# Package 'mpersonalized'

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tle An R Package for Personalized Medicine in Meta-analysis and Multiple Outcomes			
0.1.0			
Chensheng Kuang			
ner Chensheng Kuang <ckuang@wisc.edu></ckuang@wisc.edu>			
ion Implements a general framework to solve the problem of personalized medicine meta-analysis and multiple outcomes. This framework allows either separate rules each study/outcome or a single rule for all the studies/outcomes, depending on the uirement of user. A flexible choice of penalty functions to increase estimation ciency is also provided.			
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coef.mp

Coefficients of a Fitted "mp" Object

# **Description**

This function provides coef method for "mp" class objects.

### Usage

```
## S3 method for class 'mp'
coef(mp)
```

# Arguments

mp

A fitted "mp" object returned by "mpersonalized".

### Value

A list object. Each element in the list is the fitted coefficients corresponding to one penalty parameter value in mp\$penalty\_parameter\_sequence.

# **Examples**

coef.mp\_cv

Coefficients of a Fitted "mp\_cv" Object

# **Description**

This function provides coef method for "mp\_cv" class objects.

# Usage

```
## S3 method for class 'mp_cv'
coef(mp_cv)
```

### **Arguments**

mp\_cv

A fitted "mp" object returned by "mpersonalized".

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#### Value

The fitted coefficients corresponding to the optimal penalty parameter.

### **Examples**

mpersonalized

A General Framework to Solve Personalized Medicine in the Settings of Meta-analysis/Multiple Outcomes

### **Description**

This function solves the personalized medicine problem by extending the contrast classification framework (Zhang, 2012). By adding proper penalty to the original classification loss, variable selection could be implemented and estimation efficiency could be improved. Computation algorithm differs based on the penalty function employed, but mainly through ADMM algorithm, glmnet package and SGL package. This function is also flexible enough to let user choose whether different classification rules or a single rule should be estimated for multiple studies/outcomes.

# Usage

```
mpersonalized(problem = c("meta-analysis", "multiple outcomes"), X, Trt,
   P = NULL, Xlist, Ylist, Trtlist, Plist = replicate(length(Xlist), NULL,
   simplify = FALSE), typelist = replicate(length(Xlist), "continuous",
   simplify = FALSE), penalty = c("none", "lasso", "GL", "SGL", "fused",
   "lasso+fused", "GL+fused", "SGL+fused"), lambda1 = NULL, lambda2 = NULL,
   single_rule_lambda = NULL, num_lambda1 = ifelse(!is.null(lambda1),
   length(lambda1), 10), num_lambda2 = ifelse(!is.null(lambda2),
   length(lambda2), 10),
   num_single_rule_lambda = ifelse(!is.null(single_rule_lambda),
   length(single_rule_lambda), 50), alpha = NULL, single_rule = FALSE,
   admm_control = NULL, contrast_builder_control = NULL)
```

### **Arguments**

problem

A character string specifiy whether user want to solve "meta-analysis" or "multiple outcomes" problem. For problem = "meta-analysis", user should also supply Xlist, Ylist, Trtlist. For problem = "multiple outcomes", user should supply X, Ylist, Trt.

Χ

Covariate matrix that should be supplied when problem = "multiple outcomes" with rows indicating subjects and columns indicating covariates.

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Trt Treatment vector that should be supplied when problem = "multiple outcomes", which should be coded as 0 or 1. Propensity score vector when problem = "multiple outcomes". If not sup-Ρ plied, then study is treated as randomzied trial and the propensity score is estimated as the proportion of 1's in Trt for every subject. Xlist A list object that should be supplied when problem = "meta-analysis", with kth element denoting the covariate matrix of study k. Ylist When problem = "meta-analysis", Ylist should be a list object with kth element denoting the response vector of study k. When problem = "multiple outcomes", Ylist should be a list object with kth element denoting the kth outcome. A list object that should be supplied when problem = "meta-analysis", with Trtlist kth element denoting the treatment vector of study k (coded as 0 or 1). Plist A list object that should be supplied when problem = "meta-analysis", with kthe element denoting the propensity score vector of study k. If not supplied, then each study is treated as randomized trial and the corresponding propensity score is estimated as the proportion of 1's in the kth element of Trtlist for all subjects. A list object with kth element denoting the type of outcome corresponding to typelist the kth element in Ylist. Each element could be "continuous" or "binary". For different rules, the penalty could be "none", "lasso", "GL", "SGL", "fused", penalty "lasso+fused", "GL+fused", "SGL+fused". For single rule, the penalty could be "none" or "lasso". User should always input penalty and then supply correponding penalty parameters sequence if needed. Default option is "none". lambda1  $\lambda_1$  in the framework of different rules. If not supplied, a default sequence will be computed. lambda2  $\lambda_2$  in the framework of different rules. If not supplied, a default sequence will be computed. single\_rule\_lambda  $\lambda_{single}$  in the framework of single rule. num\_lambda1 If lambda1 is not specified by user, user could still specify the length of the lambda1 sequence. The default length is 10. num\_lambda2 If lambda2 is not specified by user, user could still specify the length of the lambda2 sequence. The default length is 10.  ${\tt num\_single\_rule\_lambda}$ If single\_rule\_lambda is not specified, user could still specify the length of the single\_rule\_lambda sequence. The default length is 50.  $\alpha$  in the framework of different rules. If not supplied, a default value will be alpha used depending on penalty. single\_rule A logical value, whether the single rule framework is used. Deafult is FALSE. admm\_control A list of parameters which user can specify to control the admm algorithm. In admm\_control, the following parameters can be supplied: abs.tol, absolute tolerance; rel.tol, relative tolerance; maxit, maximum number of iterations; rho, Lagrangian parameter. contrast\_builder\_control A list of parameters which user can specify to control estimation of contrast function. In contrast\_builder\_control, the following parameters could be

supplied: eff\_aug, a logical value whether efficiency augmentation should be implemented; response\_model, a character string specify what outcome model

the number of folds used in cross validation when response\_model = "lasso".

to use if eff\_aug = TRUE, response\_model could be "lasso" or "linear"; contrast\_builder\_folds,

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#### **Details**

Assume the total number of studies/outcomes is K and we denote the contrast estimator for the kth study/outcome as  $\hat{C}_k$  and the corresponding recommendation rule as  $g_k$ .

If we want different rules for each study/outcome, this function solves meta-analysis/multiple outcomes problems for personalized medicine based on the framework

$$\min_{g_1,\dots,g_K} \frac{1}{2} \sum_{k=1}^K \sum_{i=1}^{n_k} \frac{|\hat{C}_k(X_i)|}{\sum_{i=1}^{n_k} |\hat{C}_k(X_i)|} \left[ 1\{\hat{C}_k(X_i) > 0\} - g_k(X_i) \right]^2 + h(g_1,\dots,g_K)$$

Here the regularization function h is of the form of a sum of sparse group lasso and fused lasso penalty

$$h = (1 - \alpha)\lambda_1 \sqrt{q} \sum_{j=1}^p \|\beta_j\|_2 + \alpha \lambda_1 \sum_{j=1}^p \|\beta_j\|_1 + \lambda_2 \sum_{j=1}^p \sum_{1 \le a < b \le K} |\beta_{ja} - \beta_{jb}|$$

where  $\beta_j = (\beta_{j1}, \dots, \beta_{jK})$ 

By setting  $\lambda_1, \lambda_2, \alpha$  differently, different penalties can be obtained.

- If  $\lambda_1, \lambda_2 \neq 0$  and  $\alpha \neq 0$  or 1, the penalty is "SGL+fused".
- If  $\lambda_1, \lambda_2 \neq 0$  and  $\alpha = 0$ , the penalty is "GL+fused".
- If  $\lambda_1, \lambda_2 \neq 0$  and  $\alpha = 1$ , the penalty is "lasso+fused".
- If  $\lambda_1 = 0, \lambda_2 \neq 0$ , the penalty is "fused".
- If  $\lambda_1 \neq 0, \lambda_2 = 0$  and  $\alpha \neq 0$  or 1, the penalty is "SGL".
- If  $\lambda_1 \neq 0, \lambda_2 = 0$  and  $\alpha = 0$ , the penalty is "GL".
- If  $\lambda_1 \neq 0, \lambda_2 = 0$  and  $\alpha = 1$ , the penalty is "lasso".
- If  $\lambda_1, \lambda_2 = 0$ , there is no penalty.

On the other hand, if we would like to fit a single rule for all studies/outcomes, we let  $g_1 = \ldots = g_K$  and solve the following problem instead

$$\min_{g} \frac{1}{2} \sum_{k=1}^{K} \sum_{i=1}^{n_k} \frac{|\hat{C}_k(X_i)|}{\sum_{i=1}^{n_k} |\hat{C}_k(X_i)|} \left[ 1\{\hat{C}_k(X_i) > 0\} - g(X_i) \right]^2 + h(g_1, \dots, g_K) + \lambda_{single} \|\beta\|_1$$

Depending on the value of  $\lambda_{single}$ 

- If  $\lambda_{single} \neq 0$ , the penalty is "lasso".
- If  $\lambda_{single} = 0$ , there is no penalty.

### Value

An S3 object of class "mp", which contains the information of the fitted model. It could be supplied to some other functions in mperosnalized package for further analysis or prediction.

penalty\_parameter\_sequence

A matrix object with each row denoting a configuration of the penalty parameters.

interceptlist A list object with each element denoting a vector of intercepts. The *k*th element corresponds to the *k*th row in penalty\_parameter\_sequence.

A list object with each element denoting a coefficient matrix. The *k*th element corresponds to the *k*th row in penalty\_parameter\_sequence.

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number\_covariates

Number of candidate covariates considered.

number\_studies\_or\_outcomes

Number of studies if problem = "meta-analysis" or number of outcomes if problem = "multiple outcomes".

### References

Zhang, B. and Tsiatis, A. A. and Davidian, M. and Zhang, M. and Laber, E.(2012) *Estimating optimal treatment regimes from a classification perspective, Stat, 1(1):103-114.* 

### **Examples**

mpersonalized\_cv

Cross Validation for mpersonalized

### **Description**

This function implments mpersonalized and use cross validatation to tune penalty parameter. The optimal penalty parameter is selected by minimizing

$$\sum_{i=1}^{n_k} \frac{|\hat{C}_k(X_i)|}{\sum_{i=1}^{n_k} |\hat{C}_k(X_i)|} \left[ 1\{\hat{C}_k(X_i) > 0\} - g_k(X_i) \right]^2$$

in the leave-out fold, where  $\hat{C}_k(X_i)$  in the leave-out fold is independently estimated from the training set.

# Usage

```
mpersonalized_cv(problem = c("meta-analysis", "multiple outcomes"), X, Trt,
  P = NULL, Xlist, Ylist, Trtlist, Plist = replicate(length(Xlist), NULL,
  simplify = FALSE), typelist = replicate(length(Xlist), "continuous",
  simplify = FALSE), penalty = c("lasso", "GL", "SGL", "fused", "lasso+fused",
  "GL+fused", "SGL+fused"), lambda1 = NULL, lambda2 = NULL,
  single_rule_lambda = NULL, num_lambda1 = ifelse(!is.null(lambda1),
  length(lambda1), 10), num_lambda2 = ifelse(!is.null(lambda2),
  length(lambda2), 10),
```

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```
num_single_rule_lambda = ifelse(!is.null(single_rule_lambda),
length(single_rule_lambda), 50), alpha = NULL, single_rule = FALSE,
cv_folds = 5, admm_control = NULL, contrast_builder_control = NULL)
```

# Arguments

-	,		
	problem	A character string specifiy whether user want to solve "meta-analysis" or "multiple outcomes" problem. For problem = "meta-analysis", user should also supply Xlist, Ylist, Trtlist. For problem = "multiple outcomes", user should supply X, Ylist, Trt.	
	X	Covariate matrix that should be supplied when problem = "multiple outcomes" with rows indicating subjects and columns indicating covariates.	
	Trt	Treatment vector that should be supplied when problem = "multiple outcomes", which should be coded as 0 or 1.	
	P	Propensity score vector when problem = "multiple outcomes". If not supplied, then study is treated as randomzied trial and the propensity score is estimated as the proportion of 1's in Trt for every subject.	
	Xlist	A list object that should be supplied when problem = "meta-analysis", with $k$ th element denoting the covariate matrix of study $k$ .	
	Ylist	When problem = "meta-analysis", Ylist should be a list object with $k$ th element denoting the response vector of study $k$ . When problem = "multiple outcomes' Ylist should be a list object with $k$ th element denoting the $k$ th outcome.	
	Trtlist	A list object that should be supplied when problem = "meta-analysis", with $k$ th element denoting the treatment vector of study $k$ (coded as 0 or 1).	
	Plist	A list object that should be supplied when problem = "meta-analysis", with $k$ the element denoting the propensity score vector of study $k$ . If not supplied, then each study is treated as randomized trial and the corresponding propensity score is estimated as the proportion of 1's in the $k$ th element of Trtlist for all subjects.	
	typelist	A list object with $k$ th element denoting the type of outcome corresponding to the $k$ th element in Ylist. Each element could be "continuous" or "binary".	
	penalty	For different rules, the penalty could be "lasso", "GL", "SGL", "fused", "lasso+fused", "GL+fused", "SGL+fused". For single rule, the penalty could only be "lasso". For penalty = "none", use function mpersonalized instead. User should always input penalty and then supply correponding penalty parameters sequence if needed.	
	lambda1	$\lambda_1$ in the framework of different rules. If not supplied, a default sequence will be computed.	
	lambda2	$\lambda_2$ in the framework of different rules. If not supplied, a default sequence will be computed.	
	single_rule_lam		
		$\lambda_{single}$ in the framework of single rule.	
	num_lambda1	If lambda1 is not specified by user, user could still specify the length of the lambda1 sequence. The default length is 10.	
	num_lambda2	If lambda2 is not specified by user, user could still specify the length of the lambda2 sequence. The default length is 10.	
num_single_rule_lambda			

If single\_rule\_lambda is not specified, user could still specify the length of

the single\_rule\_lambda sequence. The default length is 50.

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alpha  $\alpha$  in the framework of different rules. If not supplied, a default value will be

used depending on penalty.

single\_rule A logical value, whether the single treatment framework is used. Deafult is

FALSE.

cv\_folds Number of folds needed for cross-validation. Default is 5

admm\_control A list of parameters which user can specify to control the admm algorithm. In

admm\_control, the following parameters can be supplied: abs.tol, absolute tolerance; rel.tol, relative tolerance; maxit, maximum number of iterations;

rho, Lagrangian parameter.

contrast\_builder\_control

A list of parameters which user can specify to control estimation of contrast function. In contrast\_builder\_control, the following parameters could be supplied: eff\_aug, a logical value whether efficiency augmentation should be implemented; response\_model, a character string specify what outcome model

to use if eff\_aug = TRUE, response\_model could be "lasso" or "linear"; contrast\_builder\_folds,

the number of folds used in cross validation when response\_model = "lasso".

### Value

An S3 object of class "mp\_cv", which contains the information of the model with the optimal lambda. It can be supplied to some other functions in mperosnalized package for further analysis or prediction.

penalty\_parameter\_sequence

A matrix object with each row denoting a configuration of the penalty parameters

opt\_penalty\_parameter

Optimal penalty parameter chosen by minimizing the cross validation error.

interccept The vector of intercepts corresponding to the optimal penalty parameter.

beta The coefficient matrix corresponding to the optimal penalty parameter.

number\_covariates

Number of candidate covariates considered.

number\_studies\_or\_outcomes

Number of studies if problem = "meta-analysis" or number of outcomes if problem = "multiple outcomes".

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```
Xlist = Xlist, Ylist = Ylist, Trtlist = Trtlist,
penalty = "lasso", single_rule = TRUE)
```

plot.mp

Interaction Plot for an "mp" Class Object.

# **Description**

This function plots interaction between received treatment and recommended treatment, which provides an estimate of treatment effect of the identified subgroup.

# Usage

```
## S3 method for class 'mp'
plot(mp, penalty_index)
```

mp\_cvmod\_single\$intercept
mp\_cvmod\_single\$beta
set.seed(NULL)

## **Arguments**

mp A fitted "mp" class object returned by mpersonalzied function

penalty\_index The index of penalty parameter configuration in mp\$penalty\_parameter\_sequence.

When mp\$penalty = "none", penalty\_index is automatically set to be 1.

### **Details**

In the interaction plot, each point is the group mean given a received treatment and a recommended treatment. Although usually overestimating treatment effect in training set, interaction plots provides a sanity check for treatment recommendation rules. Given a specific index of penalty parameter, the function plots corresponding interaction plots.

### Value

A list object with each element as the interaction plots for a penalty parameter configuration.

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plot.mp\_cv

Interaction Plot for an "mp\_cv" Class Object.

# **Description**

This function plots interaction between received treatment and recommended treatment, given the optimal penalty parameter.

# Usage

```
## S3 method for class 'mp_cv'
plot(mp_cv)
```

# **Arguments**

mp\_cv

A fitted 'mp\_cv' class object returned by mpersonalzied\_cv function

### Value

A list object representing the interaction plots for the optimal penalty parameter configuration. Specifically, kth element is the interaction plot for the kth study/outcome.

# **Examples**

predict.mp

Prediction for a Fitted "mp" Object

# Description

This function predicts optimal treatment of new subjects for a mpersonalized model. If different rules are used in the fitting procedure, an overall treatment recommendation based on all stuides/outcomes could be provided together with optimal treatments for each study/outcome.

# Usage

```
## S3 method for class 'mp'
predict(mp, newx = NULL, weight = NULL, overall_rec = TRUE)
```

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### **Arguments**

mp A fitted "mp" object returned by "mpersonalized"

newx Covariate matrix of new patients. If not supplied, by default the prediction is for

the original dataset in the "mp" object. Notice: when problem = "meta-analysis" and the prediction is for the original dataset, subjects in each study are only predicted using the treatment recommendation rule of the study they belong to.

weight A weight vector for the overall recommendation, only needed when overall\_rec = TRUE.

By default, equal weights are assigned to each study/outcome.

overall\_rec A logical value. If overall\_rec = TRUE, an overall recommendation will be

provided as an weighted average of the optimal treatment from each individual

study/outcome. Only useful when newx is provided.

### **Details**

This function predicts for each penalty parameter in the penalty\_parameter\_sequence of the "mp" object. The overall recommended treatment is given as an weighted average of the recommended treatments from each study/outcome, and the weight can be specified by user.

### Value

A list object of two elements. .

opt\_treatment A list object with each element denoting the prediction based on a penalty pa-

rameter configuration in mp\$penalty\_parameter\_sequence. Specifically, if newx is provided, each element is a recommendation matrix with each row denoting a subject and each column denoting a study/outcome; otherwise, each element is a list of vectors with each vector representing the optimal treatment for each study/outcome. If overall\_rec = TRUE, the weighted overall recommended treatment will be further provided as well. If the overall recommended treatment will be further provided as well.

treatment is equal to 0.5, it means the weighted sum is equal for 0 and 1.

benefit\_score A list object of benefit scores computed from  $g_1, \ldots, g_K$ . Similar structure as

opt\_treatment.

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predict.mp_cv Prediction for a Fitted "mp_cv" Object
--

# **Description**

This function predicts optimal treatment of new subjects for a cross-validated mpersonalized model.

### Usage

```
## S3 method for class 'mp_cv'
predict(mp_cv, newx = NULL, weight = NULL,
  overall_rec = TRUE)
```

# **Arguments**

mp_cv	A fitted "mp_cv" object returned by "mpersonalized_cv" function
newx	Covariate matrix of new patients. If not supplied, by default the prediction is for the original dataset in the "mp_cv" object. Prediction results will differ based on whether newx is provided or not. Similar to predict.mp.
weight	A weight vector for the overall recommendation, only needed when overall_rec = TRUE. By default, equal weights are assigned to each study/outcome.
overall_rec	A logical value. If overall_rec = TRUE, an overall recommendation will be

provided as an weighted average of the optimal treatment from each individual

study/outcome. Only useful when newx is provided.

# Value

A list object with two elements. Similar to the returned value of predict.mp, but now it only predicts for the optimal parameter penalty.

If newx is provided, a recommendation matrix with each row denoting a subopt\_treatment ject and each column denoting a study/outcome; otherwise, each element is a list of vectors with each vector representing the optimal treatment for each study/outcome. If overall\_rec = TRUE, the weighted overall recommended treatment will be further provided as well. If the overall recommened treatment is equal to 0.5, it means the weighted sum is equal for 0 and 1.

Benefit scores computed from  $g_1, \dots, g_K$ . Similar to structure of opt\_treatment. benefit\_score

```
set.seed(123)
sim_dat = simulated_dataset(n = 200, problem = "meta-analysis")
Xlist = sim_dat$Xlist; Ylist = sim_dat$Ylist; Trtlist = sim_dat$Trtlist
# fit different rules with group lasso penalty
mp_cvmod_diff = mpersonalized_cv(problem = "meta-analysis",
                                 Xlist = Xlist, Ylist = Ylist, Trtlist = Trtlist,
                                 penalty = "GL", single_rule = FALSE)
newx = matrix(rnorm(100 * mp_cvmod_diff$number_covariates), nrow = 100)
```

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```
# predict on newx
pred_new = predict(mp_cv = mp_cvmod_diff, newx = newx, overall_rec = TRUE)
# predict on old dataset
pred_old = predict(mp_cv = mp_cvmod_diff)
set.seed(NULL)
```

 $simulated\_dataset$ 

Simulated Dataset Generator

### **Description**

Generate a simulated dataset, which could be used to demonstrate the features of the mpersonalized package.

# Usage

```
simulated_dataset(n, problem = c("meta-analysis", "multiple outcomes"))
```

### **Arguments**

n Sample size for each study/outcome.

problem A character string specified what problem the simulated dataset is generated for.

problem can be set to "meta-analysis" or "multiple outcomes".

# **Details**

In the simulated dataset, outcomes are generated from the model

$$Y = \delta_0 + X\delta + A(\theta_0 + X\theta) + \epsilon,$$

where X is the baseline covariates and A is the treatment indicator coded as 0,1. For different outcomes or studies, values of  $\delta_0$ ,  $\delta$ ,  $\theta_0$  and  $\theta$  are also different so as to represent the heterogeneity in real problems.

The number of different studies/outcomes is set to be 6 and total number of candidate covariates is 50. Treatment indicator A is generated with equal probability of 0 or 1.

This function randomly generates the coefficients for each study/outcome and then generates the baseline covariates and error term for each subject. Depending on the value of problem, generation of baseline covariates are slightly different. For problem = "meta-analysis", baseline covariates are generated independently for each study; for problem = "multiple outcomes", baseline covariates are the same across different outcomes.

# Value

A list object of the ingredients from the simulated dataset. The elements of this list depends on value of problem.

For problem = "meta-analysis",

X1ist a list object with kth element denoting the baseline covariate matrix of kth study

Ylist a list object with kth element denoting the response vector of kth study

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Trtlist a list object with kth element denoting the treatment vector of kth study and

coded as 0 or 1

B the coefficient matrix containing  $\delta_0$ ,  $\delta$ ,  $\theta_0$  and  $\theta$ 

For problem = "multiple outcomes",

X a matrix object denoting the baseline covariate matrix

Ylist a list object with kth element denoting the response vector of kth outcome

Trt a vector denoting the treatment and coded as 0 or 1) B the coefficient matrix containing  $\delta_0$ ,  $\delta$ ,  $\theta_0$  and  $\theta$ 

```
set.seed(123)
sim_dat = simulated_dataset(n = 200, problem = "meta-analysis")
str(sim_dat$Xlist)
str(sim_dat$Ylist)
str(sim_dat$Trtlist)
set.seed(NULL)
```

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