# Package 'mpersonalized'

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Type Package

Title What the Package Does (Title Case)

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<b>Description</b> Implements a general framework to solve the problem of personalized medicine in meta-analysis and multiple outcomes. This framework allows either separate rules for each study/outcome or a single rule for all the studies/outcomes, depending on the requirement of user. A flexible choice of penalty functions to increase estimation efficiency is also provided.
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R topics documented:
admm_optim       2         lambda_estimate       2         mpersonalized       2         mpersonalized_cv       5         plot.mp       8         plot.mp_cv       8         predict.mp       9         predict.mp_cv       9         simulated_dataset       10
Index 12

2 mpersonalized

admm_optim	ADMM Algorithm for Meta-analysis/Multiple Outcomes Personalized Medicine	
admm_optim		

#### Usage

```
admm_optim(x, y, p, q, lambda1, lambda2, lambda3, abs.tol = 1e-05,
rel.tol = 1e-05, maxit = 500L, rho = NULL)
```

lambda\_estimate

Default Penalty Parameter Sequence if Not Given

#### **Usage**

```
lambda_estimate(modelXlist, modelYlist, penalty, single_rule, alpha,
   num_lambda1, num_lambda2, num_single_rule_lambda)
```

# **Arguments**

modelXlist the Xlist in contrast framework after standardization modelYlist the Ylist in contrast framework after standardization

penalty penalty type

single\_rule whether a single treatment rule is required

#### Value

estimated lambda for required penalty if not provided

mpersonalized A General Framework to Solve Personalized Medicine in the Settings of Meta-analysis/Multiple Outcomes

# Usage

```
mpersonalized(problem = c("meta-analysis", "multiple outcomes"), X, Trt,
   P = NULL, Xlist, Ylist, Trtlist, Plist = replicate(length(Xlist), NULL,
   simplify = FALSE), typelist = replicate(length(Xlist), "continuous",
   simplify = FALSE), penalty = c("none", "lasso", "GL", "SGL", "fused",
   "lasso+fused", "GL+fused", "SGL+fused"), lambda1 = NULL, lambda2 = NULL,
   single_rule_lambda = NULL, num_lambda1 = ifelse(!is.null(lambda1),
   length(lambda1), 10), num_lambda2 = ifelse(!is.null(lambda2),
   length(lambda2), 10),
   num_single_rule_lambda = ifelse(!is.null(single_rule_lambda),
   length(single_rule_lambda), 50), alpha = NULL, single_rule = FALSE,
   admm_control = NULL, contrast_builder_control = NULL)
```

mpersonalized 3

#### **Arguments**

problem A character string specifiy whether the user want to solve "meta-analysis" or "multiple outcomes" problem. For problem = "meta-analysis", the user should also supply Xlist, Ylist, Trtlist. For problem = "multiple outcomes", the user should supply X, Ylist, Trt. Χ Covariate matrix that should be supplied when problem = "multiple outcomes" with rows indicating subjects and columns indicating covariates. Trt Treatment vector that should be supplied when problem = "multiple outcomes", which should be coded as 0 or 1. Ρ Propensity score vector when problem = "multiple outcomes". If not supplied, then study is treated as randomzied trial and the propensity score is estimated as the proportion of 1's in Trt for every subject. A list object that should be supplied when problem = "meta-analysis", with Xlist kth element denoting the covariate matrix of study k. When problem = "meta-analysis", Ylist should be a list object with kth ele-Ylist ment denoting the response vector of study k. When problem = "multiple outcomes", Ylist should be a list object with kth element denoting the kth outcome. Trtlist A list object that should be supplied when problem = "meta-analysis", with kth element denoting the treatment vector of study k (coded as 0 or 1). Plist A list object that should be supplied when problem = "meta-analysis", with kthe element denoting the propensity score vector of study k. If not supplied, then each study is treated as randomized trial and the corresponding propensity score is estimated as the proportion of 1's in the kth element of Trtlist for all subjects. For different rules, the penalty could be "none", "lasso", "GL", "SGL", "fused", penalty "lasso+fused", "GL+fused", "SGL+fused". For single rule, the penalty could be "none" or "lasso". User should always input penalty and then supply correponding penalty parameters sequence if needed. Default option is "none". lambda1  $\lambda_1$  in the framework of different rules. If not supplied, a default sequence will be computed.  $\lambda_2$  in the framework of different rules. If not supplied, a default sequence will lambda2 be computed. single\_rule\_lambda  $\lambda_{single}$  in the framework of single rule. num\_lambda1 If lambda1 is not specified by user, user could still specify the length of the lambda1 sequence. The default length is 10. If lambda2 is not specified by user, user could still specify the length of the num\_lambda2 lambda2 sequence. The default length is 10. num\_single\_rule\_lambda If single\_rule\_lambda is not specified, user could still specify the length of the single\_rule\_lambda sequence. The default length is 50. alpha  $\alpha$  in the framework of different rules. If not supplied, a default value will be used depending on penalty. single\_rule A logical value, whether the single treatment framework is used. Deafult is FALSE.

4 mpersonalized

admm\_control

A list of parameters which user can specify to control the admm algorithm. In admm\_control, the following parameters can be supplied: abs.tol, absolute tolerance; rel.tol, relative tolerance; maxit, maximum number of iterations; rho, Lagrangian parameter.

contrast\_builder\_control

A list of parameters which user can specify to control estimation of contrast function. In contrast\_builder\_control, the following parameters could be supplied: response\_model, this could be "lasso" or "linear"; contrast\_builder\_folds, the number of folds used in cross validation when response\_model = "lasso".

typlelist

A list object with kth element denoting the type of outcome corresponding to the kth element in Ylist. Each element could be "continuous" or "binary".

#### **Details**

Assume the total number of studies/outcomes is K and we denote the contrast estimator for the kth study/outcome as  $\hat{C}_k$  and the corresponding recommendation rule as  $g_k$ .

If we want different rules for each study/outcome, this function solves meta-analysis/multiple outcomes problems for personalized medicine based on the framework

$$\min_{g_1, \dots, g_K} \frac{1}{2} \sum_{k=1}^K \sum_{i=1}^{n_k} \frac{|\hat{C}_k(X_i)|}{\sum_{i=1}^{n_k} |\hat{C}_k(X_i)|} \left[ 1\{\hat{C}_k(X_i) > 0\} - g_k(X_i) \right]^2 + h(g_1, \dots, g_K)$$

Here the regularization function h is of the form of a sum of sparse group lasso and fused lasso penalty

$$h = (1 - \alpha)\lambda_1 \sqrt{q} \sum_{j=1}^p \|\beta_j\|_2 + \alpha \lambda_1 \sum_{j=1}^p \|\beta_j\|_1 + \lambda_2 \sum_{j=1}^p \sum_{1 \le a < b \le K} |\beta_{ja} - \beta_{jb}|$$

where  $\boldsymbol{\beta_j} = (\beta_{j1}, \dots, \beta_{jK})$ 

By setting  $\lambda_1, \lambda_2, \alpha$  differently, different penalties can be obtained.

- If  $\lambda_1, \lambda_2 \neq 0$  and  $\alpha \neq 0$  or 1, the penalty is "SGL+fused".
- If  $\lambda_1, \lambda_2 \neq 0$  and  $\alpha = 0$ , the penalty is "GL+fused".
- If  $\lambda_1, \lambda_2 \neq 0$  and  $\alpha = 1$ , the penalty is "lasso+fused".
- If  $\lambda_1 = 0, \lambda_2 \neq 0$ , the penalty is "fused".
- If  $\lambda_1 \neq 0, \lambda_2 = 0$  and  $\alpha \neq 0$  or 1, the penalty is "SGL".
- If  $\lambda_1 \neq 0, \lambda_2 = 0$  and  $\alpha = 0$ , the penalty is "GL".
- If  $\lambda_1 \neq 0, \lambda_2 = 0$  and  $\alpha = 1$ , the penalty is "lasso".
- If  $\lambda_1, \lambda_2 = 0$ , there is no penalty.

On the other hand, if we would like to fit a single rule for all studies/outcomes, we let  $g_1 = \ldots = g_K$  and solve the following problem instead

$$\min_{g} \frac{1}{2} \sum_{k=1}^{K} \sum_{i=1}^{n_k} \frac{|\hat{C}_k(X_i)|}{\sum_{i=1}^{n_k} |\hat{C}_k(X_i)|} \left[ 1\{\hat{C}_k(X_i) > 0\} - g(X_i) \right]^2 + h(g_1, \dots, g_K) + \lambda_{single} \|\beta\|_1$$

Depending on the value of  $\lambda_{single}$ 

- If  $\lambda_{single} \neq 0$ , the penalty is "lasso".
- If  $\lambda_{single} = 0$ , there is no penalty.

mpersonalized\_cv 5

#### Value

An S3 object of class "mp", which contains the information of the fitted model. It could be supplied to some other functions in mperosnalized package for further analysis or prediction.

```
penalty_parameter_sequence configuration of the penalty parameters. interceptlist kth element corresponds to the kth row in penalty_parameter_sequence. betalist kth element corresponds to the kth row in penalty_parameter_sequence. number_covariates number_studies_or_outcomes
```

problem = "meta-analysis" or number of outcomes if problem = "multiple outcomes".

# Examples

mpersonalized\_cv

Cross Validation for mpersonalized

#### Usage

```
mpersonalized_cv(problem = c("meta-analysis", "multiple outcomes"), X, Trt,
   P = NULL, Xlist, Ylist, Trtlist, Plist = replicate(length(Xlist), NULL,
   simplify = FALSE), typelist = replicate(length(Xlist), "continuous",
   simplify = FALSE), penalty = c("lasso", "GL", "SGL", "fused", "lasso+fused",
   "GL+fused", "SGL+fused"), lambda1 = NULL, lambda2 = NULL,
   single_rule_lambda = NULL, num_lambda1 = ifelse(!is.null(lambda1),
   length(lambda1), 10), num_lambda2 = ifelse(!is.null(lambda2),
```

6 mpersonalized\_cv

```
length(lambda2), 10),
num_single_rule_lambda = ifelse(!is.null(single_rule_lambda),
length(single_rule_lambda), 50), alpha = NULL, single_rule = FALSE,
cv_folds = 5, admm_control = NULL, contrast_builder_control = NULL)
```

# **Arguments**

Suments	
problem	A character string specifiy whether the user want to solve "meta-analysis" or "multiple outcomes" problem. For problem = "meta-analysis", the user should also supply Xlist, Ylist, Trtlist. For problem = "multiple outcomes", the user should supply X, Ylist, Trt.
Χ	Covariate matrix that should be supplied when problem = "multiple outcomes" with rows indicating subjects and columns indicating covariates.
Trt	Treatment vector that should be supplied when problem = "multiple outcomes", which should be coded as 0 or 1.
Р	Propensity score vector when problem = "multiple outcomes". If not supplied, then study is treated as randomzied trial and the propensity score is estimated as the proportion of 1's in Trt for every subject.
Xlist	A list object that should be supplied when problem = "meta-analysis", with $k$ th element denoting the covariate matrix of study $k$ .
Ylist	When problem = "meta-analysis", Ylist should be a list object with $k$ th element denoting the response vector of study $k$ . When problem = "multiple outcomes" Ylist should be a list object with $k$ th element denoting the $k$ th outcome.
Trtlist	A list object that should be supplied when problem = "meta-analysis", with $k$ th element denoting the treatment vector of study $k$ (coded as 0 or 1).
Plist	A list object that should be supplied when problem = "meta-analysis", with $k$ the element denoting the propensity score vector of study $k$ . If not supplied, then each study is treated as randomized trial and the corresponding propensity score is estimated as the proportion of 1's in the $k$ th element of Trtlist for all subjects.
penalty	For different rules, the penalty could be "lasso", "GL", "SGL", "fused", "lasso+fused", "GL+fused", "SGL+fused". For single rule, the penalty could only be "lasso". For penalty = "none", use function mpersonalized instead. User should always input penalty and then supply correponding penalty parameters sequence if needed.
lambda1	$\lambda_1$ in the framework of different rules. If not supplied, a default sequence will be computed.
lambda2	$\lambda_2$ in the framework of different rules. If not supplied, a default sequence will be computed.
single_rule_l	
	$\lambda_{single}$ in the framework of single rule.
num_lambda1	If lambda1 is not specified by user, user could still specify the length of the

num\_lambda1 If lambda1 is not specified by user, user could still specify the length of the lambda1 sequence. The default length is 10.

If lambda2 is not specified by user, user could still specify the length of the lambda2 sequence. The default length is 10.

num\_single\_rule\_lambda

num\_lambda2

If single\_rule\_lambda is not specified, user could still specify the length of the single\_rule\_lambda sequence. The default length is 50.

mpersonalized\_ev 7

alpha  $\alpha$  in the framework of different rules. If not supplied, a default value will be

used depending on penalty.

single\_rule A logical value, whether the single treatment framework is used. Deafult is

FALSE.

cv\_folds Number of folds needed for cross-validation. Default is 5

admm\_control A list of parameters which user can specify to control the admm algorithm. In

admm\_control, the following parameters can be supplied: abs.tol, absolute tolerance; rel.tol, relative tolerance; maxit, maximum number of iterations;

rho, Lagrangian parameter.

contrast\_builder\_control

A list of parameters which user can specify to control estimation of contrast function. In contrast\_builder\_control, the following parameters could be supplied: response\_model, this could be "lasso" or "linear"; contrast\_builder\_folds,

the number of folds used in cross validation when response\_model = "lasso".

typlelist A list object with kth element denoting the type of outcome corresponding to

the *k*th element in Ylist. Each element could be "continuous" or "binary".

#### **Details**

This function implments mpersonalized but use cross validatation for the tuning of penalty parameter. The optimal penalty parameter is selected by minimizing

$$\sum_{i=1}^{n_k} \frac{|\hat{C}_k(X_i)|}{\sum_{i=1}^{n_k} |\hat{C}_k(X_i)|} \left[ 1\{\hat{C}_k(X_i) > 0\} - g_k(X_i) \right]^2$$

in the leave-out fold, where  $\hat{C}_k(X_i)$  in the leave-out fold is separately estimated from the training set.

# Value

An S3 object of class "mp\_cv", which contains the information of the model with the optimal lambda. It can be supplied to some other functions in mperosnalized package for further analysis or prediction.

penalty\_parameter\_sequence

configuration of the penalty parameters.

opt\_penalty\_parameter

interccept

\teimbeta The coefficient matrix corresponding to the optimal penalty parameter.

number\_covariates

number\_studies\_or\_outcomes

problem = "meta-analysis" or number of outcomes if problem = "multiple outcomes".

8 plot.mp\_cv

	_	
р	lot	. mp

Plot for a 'mp' Class Object.

#### **Usage**

```
## S3 method for class 'mp'
plot(mp, ind1, ind2, single_ind)
```

#### **Arguments**

mp the 'mp' class object returned by mpersonalzied function

ind1 the index of the lambda1 if different rules are used ind2 the index of the lambda2 if different rules are used

single\_ind the index of the single\_rule\_lambda if an single rule is used

#### **Details**

This function plots the results for estimated treatment effects. Depending on the received treatment and recommended treatment, the group means of the outcome are computed and the relations between them are plotted. This plot provides a sanity check of the treatment recommendation rule. By specifying the index of the penalty parameters, we can obtain the plots of the corresponding treatment recommendation rule.

#### Value

a list object with kth element denoting the plot of study k

```
plot.mp_cv
```

Plot for a 'mp' Class Object.

# Usage

```
## S3 method for class 'mp_cv'
plot(mp_cv)
```

#### **Arguments**

mp\_cv

the 'mp\_cv' class object returned by mpersonalzied\_cv function

#### **Details**

This function plots the results for estimated treatment effects by using the estimated optimal treatment recommendation rule obtained from corss validation.

# Value

a list object with kth element denoting the plot of study  $\mathbf{k}$ 

predict.mp 9

#### **Description**

This function predict the benefit scores and optimal treatment for new patients

#### Usage

```
## S3 method for class 'mp'
predict(mp, newx = NULL, weight = NULL, overall_rec = TRUE)
```

# **Arguments**

mp the fitted "mp" object returned by "mpersonalized"

news the covariate matrix of the new patients. If news = NULL, then the prediction is

made for each data set based on the rule of that study/outcome.

weight a weight vector for the overall recommendation. If leave as NULL, a equally

weighted recommendation will be made.

overall\_rec a logical value. If TRUE, an overall recommendation will be made weighted by

the "weight" parameter.

#### Value

a list of results with each element in the list corresponding to the prediciton by each different penalty parameter. Each element in this list contains:

treatment recommended treatment for each patient for each study/outcome. If overall\_rec = TRUE,

the weighted overall recommended treatment will be computed as well. If the overall recommend treatment is equal to 0.5, it means the sum of weight is

equal for 0 and 1.

benefit\_score  $\ \ \$  the benefit score computed from  $g_1,\ldots,g_K$ 

# Description

This function predict the benefit scores and optimal treatment for new patients

### Usage

```
## S3 method for class 'mp_cv'
predict(mp_cv, newx = NULL, weight = NULL,
    overall_rec = TRUE)
```

10 simulated\_dataset

#### **Arguments**

mp\_cv the fitted "mp\_cv" object returned from "mpersonalized\_cv" function

newx the covariate matrix of the new patients. If newx = NULL, then the prediction is

made for each data set based on the rule of that study/outcome.

weight a weight vector for the overall recommendation. If leave as NULL, a equally

weighted recommendation will be made.

overall\_rec a logical value. If TRUE, an overall recommendation will be made weighted by

the "weight" parameter.

#### Value

the prediciton by using the optimal penalty parameter selected by cross validation. It contains:

treatment recommended treatment for each patient for each study/outcome. If overall\_rec = TRUE,

the weighted overall recommended treatment will be computed as well. If the overall recommend treatment is equal to 0.5, it means the sum of weight is

equal for 0 and 1.

benefit\_score the benefit score computed from  $g_1, \ldots, g_K$ 

#### **Description**

Generate a simulated dataset, which could be used to demonstrate the features of the mpersonalized package.

# Usage

simulated\_dataset(n, problem = c("meta-analysis", "multiple outcomes"))

#### **Arguments**

n Sample size for each study/outcome.

problem A character string specified what problem the simulated dataset is generated for.

problem can be set to "meta-analysis" or "multiple outcomes".

#### Details

In the simulated dataset, outcomes are generated from the model

$$Y = \delta_0 + X\delta + A(\theta_0 + X\theta) + \epsilon,$$

where X is the baseline covariates and A is the treatment indicator coded as 0,1. For different outcomes or studies, values of  $\delta_0$ ,  $\delta$ ,  $\theta_0$  and  $\theta$  are also different so as to represent the heterogeneity in real problems.

The number of different studies/outcomes is set to be 6 and total number of candidate covariates is 50. Treatment indicator A is generated with equal probability of 0 or 1.

This function randomly generates the coefficients for each study/outcome and then generates the baseline covariates and error term for each subject. Depending on the value of problem, generation of baseline covariates are slightly different. For problem = "meta-analysis", baseline covariates are generated independently for each study; for problem = "multiple outcomes", baseline covariates are the same across different outcomes.

simulated\_dataset 11

#### Value

A list object of the ingredients from the simulated dataset. The elements of this list depends on value of problem.

For problem = "meta-analysis",

Xlist a list object with kth element denoting the baseline covariate matrix of kth study

Ylist a list object with kth element denoting the response vector of kth study

Trtlist a list object with kth element denoting the treatment vector of kth study and

coded as 0 or 1

B the coefficient matrix containing  $\delta_0$ ,  $\delta$ ,  $\theta_0$  and  $\theta$ 

For problem = "multiple outcomes",

X a matrix object denoting the baseline covariate matrix

Ylist a list object with kth element denoting the response vector of kth outcome

Trt a vector denoting the treatment and coded as 0 or 1) B the coefficient matrix containing  $\delta_0$ ,  $\delta$ ,  $\theta_0$  and  $\theta$ 

# **Examples**

```
set.seed(123)
sim_dat = simulated_dataset(200, problem = "meta-analysis")
str(sim_dat$Xlist)
str(sim_dat$Ylist)
str(sim_dat$Trtlist)
set.seed(NULL)
```

# **Index**

```
admm_optim, 2
lambda_estimate, 2
mpersonalized, 2
mpersonalized_cv, 5
plot.mp, 8
plot.mp_cv, 8
predict.mp, 9
predict.mp_cv, 9
simulated_dataset, 10
```