Strong-field frustrated double ionization of argon atoms

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Using a three-dimensional semiclassical method, we theoretically investigate frustrated double ionization (FDI) of Ar atoms subjected to strong laser fields. The double-hump photoelectron momentum distribution generated from FDI observed in a recent experiment [S. Larimian et al., Phys. Rev. Research 2, 013021 (2020)] is reproduced by our simulation. We confirm that the observed spectrum is due to recollision. The laser intensity dependence of FDI is investigated. We reveal that the doubly excited states of Ar atoms and excited states of Ar+ are the dominant pathways for producing FDI at relatively low and high intensities, respectively. The information of which pathway leads to FDI is encoded in the electron momentum distributions. Our work demonstrates that FDI is a general strong-field physical process accompanied with nonsequential double ionization and it can be well understood within the context of recollision scenario.

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I. INTRODUCTION

When exposed to a strong laser field, the outermost electron of atoms or molecules can be ionized through tunneling. The electron is then accelerated and possibly driven back by the oscillating laser electric field to recollide with its parent ion [1], resulting in various strong-field phenomena such as above-threshold ionization plateau [2], high-order harmonic generation [3,4], and nonsequential double ionization (NSDI) [5]. Alternatively, due to the presence of the Coulomb field of the ion, the electron may also be captured into an Rydberg state after the end of the laser pulse, leading to excited atoms or molecules [6–13]. This is known as frustrated tunneling ionization (FTI) [7]. The capture of electrons into Rydberg states was also found when strong-field double ionization (DI) occurs [14,15], which can be referred to as frustrated double ionization (FDI). It has been mainly observed in atomic fragments produced by Coulomb explosion of molecules and also dimers [15–20], which can be explained as neutralization during the dissociative ionization process [21,22]. Taking FDI of hydrogen molecules for example [15,22], two electrons tunnel ionize sequentially and one of them may be captured by one of the protons when the molecular ions fragment, leading to the formation of a highly excited neutral hydrogen atom and a proton. Experimentally, the capture process is identified by measuring the kinetic energies of the excited neutral fragments after molecular dissociative ionization [15]. Unfortunately, this method is not applicable for atomic targets since atomic FDI happens without dissociation and the products are excited ions rather than excited neutral fragments. Consequently, there is a lack of experimental and theoretical studies on atomic FDI.

Very recently, FDI of Ar atoms was experimentally identified by measuring the dc-field ionized electrons from the excited singly charged ions (Ar^{+*}), the photoelectrons, and the corresponding doubly charged ions (Ar²⁺) in coincidence [23]. The measured photoelectron momentum distributions corresponding to an FDI event display a clear transition from a double-hump to a single-hump structure as the laser intensity is increased, quite similar to DI. The observation suggests that the physical mechanism of FDI differs for different intensity regions where NSDI or sequential double ionization (SDI) dominate, respectively. For SDI occurring at high intensities, the two electrons are ionized independently. The narrow single-hump structure for FDI at such high intensities, which has a width close to that for single ionization, strongly suggests that the trapped electrons mainly arise from the second ionization step. For modest intensities, where NSDI dominates, it has been speculated that the electron-electron interaction during recollision causes the double-hump momentum spectrum for FDI [23]. Yet, how exactly recollision results in such a spectrum remains unclear.

In this paper, we theoretically study FDI of Ar atoms using a semiclassical model. The main purpose of the current work is to offer a transparent physical picture of FDI at modest

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intensities where NSDI dominates. We calculate the ratio of FDI to single ionization (SI) and the ratio of FDI to DI as functions of laser intensity. Our calculation reproduces the experimental double-hump photoelectron momentum distribution for FDI as reported in Ref. [23]. We confirm that recollision is responsible for this structure and further show how recollision leads to different photoelectron momentum distributions for FDI at different intensities. By analyzing the electron trajectories, we find that the dominant pathways for FDI at relatively low and high intensities are doubly excited states of Ar and excited states of Ar⁺, respectively. This work indicates that FDI is a general strong-field process accompanied with NSDI and it can be fully understood based on the recollision picture.

The paper is organized as follows. In Sec. II, we introduce the semiclassical model. Section III shows our main results. Finally, we present our conclusion in Sec. IV.

II. THEORETICAL MODEL

A well-established three-dimensional semiclassical model (see, e.g., [24,25]) is employed to describe FDI and NSDI. The semiclassical model has achieved great success in explaining various NSDI experiments [26,27]. Within this model, one can trace back the electron trajectories leading to specific features and gain intuitive physical insights into the underlying mechanism [27–29]. The main limitations of this model are that, firstly, some quantum effects are ignored. For instance, the contributions of quantum transitions to intermediate excited states in NSDI and the coherent superpositions of these channels are not considered [30,31]. Secondly, the semiclassical model is based on quasistatic field approximation. It works particularly well when the Keldysh parameter is smaller than (or around) 1 and thus fails to describe few-photon double ionization. Furthermore, the semiclassical model is usually unable to quantitatively reproduce experimental observables such as DI yields [32].

In this model, we consider the interaction of a two-activeelectron atom with a linearly polarized laser field:

$$\mathbf{E}(t) = f(t)E_0\cos\omega t \,\,\hat{\mathbf{z}},\tag{1}$$

where ω is the laser frequency and E_0 is the peak amplitude of the laser electric field. The pulse envelope function f(t) is a constant equal to 1 for the first ten laser cycles and then reduced to zero with a three-cycle ramp in the form of \cos^2 .

Following the same procedure as used in previous studies [32–34], the outermost electron e_1 is assumed to be ionized by quantum tunneling through the field-suppressed atomic potential. The tunneling process can be described by the Schrödinger equation in parabolic coordinates (atomic units are used throughout this paper) [35]:

$$\frac{d^2\phi}{d\eta^2} + \left(-\frac{I_{p1}}{2} + \frac{1}{2\eta} + \frac{1}{4\eta^2} + \frac{E\eta}{4}\right)\phi = 0,\tag{2}$$

where I_{p1} is the first ionization potential of atoms. Note here that the Stark shift of the ground state energy of atoms has been neglected. This is a good approximation for Ar due to the small static polarizabilities (11.08 a.u. for Ar⁺ and 7.2 a.u. for Ar, respectively) [36,37]. Equation (2) describes the tunneling process for an electron with energy of $-I_{p1}/4$ within

an effective potential $U(\eta) = -1/4\eta - 1/8\eta^2 - E\eta/8$. Thus, the tunnel exit point η_0 is determined by solving the equation $U(\eta) = -I_{p1}/4$. The corresponding initial positions of e_1 are $x_0 = y_0 = 0$, $z_0 = -\eta_0/2$. This slightly differs from the widely used tunneling exit derived in the Cartesian coordinates $z_{0c} \approx -I_{p1}/E$ [8,13,38]. We have found that the calculated photoelectron momentum distribution from FDI agrees better with the experimental result when using the tunneling exit derived in parabolic coordinates.

A nonzero initial velocity perpendicular to the laser polarization direction is introduced [39]. The initial longitudinal velocity is reasonably assumed to be zero [27–29,40], which is consistent with the Keldysh theory (for a review, see [41]). As we will show below, the good agreement between our calculation and the experiment suggests that the longitudinal velocity spread plays a negligible role here. The corresponding initial velocities are thus $v_{x0} = v_{\perp} \cos \theta$, $v_{y0} = v_{\perp} \sin \theta$, and $v_{z0} = 0$, where θ is the angle between the transverse velocity v_{\perp} and the x axis. For the bound electron e_2 , its initial conditions are determined by assuming this electron in the ground state of singly charged ions and the corresponding positions and momenta are depicted by a microcanonical distribution [42].

After setting the initial conditions of e_1 and e_2 , the propagation of the two electrons is governed by the classical Newtonian equation of motion:

$$\frac{d^2\mathbf{r_i}}{dt^2} = -\mathbf{E}(t) - \nabla \left(V_{ne}^i + V_{ee}\right) \tag{3}$$

until the end of the laser pulse. The index i=1,2 in Eq. (3) denotes e_1 and e_2 , respectively. $V_{ne}^i = -\frac{2}{|\mathbf{r}_i|}$ and $V_{ee} = \frac{1}{|\mathbf{r}_1 - \mathbf{r}_2|}$ are the Coulomb interactions between the nucleus and the *i*th electron and between the two electrons, respectively.

In our model calculation, 10^8 initial points are randomly distributed in the parameter space $-\pi/2 < wt_0 < \pi/2, v_\perp > 0$, and $0 < \theta < 2\pi$ for e_1 and in the microcanonical distribution for e_2 at each laser intensity. Here t_0 is the tunneling ionization instant. The laser frequency ω is chosen as 0.056 42 a.u., corresponding to a laser wavelength of 800 nm. Each electron trajectory is weighted by $W(t_0, v_\perp) = W_0(t_0)W_1(t_0, v_\perp)$, where

$$W_0(t_0) = I_{p1} C_{n^* l}^2 \left[\frac{2(2I_{p1})^{3/2}}{|E(t_0)|} \right]^{2n^* - 1} \exp\left[-\frac{2(2I_{p1})^{3/2}}{3|E(t_0)|} \right]$$
(4)

is the tunneling rate [43,44]. Here $C_{n^*l} = (\frac{2e}{n^*})^{n^*} \frac{1}{\sqrt{2\pi n^*}}$ is a constant with the effective principal quantum number $n^* = \frac{1}{\sqrt{2I_{p^1}}}$ and the e constant. $W_1(t_0, v_\perp)$ denotes the distribution of the transverse velocity v_\perp , which is given by

$$W_1(t_0, v_\perp) = \frac{v_\perp (2I_{p1})^{1/2}}{|E(t_0)|\pi} \exp\left[-\frac{v_\perp^2 (2I_{p1})^{1/2}}{|E(t_0)|}\right].$$
 (5)

As shown in Fig. 1(a), different groups of electron trajectories can be identified, depending on the final energies of the two electrons. Here we choose Ar as the target. DI events are identified when the final energies of both electrons are larger than zero. FDI events are identified when one electron has positive final energy and the other is captured into highly excited Rydberg states Ar^{+*} after the end of the laser pulse. The corresponding quantum number n of Ar^{+*}

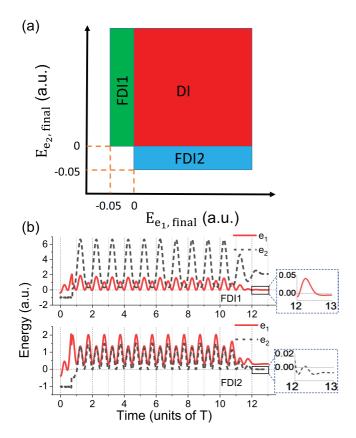


FIG. 1. (a) Schematic diagram of different types of electron trajectories for Ar. $E_{e_1,\mathrm{final}}$ and $E_{e_2,\mathrm{final}}$ are the final energies of e_1 and e_2 , respectively. See text for details. (b) Typical time evolutions (in laser cycle T) of the two-electron energies for FDI1 (upper panel) and FDI2 (lower panel).

is larger than 6 (the energy of Ar^{+*} is $E_{Ar^{+*}} = -2/n^2$). We note that the analysis and main conclusion presented in this work also hold true if we choose even higher quantum numbers (e.g., n > 10 or 20). Depending on which electron is recaptured, FDI events can thus be distinguished into FDI1 events: $E_{e_2, \text{final}} > 0 > E_{e_1, \text{final}} > -0.05$ a.u. and FDI2 events: $E_{e_1, \text{final}} > 0 > E_{e_2, \text{final}} > -0.05$ a.u., respectively. Here FDI1 and FDI2 correspond to the rescattered electrons e_1 and the initially stuck electrons e_2 being captured after the laser turnoff, respectively. Such separation is particularly useful for interpreting FDI dynamics.

Figure 1(b) displays typical time evolutions of the twoelectron energies for FDI1 and FDI2. In our calculation, the returning electrons do not directly populate the high-lying Rydberg states of Ar⁺ associated with FDI via impact excitation. Instead, the energies of the two electrons can be larger than zero after recollision and one of them is captured at the end of the laser pulse, as shown in Fig. 1(b).

III. RESULTS AND DISCUSSION

For Ar, SDI dominates when laser intensity is higher than $\sim 3 \times 10^{14}$ W/cm² [45]. To explore FDI in the NSDI regime we here choose the intensity range from 4×10^{13} W/cm² to 3.1×10^{14} W/cm². Figure 2(a) shows the calculated ratio of FDI to SI and the ratio of DI to SI as functions of laser

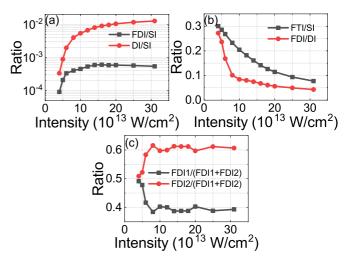


FIG. 2. (a) Calculated ratios of FDI to SI and DI to SI as functions of laser intensity. (b) Same as (a) but for the ratios of FTI to SI and FDI to DI. (c) Calculated ratio of FDI1 to FDI (the sum of FDI1 and FDI2) and the ratio of FDI2 to FDI as functions of intensity.

intensity. The intensity dependence of the ratio of DI to SI is similar to previous experiments on NSDI [45]. Interestingly, the ratio of FDI to SI shows a similar dependence on the intensity. The intensity-dependent ratio of FDI to DI is shown in Fig. 2(b). For comparison, we also calculate FTI events, which are identified when $E_{e_1,\text{final}} < 0$ and $E_{e_2,\text{final}} = -I_{p2}$, where I_{p2} is the second ionization potential of Ar. We find that both the calculated ratios of FTI to SI and FDI to DI decrease with the increase of intensity. Most FTI events are contributed by directly ionized trajectories rather than recollision trajectories because recollision tends to increase the drift momentum of e_1 [8,46]. As the intensity is increased, the directly ionized e_1 obtains larger momentum and the distance between e_1 and the ionic core becomes larger. Correspondingly, its kinetic energy becomes larger and the Coulomb attraction between e_1 and the core becomes weaker. As a result, it is harder for e_1 to be captured and the ratio of FTI to SI decreases as the intensity is increased. In our calculation, the ratio of FTI to SI decreases from 0.3 to 0.077 when the intensity is increased from 4×10^{13} W/cm² to 3.1×10^{14} W/cm². This is in excellent agreement with the theoretical derivation in Ref. [8] that this ratio will decrease from 0.3 to 0.072 $[Ar^*/Ar^+ \propto \frac{1}{I^{3/4}}(1-\frac{\sqrt{I}}{2I_{pl}^2})^{-1}$, where *I* is the laser intensity] for the same range of intensities. As for FDI, all the events are due to recollision in our calculation. When the intensity is increased, the returning energy of e_1 becomes larger and the energies of both e_1 and e_2 right after recollision thus become larger. Hence, it is harder for any one of the two electrons to be captured at the end of the laser pulse and the ratio of FDI to DI decreases.

Figure 2(b) shows that the electron trapping probability after SI is higher than the probability of FDI, which is in contrast with the observation mainly in the SDI regime [23]. As explained in Ref. [23], this can be understood because for the intensity region where NSDI dominates, the probability of FDI is suppressed due to the momentum offset of the electrons caused by recollision. When the intensity is increased to

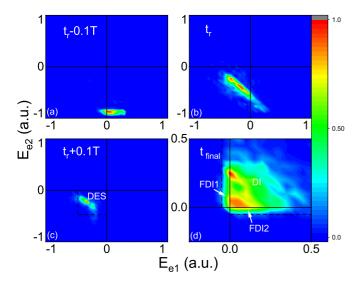


FIG. 3. Electron-electron energy distributions at different times for the intensity of 4×10^{13} W/cm². The two dashed lines in (c) for $E_{\rm e_1} = -0.52$ a.u. and $E_{\rm e_2} = -0.52$ a.u. are used to confine the region for doubly excited states of Ar. Here -0.52 a.u. is the energy of the first excited state of Ar. The two dashed lines in (d) for $E_{\rm e_1} = -0.05$ a.u. and $E_{\rm e_2} = -0.05$ a.u. are plotted to confine the regions for FDI1 and FDI2, respectively. The color scale of each panel has been normalized for comparison purposes.

the SDI regime, many more DI events occur sequentially and this leads to the rapid increase of the probability of FDI. The difference between our calculation and experiment around 3×10^{14} W/cm² may be due to the uncertainty of the experimental intensity and also that the semiclassical model can reproduce experimental DI and SI probabilities only qualitatively [32].

Figure 2(c) shows the ratios of FDI1 to FDI and FDI2 to FDI as functions of laser intensity. In the relatively high intensity regime ($I > 7 \times 10^{13} \text{ W/cm}^2$), the probability of FDI2 is significantly higher than the probability of FDI1. In the low intensity regime ($I \leq 5 \times 10^{13} \text{ W/cm}^2$), the probability of FDI1 is close to that of FDI2. For even lower intensities, the probability of FDI is extremely low and it is very challenging to calculate.

In the previous theoretical study [14], it was demonstrated that the recapture of the initially stuck electrons e_2 , corresponding to FDI2 in the current work, mainly contributes to atomic FDI. In contrast, our calculation shows that FDI1 also plays a significant role in FDI.

In order to understand the dependence of FDI on intensity, we investigate the energy distributions of the two electrons at 4×10^{13} W/cm² and 3.1×10^{14} W/cm², respectively. Figures 3(a)–3(c) display the electron-electron energy distributions of both DI and FDI events around the recollision time (denoted as t_r) when the two electrons are closest to each other for 4×10^{13} W/cm². Right before t_r , the returning energy of e_1 has a cutoff of 0.33 a.u., which is slightly larger than $3.17U_p$ (U_p is the ponderomotive energy) due to the existence of the tunneling exit and the Coulomb potential. The energy of e_2 is around -1.02 a.u. ($-I_{p2}$). At t_r , e_1 transfers some energy to e_2 . We find that doubly excited states (DESs) of Ar are largely

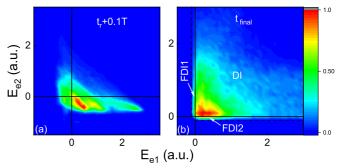


FIG. 4. (a) and (b) Electron-electron energy distributions at different times for the intensity of $3.1 \times 10^{14} \text{ W/cm}^2$. The dashed lines have the same meanings as in Fig. 3(d). The color scales have been normalized for comparison purposes.

populated shortly after t_r and the binding energy of e_1 is close to that of e_2 [Fig. 3(c)], which is consistent with a previous study of NSDI [47]. As e_1 and e_2 share the energy evenly during recollision and experience the same laser electric field afterwards, one can expect no preference for each electron with higher final energy than the other one. Hence, the probabilities of FDI1 and FDI2 are close to each other, as shown in Fig. 2(c).

As seen in Fig. 4(a), the energy of e_1 shortly after recollision is larger than zero for most DI and FDI events at $3.1 \times$ 10^{14} W/cm², which indicates that the DESs are no longer the main pathways for producing DI and FDI events for such high intensity. At 3.1×10^{14} W/cm², DI of Ar proceeds mainly via recollision impact ionization (RII) [48]. Despite the formation of Ar^{+*} shown in Fig. 4(a), the excited electron e_2 is ionized quickly after recollision for DI. It has been recently shown that, both theoretically [34] and experimentally [49], there exists a time delay lasting for a small fraction of T between t_r and double ionization time for RII. Here we show that a significant time delay between t_r and t' occurs for both FDI and DI events [Figs. 5(a) and 5(b)], where t' is the instant when both the energies of e_1 and e_2 are larger than zero for the first time for FDI events [see Fig. 1(b)] and the double ionization time for DI events. In accordance with Ref. [34], the time delay distribution shows three pronounced peaks for DI events [Fig. 5(b)]. As for FDI events, our calculation reveals five pronounced peaks, denoted as P1–P5 in Fig. 5(a). The substantial probability distributions for the time delay longer than 0.25T indicate that FDI is closely related to recollision excitation with subsequent ionization mechanism for NSDI. This is consistent with the previous work with a comparable intensity [14]. In the following, we will show that this time delay distribution is the key to understand the relative contribution of FDI1 (FDI2) at high intensities shown in Fig. 2(c).

Firstly, we discuss the mechanism of FDI events corresponding to the first peak (P1) in Fig. 5(a). The sum energy of the two electrons right after recollision is $E_{r_1} - I_{p2}$, where E_{r_1} is the returning kinetic energy of e_1 at recollision time. We have found that the energy of e_2 right after recollision is close to zero for most FDI events corresponding to P1. Neglecting Coulomb potential, the final kinetic energies of the

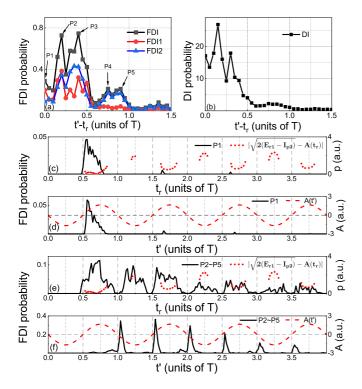


FIG. 5. (a) and (b) Time delay distributions for FDI and DI events at the intensity of 3.1×10^{14} W/cm², respectively. (c) and (d) Probability distributions (black curves) of t_r and t' for FDI events corresponding to P1 in (a), respectively. Corresponding distributions of $|\sqrt{2(E_{r_1} - I_{p2})} - A(t_r)|$ (red dotted curves) and A(t') (red dashed lines) are also shown. See text for details. (e) and (f) Same as (c) and (d) but for FDI events corresponding to P2–P5 in (a), respectively.

two electrons can thus be expressed as

$$E_{e_1,\text{final}} \approx \frac{|\vec{p}_r(t_r) + \vec{p}_d(t_r)|^2}{2} \approx \frac{\left[\sqrt{2(E_{r_1} - I_{p2})} - A(t_r)\right]^2}{2}$$
(6)

and

$$E_{e_2,\text{final}} \approx \frac{|\vec{p}_d(t')|^2}{2} = \frac{A(t')^2}{2},$$
 (7)

respectively, where $\vec{p}_r(t_r)$ is the residual momentum of e_1 right after recollision and \vec{p}_d is the drift momentum obtained from the laser field subsequently. Note that in Eq. (6), the transverse component of $\vec{p}_r(t_r)$ is negligibly small, which has been validated by the examination of recollision trajectories. In Fig. 5(c) we show the probability distribution of t_r for P1 and the corresponding distribution of $|\sqrt{2(E_{r_1} - I_{p2})} - A(t_r)|$, predicted by the simple-man theory [50]. One can find that t_r is mainly distributed from 0.5T to 0.75T where the value of $|\sqrt{2(E_{r_1}-I_{p2})}-A(t_r)|$ is close to zero, indicating that $\vec{p}_r(t_r)$ is canceled out by $\vec{p}_d(t_r)$. According to Eq. (6), $E_{e_1,\text{final}}$ is thus close to zero. As shown in Fig. 5(d), the probability distribution of t' is similar to that of t_r and the vector potential A(t') is nonzero for most trajectories. Consequently, for P1, e_1 is more likely to be captured after the end of the laser pulse, leading to FDI1.

For most FDI events corresponding to P2–P5 in Fig. 5(a), the energy of e_1 is larger than zero while the energy of e_2 is slightly smaller than zero right after t_r , which is similar

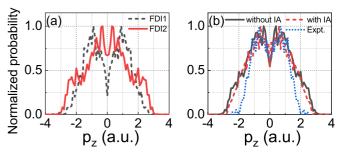


FIG. 6. (a) Calculated photoelectron momentum distributions for FDI1 and FDI2 at 3.1×10^{14} W/cm². (b) Comparison between the calculated photoelectron momentum distribution with and without intensity averaging (IA) for FDI at 3.1×10^{14} W/cm² and corresponding experimental result in Ref. [23].

to Fig. 4(a). As shown in Fig. 5(e), $\vec{p}_r(t_r)$ and $\vec{p}_d(t_r)$ do not cancel each other out for multiple returning trajectories, which contribute to FDI significantly. Consequently, the final energy of e_1 can be quite large for most FDI events. As for e_2 , it stays in the excited state of Ar⁺ until t'. Figure 5(f) displays the corresponding probability distribution of t'. One can find that the distribution peaks close to $\frac{n+1}{2}T$ ($n=1,2,3,\ldots$) where the vector potential A(t') is around zero. This is different from the case for P1. Therefore, e_2 tends to be captured after the end of the laser pulse [Eq. (7)], leading to FDI2. Due to the greater contribution of P2–P5 as compared with P1 [Fig. 5(a)], the probability of FDI2 is larger than that of FDI1, as shown in Fig. 2(c). This is consistent with the time delay distributions for FDI1 and FDI2 shown separately in Fig. 5(a).

To compare with the experiment, we further calculate the photoelectron momentum distribution for FDI at $3.1 \times$ 10¹⁴ W/cm². As shown in Fig. 6(a), the photoelectron momentum distribution for FDI1 displays a double-hump structure. For the calculation of FDI2, two additional "shoulders" around $p_z = \pm 2$ a.u. can be seen. For FDI2, the photoelectron (e_1) has the final momentum approximately equal to $\vec{p}_r(t_r)$ + $\vec{p}_d(t_r)$, which is close to zero for the first-returning trajectories [Fig. 5(e)], leading to the shallow dip around $p_z = 0$ a.u. shown in Fig. 6(a). The sum of $\vec{p}_r(t_r)$ and $\vec{p}_d(t_r)$ is much larger for even-order-returning trajectories [Fig. 5(e)], leading to the shoulderlike structures around $p_z = \pm 2$ a.u. For FDI1, e_1 is captured at the end of the laser pulse. The momentum of e_2 right after recollision is close to zero. As shown in Fig. 5(d), the distribution of t' peaks around 0.6T and the corresponding vector potential A(t') is 0.97 a.u. [A(t')] $-\frac{E}{w}\sin(wt')$]. Therefore, the final momentum distribution of the photoelectrons peaks around ± 0.97 a.u. considering the laser polarization direction along the z axis, which is consistent with the position of the double-hump structure for FDI1 in Fig. 6(a).

Figure 6(b) compares the calculated photoelectron momentum distribution (black solid line) for FDI (the sum of FDI1 and FDI2) and the experimental result in Ref. [23]. The calculation is in good agreement with the experiment, confirming the above analysis based on the recollision picture. Assuming that the spatial distribution of the intensity is Lorentzian in the propagation direction and Gaussian in the transverse direction

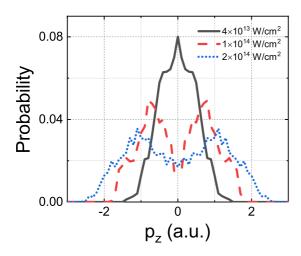


FIG. 7. Calculated photoelectron momentum distributions for FDI at different intensities.

[51], we also perform calculation including the focus intensity averaging effect [see the red dashed line in Fig. 6(b)] and find no obvious changes of the electron momentum distribution. Note that both the calculations are wider than the experimental result. One possible reason for the disagreement is that in the semiclassical model the rescattering effect can be overestimated. This results in a broader momentum distribution than the experiment [26].

A similar double-hump structure of photoelectron momentum distribution from SI has been revealed experimentally and theoretically, which is coined as a very-low-energy structure [52]. It can be fully understood with the single active electron approximation [52,53]. Differently, the two-hump structure for FDI here is due to recollision. The electron-electron interaction therein is indispensable to understand the mechanism of FDI.

Finally, we show the calculated photoelectron momentum distributions for FDI at different intensities in Fig. 7. The intensity dependence can be understood as follows. For FDI2 events, with the decrease of the intensity, $|\vec{p}_r(t_r)|$ becomes smaller than $|\vec{p}_d(t_r)|$ so that the final momenta of the photoelectrons (e_1) are no longer close to zero. This suppresses the FDI2 events around $p_z = 0$ a.u. As a result, the dip of the electron momentum distribution for FDI becomes more pronounced. When the intensity is further decreased to the regime where the DESs of Ar are the dominant pathways leading to FDI ($I \le 5 \times 10^{13} \text{ W/cm}^2$), the two electrons stay in the DESs for a while and one of them is then ionized around the maximum of the laser field where the vector potential is close to zero. Therefore, the final momenta of the photoelectrons peak around zero, resulting in a single-hump distribution with a much narrower width. The photoelectron momentum spectra thus provide access to identifying different pathways leading to FDI. The predicted intensity-dependent spectra can be verified by further experiments.

Note that Ref. [23] reported the transition of electron momentum distribution of FDI from the NSDI to the SDI regime. The width of the momentum distributions of electrons from FDI and SI measured at 7.9×10^{14} W/cm² are very similar. This represents solid experimental evidence that the electron trapping for FDI happens during the second ionization step of SDI. Here we focus on the intensity dependence of FDI in the NSDI regime. Although the electron momentum distribution at 4×10^{13} W/cm² in Fig. 7 shows a similar single-hump structure, the electron trapping is closely related to the recollision-induced DESs. The underlying mechanism of FDI is different from that at 7.9×10^{14} W/cm² (SDI regime) in Ref. [23].

IV. CONCLUSION

In conclusion, we theoretically investigate intensity dependence of the FDI process of Ar atoms. The calculated ratio of FDI to SI as a function of intensity shows a pronounced knee structure and the ratio of FDI to DI decreases with the increase of intensity. In the relatively low intensity regime, we demonstrate that the DESs of Ar are the dominant pathways for producing FDI. The probabilities of FDI1 and FDI2 are close to each other and the photoelectron momentum distribution shows a single-hump structure. For the relatively high intensity regime, the excited states of Ar⁺ are the dominant pathways leading to FDI. The probability of FDI2 is significantly higher than that of FDI1 and the photoelectron momentum distribution exhibits the double-hump structure, which is in good agreement with the recent experimental result [23]. Our work confirms that this observation stems from recollision and explains how recollision results in different photoelectron momentum distributions for different intensities. The predicted intensity-dependent electron momentum spectra encode information of the pathway leading to FDI, which is experimentally accessible. The current work demonstrates that atomic FDI generally exists as a companion with the strong-field NSDI process and offers novel physical insights into its dynamics.

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