the inline keyword.

```
let inline Product x y = x * y

let multiply2Int = Product 2 3

printfn "Multiply the two numbers gives: %i" multiply2Int

// Output: "Multiply the two numbers gives: 6"

let multiply2Double = Product 3.0 4.0

printfn "Multiply the two numbers gives: %f"
    multiply2Double

// Output: "Multiply the two numbers gives: 12.000000"
```

However, not every datatype supports multiplication (\*)

```
let multiply2WordsError = Product "word1" "word2"
   "ERROR!!!!!!!!"
```

#### INPUT PICTURE HERE!

Similarly, we can do this:

```
let inline CustomAdd x y z = x + y + z
let add3IntegerResult = CustomAdd 4 5 6
printfn "Adding the three integers give: %i"
    add3IntegerResult

// Output: "Adding the three integers give: 15"

let add3StringResult = CustomAdd "John " "F." " Kennedy"
printfn "Concatenate the three strings give: %s"
    add3StringResult

// Output:
// "Concatenate the three strings give: John F. Kennedy"

let add3DecimalResult = CustomAdd 10.3 10.2 10.1
printfn "Adding the three decimals give: %f"
    add3DecimalResult
// Output: "Adding the three decimals give: 30.600000"
```

However, not every datatype supports addition (+)

```
let add3BooleanError = CustomAdd true false false
"ERROR!!!!!!!!"
```

INPUT PICTURE HERE!