## 7 Maps

1.

```
scheme
MAP_UNIVERSITY_SYSTEM =
   class
      type
        Student,
        Course,
        Course_infos = Course \( \frac{1}{m} \) Student-set,
        University = {|(ss, cis) : Student-set \times Course\_infos \cdot is\_wf(ss, cis) |}
      value
        is\_wf : Student\_set \times Course\_infos \rightarrow Bool
        is\_wf(ss, cis) \equiv (\forall ss' : Student-set \cdot ss' \in rng cis \Rightarrow ss' \subseteq ss),
        students: University \rightarrow Student\text{-}\mathbf{set}
        students(ss, cis) \equiv ss,
        courses : University → Course-set
        courses(ss, cis) \equiv dom cis,
        stud\_of : Course \times University \xrightarrow{\sim} Student-set
        \operatorname{stud\_of}(c, (ss, cis)) \equiv \operatorname{cis}(c) \operatorname{\mathbf{pre}} c \in \operatorname{\mathsf{courses}}(ss, cis),
        attending: Student \times University \stackrel{\sim}{\to} Course-set
        attending(s, (ss, cis)) \equiv
           \{c \mid c : Course \cdot c \in \mathbf{dom} \ cis \land s \in cis(c)\}
           \mathbf{pre} \ \mathbf{s} \in \mathrm{students}(\mathbf{ss}, \ \mathrm{cis}),
        new_stud : Student \times University \stackrel{\sim}{\rightarrow} University
        new\_stud(s, (ss, cis)) \equiv (ss \cup \{s\}, cis) pre s \notin students(ss, cis),
        drop_stud : Student \times University \stackrel{\sim}{\rightarrow} University
        drop\_stud(s, (ss, cis)) \equiv
           (ss \setminus \{s\}, [c \mapsto cis(c) \setminus \{s\} \mid c : Course \cdot c \in dom cis])
           \mathbf{pre} \ \mathbf{s} \in \mathrm{students}(\mathbf{ss}, \ \mathrm{cis}),
        sizes\_ok : University \rightarrow Bool
        sizes\_ok(ss, cis) \equiv
           (\forall c : Course \cdot c \in dom \ cis \Rightarrow (card \ cis(c) \leq 100 \land card \ cis(c) \geq 5))
   end
```