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Homework 2 – Q5

To match the sequence expression provided, x is a sequence with the length $5 - 3 + 1 = 3$, and we write it as $\langle a, b, c \rangle$. Then, we find the polynomials corresponding to sequences $\langle a, b, c \rangle$ and $\langle 1, 1, -1 \rangle$ and multiply them.

$$\begin{aligned} & (a + bx + cx^2) \cdot (1 + x - x^2) \\ &= a + bx + cx^2 + ax + bx^2 + cx^3 - ax^2 - bx^3 - cx^4 \\ &= a + (a + b)x + (b + c - a)x^2 + (c - b)x^3 - cx^4 \end{aligned}$$

Equate the coefficients of this polynomials with the terms of the sequence $\langle 1, 0, -1, 2, -1 \rangle$. We can work out that $a = 1, b = -1, c = 1$.

So, the sequence x is $\langle 1, -1, 1 \rangle$.