# Package 'mpersonalized'

March 18, 2018

Type Package

Title What the Package Does (Title Case)

Version 0.1.0
Author Chensheng Kuang
Maintainer Chensheng Kuang < ckuang@wisc.edu>
<b>Description</b> Implements a general framework to solve the problem of personalized medicine in meta-analysis and multiple outcomes. This framework allows either separate rules for each study/outcome or a single rule for all the studies/outcomes, depending on the requirement of user. A flexible choice of penalty functions to increase estimation efficiency is also provided.
License GPL-2
Encoding UTF-8
LazyData true
RoxygenNote 6.0.1
Imports glmnet, SGL, caret, ggplot2, gridExtra, genlasso, Matrix
Suggests knitr, rmarkdown
VignetteBuilder knitr
LinkingTo Rcpp
R topics documented:
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 ${\it admm\_optim} \qquad {\it ADMM\ Algorithm\ for\ Meta-analysis/Multiple\ Outcomes\ Personalized} \\ {\it Medicine}$ 

## Usage

```
admm_optim(x, y, p, q, lambda1, lambda2, lambda3, abs.tol = 1e-05,
  rel.tol = 1e-05, maxit = 500L, rho = NULL)
```

lambda\_estimate

Default Penalty Parameter Sequence if Not Given

#### **Usage**

```
lambda_estimate(modelXlist, modelYlist, penalty, unique_rule, alpha,
   num_lambda1, num_lambda2, num_unique_rule_lambda)
```

#### **Arguments**

modelXlist the Xlist in contrast framework after standardization modelYlist the Ylist in contrast framework after standardization

penalty penalty type

unique\_rule whether a unique treatment rule is required

#### Value

estimated lambda for required penalty if not provided

mpersonalized

Meta-analysis/Multiple Outcomes for Personalized Medicine

# Usage

```
mpersonalized(problem = c("meta-analysis", "multiple outcomes"), X, Trt,
   P = NULL, Xlist, Ylist, Trtlist, Plist = replicate(length(Xlist), NULL,
   simplify = FALSE), typelist = replicate(length(Xlist), "continuous",
   simplify = FALSE), penalty = c("none", "lasso", "GL", "SGL", "fused",
   "lasso+fused", "GL+fused", "SGL+fused"), lambda1 = NULL, lambda2 = NULL,
   unique_rule_lambda = NULL, num_lambda1 = ifelse(!is.null(lambda1),
   length(lambda1), 10), num_lambda2 = ifelse(!is.null(lambda2),
   length(lambda2), 10),
   num_unique_rule_lambda = ifelse(!is.null(unique_rule_lambda),
   length(unique_rule_lambda), 50), alpha = NULL, unique_rule = FALSE,
   admm_control = NULL, contrast_builder_control = NULL)
```

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## **Arguments**

typlelist

problem a character specifiy whether the user want to solve "meta-analysis" or "multiple outcomes" problem. For "meta-analysis" problem, the user should supply Xlist, Ylist, Trtlist and Plist. For "multiple outcomes" problem, the user should supply X, Ylist, Trt and P. Χ the covariate matrix that should be supplied when the problem is "multiple outcomes" with rows indicating subjects and columns indicating covariates. Trt the treatment vector that should be supplied when the problem is "multiple outcomes". It should be coded as 0 or 1. Ρ the propensity score vector when the problem is "multiple outcomes". If not supplied, then study is treated as randomzied trial and the propensity score is estimated as the proportion of 1's in Trt. Xlist a list object with kth element denoting the covariate matrix of study k. This should be supplied when the problem is "meta-analysis". Ylist When the problem is "meta-analysis", Ylist should be a list object with kth element denoting the response vector of study k. When the problem is "multiple outcomes", Ylist should be a list object with kth element denoting the kth Trtlist a list object with kth element denoting the treatment vector of study k (coded as 0 or 1). This should be supplied when the problem is "meta-analysis". Plist a list object with kthe element denoting the propensity score vector of study k. If not supplied, then each study is treated as randomized trial and the corresponding propensity score is estimated as the proportion of 1's in Trt. For different rules, the penalty could be "none", "lasso", "GL", "SGL", "fused", penalty "lasso+fused", "GL+fused", "SGL+fused". For unique rule, the penalty could be "none" or "lasso". lambda1 lambda1 supplied in the framework when different rules are used. lambda2 lambda2 supplied in the framework when different rules are used. unique\_rule\_lambda  $\lambda$  when unique rule is used. length of the lambda1 sequence and default to be 10 if lambda1 is not provided num\_lambda1 num\_lambda2 length of the lambda2 sequence and default to be 10 if lambda2 is not provided num\_unique\_rule\_lambda length of the unique\_rule\_lambda sequence and default to be 50 if unique\_rule\_lambda is not provided alpha alpha in the framework when different rules are used. a logical value, whether a unique treatment rule is required unique\_rule a list of parameters which control the admm algorithm. In admm\_control, the admm\_control following parameters can be supplied: abs.tol, absolute tolerance; rel.tol, relative tolerance; maxit, maximum number of iterations; rho, Lagrangian paramecontrast\_builder\_control a list of parameters which control the contrast building process. In contrast\_builder\_control, the following parameters could be supplied: response\_model, this could be "lasso" or "linear"; contrast builder folds, the number of folds used in cross

validation when response\_model = "lasso".

a list object with kth element denoting the type of response corresponding to the

kth element in the list Ylist. Each element should be "continuous" or "binary".

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#### **Details**

Assume the total number of studies is K. This function is aimed to solve meta-analysis/multiple outcomes problems for personalized medicine based on the following framework:

$$\min_{g_1,\dots,g_K} \frac{1}{2} \sum_{k=1}^K \sum_{i=1}^{n_k} \frac{|\hat{C}_k(X_i)|}{\sum_{i=1}^{n_k} |\hat{C}_k(X_i)|} \left[ 1\{\hat{C}_k(X_i) > 0\} - g_k(X_i) \right]^2 + h(g_1,\dots,g_K)$$

Here the regularization function h is of the form of a sum of sparse group lasso and fused lasso penalty

$$h = (1 - \alpha)\lambda_1 \sqrt{q} \sum_{j=1}^p \|\beta_j\|_2 + \alpha \lambda_1 \sum_{j=1}^p \|\beta_j\|_1 + \lambda_2 \sum_{j=1}^p \sum_{1 \le a < b \le K} |\beta_{ja} - \beta_{jb}|$$

where 
$$\boldsymbol{\beta_j} = (\beta_{j1}, \dots, \beta_{jK})$$

If we would like a unique rule to be obtained, we let  $g_1 = \ldots = g_K$  and solve the following question instead

$$\min_{g} \frac{1}{2} \sum_{k=1}^{K} \sum_{i=1}^{n_k} \frac{|\hat{C}_k(X_i)|}{\sum_{i=1}^{n_k} |\hat{C}_k(X_i)|} \left[ 1\{\hat{C}_k(X_i) > 0\} - g(X_i) \right]^2 + h(g_1, \dots, g_K) + \lambda_{uni} \|\beta\|_1$$

If we want different rules, by setting  $\lambda_1, \lambda_2, \alpha$  differently, different penalties can be obtained.

- If  $\lambda_1, \lambda_2 \neq 0$  and  $\alpha \neq 0$  or 1, the penalty is "SGL+fused".
- If  $\lambda_1,\lambda_2\neq 0$  and  $\alpha=0$ , the penalty is "GL+fused".
- If  $\lambda_1, \lambda_2 \neq 0$  and  $\alpha = 1$ , the penalty is "lasso+fused".
- If  $\lambda_1 = 0, \lambda_2 \neq 0$ , the penalty is "fused".
- If  $\lambda_1 \neq 0, \lambda_2 = 0$  and  $\alpha \neq 0$  or 1, the penalty is "SGL".
- If  $\lambda_1 \neq 0, \lambda_2 = 0$  and  $\alpha = 0$ , the penalty is "GL".
- If  $\lambda_1 \neq 0, \lambda_2 = 0$  and  $\alpha = 1$ , the penalty is "lasso".
- If  $\lambda_1, \lambda_2 = 0$ , there is no penalty.

If we want unique rule,

- If  $\lambda \neq 0$ , the penalty is "lasso".
- If  $\lambda = 0$ , there is no penalty.

# Value

an S3 object of class "mp", which contains the information of the fitted model. It could be supplied to the predict function

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mpersonalized_cv	Meta-analysis/Multiple Outcomes for Personalized Medicine with Cross Validation	

#### Usage

```
mpersonalized_cv(problem = c("meta-analysis", "multiple outcomes"), X, Trt,
   P = NULL, Xlist, Ylist, Trtlist, Plist = replicate(length(Xlist), NULL,
   simplify = FALSE), typelist = replicate(length(Xlist), "continuous",
   simplify = FALSE), penalty = c("lasso", "GL", "SGL", "fused", "lasso+fused",
   "GL+fused", "SGL+fused"), lambda1 = NULL, lambda2 = NULL,
   unique_rule_lambda = NULL, num_lambda1 = ifelse(!is.null(lambda1),
   length(lambda1), 10), num_lambda2 = ifelse(!is.null(lambda2),
   length(lambda2), 10),
   num_unique_rule_lambda = ifelse(!is.null(unique_rule_lambda),
   length(unique_rule_lambda), 50), alpha = NULL, unique_rule = FALSE,
   cv_folds = 5, admm_control = NULL, contrast_builder_control = NULL)
```

# **Arguments**

problem	a character specifiy whether you want to solve "meta-analysis" or "multiple outcomes" problem. For "meta-analysis" problem, the user should supply Xlist, Ylist, Trtlist and Plist. For "multiple outcomes" problem, the user should supply X, Ylist, Trt and P.	
X	the covariate matrix that should be supplied when the problem is "multiple outcomes" with rows indicating subjects and columns indicating covariates.	
Trt	the treatment vector that should be supplied when the problem is "multiple outcomes". It should be coded as 0 or 1.	
Р	the propensity score vector when the problem is "multiple outcomes". If not supplied, then study is treated as randomzied trial and the propensity score is estimated as the proportion of 1's in Trt.	
Xlist	a list object with $k$ th element denoting the covariate matrix of study $k$ . This should be supplied when the problem is "meta-analysis".	
Ylist	When the problem is "meta-analysis", Ylist should be a list object with $k$ th element denoting the response vector of study $k$ . When the problem is "multiple outcomes", Ylist should be a list object with $k$ th element denoting the $k$ th outcome.	
Trtlist	a list object with $k$ th element denoting the treatment vector of study $k$ (coded as 0 or 1). This should be supplied when the problem is "meta-analysis".	
Plist	a list object with $k$ the element denoting the propensity score vector of study $k$ . If not supplied, then each study is treated as randomized trial and the corresponding propensity score is estimated as the proportion of 1's in Trt.	
penalty	For different rules, the penalty could be "none", "lasso", "GL", "SGL", "fused", "lasso+fused", "GL+fused", "SGL+fused". For unique rule, the penalty could be "none" or "lasso".	
lambda1	lambda1 supplied in the framework when different rules are used.	
lambda2	lambda2 supplied in the framework when different rules are used.	

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unique\_rule\_lambda

 $\lambda$  when unique rule is used.

num\_lambda1 length of the lambda1 sequence and default to be 10 if lambda1 is not provided num\_lambda2 length of the lambda2 sequence and default to be 10 if lambda2 is not provided num\_unique\_rule\_lambda.

num\_unique\_rule\_lambda

length of the unique\_rule\_lambda sequence and default to be 50 if unique\_rule\_lambda

is not provided

alpha alpha in the framework when different rules are used.

unique\_rule a logical value, whether a unique treatment rule is required cv\_folds number of folds needed for cross-validation, default is 5

admm\_control a list of parameters which control the admm algorithm. In admm\_control, the

following parameters can be supplied: abs.tol, absolute tolerance; rel.tol, relative tolerance; maxit, maximum number of iterations; rho, Lagrangian parame-

ter.

contrast\_builder\_control

a list of parameters which control the contrast building process. In contrast\_builder\_control,

the following parameters could be supplied: response\_model, this could be "lasso" or "linear"; contrast\_builder\_folds, the number of folds used in cross

validation when response\_model = "lasso".

typlelist a list object with kth element denoting the type of response corresponding to the

kth element in the list Ylist. Each element should be "continuous" or "binary".

#### **Details**

This function implments mpersonalized but use cross validatation for the tuning of penalty parameter. The optimal penalty parameter is selected by minimizing

$$\sum_{i=1}^{n_k} \frac{|\hat{C}_k(X_i)|}{\sum_{i=1}^{n_k} |\hat{C}_k(X_i)|} \left[ 1\{\hat{C}_k(X_i) > 0\} - g_k(X_i) \right]^2$$

in the leave-out fold, where  $\hat{C}_k(X_i)$  in the leave-out fold is separately estimated from the training set

#### Value

an S3 object of class "mp\_cv", which contains the information of the model with the best fitted lambda. It can be supplied to the predict function.

plot.mp

Plot for a 'mp' Class Object.

# Usage

```
## S3 method for class 'mp'
plot(mp, ind1, ind2, unique_ind)
```

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# **Arguments**

mp	the 'mp' class object returned by mpersonalzied function
ind1	the index of the lambda1 if different rules are used
ind2 the index of the lambda2 if different rules are used	
unique_ind	the index of the unique_rule_lambda if an unique rule is used

#### **Details**

This function plots the results for estimated treatment effects. Depending on the received treatment and recommended treatment, the group means of the outcome are computed and the relations between them are plotted. This plot provides a sanity check of the treatment recommendation rule. By specifying the index of the penalty parameters, we can obtain the plots of the corresponding treatment recommendation rule.

# Value

a list object with kth element denoting the plot of study k

plot.mp_cv	Plot for a 'mp' Class Object.

# Usage

```
## S3 method for class 'mp_cv'
plot(mp_cv)
```

# **Arguments**

mp\_cv the 'mp\_cv' class object returned by mpersonalzied\_cv function

#### **Details**

This function plots the results for estimated treatment effects by using the estimated optimal treatment recommendation rule obtained from corss validation.

### Value

a list object with kth element denoting the plot of study k

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#### **Description**

This function predict the benefit scores and optimal treatment for new patients

# Usage

```
## S3 method for class 'mp'
predict(mp, newx = NULL, weight = NULL, overall_rec = TRUE)
```

# **Arguments**

mp the fitted "mp" object returned by "mpersonalized"

news the covariate matrix of the new patients. If news = NULL, then the prediction is

made for each data set based on the rule of that study/outcome.

weight a weight vector for the overall recommendation. If leave as NULL, a equally

weighted recommendation will be made.

overall\_rec a logical value. If TRUE, an overall recommendation will be made weighted by

the "weight" parameter.

#### Value

a list of results with each element in the list corresponding to the prediciton by each different penalty parameter. Each element in this list contains:

treatment recommended treatment for each patient for each study/outcome. If overall\_rec = TRUE,

the weighted overall recommended treatment will be computed as well. If the overall recommend treatment is equal to 0.5, it means the sum of weight is

equal for 0 and 1.

benefit\_score  $\ \ \$  the benefit score computed from  $g_1,\ldots,g_K$ 

# Description

This function predict the benefit scores and optimal treatment for new patients

# Usage

```
## S3 method for class 'mp_cv'
predict(mp_cv, newx = NULL, weight = NULL,
    overall_rec = TRUE)
```

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## **Arguments**

mp\_cv the fitted "mp\_cv" object returned from "mpersonalized\_cv" function

newx the covariate matrix of the new patients. If newx = NULL, then the prediction is

made for each data set based on the rule of that study/outcome.

weight a weight vector for the overall recommendation. If leave as NULL, a equally

weighted recommendation will be made.

overall\_rec a logical value. If TRUE, an overall recommendation will be made weighted by

the "weight" parameter.

#### Value

the prediciton by using the optimal penalty parameter selected by cross validation. It contains:

treatment recommended treatment for each patient for each study/outcome. If overall\_rec = TRUE,

the weighted overall recommended treatment will be computed as well. If the overall recommend treatment is equal to 0.5, it means the sum of weight is

equal for 0 and 1.

benefit\_score the benefit score computed from  $g_1, \ldots, g_K$ 

#### **Description**

Generate a simulated dataset, which could be used to demonstrate the features of the mpersonalized package.

# Usage

simulated\_dataset(n, problem = c("meta-analysis", "multiple outcomes"))

#### **Arguments**

n Sample size for each study/outcome.

problem A character string specified what problem the simulated dataset is generated for.

problem can be set to "meta-analysis" or "multiple outcomes".

## Details

In the simulated dataset, outcomes are generated from the model

$$Y = \delta_0 + X\delta + A(\theta_0 + X\theta) + \epsilon,$$

where X is the baseline covariates and A is the treatment indicator coded as 0,1. For different outcomes or studies, values of  $\delta_0$ ,  $\delta$ ,  $\theta_0$  and  $\theta$  are also different so as to represent the heterogeneity in real problems.

The number of different studies/outcomes is set to be 6 and total number of candidate covariates is 50. Treatment indicator A is generated with equal probability of 0 or 1.

This function randomly generates the coefficients for each study/outcome and then generates the baseline covariates and error term for each subject. Depending on the value of problem, generation of baseline covariates are slightly different. For problem = "meta-analysis", baseline covariates are generated independently for each study; for problem = "multiple outcomes", baseline covariates are the same across different outcomes.

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# Value

A list object of the ingredients from the simulated dataset. The elements of this list depends on value of problem.

For problem = "meta-analysis",

Xlist a list object with kth element denoting the baseline covariate matrix of kth study

Ylist a list object with kth element denoting the response vector of kth study

Trtlist a list object with kth element denoting the treatment vector of \endkth study and

coded as 0 or 1

B the coefficient matrix containing  $\delta_0$ ,  $\delta$ ,  $\theta_0$  and  $\theta$ 

For problem = "multiple outcomes",

X a matrix object denoting the baseline covariate matrix

Ylist a list object with kth element denoting the response vector of kth outcome

Trt a vector denoting the treatment and coded as 0 or 1) B the coefficient matrix containing  $\delta_0$ ,  $\delta$ ,  $\theta_0$  and  $\theta$ 

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