



Formalization of Android Activity-Fragment Multitasking Mechanism and Static Analysis of Mobile Apps

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The multitasking mechanism between activities and fragments plays a fundamental role in the Android operating system, which involves a wide range of features, including launch modes, intent flags, task affinities, and structured activities containing fragments. All of them are being widely used in Android apps, both open source and commercial ones. In this article, we present a formal semantics of the Android multitasking mechanism between activities and fragments, which accommodates all the important features and gives insofar the most comprehensive and accurate formalization. In particular, our semantics is formulated based on multi-stack systems, and fully captures the behavior of task stacks and activity stacks regarding fragments. Based on the semantics, we provide new static analysis algorithms, which are both multi-stack aware and fragment sensitive, thus achieve more precise static analysis for Android apps. We validate our approach by extensive experiments on both open source and commercial Android apps. The results highlight the benefits of the considering the semantics of the multitasking mechanism between activities and fragments in static analysis, and confirm the efficacy of our approach.

CCS Concepts: • Theory of computation → Operational semantics; • Software and its engineering → Formal software verification;

Additional Key Words and Phrases: Android multitasking mechanism, activities and fragments, formal semantics, stack unboundedness, static analysis

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1 Introduction

Android, a mobile operating system developed by Google, serves more than 2 billion monthly active users and occupies more than 80% of the share of the global mobile operating system market.¹ The Google Play App store, Google's official pre-installed app store on Android devices, has supplied 2 million apps since 2016.²

The multitasking mechanism between activities and fragments plays a fundamental role in the Android operating system. Mobile apps provide diverse functionalities with seamless user experience by interacting with other apps. For example, the Gallery app utilizes the Email app to send pictures rather than implements its own e-mail functionality.³ These features require the support of frequent switch between apps. Moreover, Android provides a “back” button by which users can easily switch between apps.

To facilitate smooth app switching and history recalling, Android introduces a last-in-first-out data structure, generally referred to as *back stack*, to store users' histories. Technically speaking, the back stack exhibits a three-tier nested structure. At the highest layer, there is a stack of tasks where each task can be considered as a stack of activities (the middle layer), and each activity may contain fragment stacks (the lowest layer). In other words, the back stack exhibits a hierarchy of task stack, activity stack, and fragment stack. From the functionality perspective, a task is a collection of activities that users interact with when performing a certain job (e.g., view e-mail); an activity is a type of app component, which provides a **graphical user interface (GUI)** on screen and serves the entry point of the interaction with users. To facilitate GUI reuse, an activity may be further divided into fragments. A fragment defines and manages its own layout, has its own lifecycle, and can handle its own input events. It cannot live on its own (i.e., must be hosted by an activity).

Activities are a central concept in the Android multitasking mechanism. In particular, the evolution of the back stack depends on various attributes of activities, including launch modes and task affinities, as well as the intent flags when starting activities. Moreover, the updates of the fragment containers in activities are controlled by fragment transactions (cf. Section 2 for more details).

In light of its central role in analyzing Android apps, the multitasking mechanism between activities and fragments has been considered in the literature. First, there has been decent work toward its formalization, and we refer to readers to Section 1.1 for some introduction. However, the existing formal semantics is far from complete. A primary drawback is that the activities are treated as an atomic object therein, whereas the internal structures (e.g., fragments) were abstracted away. The understanding of semantics may play a significant role in carrying out semantics-aware analysis of the mobile app, which can capture more features of the Android platform and thus is more precise. In contrast, the state-of-the-art analysis largely applied a syntactic approach. The underlying stack semantics of the multitasking mechanism between activities and fragments is either ignored completely ([2, 5, 10]) or considered in a very much restricted form (e.g., single stack [17]), or otherwise important features (e.g., task affinities or fragments) are skipped [14, 17, 18].

¹<https://expandedramblings.com/index.php/android-statistics/>

²<https://www.statista.com/statistics/266210/number-of-available-applications-in-the-google-play-store/>

³https://play.google.com/store/apps/details?id=com.google.android.apps.photosgo&hl=en_US

The status quo is clearly unsatisfying. Indeed, all the multitasking features, including task affinities and fragments, are widely used in Android apps, especially the commercial ones. A small-scale survey on the 3,000 most downloaded commercial Android apps in Google Play shows that almost all apps use launch modes and intent flags, about 10% of the apps use non-default task affinities, and about 50% of the apps involve fragments. We address these shortcomings in the current article.

Main Contributions. In this article, we make the following contributions:

- We introduce a new model, AMASS(Android Multitasking Stack System), to define the formal semantics of the multitasking mechanism between activities and fragments. AMASS covers all the important multitasking features (e.g., task affinities and fragments) and provides, to the best of our knowledge, insofar the most comprehensive formal account of the Android multitasking mechanism between activities and fragments. Moreover, we validate the formal semantics of AMASS models against the actual behavior of Android apps by designing a special-purpose app and doing large-scale experiments with the app.
- We harness the semantics to design novel algorithms for static analysis of the abnormal behaviors of task unboundedness and fragment container unboundedness.
- We implement the algorithms into a static analysis tool called *TaskDroid* and experiment on a corpus of open source and commercial Android apps. The results show that TaskDroid can detect the task/fragment container unboundedness problems for open source and commercial Android apps and the unboundedness problems entail abnormal behaviors of Android apps, including black screen, app crash, and device reboot, owing to a fine-grained semantic modeling of the Android multitasking mechanism between activities and fragments.

1.1 Related Work

Formalization of Android Multitasking Semantics. In light of its central role in analyzing Android apps, the multitasking mechanism between activities and fragments has been considered in the literature. To the best of our knowledge, this line of work was initiated in the work of Azim and Neamtiu [2], where the concept of **activity transition graphs (ATGs)** was proposed. ATGs are directed graphs where nodes are activities and edges describe the relationships that an activity can start the other. ATGs can be used for generating traces in GUI testing. An extension of ATGs (i.e., window transition graphs) were proposed by Yang et al. [17]. In window transition graphs, windows are assumed to be stored in one stack; nodes are windows that include not only activities but also menus and dialogs; transitions represent a sequence of push/pop operations associated with sequences of callbacks. ATGs were also extended in the work of Yan et al. [14], giving rise to the LATTE model, a finite-state machine model that stores the activities in a bounded-height stack as well as some state information transferred across activities. Moreover, in the work of Zhang et al. [18], activities were assumed to be stored into a stack and its contents were used as contexts for GUI testing and pointer analysis. In the work of Liu et al. [10], a tool called *TDroid* was developed to utilize the syntactic patterns on the launch modes, intent flags, and task affinities to detect the app switching attacks. All of the preceding work did not consider fragments which were addressed by Chen et al. [5], where **activity fragment transition graphs (AFTGs)** were proposed and used for GUI testing. Furthermore, in other works [6–8], formal semantics for the Android multitasking mechanism were proposed.

One serious drawback of the current formalization is that the activities are treated as an atomic object therein, whereas the internal structures (e.g., fragments) were abstracted away. In this article, to the best of our knowledge, we provide the first complete formal account of the operational

semantics, differentiating different versions of Android, and carry out validation ensuring its conformance to the actual behavior.

Static Analysis. Static analysis approaches have been applied to Android apps, where typical tasks include assessing the security of Android apps, detecting app clones, automating test cases generation, or uncovering non-functional issues related to performance or energy [9]. There is a large body of work where in general the analysis techniques are still those which have been thoroughly considered in the static analysis of programs (e.g., control-flow analysis, data-flow analysis, and point-to analysis) but are adapted to Android apps.

A specific purpose of static analysis that is the closest to this work is to reveal security vulnerabilities, many of which are related to the **inter-component communication (ICC)** mechanism and its potential misuses such as component hijacking. For instance, Lu et al. [11] applied reachability analysis on customized system dependence graphs to detect component hijacking vulnerabilities, and Octeau et al. [12, 13] implemented the detection of inter-component vulnerabilities. We refer to the work of Li et al. [9] for a systematic literature review for the static analysis of Android apps.

In terms of static analysis w.r.t. the multitasking mechanism between activities and fragments, the state-of-the-art analysis largely applied a syntactic approach. The underlying stack semantics of the multitasking mechanism between activities and fragments is either ignored completely (e.g., [2, 5, 10]) or considered in a restricted form (e.g., single stack [17]), or otherwise important features (e.g., task affinities or fragments) are skipped [14, 17, 18].

Lee et al. [8] develop a static analysis tool based on the operational semantics formalized therein, which can analyze Android apps. The tool extracts the necessary information (e.g., activity, intent flag) and analyzes possible activity injection cases to detect activity injection attacks. However, we are not aware of other formal approaches toward analysis of Android apps accounting for the multitasking mechanism between activities and fragments similar to what we present in the current work.

Structure. The rest of the article is organized as follows. Section 2 gives an informal introduction to the Android multitasking mechanism between activities and fragments. Section 3 motivates this work with two open source apps from F-Droid. Section 4 introduces the AMASS model and formalization of the multitasking mechanism between activities and fragments. Section 5 shows how to extract AMASS models out of Android APK files. Section 6 describes how to encode the semantics of the AMASS models into the reachability problem of finite state machines that can be tackled by the symbolic model checker nuXmv, if the stack heights are assumed to be bounded by a constant. Section 7 is devoted to the validation of the formal semantics of AMASS models against the actual behaviors of Android apps. Section 8 presents the static analysis algorithms for the task/fragment container unboundedness problems. Section 9 describes the implementation of the static analysis tool, TaskDroid, the benchmarks, and the experiments for the evaluation of TaskDroid. The article concludes in Section 10.

A preliminary version of this work appeared in the proceedings of APLAS 2019 [7]. This article extends the APLAS paper in the following five aspects. First, fragments, a crucial feature of Android multitasking which was ignored in prior work [7], is fully addressed in the current article, including the formal semantics and static analysis. Second, the semantics of the multitasking mechanism between activities and fragments for Android 6.0 through 13.0 are defined in this work, whereas only the semantics for Android 7.0 and 8.0 were defined in the prior work [7]. Third, for the semantics validation, this article extends the previous work in two ways: the relevant parts of the source code of Android OS are audited, and 20 open source F-Droid apps are included in addition to the app that is specially designed for the empirical validation. Fourth, the models are extracted both statically and dynamically in this article, whereas only static model extraction was

used in prior work [7]. Fifth, the experiments are considerably more thoroughly done with, in particular, more benchmarks.

2 Android Multitasking Mechanism between Activities and Fragments

In this section, we briefly review the core concepts regarding the Android multitasking mechanism (i.e., activities and fragments) and the evolution of the back stack.

2.1 Activity, Task, and Task Stack

For the purpose of this work, an Android app can be considered as a collection of *activities*. At any time, there is one activity displayed on the screen of the device. The activities are organized into tasks. A *task* is a collection of activities to carry out a certain job. The running activities within a task are managed as an *activity stack* following the order that an activity is opened. In the activity stack, there are two distinguished activities—that is, the *root activity* and *top activity*, which are sitting at the bottom and top of the stack respectively.

The Android system normally runs multiple tasks which are organized as the *task stack*. The top task is the *foreground* task, whereas others are *background* tasks. When a task comes to the foreground, its top activity is displayed on the device screen. When an activity finishes, it is popped from the activity stack. If the activity stack is not empty, the new top activity is displayed on the screen. Otherwise, the task itself finishes, in which case it is popped from the task stack. We mention that the Home screen comes to the foreground when a user presses the Home button (in this case, the task stack will be emptied) or when the task stack becomes empty. The task stack is the central data structure for the Android multi-tasking mechanism, and we are mostly interested in its evolution in response to activity activation. When an activity is started, there are three basic attributes which determine the resulting task stack: *launch modes*, *task affinities*, and *intent flags*.

All activities of an app, as well as their launch modes and task affinities, are defined in the *manifest file* (AndroidManifest.xml). Differently, intent flags are set by caller activities to declare how to activate target activities by calling `startActivity()` or `startActivityForResult()` with the intent flags as its arguments. The launch mode attribute specifies one of four modes to launch an activity: standard, singleTop, singleTask, and singleInstance, with standard being the default. A standard or singleTop activity can be instantiated multiple times, leading to duplicated activities in a task. In contrast, an activity with the singleTask or singleInstance launch mode should be instantiated only once. Furthermore, an activity with the singleInstance launch mode is always the root activity of a task. While a singleTask activity can contain other standard or singleTop activities in its task, a singleInstance activity does not contain any other activities in its task. It is the only activity in its task; if it starts another activity, that activity is assigned to a different task. The task affinity attribute is of the string data type and specifies to which task the activity prefers to belong. By default, all activities from the same app have the same affinity, the package name of the app (i.e., all activities in the same app prefer to be in the same task). However, one can modify the default affinity of the activity. Android allows a great degree of flexibility: activities defined in different apps can share a task affinity, whereas activities defined in the same app can be assigned with different task affinities.

Android supports ICC via *intents*. An intent is an asynchronous message that activates activities. Android provides two types of intents: *explicit* intents and *implicit* intents. Explicit intents specify directly which activity to activate. Implicit intents, however, do not directly specify the activities which should be called, but only specify actions to be performed. For example, an implicit intent with the action “ACTION_VIEW” and the data of the URL “<http://www.google.com>” will cause a web browser to open a webpage. The Android system searches for all activities which are registered for the specific action and the data type. If many activities are found, then the user can select which

Table 1. Reasons for Ignoring Some Intent Flags in This Article

Intent Flags	Reasons for Being Ignored in This Article
FLAG_ACTIVITY_REQUIRE_DEFAULT	Related to implicit intents, which we do not consider in this work
FLAG_ACTIVITY_REQUIRE_NON_BROWSER	
FLAG_ACTIVITY_MATCH_EXTERNAL	
FLAG_ACTIVITY_FORWARD_RESULT	Used for transferring results between activities, which we do not consider in this work
FLAG_ACTIVITY_RETAIN_IN_RECENTS	Related to the recent app list, which we do not consider in this work
FLAG_ACTIVITY_EXCLUDE_FROM_RECENTS	
FLAG_ACTIVITY_CLEAR_WHEN_TASK_RESET	Deprecated from Android 5.0
FLAG_ACTIVITY_BROUGHT_TO_FRONT	Can only be set by the Android operating system, not set by application code
FLAG_ACTIVITY_LAUNCHED_FROM_HISTORY	
FLAG_ACTIVITY_NO_USER_ACTION	Related to the lifecycle of activities, which we do not model in this work
FLAG_ACTIVITY_NO_ANIMATION	Used to show some animation when starting an activity and not related to the evolution of the back stack
FLAG_ACTIVITY_LAUNCH_ADJACENT	Related to the split-screen mode, which we do not consider in this work
FLAG_ACTIVITY_RESET_TASK_IF_NEEDED	Related to the “allowTaskReparenting” attribute of activities, which we do not consider in this work

activities to use. In this article, we restrict our attention to explicit intents since our focus is to understand the evolution of the back stack when activities are started, and we do not attack the (another challenging) problem of resolving which activity should be started by implicit intents.

Android provides 23 intent flags related to activities (see the Developers site [1] for the detailed description of the intent flags). Intent flags are set by caller activities to declare how to activate target activities and are passed to `startActivity()` or `startActivityForResult()` as their arguments. In this article, among the 23 intent flags, we consider the following 10 flags:

- FLAG_ACTIVITY_NEW_TASK,
- FLAG_ACTIVITY_NEW_DOCUMENT,
- FLAG_ACTIVITY_MULTIPLE_TASK,
- FLAG_ACTIVITY_SINGLE_TOP,
- FLAG_ACTIVITY_REORDER_TO_FRONT,
- FLAG_ACTIVITY_CLEAR_TOP,
- FLAG_ACTIVITY_CLEAR_TASK,
- FLAG_ACTIVITY_PREVIOUS_IS_TOP,
- FLAG_ACTIVITY_NO_HISTORY,
- FLAG_ACTIVITY_TASK_ON_HOME.

The other 13 intent flags are ignored, for various reasons as shown in Table 1.

Besides launch modes, task affinities, and intent flags, there are some other factors that may also affect the behaviors of the task stack. When a caller activity calls `startActivity()` or `startActivityForResult()` to start a callee activity, the caller activity can also call the `finish()` procedure so that when the callee activity is started, the caller activity is finished. Moreover, the *real activity*⁴ of a task also matters. The real activity of a task is the activity that was pushed into the task as the bottom activity when the task was created. If the real activity of a task is *B* and the task is not the main task, then attempting to push an instance of *B* to the task will not modify the task.

2.2 Fragment, Fragment Stack, Fragment Transaction, and Fragment Transaction Stack

Importantly, activities are *not* an atomic object and may contain subcomponents such as fragments. Previous formalism did not address these, but the current article will (cf. Section 4). In a nutshell,

⁴The name is inherited from the Android system.

a fragment represents a modular portion of the user interface within an activity. Related to fragments, *view* is a basic building block of UI in Android. Intuitively, a view is a small rectangular box that responds to user inputs (EditText, Button, CheckBox, etc.) One can simply understand that a fragment serves as a canvas where different views are aggregated which can, for instance, facilitate reuse. Fragments are stored in a fragment container as a stack, which is called *fragment stacks*. Moreover, an activity may maintain several fragment containers.

At runtime, an app can add, remove, and replace fragments in response to user interaction. The add (respectively, remove) action will push (respectively, pop) a fragment into (respectively, out of) a fragment container. The replace action will first remove all fragments in a fragment container, then push a fragment into it. Multiple fragment actions may be involved in response to one user interaction. Typically, these fragment actions are grouped into *fragment transactions*, where either all fragment actions are executed or none of them is executed. The app can choose to push some fragment transactions into a stack called the *fragment transaction stack*, which is used to restore the historical states by canceling the effects of the fragment transactions in the stack, when a user presses the back button later on.

It is worth emphasizing that, unfortunately, the terminologies in the literature (e.g., multitasking, activity stacks, task stacks) are not necessarily consistent. In particular, the notion of multitasking is sometimes used to denote the split-screen multitasking where the screen is split into regions to allow several apps to be displayed simultaneously, and moreover, the notion of back stack is widely used in Android documents but may (misleadingly) refer to any stack regarding the action of pressing the back button. In this article, we use *multitasking* to denote the fundamental mechanism of the Android operating system that utilizes the task stack, a two-tier stack system, to facilitate smooth switching between tasks, even if the device is not in the split-screen mode. Furthermore, this article will clarify the notions related to the multitasking mechanism (e.g., tasks and activities) via a proper formalization.

It turns out that there are subtle differences between the multitasking mechanisms of different versions of Android. In this article, we focus on the multitasking mechanisms of the following versions of Android: 6.0, 7.0, 8.0, 9.0, 10.0, 11.0, 12.0, and 13.0.

3 Motivating Examples

We use two simple apps from F-Droid, namely “LaunchTime Homescreen”⁵ and “ShoppingList,”⁶ to motivate this work. We use the two examples to demonstrate that a model of the Android multitasking mechanism, where the various factors related to activities and fragments, including launch modes, task affinities, intent flags, the finish() procedure, and fragment actions, are taken into account, enables a more accurate static analysis of Android apps.

3.1 The “LaunchTime Homescreen” App: A Motivating Example for Accurate Modeling of Factors of Activities

The “LaunchTime Homescreen” app contains 10 activities. Let us focus on MainActivity and SettingsActivity. A snippet of the source code of the 2 activities in the “LaunchTime Homescreen” app is shown in Figure 1. The launch modes of MainActivity and SettingsActivity are singleInstance and standard, respectively. In line 3942 of the MainActivity.java file (see Figure 1), MainActivity starts SettingsActivity by calling the function startActivity(settingsIntent), where the settingsIntent contains the intent flag FLAG_ACTIVITY_NEW_TASK. However, in line 142 of the SettingsActivity.java file (see Figure 1), SettingsActivity starts MainActivity by calling the func-

⁵ Available at <https://github.com/quaap/LaunchTime/blob/master/>

⁶ Available at <https://github.com/GroundApps/ShoppingList/blob/master/>

```

// app/src/main/AndroidManifest.xml
24     <activity
25         android:name=".MainActivity"
26         android:configChanges="orientation|keyboardHidden|screenSize"
27         android:launchMode="singleInstance"
28         android:windowSoftInputMode="stateHidden|adjustPan">
29         <intent-filter>
30             <action android:name="android.intent.action.MAIN" />
31             ...
32         </intent-filter>
33         ...
34     </activity>
35     <activity
36         android:name=".SettingsActivity"
37         ...
38     </activity>
39
// app/src/main/java/com/quaap/launchtime/MainActivity.java
3937     public static void openSettings(Activity activity) {
3938         Intent settingsIntent = new Intent(activity, SettingsActivity.class);
3939         settingsIntent.addFlags(Intent.FLAG_ACTIVITY_NEW_TASK);
3940         ...
3941         activity.startActivity(settingsIntent);
3942     }
3943 }
3944
// app/src/main/java/com/quaap/launchtime/SettingsActivity.java
139     public boolean onKeyDown(int keyCode, KeyEvent event) {
140         if(keyCode==KeyEvent.KEYCODE_HOME || keyCode==KeyEvent.KEYCODE_MENU) {
141             Intent main = new Intent(this, MainActivity.class);
142             startActivity(main);
143             setResult(RESULT_OK);
144             finish();
145         }
146         return super.onKeyDown(keyCode, event);
147     }

```

Fig. 1. Source code of the F-Droid app “LaunchTime Homescreen.”

tion `startActivity(main)`, where all intent flags are set to be false. Moreover, in line 144 of the same file, `finish()` is called after `MainActivity` is started. In other words, when `MainActivity` is started, `SettingsActivity` is finished.

Let us consider the task unboundedness problem—that is, whether there is a task where the number of activities in the task can be unbounded (i.e., arbitrarily large). In the sequel, we show how the AMASS model provides more precise information than the other models so that we can detect the task unboundedness of the “LaunchTime Homescreen” app more accurately:

- If we use the ATG to model the “LaunchTime Homescreen” app, then the resulting ATG is just a cycle with two vertices: `MainActivity` and `SettingsActivity`. Then according to the ATG model, we may conclude that the task can become unbounded, since these two activities can start each other indefinitely.
- If we use the models where the launch modes, task affinities, and intent flags are taken into account (e.g., that in the work of Lee et al. [8]), then the launch modes and intent flags are added as the labels of vertices and edges respectively in the ATG model. In other words, the vertices are `MainActivity(singleInstance)` and `SettingsActivity(standard)`, where the vertex labels (launch models) are put in brackets, and the edge from `MainActivity` to `SettingActivity` is labeled by `start(NTK)` (where `start` and `NTK` are the abbreviations of `startActivity` and `FLAG_ACTIVITY_NEW_TASK`, respectively) and the edge from `SettingActivity` to `MainActivity` is labeled by `start(\perp)` (where \perp denotes the fact that all intent flags are false). In this case, compared to the ATG model, more information is available. For instance, we know that there are at most two tasks: one task holding a unique instance of `MainActivity` (since its launch mode is `singleInstance`), and the other task holding the instances of `SettingsActivity`. Nevertheless, we may still conclude that the task where the instances of `SettingsActivity`

belong to can become unbounded, since `SettingsActivity` can be started by `MainActivity` for an unbounded number of times.

- However, if we use the AMASS model in this work, then in addition to the launch modes and intent flags, we can model the `finish()` procedure. In other words, the edge from `SettingsActivity` to `MainActivity` is labeled by `finishStart(\perp)`, where `finishStart` represents the fact that `finish()` is called after `startActivity()` is called. In this case, each time when `MainActivity` is started by `SettingsActivity`, `SettingsActivity` is finished simultaneously. As a result, the task holding `SettingsActivity` contains at most one instance of `SettingsActivity`. We conclude that the “LaunchTime Homescreen” app does not suffer from the task unboundedness problem actually.

This example motivates us to cover in the AMASS model as much as possible the information about activities, including launch modes, task affinities, and intent flags, as well as the `finish()` procedure, to facilitate a precise static analysis of the Android apps.

3.2 The “ShoppingList” App: A Motivating Example for Accurate Modeling of Factors of Fragments

If a model of the Android multitasking mechanism does not capture the fragments, then the fragment container unboundedness problem will be missed in the static analysis of Android apps. Furthermore, if the fragments are captured, but in an imprecise way, then the static analysis may still be inaccurate. Let us use the “ShoppingList” app to illustrate this point. The “ShoppingList” app comprises two activities: `MainActivity` and `SettingsActivity`. `MainActivity` contains five fragments. Let us focus on three of them, namely `ErrorFragment`, `ShoppingListFragment`, and `CacheListFragment`. From the snippet of the source code in Figure 2, `ErrorFragment` can start `ShoppingListFragment` and `CacheListFragment` via the `replace()` function (see lines 69 and 75 of the `ErrorFragment.java` file). However, `ShoppingListFragment` can start `ErrorFragment` via the `replace()` function (see line 392 of the `ShoppingListFragment` file):

- If an imprecise model for fragments, such as the AFTG model in the work of Chen et al. [5], is used, then we may wrongly reports that the “ShoppingList” app suffers from the fragment container unboundedness problem. The AFTG model extends the ATG model by taking the fragments into consideration and considering all of the transitions between them. Nevertheless, the AFTG model does not distinguish between the add and replace actions. As a result, from the existence of a cycle between `ErrorFragment` and `ShoppingListFragment` in the AFTG model, we may report that the “ShoppingList” app is fragment container unbounded.
- However, if the AMASS model is used, then we can add labels to the edges in the AFTG model and distinguish between the add and replace actions. Then we know that the two edges between `ErrorFragment` and `ShoppingListFragment` are both labeled by the replace action. As a result, before `ErrorFragment` or `ShoppingListFragment` is pushed to the fragment container, the fragment container is emptied. We conclude that the cycle between `ErrorFragment` or `ShoppingListFragment` does not lead to the fragment container unboundedness problem.

This example motivates us to capture the information about fragments, in particular, distinguish between different fragment actions, in the definition of the AMASS model.

4 Android Multitasking Stack System

In this section, we introduce AMASS, a formal model to capture the Android multitasking mechanism. Our presentation is inspired by previous work [6, 7], but the model significantly deviates from the ASM therein. Throughout the article, we let $[m] = \{1, \dots, m\}$, \mathbb{N} be the set of natural numbers, and $\mathbb{N}_{>0}$ be the set of positive natural numbers.

```

// app/src/main/java/org/janb/shoppinglist/fragments/ErrorFragment.java
63     public void onClick(View view) {
64         android.app.FragmentManager fragmentManager = getFragmentManager();
65         FragmentTransaction transaction = fragmentManager.beginTransaction();
66         switch (view.getId()) {
67             case R.id.error_btn_retry:
68                 ShoppingListFragment listFR = new ShoppingListFragment();
69                 transaction.replace(R.id.fragment_container, listFR);
70                 transaction.addToBackStack(null);
71                 transaction.commit();
72                 break;
73             case R.id.error_btn_cache:
74                 CacheListFragment cacheFR = new CacheListFragment();
75                 transaction.replace(R.id.fragment_container, cacheFR, "CACHE_FRAGMENT");
76                 transaction.addToBackStack(null);
77                 transaction.commit();
78                 break;
79             ...
80         }
81     }
// app/src/main/java/org/janb/shoppinglist/fragments/ShoppingListFragment.java
378     public void onError(ResponseHelper error) {
379         ...
380         ErrorFragment errFR;
381         ...
382         fragmentManager = getFragmentManager();
383         FragmentTransaction transaction = fragmentManager.beginTransaction();
384         transaction.replace(R.id.fragment_container, errFR);
385         transaction.addToBackStack(null);
386         transaction.commitAllowingStateLoss();
387     }
}

```

Fig. 2. Source code of the F-Droid app “ShoppingList.”

Following the overview of Section 2, we shall concentrate on the launch mode, the task affinity, the intent flags when an activity is launched, and the fragment transaction when a fragment is started:

- There are four launch modes in Android: “standard (STD),” “singleTop (STP),” “singleTask (STK),” and “singleInstance (SIT).” We shall consider all of them.
- As mentioned earlier, we focus on 10 intent flags in this article, namely
 - FLAG_ACTIVITY_NEW_TASK (NTK),
 - FLAG_ACTIVITY_NEW_DOCUMENT (NDM),
 - FLAG_ACTIVITY_MULTIPLE_TASK (MTK),
 - FLAG_ACTIVITY_SINGLE_TOP (STP),
 - FLAG_ACTIVITY_REORDER_TO_FRONT (RTF),
 - FLAG_ACTIVITY_CLEAR_TOP (CTP),
 - FLAG_ACTIVITY_CLEAR_TASK (CTK),
 - FLAG_ACTIVITY_PREVIOUS_IS_TOP (PIT),
 - FLAG_ACTIVITY_NO_HISTORY (NOH),
 - FLAG_ACTIVITY_TASK_ON_HOME (TOH).
- There are three actions in fragment transaction: “add (ADD),” “replace (REP),” and “remove (REM),” and we consider all of them. The semantics of these actions are related to the identifiers of fragment instances which we assume are from $\mathbb{N}_{>0}$.

Moreover, for fragment transactions, we use the tag TS (respectively, NTS) to represent the fact that a fragment transaction will be pushed (respectively, will not be pushed) to the fragment transaction stack.

All abbreviations and their full names are summarized in Table 2 to facilitate the later references. Note that STP is used as an abbreviation for both the SingleTop launch mode and the FLAG_ACTIVITY_SINGLE_TOP intent flag. This is acceptable since it is usually clear from the context whether STP denotes a launch mode or an intent flag.

Table 2. Abbreviations and Their Full Names

Abbreviation	Full name
STD	Standard
STP	SingleTop
STK	SingleTask
SIT	SingleInstance
STP	FLAG_ACTIVITY_SINGLE_TOP
CTP	FLAG_ACTIVITY_CLEAR_TOP
RTF	FLAG_ACTIVITY_REORDER_TO_FRONT
NTK	FLAG_ACTIVITY_NEW_TASK
NDM	FLAG_ACTIVITY_NEW_DOCUMENT
MTK	FLAG_ACTIVITY_MULTIPLE_TASK
CTK	FLAG_ACTIVITY_CLEAR_TASK
PIT	FLAG_ACTIVITY_PREVIOUS_IS_TOP
NOH	FLAG_ACTIVITY_NO_HISTORY
TOH	FLAG_ACTIVITY_TASK_ON_HOME
ADD	add
REP	replace
REM	remove
TS	added to the fragment transaction stack
NTS	not added to the fragment transaction stack

Let $\mathcal{F} = \{\text{NTK}, \text{NDM}, \text{MTK}, \text{STP}, \text{RTF}, \text{CTP}, \text{CTK}, \text{PIT}, \text{NOH}, \text{TOH}\}$ denote the set of intent flags, and let $\mathcal{B}(\mathcal{F})$ denote the set of formulas $\phi = \bigwedge_{F \in \mathcal{F}} \theta_F$, where $\theta_F = F$ or $\neg F$. For convenience, we use \perp to denote $\bigwedge_{F \in \mathcal{F}} \neg F$.

Definition 1 (Android Multitasking Stack System). An AMASS is a tuple

$$\mathcal{M} = (\text{Act}, A_0, \text{Frg}, \text{Lmd}, \text{Aft}, \text{Ctn}, \Delta),$$

where

- Act is a finite set of activities, and $A_0 \in \text{Act}$ is the main activity, let $m = |\text{Act}|$,
- Frg is a finite set of fragments,
- $\text{Lmd} : \text{Act} \rightarrow \{\text{STD}, \text{STP}, \text{STK}, \text{SIT}\}$ is the launch mode function,
- $\text{Aft} : \text{Act} \rightarrow [m]$ is the task affinity function,
- $\text{Ctn} : \text{Act} \rightarrow \mathbb{N}^*$ is the fragment container function that assigns to each activity a finite sequence of mutually distinct fragment container identifiers,
- $\Delta \subseteq (\text{Act} \cup \text{Frg}) \times (\text{ActInst} \cup \text{FrgInst}) \cup \{\text{back}\}$ is a finite set of transition rules. Here, $\text{ActInst} =$

$$\{\alpha(A, \phi) \mid \alpha \in \{\text{start}, \text{finishStart}\}, A \in \text{Act}, \phi \in \mathcal{B}(\mathcal{F})\}$$

and $\text{FrgInst} = \{\mu[T] \mid \mu \in \{\text{TS}, \text{NTS}\}, T \in \mathcal{T}\}$, where \mathcal{T} is a finite set of fragment transactions of the form $(\beta_1(F_1, i_1, x_1), \dots, \beta_k(F_k, i_k, x_k))$ where for every $j \in [k]$, $\beta_j \in \{\text{ADD}, \text{REP}, \text{REM}\}$, $F_j \in \text{Frg}$, $i_j \in \mathbb{N}$, and x_j is a variable storing the identifiers of fragment instances.

Moreover, we consider several submodels of AMASS, namely *activity-oriented* AMASS ($\text{AMASS}_{\text{ACT}}$) and *fragment-oriented* AMASS ($\text{AMASS}_{\text{FRG}}$), where all transition rules are on the activity level and fragment level respectively. More precisely, an $\text{AMASS}_{\text{ACT}}$ (respectively,

AMASS_{FRG}) is an AMASS where all transitions are *activity oriented*—that is, $\Delta \subseteq \text{Act} \times \text{ActInst} \cup \{\text{back}\}$ (respectively, *fragment oriented*, $\Delta \subseteq \text{Frg} \times \text{FrgInst} \cup \{\text{back}\}$).

For readability, we write a transition rule $(A, \alpha(B, \phi)) \in \Delta$ as $A \xrightarrow{\alpha(\phi)} B$ and $(A, \mu[T]) \in \Delta$ as $A \xrightarrow{\mu} T$. Therefore, all transitions in an AMASS_{ACT} (respectively, AMASS_{FRG}), except back, are of the form $A \xrightarrow{\alpha(\phi)} B$ (respectively, $A \xrightarrow{\mu} T$).

The rest of this section is devoted to the semantics of AMASS . We shall first define the semantics of AMASS for Android 13.0 and consider the semantics for other versions later.

4.1 Semantics of AMASS for Android 13.0

As the model of AMASS involves both activities and fragments, its semantics is rather involved. To ease the understanding, we separate the concerns and define the formal semantics of AMASS_{ACT} and AMASS_{FRG} , respectively. (The long and detailed definition of the formal semantics of AMASS is presented in the appendix.)

4.1.1 Semantics of AMASS_{ACT} . It turns out that the semantics of AMASS_{ACT} is still complicated due to the complex interplay between launch modes and intent flags. Therefore, in the sequel, we separate the concerns further and consider the two submodels of AMASS_{ACT} , namely $\text{AMASS}_{ACT,LM}$ and $\text{AMASS}_{ACT,IF}$, which focus on launch modes and intent flags of AMASS_{ACT} , respectively. More precisely,

- an $\text{AMASS}_{ACT,LM}$ is an AMASS_{ACT} where all transition rules $A \xrightarrow{\alpha(\phi)} B$ (except back) satisfy that $\phi = \perp$,
- an $\text{AMASS}_{ACT,IF}$ is an AMASS_{ACT} where all transition rules $A \xrightarrow{\alpha(\phi)} B$ (except back) satisfy that $\text{Lmd}(A) = \text{STD}$.

To ease the understanding, in the main text, we shall only define the formal semantics of the two submodels $\text{AMASS}_{ACT,LM}$ and $\text{AMASS}_{ACT,IF}$, and omit the definition of the formal semantics of AMASS_{ACT} , since the definition of the semantics of AMASS_{ACT} is rather tedious and we think that $\text{AMASS}_{ACT,LM}$ and $\text{AMASS}_{ACT,IF}$ are already sufficient to understand the meanings of the launch modes and intent flags.

To simplify the presentation, in $A \xrightarrow{\alpha(\phi)} B$, we assume that α is start. The definition of the semantics for the case that α is finishStart can be found in the appendix.

Semantics of $\text{AMASS}_{ACT,LM}$.

We start with the semantics of $\text{AMASS}_{ACT,LM}$ and assume that \mathcal{M} is an $\text{AMASS}_{ACT,LM}$. We first introduce some notations.

Tasks and Configurations. A *task* of \mathcal{M} is represented by its activity stack and is encoded as a word $S = [A_1, \dots, A_n] \in \text{Act}^+$, with A_1 (respectively, A_n) as the top (respectively, bottom) activity of S , n is called the *height* of S .

A *configuration* of \mathcal{M} is encoded as a sequence $\rho = (\Omega_1, \dots, \Omega_n)$, and for each $i \in [n]$, $\Omega_i = (S_i, A_i, \zeta_i)$, $S_i \in \text{Act}^*$ is a task, $A_i \in \text{Act}$ is the real activity of S_i , and $\zeta_i \in \{\text{MAIN}, \text{STK}, \text{SIT}\}$ represents how the task S_i is launched. For any activity A , we refer to an A -task as a task whose real activity is A . The tasks S_1 and S_n are called the top and the bottom task, respectively. (Intuitively, S_1 is the foreground task.) The symbol ε is used to denote the empty task stack. The *affinity of a task* is defined as the affinity of its real activity. A task (S_i, A_i, ζ_i) in ρ is called an SIT-task if $\zeta_i = \text{SIT}$.

A task is called the *main task* of the task stack if it is the first task that was created when launching the app. Note that the current task stack may *not* contain the main task, since it may

have been popped out from the task stack. This notion is introduced since the semantics of AMASS is also dependent on whether the task stack contains the main task.

Let Conf_M denote the set of configurations of M . The *initial* configuration of M is $(([A_0], A_0, \text{MAIN}))$. The *height* of a configuration ρ is defined as $\max_{i \in [m]} |S_i|$, where $|S_i|$ is the height of S_i . By convention, the height of ϵ is defined as 0.

Before presenting the formal semantics of $\text{AMASS}_{ACT, LM}$, we present its intuitions.

Intuitions of the Launch Modes. We call an activity of the launch mode STD as an STD activity, similarly for STP, STK, and SIT:

- *The STD mode:* When a new STD activity is started, it will be pushed into the top task.
- *The STP mode:* When a new activity of the STP mode is started, if the activity is already at the top of the top task, it will reuse this activity. Otherwise, a new activity will be pushed into the top task.
- *The STK mode:* When a new activity of the STK mode is started, it will create the activity at the root of a new task or locates the activity on an existing task with the same affinity. If the activity already exists, then all activities above it are removed from the task. Otherwise, a new activity will be pushed into the task.
- *The SIT mode:* Similar to STK, but if such an activity already exists, it will reuse this activity. Moreover, there is only one activity in the task that was created by starting the same activity.

Task Allocation Mechanism. The intuitions of the launch modes are actually not that precise. For instance, when a new STD activity is stated by an SIT activity, the STD activity will not necessarily be pushed to the top task. Task allocation mechanism is to specify to which task will it be allocated when an activity is launched. Via extensive experiments, we identify a crucial notion (i.e., real activity of tasks), which plays a pivotal role in such a mechanism.

Generally speaking, for an activity B that is not to land on the top task, the following three steps will apply: (1) if there is any task whose real activity is B , then B will be put on the task; (2) otherwise, if there is any task whose real activity has the same *task affinity* as B , then B will be put on the task; and (3) otherwise, a new task is created to hold B . In the first two cases, if there are multiple instances, the first occurrence starting from the top task will be selected.

Real Activity and Main Task. When the caller activity is an SIT activity and the callee activity is an STD or STP activity B , B will *not* always be pushed into the task S_i which is specified according to the *task allocation mechanism*. Generally speaking, the following steps will apply: (1) if the real activity of S_i is *not* B , then B will be pushed into S_i , and (2) otherwise, if S_i is the main task—that is, $\zeta_i = \text{MAIN}$ —then B will be pushed into S_i . (If S_i is not the main task, then B will not be pushed.)

Next we introduce some auxiliary functions and predicates to be used in the formal semantics of $\text{AMASS}_{ACT, LM}$.

Auxiliary Functions and Predicates. To specify the transition relation precisely and concisely, we define the following functions and predicates. Let $\rho = (\Omega_1, \dots, \Omega_n)$ be a configuration with $\Omega_i = (S_i, A_i, \zeta_i)$ for each $i \in [n]$, and let $S = [B_1, \dots, B_m]$ be a task:

- $\text{TopAct}(S) = B_1$, $\text{BtmAct}(S) = B_m$,
- $\text{TopTsk}(\rho) = S_1$, $\text{TopAct}(\rho) = \text{TopAct}(\text{TopTsk}(\rho))$,
- $\text{Push}(\rho, B) = (([B] \cdot S_1, A_1, \zeta_1), \Omega_2, \dots, \Omega_n)$,
- $\text{ClrTop}(\rho, B) = (([B] \cdot S'_1, A_1, \zeta_1), \Omega_2, \dots, \Omega_n)$ if $S_1 = S'_1 \cdot S''_1$ with $S'_1 \in (\text{Act} \setminus \{B\})^* B$,
- $\text{ClrTsk}(\rho, B) = (([B], A_1, \zeta_1), \Omega_2, \dots, \Omega_n)$,
- $\text{MvTsk2Top}(\rho, i) = (\Omega_i, \Omega_1, \dots, \Omega_{i-1}, \Omega_{i+1}, \dots, \Omega_n)$,
- $\text{NewTsk}(\rho, B, \zeta) = (([B], B, \zeta), \Omega_1, \dots, \Omega_n)$,

Table 3. Attributes of Activities

Activity	Lmd	Aft
A	STK	1
B	STP	2
C	SIT	1
D	STD	2

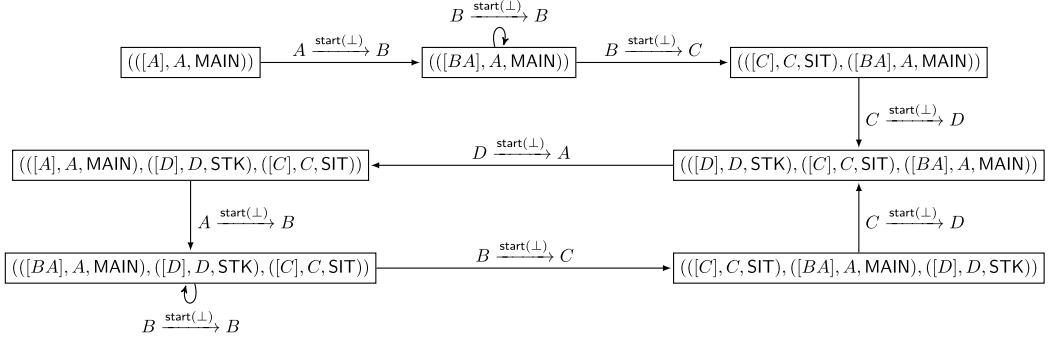


Fig. 3. Configurations reachable from the initial configuration $(([A], A, \text{MAIN}))$ in an $\text{AMASS}_{\text{ACT}, \text{LM}} \mathcal{M}$.

- $\text{GetRealTsk}(\rho, B) = S_i$ such that $i \in [n]$ is the *minimum* index satisfying $A_i = B$, if such an index i exists; $\text{GetRealTsk}(\rho, B) = *$ otherwise,
- $\text{GetTsk}(\rho, B) = S_i$ such that $i \in [n]$ is the *minimum* index satisfying $\text{Aft}(A_i) = \text{Aft}(B)$ and $\zeta_i \in \{\text{MAIN}, \text{STK}\}$, if such an index i exists; $\text{GetTsk}(\rho, B) = *$ otherwise.

The formal semantics of \mathcal{M} will be defined as a transition relation $\xrightarrow{\mathcal{M}}$. We first use the following example to illustrate the semantics.

Example 4.1. Let $\mathcal{M} = (\text{Act}, A, \text{Frg}, \text{Lmd}, \text{Aft}, \text{Ctn}, \Delta)$ be an $\text{AMASS}_{\text{ACT}, \text{LM}}$, where $\text{Act} = \{A, B, C, D\}$, and the functions Lmd and Aft are defined in Table 3.

Moreover, $\Delta = \{\text{back}, \tau_1, \tau_2, \tau_3, \tau_4, \tau_5\}$, where $\tau_1 = A \xrightarrow{\text{start}(\perp)} B$, $\tau_2 = B \xrightarrow{\text{start}(\perp)} C$, $\tau_3 = C \xrightarrow{\text{start}(\perp)} D$, and $\tau_4 = D \xrightarrow{\text{start}(\perp)} A$, $\tau_5 = B \xrightarrow{\text{start}(\perp)} B$. Then the configurations reachable from the initial configuration $(([A], A, \text{MAIN}))$ by executing the transition rules from Δ are illustrated in Figure 3, where the vertices denote the configurations and the edges denote the elements of $\xrightarrow{\mathcal{M}}$. For instance,

- if the transition rule $A \xrightarrow{\text{start}(\perp)} B$ is applied to the configuration $(([A], A, \text{MAIN}))$, then B is pushed, since $\text{Lmd}(B) = \text{STP}$ and $A \neq B$, resulting in the configuration $(([BA], A, \text{MAIN}))$,
- if $B \xrightarrow{\text{start}(\perp)} B$ is applied to the configuration $(([BA], A, \text{MAIN}))$, then B will not be pushed, since $\text{Lmd}(B) = \text{STP}$ and the top activity of the top task is B ,
- if $B \xrightarrow{\text{start}(\perp)} C$ is applied to the configuration $(([BA], A, \text{MAIN}))$, then a new task $([C], C, \text{SIT})$ is created, since $\text{Lmd}(C) = \text{SIT}$, resulting in the configuration $(([C], C, \text{SIT}), ([BA], A, \text{MAIN}))$,
- if $C \xrightarrow{\text{start}(\perp)} D$ is applied to the configuration $(([C], C, \text{SIT}), ([BA], A, \text{MAIN}))$, then a new task $([D], D, \text{STK})$ is created, since $\text{Lmd}(C) = \text{SIT}$, $\text{Lmd}(D) = \text{STD}$ and $\text{Aft}(D) = 2 \neq \text{Aft}(A)$, resulting in the configuration $(([D], D, \text{STK}), ([C], C, \text{SIT}), ([BA], A, \text{MAIN}))$,

- if $D \xrightarrow{\text{start}(\perp)} A$ is applied to the configuration $(([D], D, \text{STK}), ([C], C, \text{SIT}), ([BA], A, \text{MAIN}))$, then the task $([BA], A, \text{MAIN})$ is moved to the top and all activities above A , which is B here, are removed from the task, since $\text{Lmd}(A) = \text{STK}$,

$$\text{GetRealTsk}(([D], D, \text{STK}), ([C], C, \text{SIT}), ([BA], A, \text{MAIN})), A) = ([BA], A, \text{MAIN}),$$

and A occurs in $([BA], A, \text{MAIN})$, resulting in the configuration $(([A], A, \text{MAIN}), ([D], D, \text{STK}), ([C], C, \text{SIT}))$,

– ...

- if $C \xrightarrow{\text{start}(\perp)} D$ is applied to the configuration $(([C], C, \text{SIT}), ([BA], A, \text{MAIN}), ([D], D, \text{STK}))$, then the task $([D], D, \text{STK})$ is moved to the top, but D will not be pushed, since $\text{Lmd}(C) = \text{SIT}$, $\text{Lmd}(D) = \text{STD}$,

$$\text{GetRealTsk}(([C], C, \text{SIT}), ([BA], A, \text{MAIN}), ([D], D, \text{STK})), D) = ([D], D, \text{STK}),$$

and $([D], D, \text{STK})$ is not the main task, resulting in the configuration $(([D], D, \text{STK}), ([C], C, \text{SIT}), ([BA], A, \text{MAIN}))$.

Note that for \mathcal{M} , there are only finitely many configurations reachable from the initial configuration, which may not be the case for $\text{AMASS}_{\text{ACT}, \text{LM}}$ in general.

From the informal description and the preceding example, we have already gotten an intuitive understanding of the semantics of \mathcal{M} . To facilitate a precise understanding of the semantics of $\text{AMASS}_{\text{ACT}, \text{LM}}$, let us formally define the semantics of \mathcal{M} as a transition relation $\xrightarrow{\mathcal{M}}$ in the sequel.

Transition Relation. We define the relation $\xrightarrow{\mathcal{M}}$ which comprises the quadruples $(\rho, \tau, \rho') \in \text{Conf}_{\mathcal{M}} \times \Delta \times \text{Conf}_{\mathcal{M}}$ to formalize the semantics of \mathcal{M} . For readability, we write $(\rho, \tau, \rho') \in \xrightarrow{\mathcal{M}}$ as $\rho \xrightarrow[\tau]{\mathcal{M}} \rho'$.

Let $\rho = ((S_1, A_1, \zeta_1), \dots, (S_n, A_n, \zeta_n))$ be the current configuration for some $n \geq 1$ and $\text{TopAct}(\rho) = A$. Moreover, let $S_1 = [A'_1, \dots, A'_m]$. Evidently, $A = A'_1$.

If $\tau = \text{back}$, then $\rho' = ((S'_1, A_1, \zeta_1), (S_2, A_2, \zeta_2), \dots, (S_n, A_n, \zeta_n))$ if $m > 1$, where $S'_1 = [A'_2, \dots, A'_m]$, and $\rho' = ((S_2, A_2, \zeta_2), \dots, (S_n, A_n, \zeta_n))$ otherwise.

Then let us consider $\tau = A \xrightarrow{\text{start}(\phi)} B$.

$\boxed{\text{Lmd}(B) = \text{STD}}$

- If $\text{Lmd}(A) \neq \text{SIT}$, then $\rho' = \text{Push}(\rho, B)$.
- If $\text{Lmd}(A) = \text{SIT}$,
 - if $\text{GetRealTsk}(\rho, B) = S_i$ and $\zeta_i \neq \text{MAIN}$, then $\rho' = \text{MvTsk2Top}(\rho, i)$,
 - if $\text{GetRealTsk}(\rho, B) = S_i$ and $\zeta_i = \text{MAIN}$, or $\text{GetRealTsk}(\rho, B) = *$ $\wedge \text{GetTsk}(\rho, B) = S_i$, then $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
 - if $\text{GetTsk}(\rho, B) = *$, then $\rho' = \text{NewTsk}(\rho, B, \text{STK})$.

$\boxed{\text{Lmd}(B) = \text{STP}}$

- If $\text{Lmd}(A) \neq \text{SIT}$, then
 - if $A = B$, then $\rho' = \rho$,
 - otherwise, $\rho' = \text{Push}(\rho, B)$.
- If $\text{Lmd}(A) = \text{SIT}$,
 - if $\text{GetRealTsk}(\rho, B) = S_i$ and $\zeta_i \neq \text{MAIN}$, then $\rho' = \text{MvTsk2Top}(\rho, i)$,
 - if $\text{GetRealTsk}(\rho, B) = S_i$ and $\zeta_i = \text{MAIN}$, or $\text{GetRealTsk}(\rho, B) = *$ $\wedge \text{GetTsk}(\rho, B) = S_i$,

- * if $\text{TopAct}(S_i) = B$, then $\rho' = \text{MvAct2Top}(\rho, i)$,
- * otherwise, $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
- if $\text{GetTsk}(\rho, B) = *$, then $\rho' = \text{NewTsk}(\rho, B, \text{STK})$.

Lmd(B) = SIT

- If $\text{GetRealTsk}(\rho, B) = S_i$, then $\rho' = \text{MvTsk2Top}(\rho, i)$.
- If $\text{GetRealTsk}(\rho, B) = *$, then $\rho' = \text{NewTsk}(\rho, B, \text{SIT})$.

Lmd(B) = STK

- If $\text{GetRealTsk}(\rho, B) = S_i$, or $\text{GetRealTsk}(\rho, B) = * \wedge \text{GetTsk}(\rho, B) = S_i$ then
 - if $B \notin S_i$, then $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
 - if $B \in S_i$, then $\rho' = \text{ClrTop}(\text{MvTsk2Top}(\rho, i), B)$.
- If $\text{GetTsk}(\rho, B) = *$, then $\rho' = \text{NewTsk}(\rho, B, \text{STK})$.

From the definition of the semantics, we can see that a new task $([B], B, \text{STK})$ is created, not only when $\text{Lmd}(B) = \text{STK}$ but also when $\text{Lmd}(A) = \text{SIT}$ and $\text{Lmd}(B) = \text{STD}$.

Semantics of AMASS_{ACT,IF}.

The intuitions of the intent flags are given in Table 4. We would like to warn that although the intuitions of these intent flags may help readers get some preliminary idea of their meanings, before diving directly into the formal semantics, they are nonetheless inaccurate, especially when different flags may interfere with each other.

To ease the presentation, let us assume that $\phi \models \neg\text{NOH}$ in $A \xrightarrow{\text{start}(\phi)} B$. The full semantics of AMASS_{ACT,IF} where the situation $\phi \models \text{NOH}$ is taken into consideration can be found in Appendix B.

Let \mathcal{M} be an AMASS_{ACT,IF}, namely $\text{Lmd}(A) = \text{STD}$ for each activity A .

To define the semantics of \mathcal{M} , the concept of configurations is adapted from the definition of configurations for AMASS_{ACT,LM} as follows. A configuration of \mathcal{M} is still encoded as a sequence $\rho = (\Omega_1, \dots, \Omega_n)$ such that for each $i \in [n]$, $\Omega_i = (S_i, A_i, \zeta_i)$, where $S_i \in \text{Act}^*$ is a task, $A_i \in \text{Act}$ is the real activity of S_i , but $\zeta_i \in \{\text{MAIN}, \text{NTK}, \text{NDM}\}$. Intuitively, NTK in ζ_i plays the same role as STK in AMASS_{ACT,LM}, and NDM is added for the intent flag NDM, and moreover, SIT disappears since in AMASS_{ACT,IF}, the launch modes of all activities are assumed to be STD.

Next we introduce some additional auxiliary functions and predicates to be used in the formal semantics of \mathcal{M} .

Auxiliary Functions and Predicates. Let $\rho = (\Omega_1, \dots, \Omega_n)$ be a configuration with $\Omega_i = (S_i, A_i, \zeta_i)$ for each $i \in [n]$, and let $S = [B_1, \dots, B_m]$ be a task. The following additional auxiliary functions are defined:

- $\text{PreAct}(S) = B_2$ if $m > 1$, $\text{PreAct}(S) = B_1$ otherwise,
- $\text{PreAct}(\rho) = \text{PreAct}(\text{TopTsk}(\rho))$,
- $\text{MvAct2Top}(\rho, B) = (([B] \cdot S'_1 \cdot S''_1, A_1, \zeta_1), \Omega_2, \dots, \Omega_n)$, if $S_1 = S'_1 \cdot [B] \cdot S''_1$ with $S'_1 \in (\text{Act} \setminus \{B\})^*$.

Intuitively, $\text{PreAct}(S)$ and $\text{PreAct}(\rho)$ are used for defining the semantics of PIT, and $\text{MvAct2Top}(\rho, B)$ is used for defining the semantics of RTF. Moreover, the function GetTsk is adapted by replacing STK with NTK: $\text{GetTsk}(\rho, B) = S_i$ such that $i \in [n]$ is the *minimum* index satisfying $\text{Aft}(A_i) = \text{Aft}(B)$ and $\zeta_i \in \{\text{MAIN}, \text{NTK}\}$, if such an index i exists; $\text{GetTsk}(\rho, B) = *$ otherwise.

Before the formal definition, let us use the following example to illustrate the semantics of the AMASS_{ACT,IF}.

Table 4. Intuitions of Intent Flags

Intent Flags	Abbreviation	Intuition
FLAG_ACTIVITY_SINGLE_TOP	STP	If it is set, it has the same effect as starting an activity of the STP launch mode.
FLAG_ACTIVITY_CLEAR_TOP	CTP	If it is set, all the activities above the topmost occurrence of the started activity in the top task will be removed.
FLAG_ACTIVITY_REORDER_TO_FRONT	RTF	If it is set, it will check for the existence of the started activity in the task. If an instance of the activity exists, then the topmost occurrence of this activity will be moved to the top of this task. Otherwise, a new instance of the activity will be pushed into the top task.
FLAG_ACTIVITY_NEW_TASK	NTK	If it is set, it will look for an existing task to put the started activity according to the task allocation mechanism. If such a task exists, the task will be moved to the top and a new instance of the activity is pushed to the task, otherwise a new task is created to put this activity.
FLAG_ACTIVITY_NEW_DOCUMENT	NDM	If it is set, its behavior is similar to the STK launch mode, but the task allocation mechanism is slightly different, namely it will look for an existing task by only using real activities of tasks but not affinities.
FLAG_ACTIVITY_MULTIPLE_TASK	MTK	It is usually used together with NTK or NDM. If it is set, then it will always create a new task to put the started activity, no matter whether there already exists a task of the same affinity as this activity.
FLAG_ACTIVITY_CLEAR_TASK	CTK	It is usually used together with NTK or NDM. If it is set, it will remove all the activities in the task and push the started activity to the task.
FLAG_ACTIVITY_NO_HISTORY	NOH	If it is set, when the started activity becomes a non-topmost activity in the future, the activity will be removed.
FLAG_ACTIVITY_PREVIOUS_IS_TOP	PIT	If it is set, then when starting this activity, the activity immediately below the topmost activity will play the role of the topmost activity.
FLAG_ACTIVITY_TASK_ON_HOME	TOH	It is usually used together with NTK or NDM. If it is set, then only the top task, which is either a newly created task or an existing task moved to the top, is kept, and all the other tasks are removed.

Example 4.2. Let $\mathcal{M} = (\text{Act}, A, \text{Frg}, \text{Lmd}, \text{Aft}, \text{Ctn}, \Delta)$ be an AMASS_{ACT,IF}, where $\text{Act} = \{A, B, C, D, E, F, G\}$, and for each $A' \in \text{Act}$, $\text{Lmd}(A') = \text{STD}$ and $\text{Aft}(A') = 1$. Moreover, $\Delta = \{\text{back}\} \cup \{\tau_i \mid 1 \leq i \leq 9\}$, where $\tau_1 = A \xrightarrow{\text{start(CTP)}} B$, $\tau_2 = B \xrightarrow{\text{start}(\perp)} C$, $\tau_3 = B \xrightarrow{\text{start(NTK}\wedge\text{MTK)}} D$, $\tau_4 = B \xrightarrow{\text{start(NDM)}} F$, $\tau_5 = C \xrightarrow{\text{start(NTK)}} A$, $\tau_6 = D \xrightarrow{\text{start(STP)}} D$, $\tau_7 = D \xrightarrow{\text{start(RTF)}} E$, $\tau_8 = E \xrightarrow{\text{start(STP}\wedge\text{PIT)}} D$, and $\tau_9 = E \xrightarrow{\text{start(NTK}\wedge\text{CTK)}} F$.

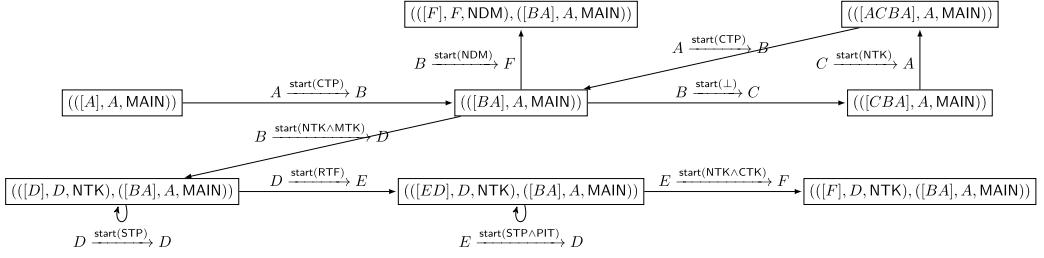


Fig. 4. Configurations that are reachable from the initial configuration $(([A], A, \text{MAIN}))$ in \mathcal{M} .

The $\xrightarrow{\mathcal{M}}$ relation on the set of configurations that are reachable from the initial configuration $(([A], A, \text{MAIN}))$ is illustrated in Figure 4.

For instance,

- from the configuration $(([A], A, \text{MAIN}))$, after executing the transition rule $A \xrightarrow{\text{start}(CTP)} B$, because $\phi \models \neg\text{NTK} \wedge \neg\text{NDM}$, B does not occur in the top task $[A]$, we have $\rho' = \text{Push}(([A], A, \text{MAIN}), B) = (([BA], A, \text{MAIN}))$,
- from the configuration $(([ACBA], A, \text{MAIN}))$, after executing $A \xrightarrow{\text{start}(CTP)} B$, because $\phi \models \neg\text{NTK} \wedge \neg\text{NDM}$, B occurs in the top task $[ACBA]$, we have $\rho' = \text{ClrTop}(([ACBA], A, \text{MAIN}), B) = (([BA], A, \text{MAIN}))$,
- from the configuration $(([BA], A, \text{MAIN}))$, after executing $B \xrightarrow{\text{start}(\perp)} C$, because $\phi \models \neg\text{NTK} \wedge \neg\text{NDM} \wedge \neg\text{CTP} \wedge \neg\text{RTF} \wedge \neg\text{STP}$, we have $\rho' = \text{Push}(([BA], A, \text{MAIN}), C) = (([CBA], A, \text{MAIN}))$,
- from the configuration $(([BA], A, \text{MAIN}))$, after executing $B \xrightarrow{\text{start}(NDM)} F$, because $\phi \models \text{NDM} \wedge \neg\text{MTK}$, $\text{GetRealTsk}(\rho, F) = *$, we have $\rho' = \text{NewTsk}(([BA], A, \text{MAIN}), F, \text{NDM}) = (([F], F, \text{NDM}), ([BA], A, \text{MAIN}))$,
- from the configuration $(([BA], A, \text{MAIN}))$, after executing $B \xrightarrow{\text{start}(NTK \wedge MTK)} D$, because $\phi \models \text{NTK} \wedge \neg\text{NDM} \wedge \text{MTK}$, we have

$$\rho' = \text{NewTsk}(([BA], A, \text{MAIN}), D, \text{NTK}) = (([D], D, \text{NTK}), ([BA], A, \text{MAIN})),$$

- from the configuration $(([CBA], A, \text{MAIN}))$, after executing $C \xrightarrow{\text{start}(NTK)} A$, because $\phi \models \text{NTK} \wedge \neg\text{NDM} \wedge \neg\text{MTK} \wedge \neg\text{CTP} \wedge \neg\text{RTF} \wedge \neg\text{STP}$, $\text{GetRealTsk}(\rho, A) = S_1, \zeta_1 = \text{MAIN}$, we have

$$\rho' = \text{Push}(([CBA], A, \text{MAIN}), A) = (([ACBA], A, \text{MAIN})),$$

- from the configuration $(([D], D, \text{NTK}), ([BA], A, \text{MAIN}))$, after executing $D \xrightarrow{\text{start}(STP)} D$, because $\phi \models \neg\text{NTK} \wedge \neg\text{NDM} \wedge \neg\text{CTP} \wedge \neg\text{RTF} \wedge \text{STP}$ and D is the top activity of the top task $[D]$, we have $\rho' = \rho$,
- from the configuration $(([D], D, \text{NTK}), ([BA], A, \text{MAIN}))$, after executing $D \xrightarrow{\text{start}(RTF)} E$, because $\phi \models \neg\text{NTK} \wedge \neg\text{NDM} \wedge \neg\text{CTP} \wedge \text{RTF}$ and E does not occur in the top task $[D]$, we have

$$\rho' = \text{Push}(([D], D, \text{NTK}), ([BA], A, \text{MAIN}), E) = (([ED], D, \text{NTK}), ([BA], A, \text{MAIN})),$$

- from the configuration $(([ED], D, \text{NTK}), ([BA], A, \text{MAIN}))$, after executing $E \xrightarrow{\text{start}(STP \wedge PIT)} D$, because $\phi \models \neg\text{NTK} \wedge \neg\text{NDM} \wedge \neg\text{CTP} \wedge \neg\text{RTF} \wedge \text{STP} \wedge \text{PIT}$ and $D = \text{PreAct}([ED])$, we have $\rho' = \rho$,

- from the configuration $(([ED], D, NTK), ([BA], A, MAIN))$, after executing $E \xrightarrow{\text{start}(NTK \wedge CTK)} F$, because $\phi \models NTK \wedge \neg NDM \wedge \neg MTK \wedge CTK$, $\text{GetRealTsk}(\rho, F) = *$ and $\text{GetTsk}(\rho, F) = S_1$, we have

$$\rho' = \text{ClrTsk}(((ED, D, NTK), (BA, A, MAIN)), F) = ((F, D, NTK), (BA, A, MAIN)),$$

The aforementioned informal description of intent flags and the example provide the intuition of the semantics of $\text{AMASS}_{ACT, IF}$. In the sequel, we formally define the semantics of \mathcal{M} as a transition relation $\rho \xrightarrow[\tau]{\mathcal{M}} \rho'$ with $\tau = A \xrightarrow{\text{start}(\phi)} B$.

Let us assume $\phi \models \neg TOH$ first.

$\boxed{\phi \models \neg NTK \wedge \neg NDM}$

- If $\phi \models CTP$ and $B \in \text{TopTsk}(\rho)$, then $\rho' = \text{ClrTop}(\rho, B)$.
- If $\phi \models CTP$ and $B \notin \text{TopTsk}(\rho)$, then $\rho' = \text{Push}(\rho, B)$.
- If $\phi \models \neg CTP$, then
 - if $\phi \models RTF$ and $B \in \text{TopTsk}(\rho)$, then $\rho' = \text{MvAct2Top}(\rho, B)$,
 - if $\phi \models RTF$ and $B \notin \text{TopTsk}(\rho)$, then $\rho' = \text{Push}(\rho, B)$,
 - if $\phi \models \neg RTF$, then
 - * if $\phi \models STP$ and $\text{TopAct}(\rho) = B$ or $\phi \models STP \wedge PIT$ and $\text{PreAct}(\rho) = B$, then $\rho' = \rho$,
 - * otherwise, $\rho' = \text{Push}(\rho, B)$.

$\boxed{\phi \models NDM}$

- If $\phi \models MTK$, then $\rho' = \text{NewTsk}(\rho, B, NDM)$.
- If $\phi \models \neg MTK$, then
 - if $\text{GetRealTsk}(\rho, B) = S_i$, then
 - * if $\phi \models CTK$, then $\rho' = \text{ClrTsk}(\text{MvTsk2Top}(\rho, i), B)$,
 - * if $\phi \models \neg CTK$, then
 - if $B \in S_i$, then $\rho' = \text{ClrTop}(\text{MvTsk2Top}(\rho, i), B)$,
 - if $B \notin S_i$, then $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
 - if $\text{GetRealTsk}(\rho, B) = *$, then $\rho' = \text{NewTsk}(\rho, B, NDM)$.

$\boxed{\phi \models NTK \wedge \neg NDM}$

- If $\phi \models MTK$, then $\rho' = \text{NewTsk}(\rho, B, NTK)$.
- If $\phi \models \neg MTK$, then
 - if $\text{GetRealTsk}(\rho, B) = S_i$ or $\text{GetRealTsk}(\rho, B) = * \wedge \text{GetTsk}(\rho, B) = S_i$, then
 - * if $\phi \models CTK$, then $\rho' = \text{ClrTsk}(\text{MvTsk2Top}(\rho, i), B)$,
 - * if $\phi \models \neg CTK$, then
 - if $\phi \models CTP$ and $B \in S_i$, then $\rho' = \text{ClrTop}(\text{MvTsk2Top}(\rho, i), B)$,
 - if $\phi \models CTP$ and $B \notin S_i$, then $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
 - if $\phi \models \neg CTP$, then
 - if $\phi \models RTF$ and $B \in S_i$, then $\rho' = \text{MvAct2Top}(\text{MvTsk2Top}(\rho, i), B)$,
 - if $\phi \models RTF$ and $B \notin S_i$, then $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
 - if $\phi \models \neg RTF$, then
 - if $\text{GetRealTsk}(\rho, B) = S_i$ and $\zeta_i \neq MAIN$, then $\rho' = \text{MvTsk2Top}(\rho, i)$,
 - otherwise,
 - ★ if $\phi \models STP$ and $\text{TopAct}(S_i) = B$, or $\phi \models STP \wedge PIT$ and $i = 1$ and $\text{PreAct}(S_1) = B$, then $\rho' = \text{MvTsk2Top}(\rho, i)$,
 - ★ otherwise, $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
 - if $\text{GetTsk}(\rho, B) = *$, then $\rho' = \text{NewTsk}(\rho, B, NTK)$.

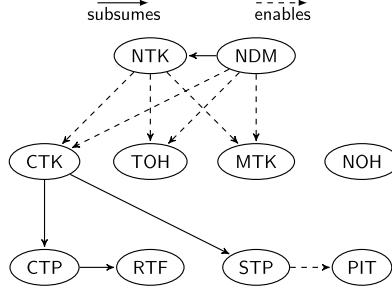


Fig. 5. Dependency graph of intent flags.

Finally we consider the situation $\phi \models \text{TOH}$. Let ϕ' be obtained from ϕ by replacing TOH with $\neg \text{TOH}$. Moreover, suppose $\rho \xrightarrow{\mathcal{M}} \rho'$, where $\tau' = A \xrightarrow{\text{start}(\phi')} B$ and $\rho' = (\Omega_1, \dots, \Omega_n)$. Then

- if $\phi \models \text{NTK} \vee \text{NDM}$, then let $\rho'' = (\Omega_1)$ and we have $\rho \xrightarrow{\mathcal{M}} \tau' \xrightarrow{\tau} \rho''$,
- otherwise, $\rho \xrightarrow{\mathcal{M}} \rho'$.

By a retrospect of the aforementioned formal semantics, we can discover that the intent flags may interfere with each other. We summarize their dependencies as follows.

Dependencies of Intent Flags. The dependencies of intent flags can exhibit in the following two forms: (1) n subsumes n' (i.e., n' is ignored if n co-occurs with n' , and the “subsume” relations are transitive) and (2) n enables n' (i.e., n' takes effect if n co-occurs with n'). The dependencies among the intent flags are summarized in Figure 5, where the solid lines represent the “subsume” relation and the dashed lines represent the “enable” relation.

4.1.2 Semantics of AMASS_{FRG}. In this case, we assume that there is only one activity A_0 and consider the fragments as the atomic objects, hence we only consider the transaction rules back, $A \xrightarrow{\mu} T$ and $F \xrightarrow{\mu} T$, where T is of the form $(\beta_1(F_1, i_1, x_1), \dots, \beta_k(F_k, i_k, x_k))$ such that for every $j \in [k]$, $\beta_j \in \{\text{ADD}, \text{REP}, \text{REM}\}$, $F_j \in \text{Frg}$, $i_j \in \mathbb{N}$, and x_j is a variable storing the identifiers of fragment instances.

Intuitions

The intuitions of the transition rules $A \xrightarrow{\mu} T$ and $F \xrightarrow{\mu} T$ are explained in the sequel:

- $\text{ADD}(F, i, x)$ denotes the action where a *new* instance of the fragment F is added to the container i of the current activity. Moreover, the identifier of the new instance is stored in x .
- $\text{REP}(F, i, x)$ is the same as $\text{ADD}(F, i, x)$, except that the container i is cleared before adding F .
- $\text{REM}(F, i, x)$ denotes the action where the instance of the fragment F of the identifier (stored in) x is removed from the container i of the current activity.
- $\text{TS}[(\beta_1(F_1, i_1, x_1), \dots, \beta_k(F_k, i_k, x_k))]$ denotes that the actions $\beta_1(F_1, i_1, x_1), \dots, \beta_k(F_k, i_k, x_k)$ are executed sequentially, and are added to the transaction stack.
- $\text{NTS}[(\beta_1(F_1, i_1, x_1), \dots, \beta_k(F_k, i_k, x_k))]$ is the same as TS , except that the transactions will *not* be added to the transaction stack.

For convenience, these transition rules are referred to as TS transition rules and NTS transition rules, respectively.

It is fair to say that the intricacy of the semantics lies in the action back. Let A be the top activity of the top task, $Ctn(A) = (i_1, \dots, i_m)$, V_1, \dots, V_m be the fragment stacks for the containers

i_1, \dots, i_m , and $\eta \in \mathcal{T}^*$ be the transaction stack. If $\eta = \epsilon$, the activity A will be popped, and otherwise the behavior of the action back is controlled by η —namely, when the back button is pressed, the top transaction of η is removed from η and its effects on the fragment stacks are to be revoked. Noticeable difficulties arise.

Mismatch between Fragment and Transaction Stacks. The transaction stack η may *not* contain all the historical transactions leading to the fragment stacks, but only those corresponding to the TS transition rules, which means that when revoking the top action of η , say $\text{ADD}(F, i_j, x_j)$, F may not be the top fragment of V_j . To deal with this issue, we

- (1) store (F, n) in V_j , where n is the identifier of the instance of F that is generated when applying $\text{ADD}(F, i_j, x_j)$,
- (2) store the concretized action $\text{ADD}(F, i_j, n)$, instead of $\text{ADD}(F, i_j, x_j)$, into the transaction stack η .

As a result, we can revoke $\text{ADD}(F, i_j, n)$ instead of $\text{ADD}(F, i_j, x_j)$ in the transaction stack, and use n to identify the fragment instance to be removed from the fragment container V_j .

Revoking REP Actions. The top transaction of η may include some action $\text{REP}(F, i_j, n)$, and revoking these actions requires restoring the historical content of the container i_j before applying this action.

To deal with this issue, when an action $\text{REP}(F, i_j, x_j)$ appears in a TS transition rule and is to be pushed into the transaction stack, suppose that the current content of the container i_j is $((F'_1, n'_1), \dots, (F'_k, n'_k))$, then $\text{REP}(F, i_j, x_j)$ is concretized into the action sequence

$$\text{REM}(F'_1, i_j, n'_1), \dots, \text{REM}(F'_k, i_j, n'_k), \text{ADD}(F, i_j, n),$$

which—instead of $\text{REP}(F, i_j, n)$ —is pushed into the transaction stack, possibly together with the other actions in the same transaction. (Note that n is the identifier of the newly created instance of F .) Hence, revoking $\text{REP}(F, i_j, x_j)$ is to apply the concretized actions $\text{REM}(F, i_j, n), \text{ADD}(F'_k, i_j, n'_k), \dots, \text{ADD}(F'_1, i_j, n'_1)$ one by one.

Therefore, only concretized actions of the form $\text{ADD}(F, i, n)$ or $\text{REM}(F, i, n)$ are stored in the transaction stack, and we use \mathcal{CT} to denote the set of these concretized actions.

Fragment Containers and Configurations

A *fragment container* is encoded as

$$V = ((F_1, n_1), \dots, (F_k, n_k)) \in (\text{Frg} \times \mathbb{N})^+,$$

where n_j is the identifier of an instance of F_j for $j \in [k]$ and k is called the *height* of V .

A *configuration* ρ is encoded as a tuple (v, η, ι) , where $v = (V_1, \dots, V_m)$ is a sequence of fragment containers associated with A_0 , where $\text{Ctn}(A_0) = (i_1, \dots, i_m)$, $\eta = (T_1, \dots, T_n) \in \mathcal{CT}^*$ is the transaction stack, and ι is the assignment function that assigns to each variable x in \mathcal{M} an identifier (i.e., a natural number). Note that it is possible that $m = 0$ and/or $n = 0$. For technical convenience, let ι_0 denote the assignment function that assigns each variable x the value 0. The initial configuration of \mathcal{M} is $((\epsilon, \dots, \epsilon), \epsilon, \iota_0)$.

Auxiliary Functions and Predicates

To specify the transition relation precisely and concisely, we define the following functions and predicates. For a container $V = ((F_1, n_1), \dots, (F_m, n_m))$, define $\text{TopFrg}(V) = F_1$.

Let $\rho = (v, \eta, \iota)$ be the configuration associated with A_0 , where $\text{Ctn}(A_0) = (i_1, \dots, i_k)$ ($k > 0$), $v = (V_1, \dots, V_k)$ is the container sequence, and $\eta = (T_1, \dots, T_l)$ ($l \geq 0$) is the transaction stack. Moreover, let $F \in \text{Frg}$, $j \in [k]$, and let x be a variable. We define the following functions:

- $\text{TopFrg}(v) = \{\text{TopFrg}(V_i) \mid i \in [k], V_i \neq \epsilon\}$ returns the set of topmost fragments of containers in v .
- $\text{ADD}(F, i_j, x)(v, \iota) = (v', \iota')$, where $v' = (V_1, \dots, V_{j-1}, (F, n) \cdot V_j, V_{j+1}, \dots, V_k)$, $\iota' = \iota[n/x]$, and n is the *minimum* identifier not occurring in v or ι . Intuitively, $\text{ADD}(F, i_j, x)(v, \iota)$ updates (v, ι) by choosing a fresh identifier n , pushing (F, n) into the container i_j , and storing n into x .
- $\text{REP}(F, i_j, x)(v, \iota) = (v', \iota')$, where $v' = (V_1, \dots, V_{j-1}, (F, n), V_{j+1}, \dots, V_k)$, $\iota' = \iota[n/x]$, and n is the *minimum* identifier not occurring in v or ι . Intuitively, $\text{REP}(F, i_j, x)(v, \iota)$ updates v by replacing the content of container i_j with (F, n) and storing n into x .
- Suppose $V_j = ((F_1, n_1), \dots, (F_m, n_m))$, then $\text{REM}(F, i_j, x)(v, \iota) = (v', \iota')$, where
 - $v' = (V_1, \dots, V_{j-1}, \tilde{V}, V_{j+1}, \dots, V_k)$ such that
 - * $\tilde{V} = V_j$, if $\iota(x) \neq n_{j'}$ for every $j' \in [m]$, and
 - * $\tilde{V} = ((F_1, n_1), \dots, (F_{l-1}, n_{l-1}), (F_{l+1}, n_{l+1}), \dots, (F_m, n_m))$, if $\iota(x) = n_l$,
 - moreover, $\iota' = \iota$.
 Intuitively, the action $\text{REM}(F, i_j, x)(v)$ updates v by removing the instance of F of the identifier $\iota(x)$ from container i_j and does not change ι .
- Furthermore, the functions $\text{ADD}(F, i_j, n)(v, \iota)$, $\text{REP}(F, i_j, n)(v, \iota)$, and $\text{REM}(F, i_j, n)(v, \iota)$ for concretized actions can be defined similarly (except that ι is unchanged).

For a transaction $T = (\beta_1(F_1, j_1, x_1), \dots, \beta_r(F_r, j_r, x_r))$ such that $\beta_s \in \{\text{ADD}, \text{REM}, \text{REP}\}$ and $F_s \in \text{Frg}$ for every $s \in [r]$, $\text{UpdateCtns}_T(v, \iota) = (v_r, \iota_r)$, where $(v_0, \iota_0) = (v, \iota)$, and for every $s \in [r]$, $(v_s, \iota_s) = \beta_s(F_s, j_s, x_s)(v_{s-1}, \iota_{s-1})$ —that is, UpdateCtns_T updates the containers and the assignment function by applying the actions in T . Furthermore, $\text{UpdateCtns}_T(v, \iota)$ can be defined similarly for concretized transactions T .

We also introduce a function that concretize the actions REP by utilizing the containers in v . Suppose $F \in \text{Frg}$, $j \in [k]$, x is a variable, and $V_j = ((F_1, n_1), \dots, (F_m, n_m))$. Let n be the minimum identifier not occurring in v or ι . Then

$$\text{Concretize}_{v, \iota}(\text{REP}(F, i_j, x)) = \text{REM}(F_1, i_j, n_1), \dots, \text{REM}(F_m, i_j, n_m), \text{ADD}(F, i_j, n).$$

Moreover, let

$$\text{Concretize}_{v, \iota}(\text{ADD}(F, i_j, x)) = \text{ADD}(F, i_j, n) \text{ and } \text{Concretize}_{v, \iota}(\text{REM}(F, i_j, x)) = \text{REM}(F, i_j, \iota(x))$$

by convention.

Let $T = (\beta_1(F_1, j_1, x_1), \dots, \beta_k(F_r, j_r, x_r))$ be a transaction such that $\beta_s \in \{\text{ADD}, \text{REM}, \text{REP}\}$, and $F_s \in \text{Frg}$ for every $s \in [r]$. We define $\text{Concretize}_{v, \iota}(T)$ as the concatenation of the concretized action sequences $\text{Concretize}_{v_0, \iota_0}(\beta_1(F_1, j_1, x_1)), \dots, \text{Concretize}_{v_{s-1}, \iota_{s-1}}(\beta_s(F_s, j_s, x_s))$, where $(v_0, \iota_0) = (v, \iota)$, and for each $s \in [r]$, $(v_s, \iota_s) = \beta_s(F_s, j_s, x_s)(v_{s-1}, \iota_{s-1})$.

Finally, we define functions $\beta^{-1}(F, i_j, n)$ for $\beta(F, i_j, n) \in C\mathcal{T}$ as follows:

- $\text{ADD}^{-1}(F, i_j, n)(v, \iota) = \text{REM}(F, i_j, n)(v, \iota)$,
- $\text{REM}^{-1}(F, i_j, n)(v, \iota) = \text{ADD}(F, i_j, n)(v, \iota)$.

Intuitively, $\text{ADD}(F, i_j, n)$ and $\text{REM}(F, i_j, n)$ are dual actions. Moreover, for a concretized transaction

$$T = (\beta_1(F_1, j_1, n_1), \dots, \beta_r(F_r, j_r, n_r))$$

such that $\beta_s \in \{\text{ADD}, \text{REM}, \text{REP}\}$, $F_s \in \text{Frg}$ for every $s \in [r]$, and $n \in \mathbb{N}$, we define T^{-1} as

$$(\beta_r^{-1}(F_r, j_r, n_r), \dots, \beta_1^{-1}(F_1, j_1, n_1)).$$

Transition Relation

We assume that the current activity is A . For $\rho \xrightarrow{\tau} \rho'$, we let $\rho = (v, \eta, \iota)$ be the current configuration, where $Ctn(A) = (i_1, \dots, i_k)$, $v = (V_1, \dots, V_k)$, and $\eta = (T_1, \dots, T_l)$:

- If $\tau = \text{back}$, then we assume that $\eta \neq \epsilon$, and otherwise A will be popped and there is no activity to store fragments. Then $\rho' = (v', \eta', \iota')$, where $(v', \iota') = \text{UpdateCtns}_{T_1^{-1}}(v, \iota)$ and $\eta' = (T_2, \dots, T_l)$. Note that T_1 is popped off the transaction stack, and the actions of T_1 are revoked on (v, ι) .
- If $\tau = A \xrightarrow{\mu} T$, or $\tau = F \xrightarrow{\mu} T$, and $F \in \text{TopFrag}(v)$, we let

$$T = (\beta_1(F_1, i_1, x_1), \dots, \beta_k(F_k, i_k, x_k)),$$

then $\rho' = (v', \eta', \iota')$ is obtained from ρ by applying all actions in T to the containers and assignment function such that $(v', \iota') = \text{UpdateCtns}_T(v, \iota)$ and $\eta' = \text{Concretize}_{v, \iota}(T) \cdot \eta$ if $\mu = \text{TS}$, $\eta' = \eta$ otherwise. Note that the difference between TS and NTS is that the concretization of T is stored into the transaction stack when $\mu = \text{TS}$.

We use the following example to illustrate the formal semantics of AMASS_{FRG} .

Example 4.3. Let $\mathcal{M} = (\text{Act}, A_0, \text{Frg}, \text{Lmd}, \text{Aft}, \text{Ctn}, \Delta)$ be an AMASS_{FRG} , where $\text{Act} = \{A_0\}$, $\text{Frg} = \{F_1, F_2, F_3\}$, and $\text{Ctn}(A_0) = (1)$. Moreover, $\Delta = \{\text{back}\} \cup \{\tau_i \mid 0 \leq i \leq 3\}$, where $\tau_0 = \text{back}$, $\tau_1 = F_1 \xrightarrow{\text{TS}} (\text{ADD}(F_2, 1, x))$, $\tau_2 = F_2 \xrightarrow{\text{NTS}} (\text{REP}(F_3, 1, x))$, and $\tau_3 = F_3 \xrightarrow{\text{NTS}} (\text{REM}(F_3, 1, x))$. Then the relation $\xrightarrow{\cdot}$ on the set of configurations that are reachable from the initial configuration $(([(F_1, 0)]), \epsilon, \{x = 0\})$ is illustrated in Figure 6.

For instance,

- from the configuration $(([(F_1, 0)]), \epsilon, \{x = 0\})$, after executing the transition rule $F_1 \xrightarrow{\text{TS}} (\text{ADD}(F_2, 1, x))$, we have

$$(v', \iota') = \text{UpdateCtns}_T(v, \iota) = \text{ADD}(F_2, 1, x)(([(F_1, 0)]), \{x = 0\}) = (([(F_2, 1)(F_1, 0)]), \{x = 1\}),$$

$$\eta' = \text{Concretize}_{v, \iota}(T) \cdot \eta = \text{Concretize}_{v, \iota}(\text{ADD}(F_2, 1, x)) = \text{ADD}(F_2, 1, 1),$$

- from the configuration $(([(F_2, 1), (F_1, 0)]), ((\text{ADD}(F_2, 1, 1))), \{x = 1\})$, after executing the transition rule $F_2 \xrightarrow{\text{NTS}} (\text{REP}(F_3, 1, x))$, we have $\eta' = \eta$ and

$$(v', \iota') = \text{UpdateCtns}_T(v, \iota) = \text{REP}(F_3, 1, x)(([(F_2, 1), (F_1, 0)]), \{x = 1\}) = (([(F_3, 2)], \{x = 2\}),$$

- from the configuration $(([(F_2, 1), (F_1, 0)]), ((\text{ADD}(F_2, 1, 1))), \{x = 1\})$, after executing the transition rule back , we have $T_1 = \text{ADD}(F_2, 1, 1)$ and $T_1^{-1} = \text{REM}(F_2, 1, 1)$, $\eta' = \epsilon$, and moreover,

$$(v', \iota') = \text{UpdateCtns}_{T_1^{-1}}(v, \iota) = \text{REM}(F_2, 1, 1)(([(F_2, 1), (F_1, 0)]), \{x = 1\}) = (([(F_1, 0)]), \{x = 1\}),$$

- from the configuration $(([(F_3, 2)]), ((\text{ADD}(F_2, 1, 1))), \{x = 2\})$, after executing the transition rule $F_3 \xrightarrow{\text{NTS}} (\text{REM}(F_3, 1, x))$, we have $\eta' = \eta$, and moreover,

$$(v', \iota') = \text{UpdateCtns}_T(v, \iota) = \text{REM}(F_3, 1, 2)(([(F_3, 2)]), \{x = 2\}) = ([\epsilon], \{x = 2\}),$$

- from the configuration $(([(F_3, 2)]), ((\text{ADD}(F_2, 1, 1))), \{x = 2\})$, after executing the transition rule back , we have $T_1 = \text{ADD}(F_2, 1, 1)$ and $T_1^{-1} = \text{REM}(F_2, 1, 1)$, $\eta' = \epsilon$, and moreover,

$$(v', \iota') = \text{UpdateCtns}_T(v, \iota) = \text{REM}(F_2, 1, 1)(([(F_3, 2)]), \{x = 2\}) = (([(F_3, 2)]), \{x = 2\}).$$

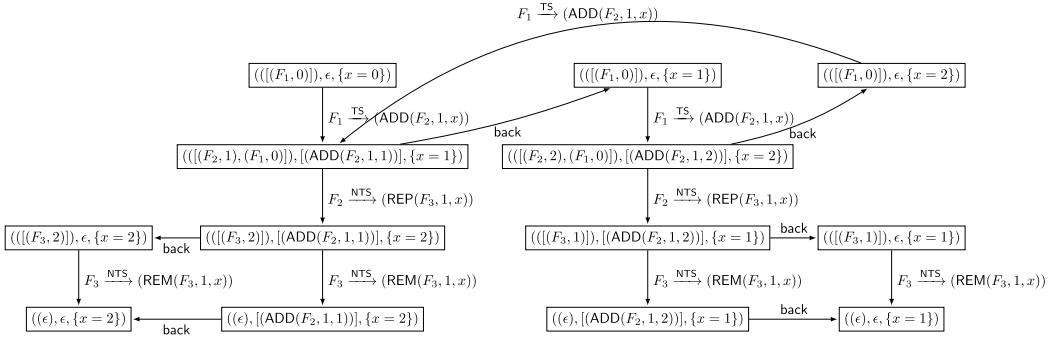


Fig. 6. Configurations that are reachable from the configuration $(([(F_1, 0)]), \epsilon, \{x = 0\})$ in \mathcal{M} .

4.2 Semantics of AMASS_{ACT} for the Other Versions of Android

As mentioned earlier, the semantics of AMASS_{ACT} of different versions of Android are different. In the sequel, we illustrate the differences by focusing on AMASS_{ACT,IF}. The differences of the semantics of AMASS_{ACT} can be found in the appendix.

Before a formal description, let us first illustrate the differences using the following example.

Example 4.4. Let $\mathcal{M} = (\text{Act}, A, \text{Frg}, \text{Lmd}, \text{Aft}, \text{Ctn}, \Delta)$ be an AMASS_{ACT,IF}, where $\text{Act} = \{A, B, C, D\}$, for each $A' \in \text{Act}$, $\text{Lmd}(A') = \text{STD}$, $\text{Aft}(A) = \text{Aft}(B) = 1$, and $\text{Aft}(C) = \text{Aft}(D) = 2$, and moreover, $\Delta = \{\text{back}\} \cup \{\tau_i \mid 1 \leq i \leq 6\} \cup \{\tau'_i \mid 1 \leq i \leq 3\}$ such that $\tau_1 = A \xrightarrow{\text{start}(\perp)} C$, $\tau_2 = C \xrightarrow{\text{start}(NTK \wedge MTK)} B$, $\tau_3 = B \xrightarrow{\text{start}(NTK)} C$, $\tau_4 = C \xrightarrow{\text{start}(\perp)} D$, $\tau_5 = D \xrightarrow{\text{start}(\perp)} A$, $\tau_6 = A \xrightarrow{\text{start}(NTK)} A$, $\tau'_1 = C \xrightarrow{\text{start}(NTK \wedge RTF)} D$, $\tau'_2 = C \xrightarrow{\text{start}(RTF)} A$, and $\tau'_3 = C \xrightarrow{\text{start}(NTK)} B$.

We use the configuration $(([CA], A, \text{MAIN}), ([ADC], C, \text{NTK}), ([B], B, \text{NTK}))$ to illustrate the difference. This configuration can be reached from the initial configuration $(([A], A, \text{MAIN}))$ by the following sequence of transition rules: $\tau_1 \tau_2 \tau_3 \tau_4 \tau_5 \tau_6 \text{ back}$. The differences of semantics for different versions of Android are demonstrated by applying $\tau'_1, \tau'_2, \tau'_3$ on the configuration $(([CA], A, \text{MAIN}), ([ADC], C, \text{NTK}), ([B], B, \text{NTK}))$ (Figure 7):

- If the transition $\tau'_1 = C \xrightarrow{\text{start}(NTK \wedge RTF)} D$ is applied, then for Android 11.0 through 13.0, the task $([ADC], C, \text{NTK})$ is moved to the top and the activity D is reordered to the front, resulting in the configuration

$$(([DAC], C, \text{NTK}), ([CA], A, \text{MAIN}), ([B], B, \text{NTK})),$$

whereas for Android 6.0 through 10.0, the activity D is pushed after the task $([ADC], C, \text{NTK})$ is moved to the top, resulting in the configuration

$$(([DADC], C, \text{NTK}), ([CA], A, \text{MAIN}), ([B], B, \text{NTK})).$$

This difference is explained by the fact that for Android 6.0 through 10.0, RTF is ignored when it is used together with NTK.

- If the transition $\tau'_2 = C \xrightarrow{\text{start}(RTF)} A$ is applied, then for all versions of Android 6.0 through 13.0, except 7.0, A is reordered to the front in the top task, resulting in the configuration

$$(([AC], A, \text{MAIN}), ([ADC], C, \text{NTK}), ([B], B, \text{NTK})).$$

In Android 7.0, the top task is cleared and A is pushed, resulting in the configuration

$$(([A], A, \text{MAIN}), ([ADC], C, \text{NTK}), ([B], B, \text{NTK})).$$

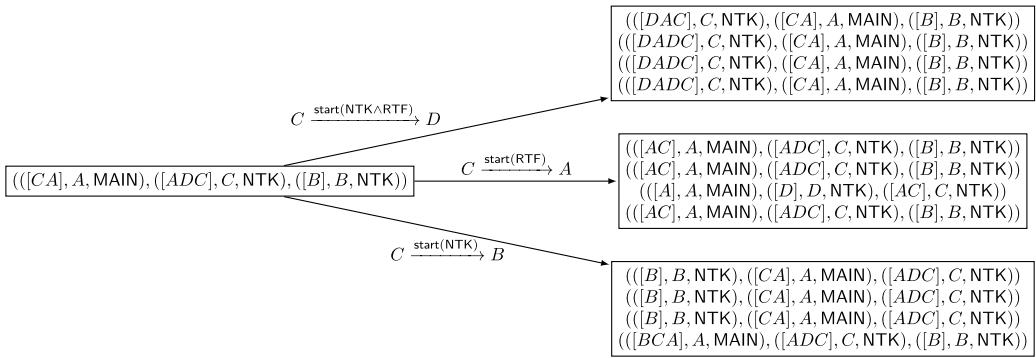


Fig. 7. Semantics of AMASS_{ACT,IF} for different versions of Android, where the first, second, third, and fourth lines of the text in the right boxes are configurations for Android 11.0 through 13.0, 8.0 through 10.0, 7.0, and 6.0, respectively.

This difference is explained by the fact that for Android 7.0, when the top task is the main task where the started activity occurs but is not the top activity, RTF has the same effect as CTK.

- If the transition $\tau'_3 = C \xrightarrow{\text{start}(NTK)} B$ is applied, then for all versions of Android 7.0 through 12.0, the B -task is moved to the top (without pushing a new instance of B), resulting in the configuration

$$(([B], B, \text{NTK}), ([CA], A, \text{MAIN}), ([ADC], C, \text{NTK})).$$

In Android 6.0, the B -task is not moved to the top, and an instance of B is pushed to the top task directly, resulting in the configuration

$$(([BCA], A, \text{MAIN}), ([ADC], C, \text{NTK}), ([B], B, \text{NTK})).$$

This difference is explained by the fact that the task allocation mechanism of Android 6.0 is different from the other versions—namely, in Android 6.0, only affinities are used for looking for a task, whereas for the other versions, real activities and affinities are used together to look for a task.

In the sequel, we state the differences of the semantics of AMASS_{ACT,IF} models in detail. To avoid tediousness, let us focus on the situation $\phi \models \neg\text{TOH}$. The differences for the situation $\phi \models \text{TOH}$ are similar.

4.2.1 Android 11.0 and 12.0. The semantics of AMASS for Android 11.0 and 12.0 are the same as Android 13.0.

4.2.2 Android 10.0, 9.0, and 8.0. The semantics for these three versions are the same and differ from that for Android 13.0 in the following sense: RTF is ignored when used together with NTK. In other words, for Android 10.0, 9.0, and 8.0, the semantics of AMASS_{ACT,IF} for the case $\phi \models \text{NTK} \wedge \neg\text{NDM}$ is adapted from Android 13.0 as follows:

- If $\phi \models \text{MTK}$, then \dots .
- If $\phi \models \neg\text{MTK}$, then
 - if $\text{GetRealTsk}(\rho, B) = S_i$ or $\text{GetRealTsk}(\rho, B) = *$ $\wedge \text{GetTsk}(\rho, B) = S_i$, then
 - * if $\phi \models \text{CTK}$, then \dots ,
 - * if $\phi \models \neg\text{CTK}$, then

- if $\phi \models \text{CTP}$ and $B \in S_i$, then \dots ,
- if $\phi \models \text{CTP}$ and $B \notin S_i$, then \dots ,
- if $\phi \models \neg\text{CTP}$, then
 - ◊ if $\text{GetRealTsk}(\rho, B) = S_i$ and $\zeta_i \neq \text{MAIN}$, then $\rho' = \text{MvTsk2Top}(\rho, i)$,
 - ◊ otherwise,
 - if $\phi \models \text{STP}$ and $\text{TopAct}(S_i) = B$, or $\phi \models \text{STP} \wedge \text{PIT}$ and $i = 1$ and $\text{PreAct}(S_1) = B$, then $\rho' = \text{MvTsk2Top}(\rho, i)$,
 - otherwise, $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
- if $\text{GetTsk}(\rho, B) = *$, then \dots .

Note that the parts of the semantics denoted by \dots are the same as Android 13.0, and in the semantics for the situation $\phi \models \neg\text{CTP}$, the flag RTF has no effects and thus is ignored.

4.2.3 Android 7.0. The semantics for Android 7.0 is close to that of Android 10.0 (or 9.0, 8.0) but differs from it in the following two aspects: (1) the effect of NDM is the same as that of NTK, and (2) when $\phi \models \neg\text{NTK} \wedge \neg\text{NDM} \wedge \neg\text{CTP}$, if the top task is the main task where the started activity occurs but is not the top activity, then RTF has the same effect as CTK. More precisely, for Android 7.0, only two cases $\phi \models \text{NTK}$ and $\phi \models \neg\text{NTK}$ are considered, where the semantics for the case $\phi \models \text{NTK}$ inherits that of $\phi \models \text{NTK} \wedge \neg\text{NDM}$ for Android 10.0, whereas the semantics for the case $\phi \models \neg\text{NTK}$ is adapted from that of $\phi \models \neg\text{NTK} \wedge \neg\text{NDM}$ for Android 10.0 as follows:

- If $\phi \models \text{CTP}$ and $B \in \text{TopTsk}(\rho)$, then \dots .
- If $\phi \models \text{CTP}$ and $B \notin \text{TopTsk}(\rho)$, then \dots .
- If $\phi \models \neg\text{CTP}$, then
 - if $\phi \models \text{RTF}$ and $B \in \text{TopTsk}(\rho)$, then
 - * if $\zeta_i = \text{MAIN}$, then $\rho' = \text{ClrTsk}(\rho, B)$,
 - * otherwise, $\rho' = \text{MvAct2Top}(\rho, B)$,
 - if $\phi \models \text{RTF}$ and $B \notin \text{TopTsk}(\rho)$, then \dots ,
 - if $\phi \models \neg\text{RTF}$, then \dots .

4.2.4 Android 6.0. The semantics for Android 6.0 differs from that of Android 10.0 (or 9.0, 8.0) in the following two aspects: (1) the effect of NDM is the same as that of NTK, and (2) the task allocation mechanism of Android 6.0 does not use the real activities of tasks and only relies on affinities. More precisely, for Android 6.0, only two cases, $\phi \models \text{NTK}$ and $\phi \models \neg\text{NTK}$, are considered, where the semantics for the case $\phi \models \neg\text{NTK}$ inherits that of $\phi \models \neg\text{NTK} \wedge \neg\text{NDM}$, and the semantics for the case $\phi \models \text{NTK}$ is adapted from that of $\phi \models \text{NTK} \wedge \neg\text{NDM}$ for Android 10.0 as follows, where the conditions involving $\text{GetRealTsk}(\rho, B)$ and $\text{GetTsk}(\rho, B)$ are simplified into the conditions involving only $\text{GetTsk}(\rho, B)$, and moreover, we do not need to distinguish whether a task is the main task or not:

- If $\phi \models \text{MTK}$, then \dots .
- If $\phi \models \neg\text{MTK}$, then
 - if $\text{GetTsk}(\rho, B) = S_i$, then
 - * if $\phi \models \text{CTK}$, then \dots ,
 - * if $\phi \models \neg\text{CTK}$, then
 - if $\phi \models \text{CTP}$ and $B \in S_i$, then \dots ,
 - if $\phi \models \text{CTP}$ and $B \notin S_i$, then \dots ,
 - if $\phi \models \neg\text{CTP}$, then
 - ◊ if $\phi \models \text{STP}$ and $\text{TopAct}(S_i) = B$, or $\phi \models \text{STP} \wedge \text{PIT}$ and $i = 1$ and $\text{PreAct}(S_1) = B$, then $\rho' = \text{MvTsk2Top}(\rho, i)$,
 - ◊ otherwise, $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
 - if $\text{GetTsk}(\rho, B) = *$, then \dots .

We remark that the unexpected behavior of RTF for Android 7.0—that is, that RTF behaves the same as CTK in some cases—does not occur in Android 6.0.

We have defined the semantics of AMASS in this section. To go one step further, we would like to validate the semantics against the actual behaviors of Android apps w.r.t. the multitasking mechanism between activities and fragments. Moreover, we would like to do some static analysis of the behaviors of Android apps related to the multitasking mechanism between activities and fragments. To facilitate these two tasks, in the next two sections, we build AMASS models out of APK files of Android apps and encode the reachability problem of AMASS models into the model checking problem in the input format of the nuXmv model checker [3].

5 Generating AMASS Models from APK Files

The goal of this section is to show how we build AMASS models out of the APK files of the Android apps.

In Android apps, switching between components is by sending ICC messages to the Android system. Each ICC message is represented by an Intent object that carries a set of data items. By resolving the ICC messages, we can extract both the source and destination of the switching and the data items it carries.

Recent work [15] studied the available ICC resolution tools and performed a practical evaluation on both hand-crafted benchmarks as well as large-scale real-world apps. The evaluation shows that (1) the fragment is a key feature that is widely used in the component transitions, and (2) most state-of-the-art ICC resolution tools miss the ICCs involving activities and fragments. A recent tool, *ICCBot* [16], resolves the component transitions connected by fragments and activities, and achieves a higher success rate and accuracy. However, ICCBot is insufficient for obtaining an AMASS model for the following two reasons:

- ICCBot fails to decompile the APK files of some commercial apps, thus their models cannot be constructed.
- AMASS models contain more information about the component transitions—in particular, ICCBot ignores the API “`addBackStack()`” that can allow pushing transactions to the fragment transaction stack, and ignores the API `finish()` that can pop the current activity.

To this end, we extend ICCBot to $\text{ICCBot}_{\text{AMASS}}$ in the following aspects:

- At first, $\text{ICCBot}_{\text{AMASS}}$ records the calls to the API `finish()` and associates them with the corresponding calls to `startActivity()` or `startActivityForResult()`. This enables $\text{ICCBot}_{\text{AMASS}}$ to accurately track the termination of the activities and identify transition rules that are affected by these terminations.
- Additionally, $\text{ICCBot}_{\text{AMASS}}$ monitors the calls of the API `addBackStack()` so that the transition rules involving fragments can be accurately constructed. In contrast, ICCBot does not record `addBackStack()`. Therefore, it misses the information $\mu \in \{\text{TS}, \text{NTS}\}$ in the transition rules $A \xrightarrow{\mu} T$ or $F \xrightarrow{\mu} T$.
- Moreover, $\text{ICCBot}_{\text{AMASS}}$ provides means to take cross-app ICCs into consideration when constructing AMASS models.
- Finally, for the commercial apps that cannot be decompiled, $\text{ICCBot}_{\text{AMASS}}$ applies a dynamic approach to extract the AMASS models.

In the sequel, we describe more details about how $\text{ICCBot}_{\text{AMASS}}$ takes cross-app ICCs into consideration as well as utilizes a dynamic approach to construct AMASS models for these apps that cannot be decompiled.

ALGORITHM 1: *AMASSExplore()*

```

/* Two global variables:  $\Delta$  and  $acts$  */;
1  $\rho \leftarrow adb.getTasks();$ 
2  $topAct \leftarrow adb.getTopActivity();$ 
3  $visitedActs \leftarrow \{topAct\};$ 
4  $DynDFS(\rho, topAct, [], d);$ 
5 while  $acts \neq \emptyset$  do
6   foreach  $(newAct, newEvents) \in acts$  do
7     if  $newAct \in visitedActs$  then
8        $acts \leftarrow acts - \{(newAct, newEvents)\};$ 
9       continue;
10    else
11       $visitedActs \leftarrow visitedActs \cup \{newAct\};$ 
12       $UIAutomator.restart();$ 
13      foreach  $event \in newEvents$  do
14        |  $UIAutomator.click(event);$ 
15       $\rho \leftarrow ADB.getTasks();$ 
16       $DynDFS(\rho, newAct, newEvents, d);$ 

```

Model Extraction for Cross-App ICCs. If for an app, the multiple APK files that are involved in the cross-app ICCs of this app are provided, then $ICCBot_{AMASS}$ can construct an AMASS model that captures the behaviors of all of these multiple APK files. The algorithm goes as follows:

- (1) At first, for the APK file corresponding to an app, $ICCBot_{AMASS}$ constructs an AMASS model, where the cross-app ICCs starting from this app are recorded but not processed.
- (2) Then for the model, we try to manually identify the APK files involved in these cross-app ICCs by searching for their package names.
- (3) If the APK files involved in the cross-app ICCs are identified successfully for the app, then all of these multiple APK files, including the original APK file for the app, are processed and an AMASS model to capture the behaviors of all of these apps is constructed.

Afterward, these models can be analyzed just as a model extracted from an app containing no cross-app ICCs.

Dynamic Model Extraction for Unsuccessfully Decompiled APK Files. Roughly speaking, the algorithm to extract AMASS models dynamically from APK files works as follows:

- (1) We first execute all click events of the foreground activity to search for new activities.
- (2) When clicking some events in the foreground activity, some new UI widgets (e.g., menu widgets) may appear (although the foreground activity is unchanged), resulting in some new click events. When executing these newly produced click events, some UI widgets may appear and even more new click events can be produced. The click events in the foreground activity are organized hierarchically.
- (3) We apply a depth-first search to execute all sequences of hierarchically organized click events, up to some depth. If a new activity is found, the associated transition rule for starting the new activity is produced, where the intent flags are guessed. For instance, if a non-top task is moved to the top and a new instance of the activity B of the “standard” launch mode is pushed to it, then the “NTK” flag can be guessed.

The pseudo-code of the dynamic model extraction algorithm is given in Algorithm 1, namely the procedure *AMASSExplore()*. The procedure utilizes two global variables, Δ and $acts$, where Δ

ALGORITHM 2: *DynDFS($\rho, srcAct, events, d$)*

```

input :  $\rho, srcAct, events, d$ 
/* Dynamic depth-first search new activity with UIAutomator, up to depth  $d$  */;
1 if  $d > 0$  then
2   foreach  $event \in UIAutomator.getClickEvents()$  do
3      $UIAutomator.click(event);$ 
4      $newAct \leftarrow ADB.getTopActivity();$ 
5      $newEvents \leftarrow events \cdot event;$ 
6     if  $newAct = srcAct$  then
7       if  $d > 1$  then
8          $DynDFS(\rho, srcAct, newEvents, d - 1);$ 
9         /* Decrement  $d$  and continue the dynamic DFS. */;
10      else
11         $UIAutomator.restart();$ 
12        foreach  $event \in events$  do
13          |  $UIAutomator.click(event);$ 
14      else
15        /* Discover new transitions and refine the AMASS model */;
16         $\rho' \leftarrow ADB.getTasks();$ 
17         $\tau' \leftarrow guessTrans(srcAct, \rho, newAct, \rho');$ 
18         $\Delta \leftarrow \Delta \cup \{\tau'\};$ 
19         $acts \leftarrow acts \cup \{(newAct, newEvents)\};$ 
20         $UIAutomator.restart();$ 
21        foreach  $event \in events$  do
22          |  $UIAutomator.click(event);$ 

```

represents the current set of transition rules that are discovered so far, and $acts$ stores the pairs $(A, events)$, where A is an activity and $events$ is a sequence of click events so that from the main activity, if these click events are executed by UIAutomator, then an instance of A is started. The procedure *AMASSExplore()* calls the procedure *DynDFS($\rho, srcAct, events, d$)* (see Algorithm 2) to do a depth-first search for new activities, starting from $srcAct$, up to the depth d (i.e., the length of the click events reaching a new activity). The two procedures rely on some APIs of UIAutomator and ADB, whose meanings are described next:

- *UIAutomator.getClickEvents()* returns the set of clickable events in the foreground activity of the app under test,
- *UIAutomator.click(e)* executes the click-event e ,
- *UIAutomator.restart()* restarts the the app under test,
- *ADB.getTasks()* returns the content of the back stack.

For each $(newAct, newEvents) \in acts$, *AMASSExplore()* calls the procedure *DynDFS($\rho, newAct, newEvents, d$)* to search dynamically for new activities, starting from $newAct$, and store the newly discovered activities as well as the corresponding sequences of click events into $acts$, up to the depth d . Here, d represents the length of the click event sequence required to reach the new activity from $newAct$. Note that $newEvents$ are used by UIAutomator to reach $newAct$ starting from the main activity. In some cases, pressing buttons may not start a new activity, but instead, new widgets appear (e.g., the menu widget), requiring us to continue searching for new click events in these widgets to reach the new activity.

If a new activity is found during the execution of the procedure *DynDFS($\rho, srcAct, Events, d$)*, with ρ' being the current configuration, then the function *guessTrans($srcAct, \rho, newAct, \rho'$)* is used

to infer the intent flags based on the evolution of the configuration so that a new transition rule τ' can be formed and put into Δ . Moreover, the sequence of click events that reach *newAct* from *srcAct* is recorded in *newEvents* and the pair (*newAct*, *newEvents*) is put into *acts*. To continue searching for new activities, we need to return to the activity *srcAct*. Instead of pressing the back button, we restart the app and execute the corresponding *events* using UIAutomator. This is necessary because in some cases, pressing the back button may not allow us to reach the previous activity, as indicated by the semantics in Section 4.

The aforementioned dynamic model extraction algorithm enables us to extract models from the APK files that cannot be decompiled successfully. Nevertheless, the models extracted dynamically may be inaccurate. Specifically, the following three types of inaccuracies may exist in the dynamically extracted models:

- The intent flags guessed in the algorithm may be incorrect, since the effects of different combinations of intent flags may be equivalent.
- Some transition rules involving fragments may be missed, since fragments are ignored in the algorithm, due to the fact that it is challenging to identify dynamically the fragment to which a UI widget belongs.
- Furthermore, even the transition rules for activities may be incomplete, since it is typical that the dynamic exploration does not cover all of the possible behaviors of Android apps.

Finally, compared to the static model extraction, the dynamic model extraction is slower in general, as demonstrated by the experiments in Section 9 (see Tables 9 and 10 for details).

6 Encoding AMASS Models into nuXmv

In this section, we show how to encode the semantics of these AMASS models into the reachability problem of finite state machines that can be tackled by the symbolic model checker nuXmv [4]. This encoding will facilitate the automated validation of the formal semantics of AMASS models (Section 7) and static analysis of Android apps (Section 8).

In general, AMASS models are infinite state systems, since both the number of tasks (stacks) and the heights of stacks can be unbounded. We impose two pre-defined upper bounds: c_t on the maximum number of tasks of the same affinity and \hbar on the height of stacks. As a result, we can obtain a finite state system. Nevertheless, even with these upper bounds, the number of configurations of an AMASS model can be *exponential* in the size of the model and c_t and \hbar , for which we resort to nuXmv [4] and translate an AMASS \mathcal{M} (with given c_t and \hbar) to an FSM $\mathcal{A}_{\mathcal{M}}$.

In nuXmv, an FSM \mathcal{A} is triplet $(\vec{x}, \vec{s}, \delta)$, where

- \vec{x} is a tuple of Boolean variables representing the inputs,
- \vec{s} is a tuple of Boolean variables representing the states,
- δ is a Boolean formula involving the variables \vec{s} , \vec{x} , and \vec{s}' to describe the transitions, where \vec{s}' is a tuple of primed state variables that represent their new values after a transition.

Let $\mathcal{M} = (\text{Act}, A_0, \text{Frg}, \text{Ctn}, \text{Lmd}, \text{Aft}, \Delta)$ be an AMASS and $\text{Conf}_{\mathcal{M}, c_t, \hbar}$ denote the set of configurations of \mathcal{M} where the number of tasks of the same affinity is no more than c_t and the heights of all stacks are no more than \hbar . It follows that $(\text{Conf}_{\mathcal{M}, c_t, \hbar}, \xrightarrow{\mathcal{M}})$ is a finite state system.⁷ Then we show how to encode $(\text{Conf}_{\mathcal{M}, c_t, \hbar}, \xrightarrow{\mathcal{M}})$ into an FSM $\mathcal{A}_{\mathcal{M}}$. Intuitively, the states of $\mathcal{A}_{\mathcal{M}}$ represent the configurations in $\text{Conf}_{\mathcal{M}, c_t, \hbar}$ and the transitions of $\mathcal{A}_{\mathcal{M}}$ simulate the transition rules of \mathcal{M} .

To facilitate the encoding, we first introduce the following definitions:

⁷Strictly speaking, $\xrightarrow{\mathcal{M}}$ should be the restriction of $\xrightarrow{\mathcal{M}}$ to $\text{Conf}_{\mathcal{M}, c_t, \hbar}$.

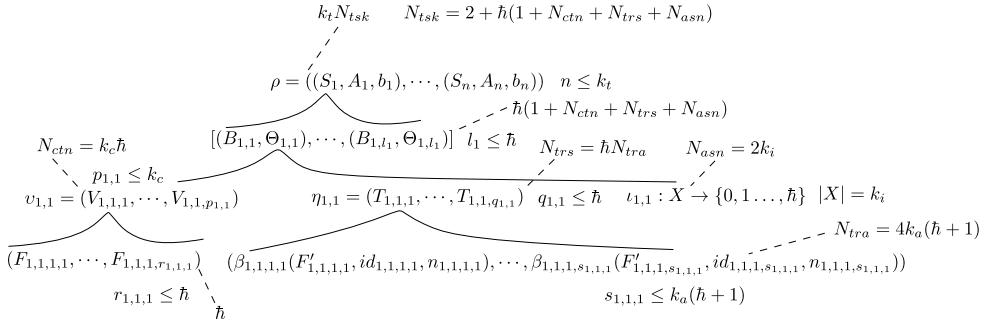


Fig. 8. Length of the word encoding a task stack.

- Let k_c denote the maximum length of $\text{Ctn}(A)$ for $A \in \text{Act}$ —that is, the maximum number of fragment containers in an activity.
- Let k_a denote the maximum number of actions occurring in the fragment transaction of one transition rule of \mathcal{M} .
- Let X denote the set of variables occurring in the transitions of \mathcal{M} for storing the identifiers of fragment instances and $k_i = |X|$.
- Let $k_t = c_t |\text{Aft}(\text{Act})|$ —namely, the maximum number of tasks in the task stacks.

Recall that each configuration in $\text{Conf}_{\mathcal{M}}$ is $\rho = ((S_1, A_1, b_1), \dots, (S_n, A_n, b_n))$. Let

$$\Sigma_{\mathcal{M}} = \text{Act} \cup \text{Frg} \cup \{\text{ADD}, \text{REM}\} \cup \text{CID}_{\mathcal{M}} \cup X \cup [k_c \hbar] \cup \{0, 1, \perp\},$$

where $\text{CID}_{\mathcal{M}}$ is the set of fragment container identifiers occurring in \mathcal{M} and \perp is a dummy symbol introduced as placeholders. Then each task stack in $\text{Conf}_{\mathcal{M}, \hbar}$ can be encoded by a word of length exactly $k_t(2 + \hbar(1 + k_c \hbar + 4k_a \hbar(\hbar + 1) + k_i))$ over the alphabet $\Sigma_{\mathcal{M}}$. The arguments for this fact go as follows (Figure 8 presents an illustration):

- According to the semantics of AMASS, ρ contains at most k_t tasks—that is, $n \leq k_t$.
- Suppose $S_i = [(B_{i,1}, \Theta_{i,1}), \dots, (B_{l,i}, \Theta_{l,i})]$, and for each $i \in [n]$ and $j \in [l_i]$, $\Theta_{i,j} = (v_{i,j}, \eta_{i,j}, \iota_{i,j})$. Then for each $i \in [n]$, $l_i \leq \hbar$, and moreover, for each $j \in [l_i]$, $v_{i,j}$ contains at most k_c fragment containers and the height of each of them is no more than \hbar , and $\iota_{i,j}$ is a function from X to $\{0\} \cup [k_c \hbar]$ (since each fragment contains at most \hbar instances in one fragment container and there are at most k_c fragment containers).
- Furthermore, $\eta_{i,j}$ contains at most \hbar transactions, each of which has at most $k_a(\hbar + 1)$ concretized actions. To see this, note that $\eta_{i,j}$ is obtained by concretizing at most k_a actions in some transition rule of \mathcal{M} and each such action is concretized into at most $\hbar + 1$ actions (because the heights of the history contents of fragment stacks are no more than \hbar). Note that each action $\beta(F', i', n')$ in the transactions of $\eta_{i,j}$ is encoded by a word of length 4.

More specifically, we have that

- each fragment container is encoded by a word of length $N_{ctn} = k_c \hbar$,
- each transaction is encoded by a word of length $N_{tra} = 4k_a(\hbar + 1)$,
- each transaction stack is encoded by a word of length $N_{trs} = \hbar N_{tra}$,
- each assignment function is encoded by a word of length $N_{asn} = 2k_i$ —that is, a word of the form $x_1 n_1 \dots x_{k_i} n_{k_i}$ (where $x_j \in X$ and $n_j \in \{0\} \cup [k_c \hbar]$),
- each activity is encoded by a word of length $N_{act} = 1 + N_{ctn} + N_{trs} + N_{asn}$, and
- each task is encoded by a word of length $N_{tsk} = 2 + \hbar N_{act}$.

Note that in the encoding, the top activity of the top task is in the first position.

We can then use $k_t N_{tsk}$ variables $X_1, \dots, X_{k_t N_{tsk}}$ ranging over Σ_M to encode a task stack. Evidently, each symbol in Σ_M can be encoded as a bit vector of length $\log_2 |\Sigma_M|$. For each $\sigma \in \Sigma_M$, assume $\text{enc}(\sigma)$ is the binary encoding of σ . Each configuration can be encoded by $k_t N_{tsk} \log_2 |\Sigma_M|$ Boolean variables. Therefore, \mathcal{A}_M uses $k_t N_{tsk} \log_2 |\Sigma_M|$ state variables to encode the configurations in $\text{Conf}_{M, c_t, \hbar}$. Moreover, \mathcal{A}_M contains the input variables to encode the transition rules of M . Equipped with these state variables and input variables, we then encode the semantics of the transition rules of M into the transitions of \mathcal{A}_M .

7 Validation of the Formal Semantics

The goal of this section is to validate the formal semantics of the AMASS models defined in Section 4. To avoid tediousness, we focus on the two submodels AMASS_{ACT} and AMASS_{FRG} of AMASS and Android 13.0. We validate the formal semantics from two different perspectives:

- At first, we audit the Java source code of the Android operating system to extract the control flows of starting an activity and executing a fragment transaction, respectively. We confirm that the formal semantics of AMASS models defined in Section 4 indeed echo the extracted control flows. See Section 7.1 for more about the code audit.
- Moreover, we select 21 Android apps to empirically validate the conformance of the formal semantics of AMASS models to the actual behaviors of these apps in the Android operating system. The details of the empirical validation are given in Section 7.2.

7.1 Validation of the Formal Semantics by Auditing the Source Code of Android OS

To validate the formal semantics of AMASS_{ACT} (respectively, AMASS_{FRG}), we audit the source code of Android OS. Specifically, we trace the control flow of the Java source code⁸ starting from the procedure `startActivity()` (respectively, `commit()`). To increase the quality of the auditing process, we audit the source code in two phases. In the first phase, the three authors audit the relevant parts of the source code of Android OS separately. Then in the second phase, the three authors have a joint discussion and achieve a consensus on the understanding of the source code.

We first consider AMASS_{ACT} , then AMASS_{FRG} .

7.1.1 Auditing the Source Code of AMASS_{ACT} . Figure 9 shows the control flow starting from the procedure `startActivity()` in the `Activity` class, where the vertices represent the procedures in classes and edges represent the procedure calls:

- Starting from `startActivity()`, `startActivityForResult()` is called, then `execStartActivity()` is called, and so on, until the procedure `startActivityInner()` is reached, where the core control logic for starting an activity is implemented.
- In the procedure `startActivityInner()`, the following statements are executed sequentially: the procedure `computeLaunchingTaskFlags()`, a conditional statement where `getReusableTask()` and `computeTargetTask()` are in the two branches, respectively, the procedure `recycleTask()`, and another conditional statement where `setNewTask()` and `addOrReparentStartingActivity()` are in the two branches, respectively.
- The procedure `getReusableTask()` calls `findTask()`, in which the procedure `process()` is called, and `process()` calls the procedure `forAllLeafTasks()`, where the procedure `test()` is called.
- The procedure `recycleTask()` calls the procedure `complyActivityFlags()` and `setNewTask()` calls `reuseOrCreateTask()`, respectively.

We audit the source code of the procedures called directly or indirectly by `startActivityInner()` and confirm that the semantics of AMASS_{ACT} is consistent with its actual implementation in

⁸Available at <https://android.googlesource.com/platform/frameworks/base/>

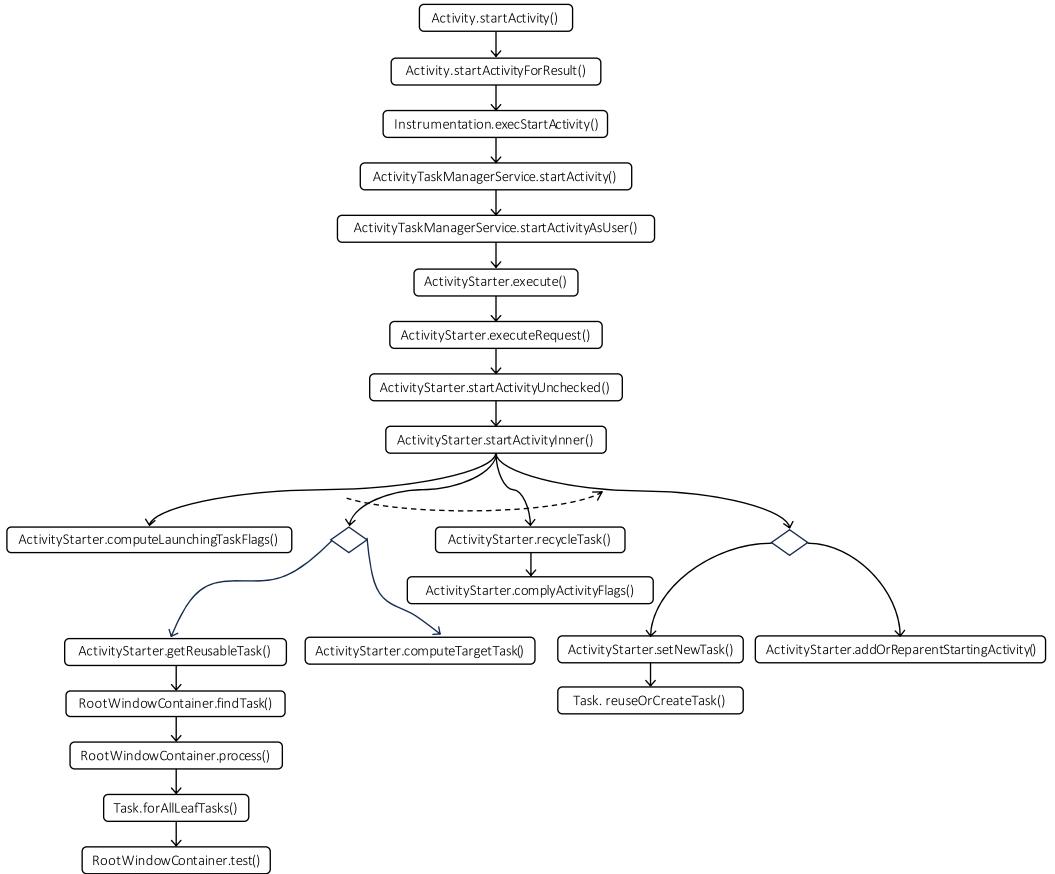


Fig. 9. Call graph for starting an activity.

Android OS. In particular, the task allocation mechanism and the intent flags in the semantics conform to the source code in Android OS. The details of the auditing are relegated to Appendix E.1.

7.1.2 Auditing the Source Code for AMASS_{FRG}. The control flows of committing and popping a fragment transaction are illustrated in Figure 10:

- We start with committing a fragment transaction first. From Figure 10, to commit a fragment transaction, `commit()` is called. Then it calls `commitInternal()`, which calls `enqueueAction()` and so on until `executeOpsTogether()` is called, where the core control logic for committing a fragment transaction is implemented. The procedure `executeOpsTogether()` calls `expandOps()` first, then `executeOps()`. Finally, `executeOps()` calls `BackStackRecord.executeOps()`.
- The call graph for popping a fragment transaction is similar. From Figure 10, to pop a fragment transaction, `popBackStack()` is called. Then it calls `commitInternal()`, which calls `enqueueAction()` and so on until `executeOpsTogether()` is called. The procedure `executeOpsTogether()` calls `trackAddedFragmentsInPop()` first, then `executeOps()`. Finally, `executeOps()` calls `BackStackRecord.executePopOps()`.

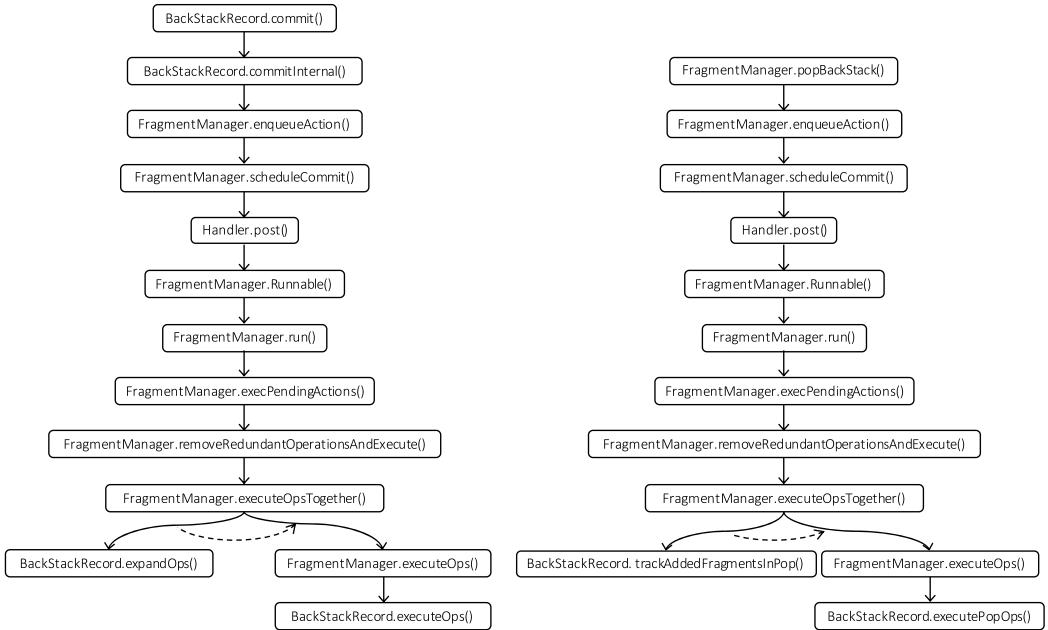


Fig. 10. Call graphs for committing and popping a fragment transaction.

We audit the source codes of the procedure `executeOpsTogether()` as well as those called by it directly or indirectly and confirm that

- the way of dealing with REP actions in the semantics of AMASS_{FRG} in Section 4.1.2 is consistent with the source code of `expandOps()`,
- the execution of fragment actions as defined in the semantics of AMASS_{FRG} in Section 4.1.2 is consistent with the source code of `BackStackRecord.executeOps()`,
- the way of revoking fragment transactions in the semantics of AMASS_{FRG} in Section 4.1.2 is consistent with the source code of `trackAddedFragmentsInPop()`.

The details of the auditing are relegated to Appendix E.2.

7.2 Empirical Validation of the Formal Semantics

The goal of this section is to validate the formal semantics empirically by comparing the actual behaviors of Android apps with their expected behaviors according to the formal semantics of the AMASS models that are extracted from them. To ease the empirical validation, we try to automate the process and propose a partially automated method for semantics validation in the sequel, by utilizing the nuXmv model checker, the Android UIAutomator testing framework, and the ADB tool.

Partially Automated Method for Semantics Validation. Let X be an Android app and \mathcal{M} be an AMASS_{ACT} (respectively, AMASS_{FRG}) model that is extracted from X , and let \mathcal{A} be the nuXmv FSM model that encodes the configuration reachability problem of \mathcal{M} , where c_t , the bound on the number of tasks of the same affinity, and \hbar , the bound on the height of the stacks, are set to be 2 and 6, respectively. Moreover, k_a , the number of actions in one fragment transaction, is set to be 2.

The partially automated method to validate the semantics goes as follows. For a transition rule τ in \mathcal{M} ,

- (1) we use nuXmv to search for a path $\pi = \pi_1 \dots \pi_m$ in \mathcal{A} , where an accepting condition corresponding to τ is set, to reach a configuration where τ can be applied (in other words, τ is enabled by the configuration),
- (2) we generate from the app X and each transition π_i with $i \in [m]$, a sequence of click events in X , say e_i ,
- (3) we use UIAutomator to execute the click events in e_1, \dots, e_m one by one (the task stack is updated), and moreover, after the execution of all click events, we use ADB to extract the resulting configuration—that is, the contents of the resulting task stack, say ρ ,
- (4) we generate the sequence of click events in X , say e , to fulfill the application of the transition rule τ ,
- (5) we use UIAutomator again to execute the click events in e one by one, and use ADB to obtain the resulting configuration ρ' ,
- (6) if $\rho' \neq \tau(\rho)$, then report the semantic inconsistency, where $\tau(\rho)$ denotes the expected configuration obtained by applying τ on ρ according to the formal semantics.

Note that the generation of sequences of click events for transition rules (namely, the second and fourth step in the aforementioned procedure) is *not* automated. For a transition rule of the form $\tau = A \xrightarrow{\alpha(\phi)} B$, we can click the widgets in the activity A to find a sequence of click events so that the activity B can be launched. Nevertheless, just from the sequence of click events and without the manual inspection of the source code, it is difficult, if not impossible, to figure out the intent flags associated with the action of starting the activity B from the activity A . As a result, it is hard to determine that a sequence of click events corresponds to the transition rule τ , even though we do know that the activity B is started from A .

Since generating sequences of click events for transitions is a manual process, it is hard to apply the aforementioned partially automated method for semantics validation to a large pool of Android apps from F-Droid or Google Play. As a result, in the sequel, we only select a small number of (more precisely, 20) apps from F-Droid to validate the formal semantics:

- At first, we select 10 apps to cover as many launch modes and intent flags as possible for validating the semantics of AMASS_{ACT} .
- Then, we select 10 apps to cover as many types of fragment transactions as possible for validating the semantics of AMASS_{FRG} .

We generate the sequences of click events from the transition rules by manually inspecting the source codes of these 20 apps. Evidently, these 20 apps are insufficient to cover the vast number of cases in the definition of the semantics of AMASS_{ACT} and AMASS_{FRG} , since there are exponentially many different combinations of intent flags. Therefore, in addition to these apps, we design a special Android app, ValApp,⁹ aiming at covering all cases in the definition of the semantics of AMASS_{ACT} and AMASS_{FRG} models. We mainly rely on ValApp to enumerate the different combinations of intent flags and carry out semantics validation for them. Note that this way is largely credible since, after the options (e.g., launch modes and intent flags) are chosen, the rest of the validation process is the same as real-world Android apps—that is, the `startActivity()` or `commit()` procedure is executed in the Android operating system and the results are collected and compared.

ValApp: A Special Android App for the Semantics Validation. A snapshot of ValApp is shown in Figure 11. ValApp includes eight activities, corresponding to the eight (launch mode, task affinity)

⁹Available at <https://github.com/Jinlong-He/ValApp/tree/main>

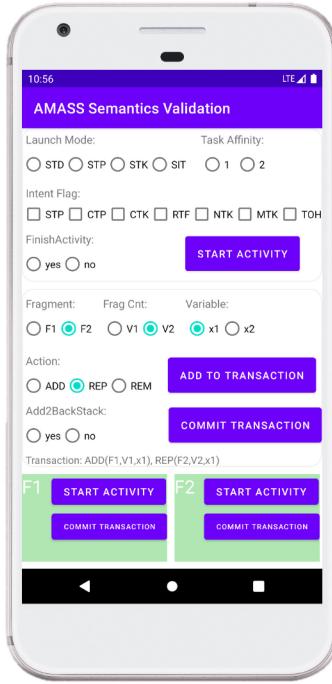


Fig. 11. ValApp: An Android app designed for validating the semantics of AMASS.

pairs from $\{\text{STD}, \text{STP}, \text{STK}, \text{SIT}\} \times \{1, 2\}$. Moreover, ValApp provides the means to choose the launch modes and intent flags, as well as “start” and “finishStart,” so that transition rules can be generated for all of their combinations. Furthermore, each activity of ValApp includes two fragments and two fragment containers. It also provides two variables for fragment identifiers and allows arbitrary combinations of actions to form fragment transactions. Finally, ValApp allows pushing arbitrarily many transactions into the fragment transaction stack. From the design, we can see that ValApp is capable of comprehensively accounting for all factors that may affect the semantics of AMASS_{ACT} and AMASS_{FRG} models. Moreover, ValApp is *universal* in the sense that a user can interact with ValApp to choose the transition rules and generate a desired AMASS model.

Let us focus on Android 13.0 in this section and validate the semantics of AMASS_{ACT} and AMASS_{FRG} models under this version. The verification of the formal semantics of AMASS_{ACT} and AMASS_{FRG} under the other versions is similar and omitted.

7.2.1 Validation of the Formal Semantics of AMASS_{ACT} . To validate the semantics, we consider the transition rules of the form $\tau = A \xrightarrow{\alpha(\phi)} B$, and generate one configuration for each combination of the launch modes of A and B , the values of α , the intent flags, and the constraints on the configuration before applying the transition—for example, $\text{GetRealTsk}(\rho, B) = *$, $\text{GetTsk}(\rho, B) = S_1$, and $\text{TopAct}(\rho) = B$. In total, there are 901,120 different combinations to be considered, and we would like to generate configurations for all of them.

We utilize the 10 apps selected from F-Droid as well as ValApp to generate the configurations. The 10 F-Droid apps are selected to cover as many launch modes and intent flags as possible. The sizes of these apps, the number of activities and transition rules of the AMASS_{ACT} models constructed out of these apps (i.e., $|\text{Act}|$ and $|\Delta|$), and the number of generated configurations can be

Table 5. Validation of the Formal Semantics of AMASS_{ACT} for Android 13.0

App (package name)	Size (MB)	Act	\Delta	# Configurations
com.fsck.k9	3.58	21	76	892
org.andstatus.app	3.37	12	29	203
com.fsck.k9.material	4.49	17	53	686
org.videolan.vlc	16.16	16	36	567
com.github.kiliakin.yalpstore	1.43	14	119	1,195
one.librem.mail	4.69	18	74	984
one.librem.tunnel	20.38	6	34	378
eu.siacs.conversations.legacy	11.12	17	82	993
org.fdroid.k9	3.12	20	70	893
info.guardianproject.otr.app.im	10.7	12	43	492
Total	–	–	–	6,231
ValApp	–	8	131,072	901,120

found in Table 5. In the end, we generate 6,231 configurations out of the F-Droid apps and 901,120 configurations out of ValApp. Then we use these configurations to validate the formal semantics. Through experiments, we discover that for every combination, the configuration obtained by applying the transition rule corresponding to the combination according to the formal semantics and the actual configuration returned by ADB are equal, thus the formal semantics of AMASS_{ACT} for Android 13.0 are confirmed to be consistent with the actual behaviors of Android apps.

7.2.2 Validation of the Formal Semantics of AMASS_{FRG}. To validate the semantics, we consider the transition rules of the form $\tau = A \xrightarrow{\mu} T$ or $F \xrightarrow{\mu} T$. Note that according to the definition of semantics of AMASS_{FRG} in Section 4.1.2, the only requirement for the enablement of $A \xrightarrow{\mu} T$ or $F \xrightarrow{\mu} T$ is that the top activity or fragment is A or F . This requirement does not constrain the configurations very much. To validate the semantics of AMASS_{FRG}, we fix the values of the following parameters and generate configurations as well as transition rules with these values:

- there is only one activity, say A_0 ,
- the number of containers associated with A_0 is 1,
- the maximum number of transactions in the transaction stack is 1,
- the maximum number of fragment actions in a transaction is 2,
- the identifiers in (concretized) fragment actions in a transaction are from the set {1, 2}.

Note that the maximum number of fragments in a container is bounded by $\hbar = 6$ (i.e., the bound on the height of the stacks). In total, there are 4,032 different configurations to be considered. We generate the 4,032 configurations, construct AMASS_{FRG} models out of these apps, and apply the transition rules in the models to the generated configurations to validate the semantics.

We utilize the 10 apps selected from F-Droid as well as ValApp to validate the semantics. The 10 F-Droid apps are selected to include as many fragments and fragment transactions as possible. Moreover, when constructing AMASS_{FRG} models out of the F-Droid apps, we restrict our attention to an activity whose number of fragments is the greatest in the app. For ValApp, since the number of actions in a transaction can be unbounded, we restrict our attention to the transition rules where the number of actions in a transaction is at most 2. The sizes of these apps, the number of activities and transition rules of the AMASS_{FRG} models constructed out of these apps (i.e., $|\text{Frg}|$ and $|\Delta|$), and the average number of actions per transaction, as well as the number of generated (configuration, transition rule) pairs, can be found in Table 6.

Table 6. Validation of the Semantics of AMASS_{FRG} Models

App (package name)	Size (MB)	Frg	\Delta	Average #actions/transaction	#(Config, trans)
org.fox.ttrss	1.15	9	18	1.2	26,405
exa.lnx.a	2.88	10	18	1.0	21,403
org.wordpress.android	4.31	7	19	1.1	7,028
de.geeksfactory.opacclient	4.06	4	23	1.0	1,919
se.oandell.riksdagen	2.66	6	23	1.5	31,012
com.secuso.privacyFriendlyCodeScanner	1.62	6	24	1.0	28,425
com.igisw.openmoneybox	9.04	9	28	1.9	38,543
xyz.hisname.fireflyiii	4.82	16	33	1.1	64,160
org.anhonesteffort.flock	4.22	8	41	1.0	51,507
dulleh.akhyou.fdroid	4.17	4	126	1.8	84,602
Total	—	—	—	—	355,004
ValApp	—	2	577	2.0	1,745,856

In the end, we generate 4,032 configurations for each of the F-Droid apps and ValApp. We also generate 577 transition rules for ValApp. Therefore, the total number of (configuration, transition rule) pairs for F-Droid apps is 355,004, whereas the number for ValApp is 1,745,856. Then for all of these pairs, we apply the transition rules on the configurations to validate the formal semantics. Through experiments, we discover that for each configuration and each transition rule, the configuration obtained by applying the transition rule according to the formal semantics and the actual configuration returned by ADB are equal, thus the formal semantics of AMASS_{FRG} for Android 13.0 are confirmed to be consistent with the actual behaviors of Android apps.

8 Static Analysis of AMASS Models

In this section, we consider the static analysis of AMASS models. We focus on two vulnerabilities which might occur in Android apps: *task unboundedness vulnerability* and *fragment container unboundedness vulnerability*. The former refers to the case that in the execution of the app, one might be in a configuration of which the height is unbounded. The latter one is similar, where the height of a fragment container of some activity of the configuration is unbounded. As we will see later, these vulnerabilities would cause abnormal behavior of apps. The stack analysis aims to detect the apps which are potentially exposed to the vulnerabilities. While the problem is generally unsolvable in theory, we appeal to sensible relaxations, as illustrated in the following two subsections.

8.1 Task Unboundedness

To detect the task unboundedness vulnerability, we consider *k-task unbounded*, where *k* is a given natural number. An AMASS \mathcal{M} is *k-task unbounded* if, for every $n \in \mathbb{N}$, there are a configuration ρ of \mathcal{M} and a task in ρ such that $\epsilon \xrightarrow{\mathcal{M}} \rho$, the height of the task is at least n , and the path from ϵ to ρ involves the interplay with at most k other tasks.

For instance, we assume that in \mathcal{M} the following two conditions are satisfied:

- (i) the main activity A_0 satisfies $\text{Aft}(A_0) = 1$, the main task is the top task, and the top activity of the main task is $A \neq A_0$ with $\text{Lmd}(A) = \text{STD}$ and $\text{Aft}(A) = 1$,
- (ii) \mathcal{M} contains two transition rules $A \xrightarrow{\text{start}(\phi_1)} B$ and $B \xrightarrow{\text{start}(\phi_2)} A$ such that $\text{Lmd}(B) = \text{STK}$, $\text{Aft}(B) = 2$, $\phi_1 \models \text{CTK}$, $\phi_2 \models \text{NTK} \wedge \neg\text{NDM} \wedge \neg\text{MTK} \wedge \neg\text{STP} \wedge \neg\text{RTF} \wedge \neg\text{CTP} \wedge \neg\text{CTK}$.

Then \mathcal{M} is 1-task unbounded since the number of A instances in the main task can go unbounded by executing the two transition rules repeatedly, during which the main task interacts with another task where B is the only activity.

We hypothesize that most task unbounded vulnerabilities only involve a small number of tasks (normally, $k \leq 2$), which will be justified by experiments in Section 9.3. As a result, we introduce algorithms to solve the k -task unboundedness problem. We will start with $k = 0$ and $k = 1$, then consider the more general case $k \geq 2$.

We will focus on the following typical situation: for any pair of distinct tasks, if none of their real activities has the SIT (SingleInstance) launch mode, then their affinities should be different. Note that the constraint in this situation is satisfied, if in all of the transitions of \mathcal{M} , MTK is set to be false, namely $\phi \models \neg\text{MTK}$. This assumption is empirically justified by the fact that in 6,388 open source F-Droid and commercial Google Play apps used for experiments (see Section 9), only less than 3% of them contain occurrences of the MTK flag.

We first introduce some notations. We use Act_{real} to denote the set of activities in \mathcal{M} that may occur as a real activity of tasks. More precisely, Act_{real} is the set of activities $A \in \text{Act}$ such that one of the following conditions holds: (1) $\text{Lmd}(A) = \text{SIT}$, (2) $\text{Lmd}(A) = \text{STK}$, (3) $\text{Lmd}(A) = \text{STD}$ or STP , and A occurs in some transition $B \xrightarrow{\alpha(\phi)} A$ such that $\text{Lmd}(B) = \text{SIT}$ or $\phi \models \text{NTK} \vee \text{NDM}$.

For each activity $A \in \text{Act}_{\text{real}}$ such that $\text{Lmd}(A) \neq \text{SIT}$, let $\text{Reach}(\Delta, A)$ denote the least subset $\Theta \subseteq \Delta$ satisfying that $B \xrightarrow{\alpha(\phi)} C \in \Theta$ (where $\alpha = \text{start}$ or finishStart) whenever the following two constraints are satisfied:

- $B = A$ or there exists a transition $A' \xrightarrow{\alpha'(\phi')} B \in \Theta$ (where $\alpha' = \text{start}$ or finishStart),
- $\text{Lmd}(C) \neq \text{SIT}$, and if $\text{Lmd}(C) = \text{STK}$ or $\phi \models \text{NTK} \vee \text{NDM}$, then $\text{Aft}(C) = \text{Aft}(A)$.

Intuitively, $\text{Reach}(\Delta, A)$ comprises all transition rules that can be applied and once applied would retain an A -task as the top task. By abusing the notation slightly, $\text{Reach}(\Delta, A)$ also denotes the graph whose edge set is $\text{Reach}(\Delta, A)$.

$\text{Reach}(\Delta, A)$ can be generalized to the case that $A \in \text{Act}_{\text{real}}$ and $\text{Lmd}(A) = \text{SIT}$, where $\text{Reach}(\Delta, A)$ is regarded as the graph that contains a single node A without edges.

Case $k = 0$

Now we will propose a procedure to check k -task unboundedness for $k = 0$. The underpinning idea is to search, for each $A \in \text{Act}_{\text{real}}$, a *witness cycle*—that is, a sequence of transitions from $\text{Reach}(\Delta, A)$, the execution of which would force the task to grow indefinitely.

Formally, a witness cycle is a simple cycle in the graph $\text{Reach}(\Delta, A)$ of the form

$$C = A_1 \xrightarrow{\alpha_1(\phi_1)} A_2 \dots A_{n-1} \xrightarrow{\alpha_{n-1}(\phi_{n-1})} A_n,$$

where $n \geq 2$ and $\alpha_i = \text{start}$ or finishStart for each $i \in [n]$ satisfying the following two constraints.

[*Non-clearing*]: The content of an A -task is *not* cleared when C is executed. Namely, for each $i \in [n-1]$, $\phi_i \models \neg\text{CTP} \wedge \neg\text{NDM}$, and moreover, either $\phi_i \models \neg\text{CTK}$, or $\phi_i \models \neg\text{NTK}$ and $\text{Lmd}(A_{i+1}) \neq \text{STK}$ (intuitively, this means that CTK is not enabled; cf. Figure 19).

[*Height-increasing*]: The height of the task content is increasing after C is executed. Namely, it is required that $\sum_{i \in [n-1]} \text{weight}_C(\tau_i) > 0$, where for each $i \in [n-1]$, $\tau_i = A_i \xrightarrow{\alpha_i(\phi_i)} A_{i+1}$ and $\text{weight}_C(\tau_i)$ specifies the modification of the height of the A -task by executing τ_i and is defined as follows:

- If $\alpha_i = \text{start}$, then
 - if $\phi_i \models \text{RTF}$, then $\text{weight}_C(\tau_i) = 0$,
 - if $\phi_i \models \neg\text{RTF}$, $A_i = A_{i+1}$, and either $\phi_i \models \text{STP}$ or $\text{Lmd}(A_{i+1}) = \text{STP}$, then $\text{weight}_C(\tau_i) = 0$,
 - otherwise, $\text{weight}_C(\tau_i) = 1$.

- If $\alpha_i = \text{finishStart}$, then
 - if $\phi_i \models \text{RTF}$, then $\text{weight}_C(\tau_i) = -1$,
 - if $\phi_i \models \neg\text{RTF}$, $A_i = A_{i+1}$, and either $\phi_i \models \text{STP}$ or $\text{Lmd}(A_{i+1}) = \text{STP}$, then $\text{weight}_C(\tau_i) = -1$,
 - otherwise, $\text{weight}_C(\tau_i) = 0$.

If a witness cycle exists for some $A \in \text{Act}_{\text{real}}$, the algorithm returns “task unbounded”; otherwise, if Δ is a directed acyclic graph, then the algorithm returns “task bounded”; otherwise, the procedure reports “unknown.”

The more general cases for $k \geq 1$ are much more technical and involved. We introduce the concept of “virtual transitions” for tasks to capture the situation that the content of a task can be indirectly modified by first jumping off the task and returning to the task later on. When this happens, the procedure adds virtual transitions for each task before checking the existence of witness cycles.

Case $k = 1$

Let $A \in \text{Act}_{\text{real}}$. In this case, we check whether the height of some A -task is unbounded but involving another task. The main difficulty of this case, in a contrast to $k = 0$, is that when the system evolves, the A -task may give away as the top task—that is, the other task may become the top task but then gives back to the A -task later on. Even worse, the content of the A -task may have been changed during the round of switch over, and there may be several rounds during which the height of the A -task grows. To accommodate such a complex analysis, we will utilize a concept of *virtual transitions* to summarize the changes of the content of the A -task for each round of top task switching.

We introduce some notations first. Let $A, B \in \text{Act}_{\text{real}}$ such that $\text{Lmd}(A) \neq \text{SIT}$ and A, B represent different tasks—specifically, one of the following conditions holds:

- (1) $\text{Lmd}(A) = \text{Lmd}(B) = \text{SIT}$ and $A \neq B$,
- (2) $\text{Lmd}(A) = \text{SIT}$ and $\text{Lmd}(B) \neq \text{SIT}$,
- (3) $\text{Lmd}(A) \neq \text{SIT}$ and $\text{Lmd}(B) = \text{SIT}$,
- (4) $\text{Lmd}(A) \neq \text{SIT}$, $\text{Lmd}(B) \neq \text{SIT}$, and $\text{Aft}(A) \neq \text{Aft}(B)$.

Let $G_A = (V, E)$ be an edge-labeled graph, where the edge labels are of the form $\alpha(\phi)$ with $\alpha \in \{\text{start}, \text{finishStart}\}$ and $\phi \in \mathcal{B}(\mathcal{F})$. Intuitively, G_A is used to capture the set of transitions that can be applied to update the content of an A -task.

A *task-switching transition* from G_A to a B -task is a transition $A' \xrightarrow{\alpha'(\phi')} B' \in \Delta$ such that $A' \in V$, and one of the following conditions holds:

- $\text{Lmd}(B') = \text{SIT}$ and $B' = B$,
- $\text{Lmd}(B') = \text{STK}$, moreover, $\text{Aft}(B') = \text{Aft}(B)$ and $\text{Lmd}(B) \neq \text{SIT}$,
- $\text{Lmd}(B') = \text{STD}$ or STP , and $\phi' \models \text{NTK} \vee \text{NDM}$, moreover, $\text{Aft}(B') = \text{Aft}(B)$ and $\text{Lmd}(B) \neq \text{SIT}$.

Intuitively, a task-switching transition from G_A to a B -task means the task switching in the situation that A -task and B -task already exist. Note that in this situation, if $\text{Lmd}(B) \neq \text{SIT}$ and $\text{Lmd}(B') \neq \text{SIT}$, then there does not exist a B' -task, as there do not exist two non-SIT tasks whose affinities are $\text{Aft}(B)$.

A transition $A' \xrightarrow{\alpha'(\phi')} A''$ is a *virtual transition* of G_A w.r.t. B if there is a task-switching transition $A' \xrightarrow{\alpha(\phi)} B'$ from G_A to a B -task and a task-switching transition $B'' \xrightarrow{\alpha'(\phi')} A''$ from $\text{Reach}(\Delta, B')$ to an A -task. Note that the virtual transition inherits the intent-flag constraint of $B'' \xrightarrow{\alpha'(\phi')} A''$.

The completion of $\text{Reach}(\Delta, A)$ by the virtual transitions w.r.t. B , denoted by $\text{Comp}_B(\text{Reach}(\Delta, A))$, is defined as the graph computed by the following three-step algorithm:

- (1) Let $G_0 := \text{Reach}(\Delta, A)$ and $i := 0$.
- (2) Iterate the following procedure until $G_{i+1} = G_i$: Let G_{i+1} be the graph obtained from G_i by adding all virtual transitions of G_i w.r.t. B . Let $i := i + 1$.
- (3) Let $\text{Comp}_B(\text{Reach}(\Delta, A)) := G_i$.

Finally, we present the algorithm to decide the 1-task unboundedness of \mathcal{M} .

Algorithm to decide the 1-task unboundedness of \mathcal{M}

- Check for each $A, B \in \text{Act}_{\text{real}}$ such that $\text{Lmd}(A) \neq \text{SIT}$ and A, B represent different tasks, whether there exists a witness cycle in $\text{Comp}_B(\text{Reach}(\Delta, A))$.
- If affirmative, then the algorithm returns “task unbounded.”
- Otherwise, if Δ is a directed acyclic graph, then the algorithm returns “task bounded.”
- Otherwise, the algorithm returns “unknown.”

Case $k \geq 2$

We first extend the concept of representing different tasks from two to multiple tasks. For $A \in \text{Act}_{\text{real}}$ and $\mathbb{A} = \{A_1, \dots, A_k\} \subseteq \text{Act}_{\text{real}}$, we say that A, A_1, \dots, A_k represent different tasks if they are mutually distinct, and additionally, for each pair of them, say A' and A'' , they represent different tasks.

Let $A \in \text{Act}_{\text{real}}$ and $\mathbb{A} = \{A_1, \dots, A_k\} \subseteq \text{Act}_{\text{real}}$ such that A, A_1, \dots, A_k represent different tasks in the sequel.

Let $G = (V, E)$ be an edge-labeled graph, where the edge labels are of the form $\alpha(\phi)$ with $\alpha \in \{\text{start}, \text{finishStart}\}$ and $\phi \in \mathcal{B}(\mathcal{F})$, with the intention of capturing the set of transitions that can be applied to update the content of an A -task. Note that if $\text{Lmd}(A) = \text{SIT}$, then G is the graph that contains a single node A and no edges. A *task-switching transition from G to \mathbb{A} -tasks* is a transition $A' \xrightarrow{\alpha'(\phi')} B' \in \Delta$ such that $A' \in V$ and one of the following constraints holds:

- $\text{Lmd}(B') = \text{SIT}$ and $B' \in \mathbb{A}$,
- $\text{Lmd}(B') = \text{STK}$ and $\text{Aft}(B') \in \text{Aft}(\mathbb{A} \setminus \text{Act}_{\text{SIT}})$,
- $\text{Lmd}(B') = \text{STD or STP}$, and $\phi' \models \text{NTK} \vee \text{NDM}$, and moreover, $\text{Aft}(B') \in \text{Aft}(\mathbb{A} \setminus \text{Act}_{\text{SIT}})$.

Intuitively, a task-switching transition from G to \mathbb{A} -tasks means the task-switching in the situation that A -task, and A_1 -task, \dots , A_k -task already exist.

For $B' \in \text{Act}$ such that either $\text{Lmd}(B') = \text{SIT}$ and $B' \in \mathbb{A}$, or $\text{Lmd}(B') \neq \text{SIT}$ and $\text{Aft}(B') \in \text{Aft}(\mathbb{A} \setminus \text{Act}_{\text{SIT}})$, we use $\text{Reach}_{\mathbb{A}}(\Delta, B')$ to denote the least set of transitions $\Theta \subseteq \Delta$ satisfying the following constraints:

- $\text{Reach}(\Delta, B') \subseteq \Theta$,
- for each transition $C \xrightarrow{\alpha(\phi)} D \in \Delta$ satisfying the following two conditions, we have $C \xrightarrow{\alpha(\phi)} D \in \Theta$:
 - (1) C is either B' or the target node of some transition in Θ ,
 - (2) if $\text{Lmd}(D) = \text{SIT}$, then $D \in \mathbb{A}$,
 - if $\text{Lmd}(D) = \text{STK}$, then $\text{Aft}(D) \in \text{Aft}(\mathbb{A} \setminus \text{Act}_{\text{SIT}})$,
 - if $\text{Lmd}(D) = \text{STD or STP}$, and $\phi \models \text{NTK} \vee \text{NDM}$, then $\text{Aft}(D) \in \text{Aft}(\mathbb{A} \setminus \text{Act}_{\text{SIT}})$.

Intuitively, $\text{Reach}_{\mathbb{A}}(\Delta, B')$ is the set of transitions that are reachable from B' that can be used to update the contents of the tasks whose real activities are from \mathbb{A} .

Suppose additionally that $\text{Lmd}(A) \neq \text{SIT}$ holds. For a graph $G = (V, E)$ capturing the set of transitions that can be applied to update the content of an A -task, a *virtual transition* of G w.r.t. \mathbb{A} is some $A' \xrightarrow{\alpha'(\phi')} A''$ such that there is a task-switching transition $A' \xrightarrow{\alpha(\phi)} B'$ from G to \mathbb{A} -tasks and a task-switching transition $B'' \xrightarrow{\alpha'(\phi')} A''$ from $\text{Reach}_{\mathbb{A}}(\Delta, B')$ to an A -task. We define the *completion* of $\text{Reach}(\Delta, A)$ by the virtual transitions w.r.t. \mathbb{A} , denoted by $\text{Comp}_{\mathbb{A}}(\text{Reach}(\Delta, A))$, as the graph computed by the following three-step algorithm:

- (1) Let $G_0 := \text{Reach}(\Delta, A)$ and $i := 0$.
- (2) Iterate the following procedure until $G_{i+1} = G_i$: Let G_{i+1} be the graph obtained from G_i by adding all the virtual transitions of G_i w.r.t. \mathbb{A} . Let $i := i + 1$.
- (3) Let $\text{Comp}_{\mathbb{A}}(\text{Reach}(\Delta, A)) := G_i$.

We are ready to present the procedure to solve the k -task boundedness problem for $k \geq 2$.

Algorithm to solve the k -task boundedness problem for $k \geq 2$

- For each $A \in \text{Act}_{\text{real}}$ and $\mathbb{A} = \{A_1, \dots, A_k\} \subseteq \text{Act}_{\text{real}}$ such that A, A_1, \dots, A_k represent different tasks and $\text{Lmd}(A) \neq \text{SIT}$, check whether there exists a witnessing cycle in the graph $\text{Comp}_{\mathbb{A}}(\text{Reach}(\Delta, A))$.
- If the answer is yes for any such a pair A and \mathbb{A} , then the procedure reports “task unbounded.” Otherwise, if Δ is a directed acyclic graph, then the procedure reports “task bounded.”
- Otherwise, the procedure reports “unknown.”

Generation of the Witnessing Transition Sequence

As mentioned previously, task unboundedness suggests a potential security vulnerability. As a result, when this is spotted, it is desirable to synthesize a concrete transition sequence so that the developers can, for instance, follow this sequence to test and improve their apps. It turns out that the synthesis can be reduced to the configuration reachability problem of the FSM \mathcal{A}_M —that is, whether there is a configuration matching a prescribed formula is reachable.

Moreover, for a witness cycle for some $A \in \text{Act}_{\text{real}}$, $C = A_1 \xrightarrow{\alpha_1(\phi_1)} A_2 \dots A_{n-1} \xrightarrow{\alpha_{n-1}(\phi_{n-1})} A_n$.

When $k > 0$, some virtual transition (i.e., $A_i \xrightarrow{\alpha_i(\phi_i)} A_{i+1} \notin \Delta$), but it summarizes the changes of the content of the A -task for some round of top task switching. Hence, the existence of a witness cycle for A is reduced to the existence of the activity sequence C' in the A -task, where C' is obtained by the following procedure:

- (1) Let $C' := [A_1]$, $i := 1$,
- (2) Iterate the following procedure until $i = n$,
 - if $\alpha_i = \text{start}$,
 - if $A_i = A_{i+1}$ and $\phi_i \models \text{STP} \vee \text{RTF}$, then $C' := C'$,
 - otherwise, $C' := [A_{i+1}] \cdot C'$,
 - if $\alpha_i = \text{finishStart}$, let $C' = [A_i] \cdot C''$, $C'' \in \text{Act}^*$,
 - if $A_i = A_{i+1}$ and $\phi_i \models \text{STP} \vee \text{RTF}$, then $C' := C''$,
 - otherwise, $C' := [A_{i+1}] \cdot C''$.

Note that among the activities in C' , the leftmost activity of C' is the topmost in the A -task.

From the encoding of task stacks in Section 6, we know that for each $i : 1 \leq i \leq k_t$,

$X_{iN_{tsk}-1}$ corresponds to the second to the last position of the word encoding the i th task and its value is the real activity of the task.

Therefore, the existence of the activity sequence $C' = [A'_1, \dots, A'_{n'}]$ (where $n' < \hbar$) in the A -task can be specified by the following formula:

$$X_{N_{tsk}-1} = A \wedge \bigvee_{0 \leq j \leq \hbar - n'} \bigwedge_{1 \leq k \leq n'} X_{(j+k-1)(1+N_{ctn}+N_{trs}+N_{asn})+1} = A'_k.$$

Therefore, the witnessing transition sequences can be generated by utilizing nuXmv to solve the resulting model checking problem, where \hbar is set to 6.

8.2 Fragment Container Unboundedness Problem

Recall that fragment containers are updated by the fragment transactions—that is, either all actions in a transaction are executed or none of them are executed. Therefore, to detect the fragment container unboundedness vulnerability, it is necessary to reason at the level of fragment transactions rather than fragment actions. Similar to the previous case, the general idea is to find witness cycle of fragment transactions.

We start by introducing some notations to summarize the effects of fragment transactions on fragment containers. Let A be an activity with $Ctn(A) = (i_1, \dots, i_k)$ and

$$T = (\beta_1(F_1, i'_1, x_1), \dots, \beta_k(F_r, i'_r, x_r))$$

be a fragment transaction such that $i'_j \in \{i_1, \dots, i_k\}$ for each $j \in [r]$.

We define $U_{T,A,i_1}, \dots, U_{T,A,i_k}$ as the subsequences of actions in T that are applied to the container i_1, \dots, i_k , respectively. Specifically, $U_{T,A,i_1}, \dots, U_{T,A,i_k}$ can be computed inductively as follows:

- (1) Initially let $j = 1$ and $U_{T,A,i_1} = \epsilon, \dots, U_{T,A,i_k} = \epsilon$.
- (2) Iterate the following procedure until $j > r$,
 - (a) update U_{T,A,i'_j} according to β_j ,
 - if $\beta_j = \text{REP}$, then let $U_{T,A,i'_j} = \text{REP}(F_j)$,
 - otherwise, let $U_{T,A,i'_j} = U_{T,A,i'_j} \cdot \beta_j(F_j)$.
 - (b) let $j = j + 1$.

Note that in the computation of $U_{T,A,i_1}, \dots, U_{T,A,i_k}$, the identifier variables are ignored.

Moreover, for $j \in [k]$, we define the *weight* of T w.r.t. the container i_j , denoted by weight_{T,A,i_j} , which describes the update of T on the height of container i_j , as follows. Let $U_{T,A,i_j} = (\beta'_1(F'_1), \dots, \beta'_l(F'_l))$:

- if $\beta'_r(F'_r) = \text{REP}$ for some $r \in [l]$ (actually in this case, $l = 1$), then $\text{weight}_{T,A,i_j} = -\infty$,
- otherwise, $\text{weight}_{T,A,i_j} = \sum_{r \in [l]} w_r$, where for $r \in [l]$, $w_r = 1$ if $\beta'_r = \text{ADD}$, and $w_r = -1$ if $\beta'_r = \text{REM}$.

Moreover, let $\text{weight}_{T,A} = (\text{weight}_{T,A,i_1}, \dots, \text{weight}_{T,A,i_k})$.

Let us first consider an easy case for the fragment container unboundedness problem. If there are $A \in \text{Act}$ with $Ctn(A) = (i_1, \dots, i_k)$ and a transition rule $A \xrightarrow{\mu} T$ such that $\text{weight}_{T,A,i_j} > 0$ for some $j \in [k]$, then report “fragment container unbounded.” The fragment container unboundedness in this case is attributed to the fact that the transition $A \xrightarrow{\mu} T$ can be applied for arbitrarily many times so that the height of fragment container i_j becomes unbounded.

Next, let us consider the general cases that there are no $A \in \text{Act}$ and transition rule $A \xrightarrow{\mu} T$ satisfying the aforementioned condition—that is, for each $A \in \text{Act}$ with $Ctn(A) = (i_1, \dots, i_k)$ and each transition rule $A \xrightarrow{\mu} T$, we have $\text{weight}_{T,A,i_j} \leq 0$ for every $j \in [k]$.

For the general cases, we need to consider the transition rules of the form $F \xrightarrow{\mu} T$. Since the enablement of these transition rules depend on the top fragment of containers, it is necessary to determine the top fragments of containers. We use a tuple $(\text{Frg} \cup \{\perp\})^k$ to denote the top fragments of containers, where \perp denotes that the container is empty or the top fragment of the container cannot be determined. Suppose the current activity is A and its top fragments of containers are $(F_1, \dots, F_k) \in (\text{Frg} \cup \{\perp\})^k$. Then the top fragments of containers after applying T to A , denoted by $\text{TopFrag}_T(F_1, \dots, F_k)$, are defined as $(\text{TopFrag}_{U_{T,A,i_1}}(F_1), \dots, \text{TopFrag}_{U_{T,A,i_k}}(F_k))$, where for every $j \in [k]$,

- if $U_{T,A,i_j} = \epsilon$, then $\text{TopFrag}_{U_{T,A,i_j}}(F_j) = F_j$,
- otherwise, let the last action of U_{T,A,i_j} be $\beta'(F')$,
 - if $\beta' \neq \text{REM}$ or $F' \neq F_j$, then $\text{TopFrag}_{U_{T,A,i_j}}(F_j) = F'$,
 - otherwise, $\text{TopFrag}_{U_{T,A,i_j}}(F_j) = \perp$. (If $\beta' = \text{REM}$ and $F' = F_j$, we cannot determine the top fragment of container i_j .)

For each $A \in \text{Act}$, we compute an edge-labeled graph $G_A = (V, E)$ by executing the following procedure. Let $\text{Ctn}(A) = (i_1, \dots, i_k)$:

- (1) Let G_0 be the graph comprising all of the edges $v_0 \xrightarrow{\text{weight}_{T,A}} (T, \text{TopFrag}_T(\perp^k))$ such that $A \xrightarrow{\mu} T$ is a transition rule in \mathcal{M} and $\text{weight}_{T,A,i_j} \leq 0$ for every $j \in [k]$, where v_0 is a special vertex.
- (2) Let $i = 0$. Iterate the following procedure until $G_{i+1} = G_i$. Obtain G_{i+1} from G_i by adding the following edges: for each vertex (T, \vec{F}) in G_i with $\vec{F} = (F_1, \dots, F_k)$ and each transition rule $F_j \xrightarrow{\mu} T'$ such that $j \in [k]$ and $F_j \neq \perp$, add the edge $(T, \vec{F}) \xrightarrow{\text{weight}_{T',A}} (T', \text{TopFrag}_{T'}(\vec{F}))$.

Note that each edge of G_A is labeled by a tuple from $(\mathbb{N} \cup \{-\infty\})^k$.

A *witness cycle* of G_A for $A \in \text{Act}$ is a cycle $(T_0, \vec{F}_0) \xrightarrow{\vec{w}_1} (T_1, \vec{F}_1) \dots \xrightarrow{\vec{w}_m} (T_m, \vec{F}_m)$ such that for some $j \in [k]$, $\sum_{r \in [m]} w_{r,j} > 0$, where $\vec{w}_r = (w_{r,1}, \dots, w_{r,k})$ for each $r \in [m]$. Intuitively, $\sum_{r \in [m]} w_{r,j} > 0$ guarantees that the height of the container i_j is strictly increased after executing all fragment transactions in the cycle. Note that in the definition of witness cycle, it is not required that $F_{r,j} \neq \perp$ for every $r \in [m]$ since the top fragments of the container i_j may not be used in the transitions and what is concerning is only the height increase of the container i_j .

Finally, the procedure is summarized as follows.

Algorithm to decide the fragment container unboundedness problem

- If there are $A \in \text{Act}$ with $\text{Ctn}(A) = (i_1, \dots, i_k)$ and a transition rule $A \xrightarrow{\mu} T$ such that $\text{weight}_{T,A,i_j} > 0$ for some $j \in [k]$, then report “fragment container unbounded.”
 - Otherwise, if there is $A \in \text{Act}$ such that G_A contains a witness cycle, then report “fragment container unbounded.”
 - Otherwise, report “unknown.”

9 Implementation and Evaluation of the Static Analysis Algorithms

In this section, we implement the static analysis algorithms proposed in the previous section, giving rise to a tool TaskDroid.¹⁰ Moreover, we evaluate the performance of TaskDroid via extensive experiments on 8,887 open source and commercial Android apps.

¹⁰ Available at <https://github.com/Jinlong-He/TaskDroid>

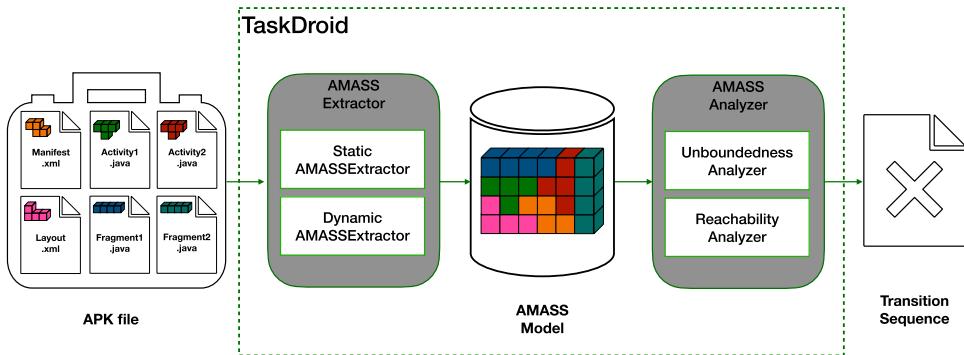


Fig. 12. Architecture of TaskDroid.

Table 7. Statistics of Benchmarks

Source	# Apps	Avg./Max. size of apps	# Extracted models (static/dynamic)
F-Droid	3,867	4.9M/285.0M	3,471 (2,580/891)
Google Play	5,020	15.7M/361.9M	4,612 (3,808/804)

9.1 Implementation

As depicted in Figure 12, TaskDroid comprises two modules—that is, AMASSExtractor and AMASSAnalyzer:

- AMASSExtractor ($\text{ICCBot}_{\text{AMASS}}$) consists of two submodules: static AMASSExtractor and dynamic AMASSExtractor. Static AMASSExtractor statically builds AMASS models from Android apps. Moreover, as described in Section 5, for those apps whose AMASS models cannot be statically built, dynamic AMASSExtractor can build the AMASS models dynamically, by utilizing the UIAutomator and ADB tools. The inputs of AMASSExtractor are Android Package (APK) files.
- AMASSAnalyzer carries out static analysis on AMASS models. AMASSAnalyzer includes a submodule of *Unboundedness Analyzer*, which implements the procedure in Section 8. It also includes a submodule of *Reachability Analyzer*, which is used to generate a path starting from the main activity and a witnessing cycle following the path, when the AMASS is found to be task unbounded and fragment container unbounded.

9.2 Evaluation

We evaluate the efficiency and effectiveness of TaskDroid on 8,887 open source and commercial apps (cf. Sections 9.2.1 and 9.2.2). Moreover, we evaluate the impact of different model extractors on the detection of task/fragment container unboundedness problems of these apps (Section 9.2.3).

The benchmark used for the evaluation consists of 8,887 Android apps collected from Androzoo¹¹ which include all 3,867 open source apps in the F-Droid repository,¹² as well as 5,020 commercial apps in the Google Play market. For Google Play, the apps are selected according to the popularity (number of downloads). Statistics of these apps can be found in Table 7.

AMASSExtractor extracts AMASS models from the APK files as described in Section 5:

¹¹<https://androzoo.uni.lu/>

¹²<https://f-droid.org/>

Table 8. Statistics of the Missing Apps Involved in Cross-App ICCs

Source	# Apps containing cross-app ICCs	Avg./Max. numbers of missing apps	Avg./Max. sizes of missing apps	Avg./Max. sizes of models		
				Act	Frg	\Delta
F-Droid	125	1.2/2	6.8M/103.2M	6.2/38	0.9/11	10.1/66
Google Play	804	1.5/2	16.1M/153.3M	7.9/19	1.1/20	14.5/97

- Out of the 3,867 F-Droid (respectively, 5,020 Google Play) apps, static AMASSExtractor extracts 2,580 (respectively, 3,808) AMASS models. Static AMASSExtractor fails on 1,287 F-Droid (respectively, 1,212 Google Play) apps, which is attributed to the fact that Soot fails to decompile the APK files or the source codes of the apps are obfuscated or encrypted.
- Out of the 2,580 models that are extracted from the F-Droid apps (called *F-Droid models* for short) by static AMASSExtractor and 3,808 models that are extracted from the Google Play apps (called *Google Play models* for short) by static AMASSExtractor, ICCBot_{AMASS} discovers that 311 F-Droid models and 501 Google Play models, respectively, involve cross-app ICCs. Note that although ICCBot_{AMASS} discovers that these models involve cross-app ICCs, each of these models is extracted from *one* APK file and the cross-app ICCs therein have not been dealt with yet. To remedy this, we tried to manually identify the APK files involved in these cross-app ICCs by searching for their package names. In the end, for 125 F-Droid apps and 211 Google Play apps, respectively, we provided the missing APK files involved in the cross-app ICCs of these apps and successfully constructed the AMASS models for them where the cross-app ICCs are modeled. The average/maximum numbers and sizes of these missing apps involved in cross-app ICCs as well as the sizes of the extracted models are shown in Table 8. Afterward, these models can be analyzed in the same way as a model that is extracted from one APK file.
- Moreover, among the 1,287 F-Droid (respectively, 1,212 Google Play) apps that cannot be decompiled, dynamic AMASS extracts 891 (respectively, 804) AMASS models. Dynamic AMASSExtractor fails on 396 F-Droid (respectively, 408 Google Play) apps, which is attributed to the fact that some apps cannot be launched, or crash after launching, or require user name and password to proceed after launching.

9.2.1 The Efficiency of TaskDroid. We investigate the efficiency and scalability of TaskDroid by examining all 3,471 F-Droid and 4,612 Google Play apps for which AMASS models are extracted. For each app, static AMASSExtractor extracts an AMASS model from the APK file statically, where the timeout is set to 300 seconds. Moreover, for the apps where static AMASSExtractor fails, dynamic AMASSExtractor extracts an AMASS model dynamically, where the time out is set to 600 seconds. The average/maximum sizes of the extracted models as well as the extraction time are shown in Tables 9 and 10.

It can be observed that for the statically extracted models, the average/maximum size (number of transition rules, activities, fragments) of F-Droid apps is much smaller than that of Google Play apps. This is expected, since the Google Play apps are considerably more complex than F-Droid open source apps. Moreover, the average time spent in the static model extraction of Google Play apps is more than times that of F-Droid apps. A similar phenomenon happens for the dynamic model extraction, although the difference is slightly smaller.

Furthermore, static AMASSExtractor can extract the AMASS models for F-Droid apps in less than 1 minute and for Google Play apps in less than 4 minutes, whereas dynamic AMASSExtractor can extract the AMASS models for F-Droid apps in around 5 minutes and for Google Play apps in around 10 minutes. The static model extraction is faster than the dynamic one, although the dynamic approach can deal with the apps in which the static approach fails.

Table 9. Static AMASSExtractor

Source	Avg./Max. size of models			Avg. time
	Act	Frg	\Delta	
F-Droid	4.9/70	0.5/16	7.9/475	43.5s
Google Play	7.1/509	1.0/121	21.0/1,956	234.6s

Table 10. Dynamic AMASSExtractor

Source	Avg./Max. size of AMASS		Avg. time
	Act	\Delta	
F-Droid	6.1/31	15.3/71	313.4s
Google Play	11.2/43	28.1/129	593.2s

Table 11. Task Unboundedness

Source	#Unbounded models	#Witnessing cycles per model	Time
F-Droid	485/3,471 (14.0%)	3.3	0.05s
Google Play	559/4,612 (12.1%)	3.9	0.1s

Table 12. Fragment Container Unboundedness

Source	#Unbounded models	#Witnessing cycles per model	Time
F-Droid	193/2,580 (7.5%)	2.5	0.05s
Google Play	293/3,808 (7.7%)	3.0	0.1s

To detect task/fragment container unboundedness vulnerabilities, the timeout is set to 30 seconds, the height \hbar of tasks is set to 6, and k (i.e., the number of interplaying tasks; cf. Section 8) is set to 2.

We first consider Android 13.0. The results of task unboundedness (respectively, fragment container unboundedness) are presented in Tables 11 and 12. As one may see, TaskDroid is highly efficient in analyzing the AMASS models, which can be done in less than 0.1 seconds per app on average. Moreover, TaskDroid identifies 485 (14.0%) F-Droid and 559 (12.1%) Google Play models as “task unbounded.” However, TaskDroid identifies 193 (5.6%) F-Droid and 293 (6.4%) Google Play models as “fragment container unbounded.” Finally, the number of witnessing cycles discovered for the unbounded models is around 3 per app on average.

We then consider Android 6.0 through 12.0 and compare the results for these versions with those for Android 13.0. As shown in Figure 13, the numbers of task unbounded F-Droid (respectively, Google Play) apps are slightly different for different versions, whereas the numbers of fragment container unbounded F-Droid (respectively, Google Play) apps are the same for different versions. This phenomenon is explained by that the semantics of AMASS_{ACT} is slightly different across Android versions, whereas the semantics of AMASS_{FRG} is the same for all of these versions. To have a closer look, we can see that the numbers of task unbounded F-Droid (respectively, Google Play) apps for Android 7.0, Android 8.0 through 10.0, and Android 11.0 through 13.0 are close to each other, and are slightly away from that of Android 6.0. This is explained by the fact that Android 6.0 uses a different task allocation mechanism from the others.

9.2.2 The Effectiveness of TaskDroid. We investigated whether TaskDroid can accurately detect task/fragment container unboundedness vulnerabilities and the abnormal behavior caused by

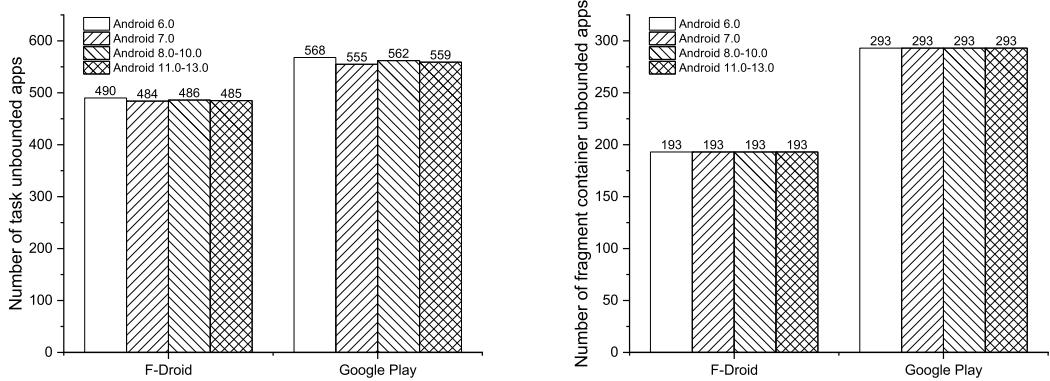


Fig. 13. Comparison of the results for different Android versions.

Table 13. Manual Confirmation of the Effectiveness of TaskDroid

Source	Unbound. vulnerability	#Apps	#Confirmed apps
F-Droid	task	25	17 (68%)
Google Play	task	25	16 (64%)
F-Droid	fragment container	25	16 (64%)
Google Play	fragment container	25	16 (64%)
F-Droid or Google Play	task	50	33 (66%)
F-Droid or Google Play	fragment container	50	32 (64%)
F-Droid or Google Play	task or fragment container	100	65 (65%)

these vulnerabilities in an Android mobile device. To this end, we randomly selected 50 apps from those that are identified as “task unbounded” and “fragment container unbounded” by TaskDroid; in each case, 25 were from F-Droid and 25 were from Google Play, respectively. Information about these apps can be found in Tables 20 through 23 in Appendix G.

We manually checked on a virtual machine (four-core CPU, 2G RAM with Android 13.0) whether these 100 apps were indeed task/fragment container unbounded by verifying whether the witnessing cycles reported by TaskDroid are executable. To ensure the reliability of the manual checking, we asked four individuals to complete the manual checking, and each of them checked all 100 apps. The results were cross checked and are summarized in Table 13.

Out of the 25 apps from F-Droid (respectively, Google Play), 17 (respectively, 16) apps were confirmed to be task unbounded, occupying 68% (respectively, 64%) of the randomly chosen apps; 16 (respectively, 16) apps were confirmed to be fragment container unbounded, occupying 64% (respectively, 64%) of the randomly chosen F-Droid (respectively, Google Play) apps. These give an overall accuracy of 65%. For the remaining 35 apps, we could not confirm the analysis result because: 9 apps required login, 9 apps crashed immediately after launching, and 17 apps could not

Table 14. Threats of Task Unboundedness Vulnerabilities to F-Droid Apps

Package name	#Repetitions of the witnessing cycle	Abnormal behavior
org.gnucash.android	215	reboot
systems.byteswap.aiproute	203	reboot
max.music_cyclon	97	reboot
com.matburt.mobileorg	204	reboot
org.npr.android.news	192	reboot
com.commonsware.android.arXiv	125	reboot
net.mabako.steamgifts	103	reboot
com.app.Zensuren	114	reboot
uk.co.busydoingnothing.prevo	122	reboot
de.drhoffmannsoftware.calcvac	208	reboot
org.sasehash.burgerwp	240	app crash
com.mikifus.padland	59	app crash
org.evilsoft.pathfinder.reference	179	app crash
com.android.keepass	150	app crash
de.bloosberg.basti.childresuscalc	288	app crash
com.samebits.beacon.locator	178	app crash
ohm.quickdice	169	app restart

execute the witnessing cycles (we suspect that the witnessing cycles in these AMASS models are spurious).

Furthermore, on the same virtual machine, for each app that was confirmed to be “task unbounded” or “fragment container unbounded,” we used UIAutomator to execute the click event sequence generated when simulating the witnessing cycle numerous times until some abnormal behavior appeared. During the execution, we used ADB to calculate the number of repetitions of the witnessing cycle as well as record the type of abnormal behavior of the virtual device. The results of the experiments are presented in Tables 14 through 17:

- Among the 18 (respectively, 16) F-Droid (respectively, Google Play) apps that were confirmed to be task unbounded, after hundreds of repetitions of the witnessing cycle, 10 (respectively, 11) apps ended up with rebooting of the device, 6 (respectively, 4) apps ended up with an app crash, and 2 (respectively, 1) apps ended up with restarting of the app.
- Among the 15 (respectively, 14) F-Droid (respectively, Google Play) apps that were confirmed to be fragment container unbounded, after thousands of repetitions of the witnessing cycle, 2 (respectively, 5) apps ended up with rebooting of the device, 10 (respectively, 8) apps ended up with an app crash, and 3 (respectively, 1) apps ended up with restarting of the app.

To further evaluate the threat of task unboundedness for the popular commercial apps, we selected nine apps from Google Play with more than 100,000 downloads, including well-known Amazon, Netflix, and YouTube, and Facebook apps. We built AMASS models of these apps dynamically and carried out static analysis. We found (with confirmation) that nine apps suffered from task unboundedness vulnerability, which, after less than 100 repetitions of the witnessing cycles, all ended up with rebooting of the device (cf. Table 18 for details).

Considering that the crashes and reboots of mobile applications can be caused by a variety of reasons and that it is common for mobile apps to experience such issues, to demonstrate the causality between the crashes and task/fragment container unboundedness, we used the Monkey

Table 15. Threats of Task Unboundedness Vulnerabilities to Google Play Apps

Package name	#Repetitions of the witnessing cycle	Abnormal behavior
com.abdulqawi.ali.mosabqa	288	reboot
com.music.star.player	189	reboot
com.drclabs.android.wootchecker	351	reboot
com.hotels.hotelsmecca	169	reboot
com.airg.hookt	137	reboot
com.holidu.holidu	197	reboot
com.appkey.english3000freakata	113	reboot
socials.com.application	99	reboot
www.genting.rwgenting	114	reboot
com.goldenhammer.beisboldominicana	125	reboot
com.travolution.seoultravelpass	144	reboot
com.ic.myMoneyTracker	179	app crash
tekcarem.gebeliktakibi	161	app restart
de.fckoeln.app	111	app restart
de.twokit.castbrowser	223	app restart
com.TWTD.FLIXMOVIE	139	app restart

Table 16. Threats of Fragment Container Unboundedness Vulnerabilities to F-Droid Apps

Package name	#Repetitions of the witnessing cycle	Abnormal behavior
org.ligi.fahrplan	1,187	reboot
io.github.allenb1.todolist	1,269	reboot
naman14.timber	815	app crash
me.anon.grow	743	app crash
com.wikijourney.wikijourney	932	app crash
com.mattallen.loaned	641	app crash
com.ymber.eleven	1,032	app crash
com.syncedsynapse.kore2	952	app crash
net.momodalo.app.vimtouch	993	app crash
com.csipsimple	1,145	app crash
ch.corten.aha.worldclock	899	app crash
org.wikimedia.commons.wikimedia	1,002	app crash
com.llamacorp.equate	1,145	app restart
koeln.mop.elpeefpe	1,137	app restart
fr.kwiatkowski.ApkTrack	1,257	app restart
eu.prismsw.lampshade	139	app restart

tool¹³ to stress test the 74 apps. The results are shown in Tables 14 through 18. We set the timeout period of Monkey to be 30 minutes. As shown in Figure 14, Monkey reports 6 apps ending up with an app crash, 4 apps ending up with an app restart, and 4 apps ending up with rebooting of the device. Namely, 14 out of 74 apps (around 19%) apps end up with abnormal behaviors, which

¹³<https://developer.android.com/studio/test/other-testing-tools/monkey>

Table 17. Threats of Fragment Container Unboundedness Vulnerabilities to Google Play Apps

Package name	#Repetitions of the witnessing cycle	Abnormal behavior
com.schoola2zlive	887	reboot
com.endless.smoothierecipes	734	reboot
com.traderumors	995	reboot
com.rakuten.room	873	reboot
com.hotels.hotelsmecca	976	reboot
br.com.prevapp03	671	app crash
com.star.mobile.video	1,056	app crash
fr.elol.yams	990	app crash
music.symphony.com.materialmusicv2	1,234	app crash
ru.sports.rfpl	891	app crash
com.discsoft.daemonsync	795	app crash
com.accually.android.accupass	931	app crash
com.directv.navigator	722	app crash
kvp.jjy.MispAndroid320	899	app crash
de.wirfahrlehrer.easytheory	971	app crash
com.ldf.gulli.view	1,103	app restart

Table 18. Threats of Task Unboundedness Vulnerabilities to Popular Commercial Apps

Package name (size)	#Repetitions of the witnessing cycle	Abnormal behavior
com.taobao.taobao (151.0)	66	reboot
com.jingdong.app.mall (92.6)	59	reboot
com.amazon.mShop.android.shopping (73.8)	73	reboot
com.contextlogic.wish (21.9)	63	reboot
com.google.android.youtube (121.3)	54	reboot
com.netflix.ninja (100.6)	76	reboot
com.instagram.android (49.2)	89	reboot
com.zhiliaoapp.musically (167.8)	65	reboot
com.facebook.katana (74.2)	96	reboot

shows that, compared to the random testing, the repeated executions of witnessing cycles indeed dramatically increase the chances of exposing abnormal behaviors.

Finally, we demonstrated the causality between the crashes and task/fragment container unboundedness by analyzing the root causes of the reported crashes.

At first, we used the “logcat” command in ADB to dump the logs of system messages when the witnessing cycles of the apps in Tables 14 through 18 were executed repeatedly. From the logs, we can see that

- when the abnormal behaviors appear, all apps with the app-crash behavior report the error message “SurfaceFlinger: AddClientLayer failed, mNumLayers (4096) >= MAX_LAYERS (4096)”, and
- all apps with the app restart or reboot behavior report the exception “android.os.DeadObjectException.”

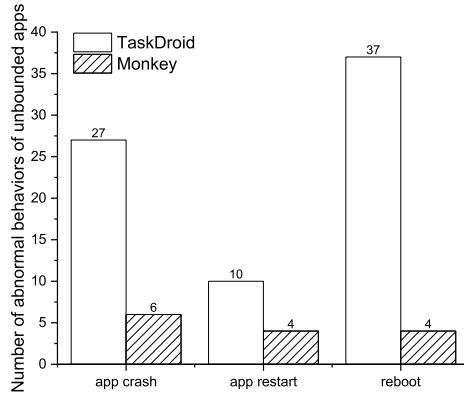


Fig. 14. Number of abnormal behaviors of unbounded apps by TaskDroid and Monkey.

Table 19. Average Memory Usage Per Witnessing-Cycle Execution

Unbound. vulnerability	Abnormal behavior	Avg. memory usage per witnessing-cycle execution
task	app crash	1.2M
	app restart	10.6M
	reboot	12.7M
fragment container	app crash	0.6M
	app restart	3.4M
	reboot	3.9M

We inspected the Android OS documentation, as well as the source code, to understand the meanings of the errors/exceptions:

- From the Android OS source code, we know that the error message “SurfaceFlinger: AddClientLayer failed, mNumLayers (4096) >= MAX_LAYERS (4096)” is produced when the number of layers in an app goes beyond the limit (i.e., 4096), where a layer is a combination of a surface and an instance of the class SurfaceControl.
- However, from the Android OS documentation, we know that “android.os.DeadObjectException” means this: “The object you are calling has died, because its hosting process no longer exists, or there has been a low-level binder error.”

Then we used the “adb shell dumpsys meminfo” command to monitor the memory usage of Android apps when the witnessing cycles are executed repeatedly and discovered that the memory sizes grow monotonically. This indicates that the abnormal behaviors result from the memory issues. In particular, when the memory is used up, either the Android OS kills the process for the app and restarts the app, or even the proper running of the system processes (e.g., the system launcher and system services) is affected and the Android OS may reboot. Finally, to understand why different abnormal behaviors appear when the witnessing cycles of different apps are executed repeatedly, we extracted the information about the growth of the memory usage when the witnessing cycle is executed *once*, which can be found in Table 19. From Table 19, we can see that the average memory usage per witnessing-cycle execution for app crash is much smaller than that for app restart or reboot. As a result, for app crash, because the execution of the witnessing cycle occupies a small amount of memory, the memory is *not* used up before reaching the limit on the number of layers. Therefore, in the end, the error “SurfaceFlinger: AddClientLayer failed” is reported and the app crashes. This (partially) explains why different abnormal behaviors appear.

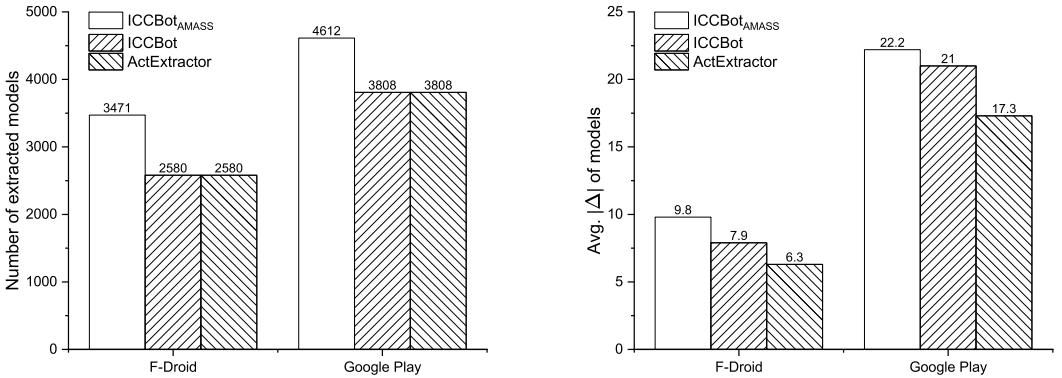


Fig. 15. Number of models extracted by different extractors and the average number of transitions in these models.

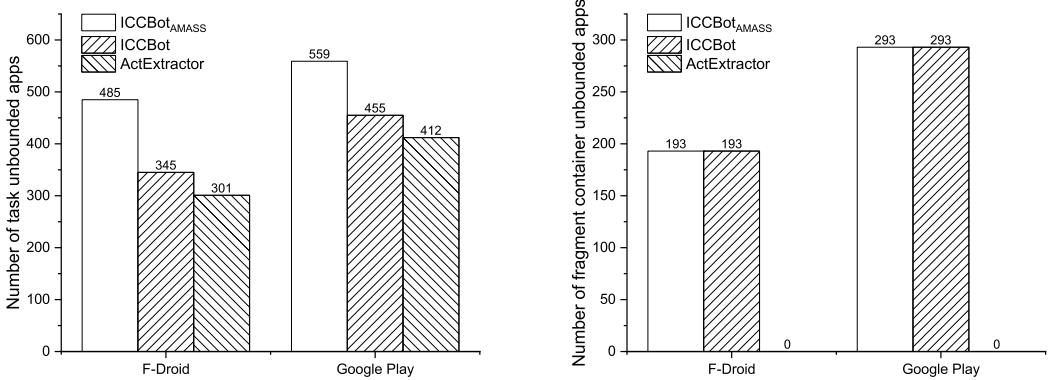
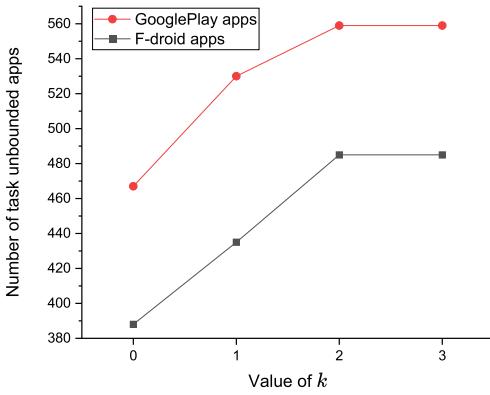
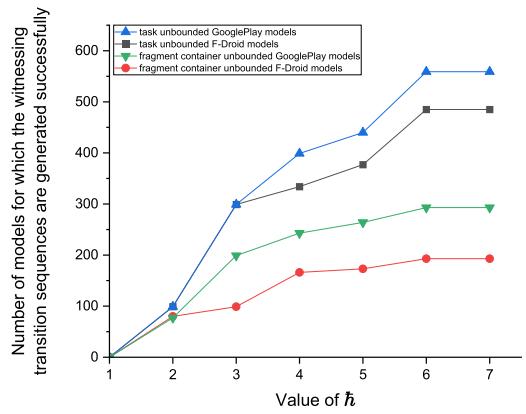


Fig. 16. Number of task/fragment container unbounded apps using different extractors.

9.2.3 Comparison of the Impact of Different Model Extractors. We compared the impact of the following three model extractors on the effectiveness of the task/fragment container unboundedness problems: ICCBot_{AMASS}, ICCBot, and ActExtractor, where ActExtractor is the model extractor from prior work [7], where only activities were considered while fragments were ignored.

We first ran experiments to compare the capabilities of the three extractors to construct AMASS models. The experiment results are shown in Figure 15, which include the numbers of models constructed by these extractors and the average number of transition rules in these models. From Figure 15, we can see that ICCBot_{AMASS} constructs more models than the other two extractors, since it is the only extractor that is able to construct models dynamically from APK files. Moreover, the average number of transition rules in the models constructed by ICCBot_{AMASS} is greater than the other two extractors, which is mainly because the models constructed dynamically by ICCBot_{AMASS} include many more transition rules than those constructed statically, as these apps are the ones that cannot be decompiled and normally are large commercial apps.

To compare the impact of different extractors on TaskDroid, for each app, we ran AMASSAnalyzer on the three models constructed by the three extractors for the app. We summarize the results in Figure 16, where we can see that the number of task unbounded apps is the greatest when ICCBot_{AMASS} is used. This is because ICCBot_{AMASS} extracts more models than the other two extractors since it utilizes the dynamic approach to extract the models from the commercial apps.

Fig. 17. “Small number of tasks” hypothesis: k .Fig. 18. “Small height of stacks” hypothesis: \bar{h} .

that cannot be decompiled. In Table 18, by repeatedly executing the witnessing cycles, we confirm that among these apps whose models are constructed dynamically by ICCBot_{AMASS}, nine apps are indeed task unbounded. Note that ICCBot and ActExtractor are unable to construct models from these apps since their APK files cannot be decompiled successfully by Soot. However, TaskDroid reports the same number of fragment container unbounded apps for ICCBot_{AMASS} and ICCBot. This is due to the fact that although ICCBot_{AMASS} extracts more information about fragments than ICCBot (e.g., the API `addToBackStack(TS)`), the information has no impact on our static analysis algorithm for the fragment container unboundedness problem (see Section 8). Moreover, no fragment unboundedness is reported for the models extracted by ActExtractor, since it only extracts the information for activities.

9.3 Validation of the “Small Number of Tasks” and “Small Height of Stacks” Hypotheses

We validate the “small number of tasks” and “small height of stacks” hypotheses used in Section 8. Recall that for the analysis of task unboundedness in Section 8, we hypothesize that only a small number k of tasks are involved.

We first evaluate the validity of the “small number of tasks” hypothesis for task unboundedness by varying k from 0 to 3 and checking the growth of the number of task unbounded apps detected by TaskDroid. The experimental results are shown in Figure 17. We observe that when k is increased from 1 to 2, the number of task unbounded apps increases only slightly. Moreover, when k is increased from 2 to 3, the number of task unbounded apps remains unchanged. This suggests that to identify those task unbounded apps, a small k suffices (in this case, $k = 2$). This also justifies our choice of k in the static analysis of task unboundedness for AMASS models. This phenomenon is explained by the observation that for a majority of apps, the number of task affinities of their activities is small (or even equal to 1).

Moreover, in Section 8, the height bound $\bar{h} = 6$ of stacks was used to generate the witnessing transition sequences for task unbounded and fragment container unbounded AMASS models. We then carried out experiments to validate this “small height of stacks” hypothesis. The experiments proceed as follows: we first set $\bar{h} = 1$, use nuXmv to generate the witnessing transition sequences for the AMASS models that are identified as “task unbounded” by TaskDroid, and count the number of models for which the witnessing transition sequences can be successfully generated. Then we experiment $\bar{h} = 2\text{--}7$. The results are summarized in Figure 18, where we can see that the number of models for which the witnessing transition sequences can be successfully generated grow when

\hbar is increased from 1 to 6, while remaining unchanged when \hbar is increased from 6 to 7. The results justify the “small height of stacks” hypothesis and our choice of $\hbar = 6$ in Section 8.

10 Conclusion

In this article, we formalized the semantics of the Android multitasking mechanism by a new model, AMASS, which was validated against the actual behaviors of Android systems. Based on the semantics, we provided new static analysis algorithms for detecting potential task unboundedness and fragment container unboundedness vulnerabilities. We implemented a static analysis tool: TaskDroid. The experiments showed that TaskDroid is able to discover the task-unboundedness and fragment container unboundedness vulnerabilities for many open source and commercial Android apps, which can be exploited to produce abnormal behaviors (e.g., black screen, app crash or even device reboot).

The formal semantics of the AMASS model defined in this article is valuable for both the developers of Android apps and the researchers on the analysis and testing of Android apps:

- The developers can read the concise and precise semantics of the AMASS model, instead of the source code of the Android OS, to understand the Android activity-fragment multitasking mechanism.
- Compared to the various models (e.g., ATGs) in the literature, the AMASS model provides refined modeling of the Android activity-fragment multitasking mechanism, and can be utilized to improve the accuracy of the analysis and testing of Android apps.
- The task unboundedness issue identified in this article is a novel type of security threat for Android apps, contributing to the understanding of the security aspect of Android UI design.

For future work, more problems in static analysis can benefit from the formalized multi-tasking semantics. Moreover, we believe that AMASS is a fundamental model in Android UI research that deserves a thorough theoretical investigation.

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Appendices

A Semantics of $A \xrightarrow{\text{finishStart}(\phi)} B$ for $\text{AMASS}_{ACT, LM}$

In the sequel, assuming that M is an $\text{AMASS}_{ACT, LM}$.

Let $\rho = (\Omega_1, \dots, \Omega_n)$ be a configuration with $\Omega_i = (S_i, A_i, \zeta_i)$ for each $i \in [n]$, and $S = [B_1, \dots, B_m]$ be a task. The following additional auxiliary function $\text{RmAct}(\rho, i, j)$ is defined for finishStart :

– let $1 \leq i \leq n$, $S_i = [C_1, \dots, C_l]$ and $1 \leq j \leq l$, then $\text{RmAct}(\rho, i, j) = (\Omega_1, \dots, \Omega_{i-1}, (S'_i, A_i, \zeta_i), \Omega_{i+1}, \dots, \Omega_n)$ if $l > 1$, where $S'_i = [C_1, \dots, C_{j-1}, C_{j+1}, \dots, C_l]$, and $\text{RmAct}(\rho, i, j) = (\Omega_1, \dots, \Omega_{i-1}, \Omega_{i+1}, \dots, \Omega_n)$ otherwise.

We present the semantics of the transition rules $A \xrightarrow{\text{finishStart}(\phi)} B$.

$\text{Lmd}(B) = \text{STD}$

- If $\text{Lmd}(A) \neq \text{SIT}$, then $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$.
- If $\text{Lmd}(A) = \text{SIT}$,
 - if $\text{GetRealTsk}(\rho, B) = S_i$ and $\zeta_i \neq \text{MAIN}$, then $\rho' = \text{RmAct}(\text{MvTsk2Top}(\rho, i), 2, 1)$,
 - if $\text{GetRealTsk}(\rho, B) = S_i$ and $\zeta_i = \text{MAIN}$, or $\text{GetRealTsk}(\rho, B) = *$ $\wedge \text{GetTsk}(\rho, B) = S_i$,
then $\rho' = \text{RmAct}(\text{Push}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - if $\text{GetTsk}(\rho, B) = *$, then $\rho' = \text{RmAct}(\text{NewTsk}(\rho, B, \text{STK}), 2, 1)$.

Lmd(B) = STP

- If $\text{Lmd}(A) \neq \text{SIT}$, then
 - if $A = B$, then $\rho' = \text{RmAct}(\rho, 1, 1)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$.
- If $\text{Lmd}(A) = \text{SIT}$, then
 - if $\text{GetRealTsk}(\rho, B) = S_i$ and $\zeta_i \neq \text{MAIN}$, then $\rho' = \text{RmAct}(\text{MvTsk2Top}(\rho, i), 2, 1)$,
 - if $\text{GetRealTsk}(\rho, B) = S_i$ and $\zeta_i = \text{MAIN}$, or $\text{GetRealTsk}(\rho, B) = *$ and $\text{GetTsk}(\rho, B) = S_i$,
 - * if $\text{TopAct}(S_i) = B$, then $\rho' = \text{RmAct}(\text{MvAct2Top}(\rho, i), 2, 1)$,
 - * otherwise, $\rho' = \text{RmAct}(\text{Push}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - if $\text{GetTsk}(\rho, B) = *$, then $\rho' = \text{RmAct}(\text{NewTsk}(\rho, B, \text{STK}), 2, 1)$.

Lmd(B) = SIT

- If $\text{GetRealTsk}(\rho, B) = S_1$, then $\rho' = \text{RmAct}(\rho, 1, 1)$.
- If $\text{GetRealTsk}(\rho, B) = S_i$ and $i > 1$, then $\rho' = \text{RmAct}(\text{MvTsk2Top}(\rho, i), 2, 1)$.
- If $\text{GetRealTsk}(\rho, B) = *$, then $\rho' = \text{RmAct}(\text{NewTsk}(\rho, B, \text{SIT}), 2, 1)$.

Lmd(B) = STK

- If $\text{GetRealTsk}(\rho, B) = S_i$, or $\text{GetRealTsk}(\rho, B) = *$ and $\text{GetTsk}(\rho, B) = S_i$, then
 - if $i = 1$,
 - * if $B \notin S_i$, then $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$,
 - * if $B \in S_i$,
 - if $\text{TopAct}(\rho) = B$, then $\rho' = \text{RmAct}(\rho, 1, 1)$,
 - if $\text{TopAct}(\rho) \neq B$, then $\rho' = \text{ClrTop}(\rho, B)$,
 - if $i > 1$,
 - * if $B \notin S_i$, then $\rho' = \text{RmAct}(\text{Push}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - * if $B \in S_i$, then $\rho' = \text{RmAct}(\text{ClrTop}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$.
- If $\text{GetTsk}(\rho, B) = *$, then $\rho' = \text{RmAct}(\text{NewTsk}(\rho, B, \text{STK}), 2, 1)$.

B Semantics of $\text{AMASS}_{ACT,IF}$

In the sequel, assuming that \mathcal{M} is an $\text{AMASS}_{ACT,IF}$. First, we need adapt the concept of configurations as follows. A configuration of \mathcal{M} is encoded as a pair (ρ, b) , where $b \in \{\text{NOH}, \neg\text{NOH}\}$ and $\rho = (\Omega_1, \dots, \Omega_n)$ such that for each $i \in [n]$, $\Omega_i = (S_i, A_i, \zeta_i)$, where $S_i \in \text{Act}^*$ is a task, $A_i \in \text{Act}$ is the real activity of S_i , but $\zeta_i \in \{\text{MAIN}, \text{NTK}, \text{NDM}\}$. Intuitively, NTK in ζ_i plays the same role as STK in $\text{AMASS}_{ACT,LM}$, and NDM is added for the intent flag NDM, and moreover, SIT disappears since in $\text{AMASS}_{ACT,IF}$, the launch modes of all activities are assumed to be STD.

Let us define the semantics of \mathcal{M} by a relation $(\rho, b) \xrightarrow[\tau]{\mathcal{M}} (\rho', b')$ with $\tau = A \xrightarrow{\alpha(\phi)} B$. Let us consider the subcase $\phi \models \neg\text{TOH}$ first.

 $\phi \models \neg\text{NTK} \wedge \neg\text{NDM}$

- If $\phi \models \text{CTP}$ and $B \in \text{TopTsk}(\rho)$, then
 - if $\text{TopAct}(\rho) \neq B$, then $\rho' = \text{ClrTop}(\rho, B)$, and moreover,
 - * if $\phi \models \neg\text{STP}$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$,
 - * otherwise, $b' = \neg\text{NOH}$,
 - if $\text{TopAct}(\rho) = B$,
 - * if $\phi \models \text{STP}$, then
 - if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - * if $\phi \models \neg\text{STP}$, then $\rho' = \rho$ and $b' = \text{NOH}$ iff $\phi \models \text{NOH}$.

- If $\phi \models \text{CTP}$ and $B \notin \text{TopTsk}(\rho)$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$.
- If $\phi \models \neg\text{CTP}$, then
 - if $\phi \models \text{RTF}$ and $B \in \text{TopTsk}(\rho)$, then
 - * if $\text{TopAct}(\rho) \neq B$, then $b' = \neg\text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{MvAct2Top}(\rho, B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{MvAct2Top}(\rho, B), 1, 2)$,
 - * if $\text{TopAct}(\rho) = B$,
 - if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - if $\alpha = \text{finishStart}$, then $\rho = \text{RmAct}(\rho, 1, 1)$, and $b' = \neg\text{NOH}$,
 - if $\phi \models \text{RTF}$ and $B \notin \text{TopTsk}(\rho)$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - * if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - * otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$.
 - If $\phi \models \neg\text{RTF}$, then
 - * if $\phi \models \text{STP}$ and $\text{TopAct}(\rho) = B$ or $\phi \models \text{STP} \wedge \text{PIT} \wedge \text{PreAct}(\rho) = B$,
 - if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - * otherwise, $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$.

$\phi \models \text{NDM}$

- If $\phi \models \text{MTK}$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{NewTsk}(\rho, B, \text{NDM})$,
 - otherwise, $\rho' = \text{RmAct}(\text{NewTsk}(\rho, B, \text{NDM}), 2, 1)$.
- If $\phi \models \neg\text{MTK}$, then
 - if $\text{GetRealTsk}(\rho, B) = S_i$, then
 - * if $i \neq 1$, then
 - if $\phi \models \neg\text{CTK}$, then
 - ◊ if $B \notin S_i$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - ◊ otherwise, $b' = \neg\text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{ClrTop}(\text{MvTsk2Top}(\rho, i), B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{ClrTop}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - if $\phi \models \text{CTK}$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - ◊ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{ClrTsk}(\text{MvTsk2Top}(\rho, i), B)$,
 - ◊ otherwise, $\rho' = \text{RmAct}(\text{ClrTsk}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - * otherwise ($i = 1$),
 - if $\phi \models \neg\text{CTK}$, then
 - ◊ if $B \notin S_1$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$,
 - ◊ if $B \in S_1$ and $\text{TopAct}(S_1) \neq B$, then $\rho' = \text{ClrTop}(\rho, B)$ and $b' = \neg\text{NOH}$,
 - ◊ if $B \in S_1$ and $\text{TopAct}(S_1) = B$ (this implies $A = B$), then
 - if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,

- if $\phi \models \text{CTK}$, then $\rho' = \text{ClrTsk}(\rho, B)$, and $b' = \text{NOH}$ iff $\phi \models \text{NOH}$,
- if $\text{GetRealTsk}(\rho, B) = *$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - * if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{NewTsk}(\rho, B, \text{NDM})$,
 - * otherwise, $\rho' = \text{RmAct}(\text{NewTsk}(\rho, B, \text{NDM}), 2, 1)$.

 $\phi \models \text{NTK} \wedge \neg\text{NDM}$

- If $\phi \models \text{MTK}$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{NewTsk}(\rho, B, \text{NTK})$,
 - otherwise, $\rho' = \text{RmAct}(\text{NewTsk}(\rho, B, \text{NTK}), 2, 1)$.
- If $\phi \models \neg\text{MTK}$, then
 - if $\text{GetRealTsk}(\rho, B) = S_i$ or $\text{GetRealTsk}(\rho, B) = *$ $\wedge \text{GetTsk}(\rho, B) = S_i$, then
 - * if $i \neq 1$, then
 - if $\phi \models \text{CTK}$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - ◊ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{ClrTsk}(\text{MvTsk2Top}(\rho, i), B)$,
 - ◊ otherwise, $\rho' = \text{RmAct}(\text{ClrTsk}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - if $\phi \models \neg\text{CTK}$, then
 - ◊ if $\phi \models \text{CTP}$ and $B \in S_i$, then
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{ClrTop}(\text{MvTsk2Top}(\rho, i), B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{ClrTop}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$, and moreover,
 - if $\phi \models \neg\text{STP}$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$,
 - otherwise, $b' = \neg\text{NOH}$,
 - ◊ if $\phi \models \text{CTP}$ and $B \notin S_i$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - ◊ if $\phi \models \neg\text{CTP}$, then
 - if $\phi \models \text{RTF}$ and $B \in S_i$, then $b' = \neg\text{NOH}$, and moreover,
 - ★ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{MvAct2Top}(\text{MvTsk2Top}(\rho, i), B)$,
 - ★ otherwise, $\rho' = \text{RmAct}(\text{MvAct2Top}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - if $\phi \models \text{RTF}$ and $B \notin S_i$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - ★ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
 - ★ otherwise, $\rho' = \text{RmAct}(\text{Push}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - if $\phi \models \neg\text{RTF}$, then
 - ★ if $\text{GetRealTsk}(\rho, B) = S_i$ and $\zeta_i \neq \text{MAIN}$, then $b' = \neg\text{NOH}$, and moreover,
 - ▷ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{MvTsk2Top}(\rho, i)$,
 - ▷ otherwise, $\rho' = \text{RmAct}(\text{MvTsk2Top}(\rho, i), 2, 1)$,
 - ★ otherwise ($\text{GetRealTsk}(\rho, B) = S_i$ and $\zeta_i = \text{MAIN}$ or $\text{GetRealTsk}(\rho, B) = *$ $\wedge \text{GetTsk}(\rho, B) = S_i$),
 - ▷ if $\phi \models \text{STP}$ and $\text{TopAct}(S_i) = B$, then $b' = \neg\text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{MvTsk2Top}(\rho, i)$,
 - otherwise, $\rho' = \text{RmAct}(\text{MvTsk2Top}(\rho, i), 2, 1)$,
 - ▷ otherwise, $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - * otherwise ($i = 1$),
 - if $\phi \models \text{CTK}$, then $\rho' = \text{ClrTsk}(\rho, B)$ and $b' = \text{NOH}$ iff $\phi \models \text{NOH}$,
 - if $\phi \models \neg\text{CTK}$, then
 - ◊ if $\phi \models \text{CTP}$ and $B \in S_1$, then $\rho' = \text{ClrTop}(\rho, B)$, and moreover,
 - if $A \neq B$, then $\rho' = \text{ClrTop}(\rho, B)$, and moreover,

- ★ if $\phi \models \neg\text{STP}$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$,
- ★ otherwise, $b' = \neg\text{NOH}$,
- if $A = B$,
 - ★ if $\phi \models \text{STP}$, then
 - ▷ if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - ▷ if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - ★ if $\phi \models \neg\text{STP}$, then $\rho' = \rho$ and $b' = \text{NOH}$ iff $\phi \models \text{NOH}$,
- if $\phi \models \text{CTP}$ and $B \notin S_1$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$,
- if $\phi \models \neg\text{CTP}$, then
 - if $\phi \models \text{RTF}$ and $B \in S_1$, then
 - ★ if $A \neq B$, then $b' = \neg\text{NOH}$, and moreover,
 - ▷ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{MvAct2Top}(\rho, B)$,
 - ▷ otherwise, $\rho' = \text{RmAct}(\text{MvAct2Top}(\rho, B), 1, 2)$,
 - ★ if $A = B$,
 - ▷ if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - ▷ if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - if $\phi \models \text{RTF}$ and $B \notin S_1$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - ★ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - ★ otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$,
 - if $\phi \models \neg\text{RTF}$, then
 - ★ if $\text{GetRealTsk}(\rho, B) = S_1$ and $\zeta_1 \neq \text{MAIN}$, then
 - ▷ if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - ▷ if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - ★ otherwise ($\text{GetRealTsk}(\rho, B) = S_1$ and $\zeta_i = \text{MAIN}$ or $\text{GetRealTsk}(\rho, B) = *$ ∧ $\text{GetTsk}(\rho, B) = S_1$),
 - ▷ if $\phi \models \text{STP}$ and $A = B$, or $\phi \models \text{STP} \wedge \text{PIT}$ and $\text{PreAct}(\rho) = B$,
 - if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - ▷ otherwise, $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$,
- if $\text{GetTsk}(\rho, B) = *$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - * if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{NewTsk}(\rho, B, \text{NTK})$,
 - * otherwise, $\rho' = \text{RmAct}(\text{NewTsk}(\rho, B, \text{NTK}), 2, 1)$.

Next, let us consider the subcase $\phi \models \text{TOH}$. Let ϕ' be obtained from ϕ by replacing TOH with $\neg\text{TOH}$. Moreover, suppose $(\rho, b) \xrightarrow[\tau']{\mathcal{M}} (\rho', b')$, where $\tau' = A \xrightarrow{\alpha(\phi')} B$ and $\rho' = (\Omega_1, \dots, \Omega_n)$:

- If $\phi \models \text{NTK} \vee \text{NDM}$, then let $\rho'' = (\Omega_1)$ and we have $(\rho, b) \xrightarrow[\tau]{\mathcal{M}} (\rho'', b')$.
- Otherwise, $(\rho, b) \xrightarrow[\tau]{\mathcal{M}} (\rho', b')$.

C Semantics of AMASS Models for Android 13.0

In this section, we present the formal semantics of AMASS models for Android 13.0, where both the activities and fragments are involved.

Fragment Containers, Activities, Tasks, Task Stacks, and Configurations

A *fragment container* is encoded as $V = ((F_1, n_1), \dots, (F_k, n_k)) \in (\text{Frg} \times \mathbb{N})^+$, where n_j is the identifier of an instance of F_j for $j \in [k]$ and k is called the *height* of V .

An *activity* A is encoded as a tuple (v, η, ι) , where $v = (V_1, \dots, V_m)$ is a sequence of fragment containers associated with A , $\eta = (T_1, \dots, T_n) \in C\mathcal{T}^*$ is the transaction stack, and ι is the assignment function that assigns to each variable x in \mathcal{M} an identifier (i.e., a natural number). Note that it is possible that $m = 0$ and/or $n = 0$. For technical convenience, let ι_0 denote the assignment function that assigns each variable x the value 0.

A *task* is represented by its activity stack and is encoded as a word $S = [(A_1, \Theta_1), \dots, (A_n, \Theta_n)]$, where $\Theta_i = (v_i, \eta_i, \iota_i)$ is a tuple of container sequence, transaction stack, and assignment function, and n is called the *height* of S . The activities A_1 and A_n are called as the *top and bottom activity* of S , respectively. By slight abuse of notation, for $L \subseteq \text{Act}^*$, we use $S \in L$ to denote that the word $A_1 \dots A_n$ is in L .

A *configuration* of \mathcal{M} is a pair (ρ, b) , where $\rho = (\Omega_1, \dots, \Omega_n)$, and for each $i \in [n]$, $\Omega_i = (S_i, A_i, \zeta_i)$, S_i is a task, $A_i \in \text{Act}$ is the real activity of S_i , $\zeta_i \in \{\text{MAIN}, \text{NTK}, \text{NDM}, \text{SIT}\}$ represents how the task S_i is launched, and $b \in \{\text{NOH}, \neg\text{NOH}\}$ denotes whether the topmost activity is started with NOH or not.

Let $\text{Conf}_{\mathcal{M}}$ denote the set of configurations of \mathcal{M} . The *initial configuration* of \mathcal{M} is

$$(([(A_0, ((\epsilon, \dots, \epsilon), \epsilon, \iota_0))], A_0, \text{MAIN}), \neg\text{NOH}).$$

Auxiliary Functions and Predicates

To specify the transition relation precisely and concisely, we define the following functions and predicates. Assume a configuration $\rho = (\Omega_1, \dots, \Omega_n)$, and for each $i \in [n]$, $\Omega_i = (S_i, A_i, b_i)$, and a task $S = [(B_1, \Theta_1), \dots, (B_m, \Theta_m)]$:

- $\text{TopAct}(S) = B_1$, $\text{BtmAct}(S) = B_m$, $\text{PreAct}(S) = B_2$ if $m > 1$, and $\text{PreAct}(S) = B_1$ otherwise,
- $\text{TopTsk}(\rho) = S_1$, $\text{TopAct}(\rho) = \text{TopAct}(\text{TopTsk}(\rho))$, $\text{PreAct}(\rho) = \text{PreAct}(\text{TopTsk}(\rho))$.
- $\text{Push}(\rho, B) = (([(B, ((\epsilon, \dots, \epsilon), \epsilon, \iota_0))] \cdot S_1, A_1, \zeta_1), \Omega_2, \dots, \Omega_n)$.
- Let $1 \leq i \leq n$, $S'_i = [(C_1, \Theta'_1), \dots, (C_l, \Theta'_l)]$ and $1 \leq j \leq l$. If $l > 1$, then

$$\text{RmAct}(\rho, i, j) = (\Omega_1, \dots, \Omega_{i-1}, (S'_i, A_i, \zeta_i), \Omega_{i+1}, \dots, \Omega_n),$$

where $S'_i = [(C_1, \Theta'_1), \dots, (C_{j-1}, \Theta'_{j-1}), (C_{j+1}, \Theta'_{j+1}), \dots, (C_l, \Theta'_l)]$. Otherwise,

$$\text{RmAct}(\rho, i, j) = (\Omega_1, \dots, \Omega_{i-1}, \Omega_{i+1}, \dots, \Omega_n).$$

- $\text{MvAct2Top}(\rho, B) = (([(B, \Theta)] \cdot S'_1 \cdot S''_1, A_1, \zeta_1), \Omega_2, \dots, \Omega_n)$, if $S_1 = S'_1 \cdot [(B, \Theta)] \cdot S''_1$ with $S'_1 \in (\text{Act} \setminus \{B\})^*$.
- $\text{ClrTop}(\rho, B) = (([(B, \Theta)] \cdot S''_1, A_1, \zeta_1), \Omega_2, \dots, \Omega_n)$ if $S_1 = S'_1 \cdot [B, \Theta] \cdot S''_1$ with $S'_1 \in (\text{Act} \setminus \{B\})^*$. (Note that the topmost occurrence of B in S_1 is kept in $\text{ClrTop}(\rho, B)$.)
- $\text{ClrTop}^*(\rho, B) = (([(B, ((\epsilon, \dots, \epsilon), \epsilon, \iota_0))] \cdot S''_1, A_1, \zeta_1), \Omega_2, \dots, \Omega_n)$ if $S_1 = S'_1 \cdot [(B, \Theta)] \cdot S''_1$ with $S'_1 \in (\text{Act} \setminus \{B\})^*$. (Note that the topmost occurrence of B in S_1 is replaced by a new B in $\text{ClrTop}^*(\rho, B)$.)
- $\text{ClrTsk}(\rho, B) = (([(B, ((\epsilon, \dots, \epsilon), \epsilon, \iota_0))], A_1, \zeta_1), \Omega_2, \dots, \Omega_n)$.
- $\text{MvTsk2Top}(\rho, i) = (\Omega_i, \Omega_1, \dots, \Omega_{i-1}, \Omega_{i+1}, \dots, \Omega_n)$.
- $\text{NewTsk}(\rho, B, \zeta) = (([(B, ((\epsilon, \dots, \epsilon), \epsilon, \iota_0))], B, \zeta), \Omega_1, \dots, \Omega_n)$.
- $\text{GetRealTsk}(\rho, B) = S_i$ such that $i \in [n]$ is the *minimum* index satisfying $A_i = B$ if such an index i exists; $\text{GetRealTsk}(\rho, B) = *$ otherwise.
- $\text{GetTsk}(\rho, B) = S_i$ such that $i \in [n]$ is the *minimum* index satisfying $\text{Aft}(A_i) = \text{Aft}(B) \wedge \zeta_i \in \{\text{NTK}, \text{MAIN}\}$, if such an index i exists; $\text{GetTsk}(\rho, B) = *$ otherwise.

For a container $V = ((F_1, n_1), \dots, (F_m, n_m))$, define $\text{TopFrg}(V) = F_1$.

Let $\Theta = (v, \eta, \iota)$ be the encoding of an activity A , where $\text{Ctn}(A) = (i_1, \dots, i_k)$ ($k > 0$), $v = (V_1, \dots, V_k)$ is the container sequence, and $\eta = (T_1, \dots, T_l)$ ($l \geq 0$) is the transaction stack. Moreover, let $F \in \text{Frg}$, $j \in [k]$, and x be a variable. We define the following functions:

- $\text{TopFrg}(v) = \{\text{TopFrg}(V_i) \mid i \in [k], V_i \neq \epsilon\}$ returns the set of topmost fragments of containers in v .
- $\text{ADD}(F, i_j, x)(v, \iota) = (v', \iota')$, where $v' = (V_1, \dots, V_{j-1}, (F, n) \cdot V_j, V_{j+1}, \dots, V_k)$, $\iota' = \iota[n/x]$, and n is the *minimum* identifier not occurring in v or ι . Intuitively, $\text{ADD}(F, i_j, x)(v, \iota)$ updates (v, ι) by choosing a fresh identifier n , pushing (F, n) into the container i_j , and storing n into x .
- $\text{REP}(F, i_j, x)(v, \iota) = (v', \iota')$, where $v' = (V_1, \dots, V_{j-1}, (F, n), V_{j+1}, \dots, V_k)$, $\iota' = \iota[n/x]$, and n is the *minimum* identifier not occurring in v or ι . Intuitively, $\text{REP}(F, i_j, x)(v, \iota)$ updates v by replacing the content of container i_j with (F, n) , and storing n into x .
- Suppose $V_j = ((F_1, n_1), \dots, (F_m, n_m))$, then $\text{REM}(F, i_j, x)(v, \iota) = (v', \iota')$, where
 - $v' = (V_1, \dots, V_{j-1}, \tilde{V}, V_{j+1}, \dots, V_k)$ such that
 - * $\tilde{V} = V_j$, if $\iota(x) \neq n_{j'}$ for every $j' \in [m]$, and
 - * $\tilde{V} = ((F_1, n_1), \dots, (F_{l-1}, n_{l-1}), (F_{l+1}, n_{l+1}), \dots, (F_m, n_m))$, if $\iota(x) = n_l$,
 - moreover, $\iota' = \iota$.
 Intuitively, the action $\text{REM}(F, i_j, x)(v)$ updates v by removing the instance of F of the identifier $\iota(x)$ from container i_j and does not change ι .
- Furthermore, the functions $\text{ADD}(F, i_j, n)(v, \iota)$, $\text{REP}(F, i_j, n)(v, \iota)$, $\text{REM}(F, i_j, n)(v, \iota)$ for concretized actions can be defined similarly (except that ι is unchanged).

For a transaction $T = (\beta_1(F_1, j_1, x_1), \dots, \beta_r(F_r, j_r, x_r))$ such that $\beta_s \in \{\text{ADD}, \text{REM}, \text{REP}\}$ and $F_s \in \text{Frg}$ for every $s \in [r]$, $\text{UpdateCtns}_T(v, \iota) = (v_r, \iota_r)$, where $(v_0, \iota_0) = (v, \iota)$, and for every $s \in [r]$, $(v_s, \iota_s) = \beta_s(F_s, j_s, x_s)(v_{s-1}, \iota_{s-1})$ —that is, UpdateCtns_T updates the containers and the assignment function by applying the actions in T . Furthermore, $\text{UpdateCtns}_T(v, \iota)$ can be defined similarly for concretized transactions T .

We also introduce a function that concretize the actions REP by utilizing the containers in v . Suppose $F \in \text{Frg}$, $j \in [k]$, x is a variable, and $V_j = ((F_1, n_1), \dots, (F_m, n_m))$. Let n be the minimum identifier not occurring in v or ι . Then

$$\text{Concretize}_{v, \iota}(\text{REP}(F, i_j, x)) = \text{REM}(F_1, i_j, n_1), \dots, \text{REM}(F_m, i_j, n_m), \text{ADD}(F, i_j, n).$$

Moreover, let

$$\text{Concretize}_{v, \iota}(\text{ADD}(F, i_j, x)) = \text{ADD}(F, i_j, n) \text{ and } \text{Concretize}_{v, \iota}(\text{REM}(F, i_j, x)) = \text{REM}(F, i_j, \iota(x))$$

by convention.

Let $T = (\beta_1(F_1, j_1, x_1), \dots, \beta_k(F_r, j_r, x_r))$ be a transaction such that $\beta_s \in \{\text{ADD}, \text{REM}, \text{REP}\}$, and $F_s \in \text{Frg}$ for every $s \in [r]$. We define $\text{Concretize}_{v, \iota}(T)$ as the concatenation of the concretized action sequences $\text{Concretize}_{v_0, \iota_0}(\beta_1(F_1, j_1, x_1)), \dots, \text{Concretize}_{v_{s-1}, \iota_{s-1}}(\beta_s(F_s, j_s, x_s))$, where $(v_0, \iota_0) = (v, \iota)$, and for each $s \in [r]$, $(v_s, \iota_s) = \beta_s(F_s, j_s, x_s)(v_{s-1}, \iota_{s-1})$.

Finally, we define functions $\beta^{-1}(F, i_j, n)$ for $\beta(F, i_j, n) \in C\mathcal{T}$ as follows:

- $\text{ADD}^{-1}(F, i_j, n)(v, \iota) = \text{REM}(F, i_j, n)(v, \iota)$,
- $\text{REM}^{-1}(F, i_j, n)(v, \iota) = \text{ADD}(F, i_j, n)(v, \iota)$.

Intuitively, $\text{ADD}(F, i_j, n)$ and $\text{REM}(F, i_j, n)$ are dual actions. Moreover, for a concretized transaction

$$T = (\beta_1(F_1, j_1, n_1), \dots, \beta_r(F_r, j_r, n_r))$$

such that $\beta_s \in \{\text{ADD}, \text{REM}, \text{REP}\}$, $F_s \in \text{Frg}$ for every $s \in [r]$, and $n \in \mathbb{N}$, we define T^{-1} as

$$(\beta_r^{-1}(F_r, j_r, n_r), \dots, \beta_1^{-1}(F_1, j_1, n_1)).$$

Transition Relation

Let us define the semantics of \mathcal{M} by a relation $(\rho, b) \xrightarrow[\tau]{\mathcal{M}} (\rho', b')$. Let (ρ, b) be the current configuration, where $\rho = ((S_1, A_1, \zeta_1), \dots, (S_n, A_n, \zeta_n))$, for some $n \geq 1$. Let $\text{Top}(\rho) = (A, \Theta)$, $\text{Ctn}(A) = (i_1, \dots, i_k)$, $\Theta = (v, \eta)$, $v = (V_1, \dots, V_k)$, and $\eta = (T_1, \dots, T_l)$. Suppose $S_1 = [(B_1, \Theta_1), \dots, (B_r, \Theta_r)]$ (where $B_1 = A$ and $\Theta_1 = \Theta$).

C.1 Case $\tau = A \xrightarrow{\alpha(\phi)} B$

We first assume that $\phi \models \neg\text{TOH}$. We will consider $\phi \models \text{TOH}$ in the end.

$\boxed{\text{Lmd}(B) = \text{STD}}$

- If $\phi \models \neg\text{NTK} \wedge \neg\text{NDM}$ and $\text{Lmd}(A) \neq \text{SIT}$, then
 - if $\phi \models \text{CTP}$ and $B \in \text{TopTsk}(\rho)$, then
 - * if $\text{TopAct}(\rho) \neq B$,
 - if $\phi \models \neg\text{STP}$, $\rho' = \text{ClrTop}^*(\rho, B)$ and $b' = \text{NOH}$ iff $\phi \models \text{NOH}$,
 - otherwise, $\rho' = \text{ClrTop}(\rho, B)$ $b' = \neg\text{NOH}$,
 - * if $\text{TopAct}(\rho) = B$,
 - if $\phi \models \neg\text{STP}$, then $\rho' = \text{ClrTop}^*(\rho, B)$ and $b' = \text{NOH}$ iff $\phi \models \text{NOH}$,
 - otherwise,
 - ◊ if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - ◊ if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - if $\phi \models \text{CTP}$ and $B \notin \text{TopTsk}(\rho)$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - * if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - * otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$,
 - if $\phi \models \neg\text{CTP}$, then
 - * if $\phi \models \text{RTF}$ and $B \in \text{TopTsk}(\rho)$, then
 - if $\text{TopAct}(\rho) \neq B$, then $b' = \neg\text{NOH}$, and moreover,
 - ◊ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{MvAct2Top}(\rho, B)$,
 - ◊ otherwise, $\rho' = \text{RmAct}(\text{MvAct2Top}(\rho, B), 1, 2)$,
 - if $\text{TopAct}(\rho) = B$,
 - ◊ if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - ◊ if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - * if $\phi \models \text{RTF}$ and $B \notin \text{TopTsk}(\rho)$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$.
 - * if $\phi \models \neg\text{RTF}$, then
 - if $\phi \models \text{STP}$ and $\text{TopAct}(\rho) = B$ or $\phi \models \text{STP} \wedge \text{PIT}$ and $\text{PreAct}(\rho) = B$, then
 - ◊ if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - ◊ if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - otherwise, $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - ◊ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - ◊ otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$.
 - If $\phi \models \text{NDM} \wedge \text{MTK}$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{NewTsk}(\rho, B, \text{NDM})$,
 - otherwise, $\rho' = \text{RmAct}(\text{NewTsk}(\rho, B, \text{NDM}), 2, 1)$.

- If $\phi \models \text{NDM} \wedge \neg\text{MTK}$, then
 - if $\text{GetRealTsk}(\rho, B) = S_i$, then
 - * if $i \neq 1$, then
 - if $\phi \models \neg\text{CTK}$, then
 - ◊ if $B \notin S_i$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - ◊ otherwise, $b' = \neg\text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{ClrTop}(\text{MvTsk2Top}(\rho, i), B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{ClrTop}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - if $\phi \models \text{CTK}$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, moreover,
 - ◊ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{ClrTsk}(\text{MvTsk2Top}(\rho, i), B)$,
 - ◊ otherwise, $\rho' = \text{RmAct}(\text{ClrTsk}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - * otherwise ($i = 1$),
 - if $\phi \models \neg\text{CTK}$, then
 - ◊ if $B \notin S_1$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$,
 - ◊ if $B \in S_1$ and $\text{TopAct}(S_1) \neq B$, then $\rho' = \text{ClrTop}(\rho, B)$ and $b' = \neg\text{NOH}$,
 - ◊ if $B \in S_1$ and $\text{TopAct}(S_1) = B$ (this implies $A = B$),
 - if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - if $\phi \models \text{CTK}$, then $\rho' = \text{ClrTsk}(\rho, B)$, and $b' = \text{NOH}$ iff $\phi \models \text{NOH}$,
 - if $\text{GetRealTsk}(\rho, B) = *$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - * if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{NewTsk}(\rho, B, \text{NDM})$,
 - * otherwise, $\rho' = \text{RmAct}(\text{NewTsk}(\rho, B, \text{NDM}), 2, 1)$.
- If $\phi \models \text{NTK} \wedge \neg\text{NDM} \wedge \text{MTK}$, or $\text{Lmd}(A) = \text{SIT}$ and $\phi \models \neg\text{NDM} \wedge \text{MTK}$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{NewTsk}(\rho, B, \text{NTK})$,
 - otherwise, $\rho' = \text{RmAct}(\text{NewTsk}(\rho, B, \text{NTK}), 2, 1)$.
- If $\phi \models \text{NTK} \wedge \neg\text{NDM} \wedge \neg\text{MTK}$, or $\text{Lmd}(A) = \text{SIT}$ and $\phi \models \neg\text{NDM} \wedge \neg\text{MTK}$, then
 - if $\text{GetRealTsk}(\rho, B) = S_i$ or $\text{GetRealTsk}(\rho, B) = *$ and $\text{GetTsk}(\rho, B) = S_i$, then
 - * if $i \neq 1$, then
 - if $\phi \models \text{CTK}$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - ◊ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{ClrTsk}(\text{MvTsk2Top}(\rho, i), B)$,
 - ◊ otherwise, $\rho' = \text{RmAct}(\text{ClrTsk}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - if $\phi \models \neg\text{CTK}$, then
 - ◊ if $\phi \models \text{CTP}$ and $B \in S_i$, then
 - if $\text{STP} \in \phi$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - ★ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{ClrTop}(\text{MvTsk2Top}(\rho, i), B)$,
 - ★ otherwise, $\rho' = \text{RmAct}(\text{ClrTop}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - otherwise, $b' = \neg\text{NOH}$, and moreover,
 - ★ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{ClrTop}^*(\text{MvTsk2Top}(\rho, i), B)$,
 - ★ otherwise, $\rho' = \text{RmAct}(\text{ClrTop}^*(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - ◊ if $\phi \models \text{CTP}$ and $B \notin S_i$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - ◊ if $\phi \models \neg\text{CTP}$, then

- if $\phi \models \text{RTF}$ and $B \in S_i$, then $b' = \neg\text{NOH}$, and moreover,
 - ★ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{MvAct2Top}(\text{MvTsk2Top}(\rho, i), B)$,
 - ★ otherwise, $\rho' = \text{RmAct}(\text{MvAct2Top}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
- if $\phi \models \text{RTF}$ and $B \notin S_i$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - ★ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
 - ★ otherwise, $\rho' = \text{RmAct}(\text{Push}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
- if $\phi \models \neg\text{RTF}$, then
 - ★ if $\text{GetRealTsk}(\rho, B) = S_i$ and $\zeta_i \neq \text{MAIN}$, then $b' = \neg\text{NOH}$, and moreover,
 - ▷ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{MvTsk2Top}(\rho, i)$,
 - ▷ otherwise, $\rho' = \text{RmAct}(\text{MvTsk2Top}(\rho, i), 2, 1)$,
 - ★ otherwise ($\text{GetRealTsk}(\rho, B) = S_i$ and $\zeta_i = \text{MAIN}$ or $\text{GetRealTsk}(\rho, B) = *$ \wedge $\text{GetTsk}(\rho, B) = S_i$),
 - ▷ if $\phi \models \text{STP}$ and $\text{TopAct}(S_i) = B$, then $b' = \neg\text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{MvTsk2Top}(\rho, i)$,
 - otherwise, $\rho' = \text{RmAct}(\text{MvTsk2Top}(\rho, i), 2, 1)$,
 - ▷ otherwise, $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
- * otherwise ($i = 1$),
 - if $\phi \models \text{CTK}$, then $\rho' = \text{ClrTsk}(\rho, B)$ and $b' = \text{NOH}$ iff $\phi \models \text{NOH}$,
 - if $\phi \models \neg\text{CTK}$, then
 - ◊ if $\phi \models \text{CTP}$ and $B \in S_1$, then $\rho' = \text{ClrTop}(\rho, B)$, and moreover,
 - if $A \neq B$,
 - ★ if $\phi \models \neg\text{STP}$, then $\rho' = \text{ClrTop}^*(\rho, B)$ and $b' = \text{NOH}$ iff $\phi \models \text{NOH}$,
 - ★ otherwise, $\rho' = \text{ClrTop}(\rho, B)$ and $b' = \neg\text{NOH}$,
 - if $A = B$,
 - ★ if $\phi \models \neg\text{STP}$, then $\rho' = \text{ClrTop}^*(\rho, B)$ and $b' = \text{NOH}$ iff $\phi \models \text{NOH}$,
 - ★ otherwise,
 - ▷ if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - ▷ if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - ◊ if $\phi \models \text{CTP}$ and $B \notin S_1$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$,
 - ◊ if $\phi \models \neg\text{CTP}$, then
 - if $\phi \models \text{RTF}$ and $B \in S_1$, then
 - ★ if $A \neq B$, then $b' = \neg\text{NOH}$, and moreover,
 - ▷ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{MvAct2Top}(\rho, B)$,
 - ▷ otherwise, $\rho' = \text{RmAct}(\text{MvAct2Top}(\rho, B), 1, 2)$,
 - ★ if $A = B$,
 - ▷ if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - ▷ if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - if $\phi \models \text{RTF}$ and $B \notin S_1$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - ★ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - ★ otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$,
 - if $\phi \models \neg\text{RTF}$, then
 - ★ if $\text{GetRealTsk}(\rho, B) = S_1$ and $\zeta_1 \neq \text{MAIN}$,
 - ▷ if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - ▷ if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,

- ★ otherwise ($\text{GetRealTsk}(\rho, B) = S_1$ and $\zeta_i = \text{MAIN}$ or $\text{GetRealTsk}(\rho, B) = *$ \wedge $\text{GetTsk}(\rho, B) = S_1$),
 - ▷ if $\phi \models \text{STP}$ and $A = B$, or $\phi \models \text{STP} \wedge \text{PIT}$ and $\text{PreAct}(\rho) = B$,
 - if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - ▷ otherwise, $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$,
- if $\text{GetTsk}(\rho, B) = *$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - * if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{NewTsk}(\rho, B, \text{NTK})$,
 - * otherwise, $\rho' = \text{RmAct}(\text{NewTsk}(\rho, B, \text{NTK}), 2, 1)$.

Lmd(B) = STP

- If $\phi \models \neg\text{NTK} \wedge \neg\text{NDM}$ and $\text{Lmd}(A) \neq \text{SIT}$, then
 - if $\phi \models \text{CTP}$ and $B \in \text{TopTsk}(\rho)$, then
 - * if $\text{TopAct}(\rho) \neq B$, then $\rho' = \text{ClrTop}(\rho, B)$ and $b' = \neg\text{NOH}$,
 - * if $\text{TopAct}(\rho) = B$,
 - if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - if $\phi \models \text{CTP}$ and $B \notin \text{TopTsk}(\rho)$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - * if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - * otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$,
 - if $\phi \models \neg\text{CTP}$, then
 - * if $\phi \models \text{RTF}$ and $B \in \text{TopTsk}(\rho)$, then
 - if $\text{TopAct}(\rho) \neq B$, then $b' = \neg\text{NOH}$, and moreover,
 - ◊ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{MvAct2Top}(\rho, B)$,
 - ◊ otherwise, $\rho' = \text{RmAct}(\text{MvAct2Top}(\rho, B), 1, 2)$,
 - if $\text{TopAct}(\rho) = B$,
 - ◊ if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - ◊ if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - * if $\phi \models \text{RTF}$ and $B \notin \text{TopTsk}(\rho)$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$,
 - * if $\phi \models \neg\text{RTF}$, then
 - if $\text{TopAct}(\rho) = B$ or $\phi \models \text{PIT}$ and $\text{PreAct}(\rho) = B$,
 - ◊ if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - ◊ if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - otherwise, $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - ◊ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - ◊ otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$.
 - If $\phi \models \text{NDM} \wedge \text{MTK}$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{NewTsk}(\rho, B, \text{NDM})$,
 - otherwise, $\rho' = \text{RmAct}(\text{NewTsk}(\rho, B, \text{NDM}), 2, 1)$.
 - If $\phi \models \text{NDM} \wedge \neg\text{MTK}$, then
 - if $\text{GetRealTsk}(\rho, B) = S_i$, then
 - * if $i \neq 1$, then
 - if $\phi \models \neg\text{CTK}$, then
 - ◊ if $B \notin S_i$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,

- if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
- otherwise, $\rho' = \text{RmAct}(\text{Push}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
- ◊ otherwise, $b' = \neg\text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{ClrTop}(\text{MvTsk2Top}(\rho, i), B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{ClrTop}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
- if $\phi \models \text{CTK}$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - ◊ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{ClrTsk}(\text{MvTsk2Top}(\rho, i), B)$,
 - ◊ otherwise, $\rho' = \text{RmAct}(\text{ClrTsk}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
- * otherwise ($i = 1$),
 - if $\phi \models \neg\text{CTK}$, then
 - ◊ if $B \notin S_1$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$,
 - ◊ if $B \in S_1$ and $\text{TopAct}(S_1) \neq B$, then $\rho' = \text{ClrTop}(\rho, B)$ and $b' = \neg\text{NOH}$,
 - ◊ if $B \in S_1$ and $\text{TopAct}(S_1) = B$ (this implies $A = B$), then
 - if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = 0$,
 - if $\phi \models \text{CTK}$, then $\rho' = \text{ClrTsk}(\rho, B)$, and $b' = \text{NOH}$ iff $\phi \models \text{NOH}$,
- if $\text{GetRealTsk}(\rho, B) = *$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - * if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{NewTsk}(\rho, B, \text{NDM})$,
 - * otherwise, $\rho' = \text{RmAct}(\text{NewTsk}(\rho, B, \text{NDM}), 2, 1)$.
- If $\phi \models \text{NTK} \wedge \neg\text{NDM} \wedge \text{MTK}$, or $\text{Lmd}(A) = \text{SIT}$ and $\phi \models \neg\text{NDM} \wedge \text{MTK}$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{NewTsk}(\rho, B, \text{NTK})$,
 - otherwise, $\rho' = \text{RmAct}(\text{NewTsk}(\rho, B, \text{NTK}), 2, 1)$.
- If $\phi \models \text{NTK} \wedge \neg\text{NDM} \wedge \neg\text{MTK}$, or $\text{Lmd}(A) = \text{SIT}$ and $\phi \models \neg\text{NDM} \wedge \neg\text{MTK}$, then
 - if $\text{GetRealTsk}(\rho, B) = S_i$ or $\text{GetRealTsk}(\rho, B) = * \wedge \text{GetTsk}(\rho, B) = S_i$, then
 - * if $i \neq 1$, then
 - if $\phi \models \text{CTK}$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - ◊ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{ClrTsk}(\text{MvTsk2Top}(\rho, i), B)$,
 - ◊ otherwise, $\rho' = \text{RmAct}(\text{ClrTsk}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - if $\phi \models \neg\text{CTK}$, then
 - ◊ if $\phi \models \text{CTP}$ and $B \in S_i$, then $b' = \neg\text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{ClrTop}(\text{MvTsk2Top}(\rho, i), B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{ClrTop}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - ◊ if $\phi \models \text{CTP}$ and $B \notin S_i$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - ◊ if $\phi \models \neg\text{CTP}$, then
 - if $\phi \models \text{RTF}$ and $B \in S_i$, then $b' = \neg\text{NOH}$, and moreover,
 - ★ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{MvAct2Top}(\text{MvTsk2Top}(\rho, i), B)$,
 - ★ otherwise, $\rho' = \text{RmAct}(\text{MvAct2Top}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - if $\phi \models \text{RTF}$ and $B \notin S_i$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - ★ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
 - ★ otherwise, $\rho' = \text{RmAct}(\text{Push}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - if $\phi \models \neg\text{RTF}$, then
 - ★ if $\text{GetRealTsk}(\rho, B) = S_i$ and $\zeta_i \neq \text{MAIN}$, then $b' = \neg\text{NOH}$, and moreover,
 - ▷ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{MvTsk2Top}(\rho, i)$,

- ▷ otherwise, $\rho' = \text{RmAct}(\text{MvTsk2Top}(\rho, i), 2, 1)$,
- ★ otherwise ($\text{GetRealTsk}(\rho, B) = S_i$ and $\zeta_i = \text{MAIN}$ or $\text{GetRealTsk}(\rho, B) = *$ \wedge $\text{GetTsk}(\rho, B) = S_i$),
 - ▷ if $\text{TopAct}(S_i) = B$, then $b' = \neg\text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{MvTsk2Top}(\rho, i)$,
 - otherwise, $\rho' = \text{RmAct}(\text{MvTsk2Top}(\rho, i), 2, 1)$,
 - ▷ otherwise, $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
- * otherwise ($i = 1$),
 - if $\phi \models \text{CTK}$, then $\rho' = \text{ClrTsk}(\rho, B)$ and $b' = \text{NOH}$ iff $\phi \models \text{NOH}$,
 - if $\phi \models \neg\text{CTK}$, then
 - ◊ if $\phi \models \text{CTP}$ and $B \in S_1$, then $\rho' = \text{ClrTop}(\rho, B)$, and moreover,
 - if $A \neq B$, then $\rho' = \text{ClrTop}(\rho, B)$ and $b' = \neg\text{NOH}$,
 - if $A = B$,
 - ★ if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - ★ if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - ◊ if $\phi \models \text{CTP}$ and $B \notin S_1$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$,
 - ◊ if $\phi \models \neg\text{CTP}$, then
 - if $\phi \models \text{RTF}$ and $B \in S_1$, then
 - ★ if $A \neq B$, then $b' = \neg\text{NOH}$, and moreover,
 - ▷ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{MvAct2Top}(\rho, B)$,
 - ▷ otherwise, $\rho' = \text{RmAct}(\text{MvAct2Top}(\rho, B), 1, 2)$,
 - ★ if $A = B$,
 - ▷ if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - ▷ if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - if $\phi \models \text{RTF}$ and $B \notin S_1$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - ★ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - ★ otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$,
 - if $\phi \models \neg\text{RTF}$, then
 - ★ if $\text{GetRealTsk}(\rho, B) = S_1$ and $\zeta_1 \neq \text{MAIN}$,
 - ▷ if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - ▷ if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - ★ otherwise ($\text{GetRealTsk}(\rho, B) = S_1$ and $\zeta_i = \text{MAIN}$ or $\text{GetRealTsk}(\rho, B) = *$ \wedge $\text{GetTsk}(\rho, B) = S_1$),
 - ▷ if $A = B$, or $\phi \models \text{PIT}$ and $\text{PreAct}(\rho) = B$,
 - if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - ▷ otherwise, $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$,
 - if $\text{GetTsk}(\rho, B) = *$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - * if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{NewTsk}(\rho, B, \text{NTK})$,
 - * otherwise, $\rho' = \text{RmAct}(\text{NewTsk}(\rho, B, \text{NTK}), 2, 1)$.

$\text{Lmd}(B) = \text{SIT}$

- If $\text{GetRealTsk}(\rho, B) = S_i$, then
 - if $i \neq 1$, then
 - * if $\phi \models \text{CTK}$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{ClrTsk}(\text{MvTsk2Top}(\rho, i), B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{ClrTsk}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - * if $\phi \models \neg\text{CTK}$, then $b' = \neg\text{NOH}$,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{MvTsk2Top}(\rho, i)$,
 - otherwise, $\rho' = \text{RmAct}(\text{MvTsk2Top}(\rho, i), 2, 1)$,
 - otherwise ($i = 1$),
 - * if $\phi \models \text{CTK}$, then $\rho' = \text{ClrTsk}(\rho, B)$ and $b' = \text{NOH}$ iff $\phi \models \text{NOH}$,
 - * if $\phi \models \neg\text{CTK}$,
 - if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
- If $\text{GetRealTsk}(\rho, B) = *$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{NewTsk}(\rho, B, \text{SIT})$,
 - otherwise, $\rho' = \text{RmAct}(\text{NewTsk}(\rho, B, \text{SIT}), 2, 1)$.

$\text{Lmd}(B) = \text{STK}$

- If $\text{GetRealTsk}(\rho, B) = S_i$, or $\text{GetRealTsk}(\rho, B) = *$ $\wedge \text{GetTsk}(\rho, B) = S_i$, then
 - if $i \neq 1$, then
 - * if $\phi \models \text{CTK}$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{ClrTsk}(\text{MvTsk2Top}(\rho, i), B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{ClrTsk}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - * if $\phi \models \neg\text{CTK}$ and $B \notin S_i$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - * if $\phi \models \neg\text{CTK}$ and $B \in S_i$, then $b' = \neg\text{NOH}$, and moreover
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{ClrTop}(\text{MvTsk2Top}(\rho, i), B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{ClrTop}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - otherwise ($i = 1$),
 - * if $\phi \models \text{CTK}$, then $\rho' = \text{ClrTsk}(\rho, B)$ and $b' = \text{NOH}$ iff $\phi \models \text{NOH}$,
 - * if $\phi \models \neg\text{CTK}$ and $B \notin S_1$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$,
 - * if $\phi \models \neg\text{CTK}$ and $B \in S_1$,
 - if $A \neq B$, then $\rho' = \text{ClrTop}(\rho, B)$ and $b' = \neg\text{NOH}$,
 - if $A = B$,
 - ◊ if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - ◊ if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
- If $\text{GetTsk}(\rho, B) = *$, then $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{NewTsk}(\rho, B, \text{NTK})$,
 - otherwise, $\rho' = \text{RmAct}(\text{NewTsk}(\rho, B, \text{NTK}), 2, 1)$.

At last, let us consider the situation $\phi \models \text{TOH}$. Let ϕ' be obtained from ϕ by replacing TOH with $\neg\text{TOH}$. Moreover, suppose $(\rho, b) \xrightarrow[\alpha(\phi')]{\mathcal{M}} (\rho', b')$, where $\rho' = (\Omega_1, \dots, \Omega_n)$:

- If $\phi \models \text{NTK} \vee \text{NDM}$ or $\text{Lmd}(A) = \text{SIT}$ or $\text{Lmd}(B) = \text{SIT}$ or $\text{Lmd}(B) = \text{STK}$, then let $\rho'' = (\Omega_1)$ and we have $(\rho, b) \xrightarrow[\alpha(\phi)]{\mathcal{M}} (\rho'', b')$.
- Otherwise, $(\rho, b) \xrightarrow[\text{start}(\phi)]{\mathcal{M}} (\rho', b')$.

C.2 Case $\tau = A \xrightarrow{\text{TS}} (\beta_1(F_1, i_1, x_1), \dots, \beta_k(F_k, i_k, x_k))$

In this case, let $T = (\beta_1(F_1, i_1, x_1), \dots, \beta_k(F_k, i_k, x_k))$. Then we have $(\rho, b) \xrightarrow[\tau]{\mathcal{M}} (\rho', b)$, where

$$\rho' = ((S'_1, A_1, \zeta_1), (S_2, A_2, \zeta_2), \dots, (S_n, A_n, \zeta_n))$$

is obtained from ρ by applying all the actions in T to the containers and assignment function in $\Theta = \Theta_1$ (recall that $\text{Top}(S_1) = (A, \Theta)$), specifically, $S'_1 = [(B_1, \Theta'_1), (B_2, \Theta_2), \dots, (B_r, \Theta_r)]$, where $\Theta'_1 = (v', \eta', \iota')$ such that $(v', \iota') = \text{UpdateCtns}_T(v, \iota)$ and $\eta' = \text{Concretize}_{v, \iota}(T) \cdot \eta$.

C.3 Case $\tau = A \xrightarrow{\text{NTS}} (\beta_1(F_1, i_1, x_1), \dots, \beta_k(F_k, i_k, x_k))$

In this case, let $T = (\beta_1(F_1, i_1, x_1), \dots, \beta_k(F_k, i_k, x_k))$. Then we have $(\rho, b) \xrightarrow[\tau]{\mathcal{M}} (\rho', b)$, where

$$\rho' = ((S'_1, A_1, \zeta_1), (S_2, A_2, \zeta_2), \dots, (S_n, A_n, \zeta_n))$$

such that

$$S'_1 = [(B_1, \Theta'_1), (B_2, \Theta_2), \dots, (B_r, \Theta_r)],$$

where $\Theta'_1 = (v', \eta', \iota')$, and $(v', \iota') = \text{UpdateCtns}_T(v, \iota)$. Note that in this case, the concretization of T is not stored into the transaction stack.

C.4 Case $\tau = \text{back}$

In this case, we distinguish two subcases: $\eta = \epsilon$ or $\eta \neq \epsilon$.

Case $\eta = \epsilon$

In this case, if S_1 contains exactly one activity (i.e., A), then S_1 disappears after the back action—that is, $(\rho, b) \xrightarrow[\tau]{\mathcal{M}} (\rho', \neg \text{NOH})$, where $\rho' = ((S_2, A_2, \zeta_2), \dots, (S_n, A_n, \zeta_n))$. However, if S_1 contains at least two activities, then $(\rho, b) \xrightarrow[\tau]{\mathcal{M}} (\rho', \neg \text{NOH})$, where $\rho' = ((S'_1, A_1, \zeta_1), (S_2, A_2, \zeta_2), \dots, (S_n, A_n, \zeta_n))$ and S'_1 is obtained from S_1 by removing the top activity A from S_1 .

Case $\eta \neq \epsilon$

In this case, $(\rho, b) \xrightarrow[\tau]{\mathcal{M}} (\rho', b)$, where

$$\rho' = ((S'_1, A_1, \zeta_1), (S_2, A_2, \zeta_2), \dots, (S_n, A_n, \zeta_n))$$

such that

$$S'_1 = [(B_1, \Theta'_1), (B_2, \Theta_2), \dots, (B_r, \Theta_r)],$$

where $\Theta'_1 = (v', \eta', \iota')$, $(v', \iota') = \text{UpdateCtns}_{T_1^{-1}}(v, \iota)$, and $\eta' = (T_2, \dots, T_l)$. Note that T_1 is popped off the transaction stack and the actions of T_1 are revoked on (v, ι) .

C.5 Other Cases

When $v \neq (\epsilon, \dots, \epsilon)$ —that is, the fragment stacks of A contains at least one fragment and $F \in \text{TopFrg}(v)$ —then the transition rules of the following form are applicable: $F \xrightarrow{\text{start}(\phi)} B$, $F \xrightarrow{\text{finishStart}(\phi)} B$, $F \xrightarrow{\text{TS}} (\beta_1(F_1, i_1, x_1), \dots, \beta_k(F_k, i_k, x_k))$, and $F \xrightarrow{\text{NTS}} (\beta_1(F_1, i_1, x_1), \dots, \beta_k(F_k, i_k, x_k))$. The semantics of these rules are similar to the transition rules $A \xrightarrow{\text{start}(\phi)} B$, $A \xrightarrow{\text{finishStart}(\phi)} B$, $A \xrightarrow{\text{TS}} (\beta_1(F_1, i_1, x_1), \dots, \beta_k(F_k, i_k, x_k))$, and $A \xrightarrow{\text{NTS}} (\beta_1(F_1, i_1, x_1), \dots, \beta_k(F_k, i_k, x_k))$.

Dependencies between Launch Modes and Intent Flags

For transitions $A \xrightarrow{\alpha(\phi)} B$, the launch modes of A, B and the intent flags in ϕ may also depend on each other. The dependency can exhibit in the following three forms: n subsumes n' (i.e., n' is ignored if n co-occurs with n'), (2) n enables n' (i.e., n' takes effect if n co-occurs with n'), and (3) n implies n' (i.e., if n' subsumes (respectively, enables) n'' , then n subsumes (respectively, enables) n'' as well). We summarize these dependencies in Figure 19, where the solid lines represent the “subsume” relation, the dashed lines represent the “enable” relation, the dotted lines represent the “implies” relation.

The following properties hold for these relations: (1) the “subsume” and “imply” relations are transitive, and (2) the composition of the “imply” relation and the “subsume” (respectively, “enable”) relation is a subset of the “subsume” (respectively, “enable”) relation.

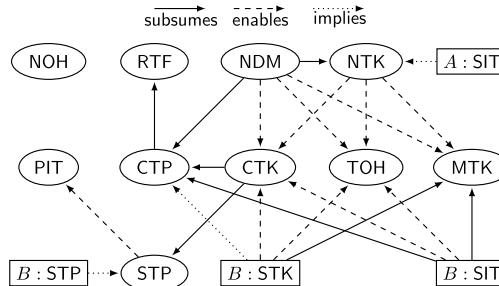


Fig. 19. Dependency graph for launch modes and intent flags in transitions $A \xrightarrow{\alpha(\phi)} B$. The launch modes (respectively, the intent flags) are in boxes (respectively, circles).

D Semantics of AMASS Models for the Other Versions of Android

We state the differences of the semantics of AMASS models in detail. To avoid tediousness, let us focus on the situation $\phi \models \neg\text{TOH}$. The differences for the situation $\phi \models \text{TOH}$ are similar.

D.1 Android 11.0 and 12.0

The semantics of AMASS for Android 11.0 and 12.0 are the same as Android 13.0.

D.2 Android 10.0, 9.0, and 8.0

The semantics for these three versions are the same and differ from that for Android 13.0 in the following sense: RTF is ignored when used together with NTK or $\text{Lmd}(A) = \text{SIT}$. In other words, for Android 10.0, 9.0, and 8.0, the semantics of AMASS for the case $\text{Lmd}(B) = \text{STD}$ and $\phi \models \neg\text{NTK} \wedge \neg\text{NDM} \wedge \neg\text{MTK}$, or $\text{Lmd}(A) = \text{SIT}$ and $\phi \models \neg\text{NDM} \wedge \neg\text{MTK}$, is adapted from Android 13.0 as follows:

- If $\text{GetRealTsk}(\rho, B) = S_i$ or $\text{GetRealTsk}(\rho, B) = *$ $\wedge \text{GetTsk}(\rho, B) = S_i$, then
 - if $i \neq 1$, then
 - * if $\phi \models \text{CTK}$, then ...
 - * if $\phi \models \neg\text{CTK}$, then ...
 - if $\phi \models \text{CTP}$ and $B \in S_i$, then ...
 - if $\phi \models \text{CTP}$ and $B \notin S_i$, then ...
 - if $\phi \models \neg\text{CTP}$, then
 - ◊ if $\text{GetRealTsk}(\rho, B) = S_i$ and $\zeta_i \neq \text{MAIN}$, then $b' = \neg\text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{MvTsk2Top}(\rho, i)$,
 - otherwise, $\rho' = \text{RmAct}(\text{MvTsk2Top}(\rho, i), 2, 1)$,
 - ◊ otherwise ($\text{GetRealTsk}(\rho, B) = S_i$ and $\zeta_i = \text{MAIN}$ or $\text{GetRealTsk}(\rho, B) = *$ $\wedge \text{GetTsk}(\rho, B) = S_i$),
 - if $\phi \models \text{STP}$ and $\text{TopAct}(S_i) = B$, then $b' = \neg\text{NOH}$, and moreover,
 - ★ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{MvTsk2Top}(\rho, i)$,
 - ★ otherwise, $\rho' = \text{RmAct}(\text{MvTsk2Top}(\rho, i), 2, 1)$,
 - otherwise, $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - ★ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
 - ★ otherwise, $\rho' = \text{RmAct}(\text{Push}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - otherwise ($i = 1$),
 - * if $\phi \models \text{CTK}$, then ...,
 - * if $\phi \models \neg\text{CTK}$, then
 - if $\phi \models \text{CTP}$ and $B \in S_1$, then ...
 - if $\phi \models \text{CTP}$ and $B \notin S_1$, then ...
 - if $\phi \models \neg\text{CTP}$, then
 - ◊ if $\text{GetRealTsk}(\rho, B) = S_1$ and $\zeta_1 \neq \text{MAIN}$,
 - if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - ◊ otherwise ($\text{GetRealTsk}(\rho, B) = S_1$ and $\zeta_i = \text{MAIN}$ or $\text{GetRealTsk}(\rho, B) = *$ $\wedge \text{GetTsk}(\rho, B) = S_1$),
 - if $\phi \models \text{STP}$ and $A = B$, or $\phi \models \text{STP} \wedge \text{PIT} \wedge \text{PreAct}(\rho) = B$,
 - ★ if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - ★ if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - otherwise, $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - ★ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - ★ otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$,
 - If $\text{GetTsk}(\rho, B) = *$, then

Similarly the semantics of AMASS for the case $\text{Lmd}(B) = \text{STP}$ and $\phi \models \text{NTK} \wedge \neg\text{NDM} \wedge \neg\text{MTK}$ or $\text{Lmd}(A) = \text{SIT}$ and $\phi \models \neg\text{NDM} \wedge \neg\text{MTK}$ is adapted from Android 13.0 as follows:

- If $\text{GetRealTsk}(\rho, B) = S_i$ or $\text{GetRealTsk}(\rho, B) = *$ $\wedge \text{GetTsk}(\rho, B) = S_i$, then
 - if $i \neq 1$, then
 - * if $\phi \models \text{CTK}$, then ...
 - * if $\phi \models \neg\text{CTK}$, then ...
 - if $\phi \models \text{CTP}$ and $B \in S_i$, then ...
 - if $\phi \models \text{CTP}$ and $B \notin S_i$, then ...
 - if $\phi \models \neg\text{CTP}$, then
 - ◊ if $\text{GetRealTsk}(\rho, B) = S_i$ and $\zeta_i \neq \text{MAIN}$, then $b' = \neg\text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{MvTsk2Top}(\rho, i)$,

- otherwise, $\rho' = \text{RmAct}(\text{MvTsk2Top}(\rho, i), 2, 1)$,
- otherwise ($\text{GetRealTsk}(\rho, B) = S_i$ and $\zeta_i = \text{MAIN}$ or $\text{GetRealTsk}(\rho, B) = *$ \wedge $\text{GetTsk}(\rho, B) = S_i$),
 - if $\text{TopAct}(S_i) = B$, then $b' = \neg\text{NOH}$, and moreover,
 - ★ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{MvTsk2Top}(\rho, i)$,
 - ★ otherwise, $\rho' = \text{RmAct}(\text{MvTsk2Top}(\rho, i), 2, 1)$,
 - otherwise, $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - ★ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
 - ★ otherwise, $\rho' = \text{RmAct}(\text{Push}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
- otherwise ($i = 1$),
 - * if $\phi \models \text{CTK}$, then \dots ,
 - * if $\phi \models \neg\text{CTK}$, then
 - if $\phi \models \text{CTP}$ and $B \in S_1$, then \dots
 - if $\phi \models \text{CTP}$ and $B \notin S_1$, then \dots
 - if $\phi \models \neg\text{CTP}$, then
 - if $\text{GetRealTsk}(\rho, B) = S_1$ and $\zeta_1 \neq \text{MAIN}$,
 - if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - otherwise ($\text{GetRealTsk}(\rho, B) = S_1$ and $\zeta_i = \text{MAIN}$ or $\text{GetRealTsk}(\rho, B) = *$ \wedge $\text{GetTsk}(\rho, B) = S_1$),
 - if $A = B$, or $\phi \models \text{PIT}$ and $\text{PreAct}(\rho) = B$,
 - ★ if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - ★ if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - otherwise, $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - ★ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - ★ otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$,
 - If $\text{GetTsk}(\rho, B) = *$, then \dots .

Note that the parts of the semantics denoted by \dots are the same as Android 13.0, and in the semantics for the situation $\phi \models \neg\text{CTP}$, the flag RTF has no effects, thus is ignored.

D.3 Android 7.0

The semantics for Android 7.0 is close to that of Android 10.0 (or 9.0, 8.0) but differs from it in the following two aspects: (1) the effect of NDM is the same as that of NTK, and (2) when $\phi \models \neg\text{NTK} \wedge \neg\text{NDM} \wedge \neg\text{CTP}$, if the top task is the main task where the started activity occurs but is not the top activity, then RTF has the same effect as CTK. More precisely, for Android 7.0, only two cases “ $\phi \models \text{NTK}$ or $\text{Lmd}(A) = \text{SIT}$ ” and “ $\phi \models \neg\text{NTK}$ and $\text{Lmd}(A) \neq \text{SIT}$ ” are considered, where the semantics for the case “ $\phi \models \text{NTK}$ or $\text{Lmd}(A) = \text{SIT}$ ” inherits that of “ $\phi \models \text{NTK} \wedge \neg\text{NDM}$ or $\text{Lmd}(A) = \text{SIT}$ ” for Android 10.0, whereas the semantics for the case “ $\phi \models \neg\text{NTK}$ and $\text{Lmd}(A) \neq \text{SIT}$ ” is adapted from that of “ $\phi \models \neg\text{NTK} \wedge \neg\text{NDM}$ and $\text{Lmd}(A) \neq \text{SIT}$ ” for Android 10.0 as follows:

- If $\phi \models \text{CTP}$ and $B \in \text{TopTsk}(\rho)$, then \dots .
- If $\phi \models \text{CTP}$ and $B \notin \text{TopTsk}(\rho)$, then \dots .
- If $\phi \models \neg\text{CTP}$, then
 - if $\phi \models \text{RTF}$ and $B \in \text{TopTsk}(\rho)$, then
 - * if $\text{TopAct}(\rho) \neq B$, then $b' = \neg\text{NOH}$, and moreover,
 - if $\zeta_i = \text{MAIN}$, then $\rho' = \text{ClrTsk}(\rho, B)$,
 - otherwise,

- ◊ if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{MvAct2Top}(\rho, B)$,
- ◊ otherwise, $\rho' = \text{RmAct}(\text{MvAct2Top}(\rho, B), 1, 2)$,
- * if $\text{TopAct}(\rho) = B$,
 - if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
- if $\phi \models \text{RTF}$ and $B \notin \text{TopTsk}(\rho)$, then ···,
- if $\phi \models \neg\text{RTF}$, then ···.

D.4 Android 6.0

The semantics for Android 6.0 differs from that of Android 10.0 (or 9.0, 8.0) in the following two aspects: (1) the effect of NDM is the same as that of NTK, and (2) the task allocation mechanism of Android 6.0 does not use the real activities of tasks and only relies on affinities. More precisely, for Android 6.0, only two cases “ $\phi \models \text{NTK}$ or $\text{Lmd}(A) = \text{SIT}$ ” and “ $\phi \models \neg\text{NTK}$ and $\text{Lmd}(A) \neq \text{SIT}$ ” are considered, where the semantics for the case “ $\phi \models \text{NTK}$ or $\text{Lmd}(A) = \text{SIT}$ ” inherits that of “ $\phi \models \text{NTK} \wedge \neg\text{NDM}$ or $\text{Lmd}(A) = \text{SIT}$ and $\phi \models \neg\text{NDM}$ ” for Android 10.0, whereas the semantics for the case “ $\phi \models \text{NTK}$ or $\text{Lmd}(A) = \text{SIT}$ and $\phi \models \neg\text{MTK}$ ” is adapted from that of “ $\phi \models \text{NTK} \wedge \neg\text{NDM} \wedge \neg\text{MTK}$ or $\text{Lmd}(A) = \text{SIT}$ and $\phi \models \neg\text{NDM} \wedge \text{MTK}$ ” for the case $\text{Lmd}(B) = \text{STD}$ for Android 10.0 as follows, where the conditions involving $\text{GetRealTsk}(\rho, B)$ and $\text{GetTsk}(\rho, B)$ are simplified into the conditions involving only $\text{GetTsk}(\rho, B)$, and moreover, we do not need to distinguish whether a task is the main task or not:

- If $\text{GetTsk}(\rho, B) = S_i$, then
 - if $i \neq 1$, then
 - * if $\phi \models \text{CTK}$, then ···
 - * if $\phi \models \neg\text{CTK}$, then ···
 - if $\phi \models \text{CTP}$ and $B \in S_i$, then ···
 - if $\phi \models \text{CTP}$ and $B \notin S_i$, then ···
 - if $\phi \models \neg\text{CTP}$, then
 - ◊ if $\phi \models \text{STP}$ and $\text{TopAct}(S_i) = B$, then $b' = \neg\text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{MvTsk2Top}(\rho, i)$,
 - otherwise, $\rho' = \text{RmAct}(\text{MvTsk2Top}(\rho, i), 2, 1)$,
 - ◊ otherwise, $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - otherwise ($i = 1$),
 - * if $\phi \models \text{CTK}$, then ···,
 - * if $\phi \models \neg\text{CTK}$, then
 - if $\phi \models \text{CTP}$ and $B \in S_1$, then ···
 - if $\phi \models \text{CTP}$ and $B \notin S_1$, then ···
 - if $\phi \models \neg\text{CTP}$, then
 - ◊ if $\phi \models \text{STP}$ and $A = B$, or $\phi \models \text{STP} \wedge \text{PIT}$ and $\text{PreAct}(\rho) = B$,
 - if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - ◊ otherwise, $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$,
 - If $\text{GetTsk}(\rho, B) = *$, then ···.

Similarly for the case $\text{Lmd}(B) = \text{STP}$, the semantics is adapted as follows:

- If $\text{GetTsk}(\rho, B) = S_i$, then
 - if $i \neq 1$, then
 - * if $\phi \models \text{CTK}$, then ...
 - * if $\phi \models \neg\text{CTK}$, then ...
 - if $\phi \models \text{CTP}$ and $B \in S_i$, then ...
 - if $\phi \models \text{CTP}$ and $B \notin S_i$, then ...
 - if $\phi \models \neg\text{CTP}$, then
 - ◊ if $\text{TopAct}(S_i) = B$, then $b' = \neg\text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{MvTsk2Top}(\rho, i)$,
 - otherwise, $\rho' = \text{RmAct}(\text{MvTsk2Top}(\rho, i), 2, 1)$,
 - ◊ otherwise, $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\text{MvTsk2Top}(\rho, i), B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\text{MvTsk2Top}(\rho, i), B), 2, 1)$,
 - otherwise ($i = 1$),
 - * if $\phi \models \text{CTK}$, then ... ,
 - * if $\phi \models \neg\text{CTK}$, then
 - if $\phi \models \text{CTP}$ and $B \in S_1$, then ...
 - if $\phi \models \text{CTP}$ and $B \notin S_1$, then ...
 - if $\phi \models \neg\text{CTP}$, then
 - ◊ if and $A = B$, or $\phi \models \text{PIT}$ and $\text{PreAct}(\rho) = B$,
 - if $\alpha = \text{start}$, then $\rho' = \rho$ and $b' = b$,
 - if $\alpha = \text{finishStart}$, then $\rho' = \text{RmAct}(\rho, 1, 1)$ and $b' = \neg\text{NOH}$,
 - ◊ otherwise, $b' = \text{NOH}$ iff $\phi \models \text{NOH}$, and moreover,
 - if $b = \neg\text{NOH}$ and $\alpha = \text{start}$, then $\rho' = \text{Push}(\rho, B)$,
 - otherwise, $\rho' = \text{RmAct}(\text{Push}(\rho, B), 1, 2)$,
 - If $\text{GetTsk}(\rho, B) = *$, then

Similarly for the case $\text{Lmd}(B) = \text{STK}$, the semantics is adapted as follows where the conditions involving $\text{GetRealTsk}(\rho, B)$ and $\text{GetTsk}(\rho, B)$ are simplified into the conditions involving only $\text{GetTsk}(\rho, B)$:

- If $\text{GetTsk}(\rho, B) = S_i$, then ...
- If $\text{GetTsk}(\rho, B) = *$, then

E Auditing the Source Code of Android OS

In this section, we audit the source code of Android OS for AMASS_{ACT} and AMASS_{FRG} .

E.1 Auditing the Source Code for AMASS_{ACT}

We examine the source code of the procedures called directly or indirectly by `startActivityInner()`:

- From the source code in line 2550 of the file `activityStarter.java` (Figure 20), the procedure `computeLaunchingTaskFlags()` computes the intent flags implied by the launch modes of the starting and started activities.
- From the source code in line 2678 of the file `activityStarter.java` (Figure 21), the procedure `getReusableTask()` calls `findTask()` to compute a reusable task to put the started activity, when either the intent flag `FLAG_ACTIVITY_NEW_TASK` is set to true and the flag `FLAG_ACTIVITY_MULTIPLE_TASK` is set to false, or the launch modes of the started activity is `singleInstance` or `singleTask`:

```

// +/master/services/core/java/com/android/server/wm/ActivityStarter.java
1631     int startActivityInner(final ActivityRecord r, ActivityRecord sourceRecord,
1632         IVoiceInteractionSession voiceSession, IVoiceInteractor voiceInteractor,
1633         int startFlags, ActivityOptions options, Task inTask,
1634         TaskFragment inTaskFragment, @BalCode int balCode,
1635         NeededUriGrants intentGrants, int realCallingUid) {
1636         ...
1637         computeLaunchingTaskFlags();
1638         ...
1639         final Task reusedTask = getReusableTask();
1640         ...
1641         final Task targetTask = reusedTask != null ? reusedTask : computeTargetTask();
1642         final boolean newTask = targetTask == null;
1643         ...
1644         setResult =
1645             recycleTask(targetTask, targetTaskTop, reusedTask, intentGrants);
1646         ...
1647         if (newTask) {
1648             final Task taskToAffiliate = (mLaunchTaskBehind && mSourceRecord != null)
1649                 ? mSourceRecord.getTask() : null;
1650             setNewTask(taskToAffiliate);
1651         } else if (mAddingToTask) {
1652             addOrReparentStartingActivity(targetTask, "addingtotask");
1653         }
1654         ...
1655     }
1656 }

// +/master/services/core/java/com/android/server/wm/ActivityStarter.java
2550     private void computeLaunchingTaskFlags() {
2551         ...
2552         } else if (mSourceRecord.launchMode == LAUNCH_SINGLE_INSTANCE) {
2553             ...
2554             mLaunchFlags |= FLAG_ACTIVITY_NEW_TASK;
2555         } else if (isLaunchModeOneOf(LAUNCH_SINGLE_INSTANCE, LAUNCH_SINGLE_TASK)) {
2556             ...
2557             mLaunchFlags |= FLAG_ACTIVITY_NEW_TASK;
2558         }
2559     }

```

Fig. 20. Source code of ActivityStarter.startActivityInnner() and ActivityStarter.computeLaunchingTaskFlags().

- In line 2301 of the file RootWindowContainer.java (see Figure 21), findTask() calls process(), which then calls forAllLeafTasks(this) in line 338 of the file RootWindowContainer.java, and in the procedure forAllLeafTasks(), test(this) is called in line 3221 of the file Task.java.
- In line 394 of the file RootWindowContainer.java (see Figure 21), the procedure test(Task *task*) first checks whether the real activity of *task* matches the started activity. Otherwise, in line 401, it checks whether the affinity of *task* matches the task affinity of the started activity. Therefore, from the source code of the procedure test(), we confirm that the task allocation mechanism defined in the semantics of AMASS_{ACT} in Section 4.1.1 matches its actual implementation in Android OS.
- When getReusableTask() does not find a task, computeTargetTask() (see line 1880 of Figure 21) will be called to see whether the top task in the task stack can be used to put the started activity. If the answer is yes, then computeTargetTask() returns the top task.
- If either getReusableTask() or computeTargetTask() finds an existing task to put the started activity, then recycleTask() (see line 2037 of Figure 22) is called to prepare the task to be reused for this launch, where complyActivityFlags() is called to comply with the specified intent flags.

From the source code of complyActivityFlags() (see line 2182 of ActivityStarter.java in Figure 21), we can see that it deals with the intent flags in the following way:

- In line 2191, if the intent flags FLAG_ACTIVITY_NEW_TASK and FLAG_ACTIVITY_CLEAR_TASK are both set to true, then complyActivityFlags() calls the procedure

```

// +/master/services/core/java/com/android/server/wm/ActivityStarter.java
2642  private Task getReusableTask() {
    ...
2657      boolean putIntoExistingTask = ((mLaunchFlags & FLAG_ACTIVITY_NEW_TASK) != 0 &&
2658          (mLaunchFlags & FLAG_ACTIVITY_MULTIPLE_TASK) == 0)
2659          || isLaunchModeOneOf(LAUNCH_SINGLE_INSTANCE, LAUNCH_SINGLE_TASK);
    ...
2665      if (putIntoExistingTask) {
        ...
2678          intentActivity =
2679              mRootWindowContainer.findTask(mStartActivity, mPreferredTaskDisplayArea);
        ...
2681    }
2699 }

// +/master/services/core/java/com/android/server/wm/ActivityStarter.java
1880  private Task computeTargetTask() {
    ...
1898      final ActivityRecord top = rootTask.getTopNonFinishingActivity();
    ...
1900      return top.getTask();
    ...
1907 }

// +/master/services/core/java/com/android/server/wm/RootWindowContainer.java
2301  ActivityRecord findTask(int activityType, String taskAffinity, Intent intent, ActivityInfo info,
2302      TaskDisplayArea preferredTaskDisplayArea) {
    ...
2324      mTmpFindTaskResult.process(taskDisplayArea);
    ...
2338 }

// +/master/services/core/java/com/android/server/wm/RootWindowContainer.java
326  void process(WindowContainer parent) {
    ...
338      parent.forAllLeafTasks(this);
339 }

// +/master/services/core/java/com/android/server/wm/Task.java
3209  boolean forAllLeafTasks(Predicate<Task> callback) {
    ...
3221      return callback.test(this);
    ...
3224 }

// +/master/services/core/java/com/android/server/wm/RootWindowContainer.java
342  public boolean test(Task task) {
    ...
394      if (task.realActivity != null && task.realActivity.compareTo(cls) == 0
395          && Objects.equals(documentData, taskDocumentData)) {
        ...
400          return true;
401      } else if (affinityIntent != null && affinityIntent.getComponent() != null
402          && affinityIntent.getComponent().compareTo(cls) == 0 &&
403          Objects.equals(documentData, taskDocumentData)) {
        ...
407          return true;
408      }
    ...
425 }

```

Fig. 21. Source code of ActivityStarter.getReusableTask(), RootWindowContainer.findTask(), RootWindowContainer.process(), Task.forAllLeafTasks(), and RootWindowContainer.test().

performClearTaskForReuse() in line 2199 to clear all activities in the task, and sets the Boolean variable *mAddingToTask* to true in line 2201, so that the started activity will be added into the target task when the procedure addOrReparentStartingActivity() is called.

- Otherwise—that is, FLAG_ACTIVITY_NEW_TASK or FLAG_ACTIVITY_CLEAR_TASK is set to false—then complyActivityFlags() performs the following operations:
 - * In line 2203, if FLAG_ACTIVITY_CLEAR_TOP is set to true, then complyActivityFlags() calls the procedure performClearTop() in line 2211 to clear all the activities on top of the started activity.

- * In line 2245, if FLAG_ACTIVITY_CLEAR_TOP is set to false and FLAG_ACTIVITY_REORDER_TO_FRONT is set to true, then complyActivityFlags() calls the procedure moveActivityToFront() in line 2255 to move the started activity to the top of the task.
- * In line 2271, if FLAG_ACTIVITY_CLEAR_TOP and FLAG_ACTIVITY_REORDER_TO_FRONT are both set to false, and moreover, the real activity of the target task is the same as the started activity, then the content of the target task will be not changed.
- * In line 2275, if FLAG_ACTIVITY_CLEAR_TOP and FLAG_ACTIVITY_REORDER_TO_FRONT are both set to false, and FLAG_ACTIVITY_SINGLE_TOP is set to true, and moreover, the top activity of the target task is the same as the started activity, then the content of the target task will not be changed.
- * In line 2291, if none of the aforementioned situations happens, then the Boolean variable *mAddingToTask* is set to true in line 2292 so that the started activity will be added into the target task when the procedure addOrReparentStartingActivity() is called.

Therefore, we confirm that the way of dealing with the intent flags in the semantics of AMASS_{ACT} in Section 4.1.1 is consistent with source code of complyActivityFlags().

- If neither getReusableTask() nor computeTargetTask() finds an existing task, then setNewTask() (see line 2842 of the file ActivityStarter.java in Figure 22) is called to start a new task. Moreover, in line 2844, setNewTask() calls reuseOrCreateTask() to create a new task. From the source code of reuseOrCreateTask() as illustrated in Figure 23, the procedure reuseOrCreateTask() creates a new task in line 5959. Note that since the condition canReuseAsLeafTask() matters only when multi-screen mode is enabled, we ignore it in this work. As a result, in the single-screen mode, reuseOrCreateTask() always creates a new task.
- From the source code of the procedure addOrReparentStartingActivity() in Figure 22, the started activity is added to the target task by calling addChild() in line 2910.

In summary, after auditing the Android source code for starting an activity, we confirm that the semantics of AMASS_{ACT} is consistent with its actual implementation in Android OS. In particular, the task allocation mechanism and the intent flags in the semantics conform to the source code in Android OS.

E.2 Auditing the Source Code for AMASS_{FRG}

From the source code in Figure 24, the procedure executeOpsTogether() executes multiple fragment transactions stored in *records* together. At first, for each *record* in *records*, it either calls expandOps() or trackAddedFragmentsInPop() to update the fragments in *added* and transforms each “replace” action of *record* into a sequence of “add” and “remove” actions. The actual executions of these fragment transactions are fulfilled by calling executeOps() in line 2205.

The procedure expandOps() expands the actions in a fragment transaction by transforming each “replace” action into a sequence of “add” and “remove” actions. From the source code of expandOps() (cf. Figure 24), when *op* with *op.cmd* = OP_REPLACE is processed, a sequence of “remove” actions followed by an “add” action is added to *mOps* as follows. For each fragment in the current fragment container (i.e., the fragment in *added* such that *old.mContainerId* == *containerId*), a “remove” action is added (line 932). Finally, *op.cmd* is changed from OP_REPLACE to OP_ADD (line 942). Therefore, we confirm that the way of dealing with REP actions in the semantics of AMASS_{FRG} in Section 4.1.2 is consistent with the source code of expandOps().

When committing a fragment transaction, FragmentManager.executeOps() calls BackStackRecord.executeOps(). From the source code of BackStackRecord.executeOps() in Figure 25 (line 759-809), each action in *mOps* is executed by adding a fragment to or removing a fragment from the corresponding fragment container. Evidently, the execution of fragment actions as defined

```

// +/master/services/core/java/com/android/server/wm/ActivityStarter.java
2037 int recycleTask(Task targetTask, ActivityRecord targetTaskTop, Task reusedTask,
2038     NeededUriGrants intentGrants, BalVerdict balVerdict) {
...
2090     complyActivityFlags(targetTask,
2091         reusedTask != null ? reusedTask.getTopNonFinishingActivity() : null, intentGrants);
...
2127 }

// +/master/services/core/java/com/android/server/wm/ActivityStarter.java
2182 private void complyActivityFlags(Task targetTask, ActivityRecord reusedActivity,
2183     NeededUriGrants intentGrants) {
...
2191     if ((mLaunchFlags & (FLAG_ACTIVITY_NEW_TASK | FLAG_ACTIVITY_CLEAR_TASK))
2192         == (FLAG_ACTIVITY_NEW_TASK | FLAG_ACTIVITY_CLEAR_TASK)) {
...
2199         targetTask.performClearTaskForReuse(true /* excludingTaskOverlay */);
...
2201         mAddingToTask = true;
...
2203     } else if ((mLaunchFlags & FLAG_ACTIVITY_CLEAR_TOP) != 0
...
2206         LAUNCH_SINGLE_INSTANCE_PER_TASK)) {
...
2211         final ActivityRecord clearTop = targetTask.performClearTop(mStartActivity,
...
2245     } else if ((mLaunchFlags & FLAG_ACTIVITY_CLEAR_TOP) == 0 && !mAddingToTask
2246         && (mLaunchFlags & FLAG_ACTIVITY_REORDER_TO_FRONT) != 0) {
...
2253         if (act != null) {
2254             final Task task = act.getTask();
2255             boolean actuallyMoved = task.moveActivityToFront(act);
...
2270     } else if (mStartActivity.mActivityComponent.equals(targetTask.realActivity)) {
2272         if (targetTask == mInTask) {
...
2275     } else if (((mLaunchFlags & FLAG_ACTIVITY_SINGLE_TOP) != 0
2276                 || LAUNCH_SINGLE_TOP == mLaunchMode)
2277                 && targetTaskTop.mActivityComponent.equals(mStartActivity.mActivityComponent)
2278                 && mStartActivity.resultTo == null) {
...
2291         } else if (reusedActivity == null) {
2292             mAddingToTask = true;
2293         }
...
2307     }
2308 }

// +/master/services/core/java/com/android/server/wm/ActivityStarter.java
2842 private void setNewTask(Task taskToAffiliate) {
...
2844     final Task task = mTargetRootTask.reuseOrCreateTask(
...
2856 }

// +/master/services/core/java/com/android/server/wm/ActivityStarter.java
2870 private void addOrReparentStartingActivity(@NonNull Task task, String reason) {
2871     TaskFragment newParent = task;
...
2910     newParent.addChild(mStartActivity, POSITION_TOP);
...
2914 }

```

Fig. 22. Source code of ActivityStarter.recycleTask(), ActivityStarter.complyActivityFlags(), ActivityStarter.setNewTask(), and ActivityStarter.addOrReparentStartingActivity().

in the semantics of AMASS_{FRG} in Section 4.1.2 is consistent with the source code of BackStackRecord.executeOps().

When popping a fragment transaction, executeOpsTogether() calls trackAddedFragmentsInPop(). From the source code of trackAddedFragmentsInPop() in Figure 24, the fragments in *added* are updated by revoking all “add” or “remove” actions in *mOps* (i.e., all the actions in

```
// +/master/services/core/java/com/android/server/wm/Task.java
5944     Task reuseOrCreateTask(ActivityInfo info, Intent intent, IVoiceInteractionSession voiceSession,
5945         IVoiceInteractor voiceInteractor, boolean toTop, ActivityRecord activity,
5946         ActivityRecord source, ActivityOptions options) {
5947     ...
5948     if (canReuseAsLeafTask()) {
5949         ...
5950     } else {
5951         task = new Task.Builder(mAtmService)
5952             ...
5953             .build();
5954     }
5955 }
```

Fig. 23. Source code of Task.reuseOrCreateTask().

the current fragment transaction stack). Note that *added* is a temporary data structure used for expanding “replace” actions and is different from the fragment stacks. The fragment stacks are updated by calling BackStackRecord.executePopOps() in Figure 25, where for each *op* in *mOps*, if *op.cmd*=OP_ADD (respectively, OP_REMOVE), *op.fragment* is removed from *mManager* (respectively, added to *mManager*). Therefore, we confirm that the way of revoking fragment transactions in the semantics of AMASS_{FRG} in Section 4.1.2 is consistent with the source code of trackAddedFragmentsInPop().

F Validation of the Semantics of AMASS Models

We use ValApp to validate the semantics of AMASS models. In the sequel, for each version of Android, we validate the semantics of AMASS models for this version. We utilize the automated methods as described in Section 7.2 to validate the semantics.

Recall that the transition rules of AMASS models are of the following three forms:

$$\begin{aligned} -\tau &= A \xrightarrow{\alpha(\phi)} B, \tau = F \xrightarrow{\alpha(\phi)} B, \\ -\tau &= A \xrightarrow{\mu} T, \tau = F \xrightarrow{\mu} T, \\ -\tau &= \text{back}. \end{aligned}$$

Validate the Semantics of the Transition Rules $\tau = A \xrightarrow{\alpha(\phi)} B$ or $\tau = F \xrightarrow{\alpha(\phi)} B$. We illustrate the validation of the semantics for $\tau = A \xrightarrow{\alpha(\phi)} B$. The validation of the semantics for $\tau = F \xrightarrow{\alpha(\phi)} B$ is similar. To validate the semantics of $\tau = A \xrightarrow{\alpha(\phi)} B$, we generate one configuration for each combination of the launch modes of *A* and *B*, the values of α , the intent flags, and the constraints on the configuration before applying the transition—for example, GetRealTsk(ρ, B) = *, GetTsk(ρ, B) = S_1 , and $B \in \text{TopTsk}(\rho)$. In total, there are 901,120 different combinations to be considered and we generate configurations for all of them. Then we use these configurations to validate the formal semantics. Through experiments, we discover that for every combination, the configuration obtained by applying the transition rule corresponding to the combination according to the formal semantics and the actual configuration returned by ADB are equal, thus the formal semantics of AMASS in this case for Android 13.0 are confirmed to be consistent with the actual behaviors of Android apps.

Validation of the Semantics of the Transition Rules $\tau = A \xrightarrow{\mu} T$ or $\tau = F \xrightarrow{\mu} T$. We illustrate the validation of the semantics for $\tau = A \xrightarrow{\mu} T$. The validation of the semantics for $\tau = F \xrightarrow{\mu} T$ is similar. Note that according to the definition of semantics of AMASS models in Appendix C, the only requirement for the enablement of $A \xrightarrow{\mu} T$ is that the top activity is *A*. This requirement does not

```

// +/master/core/java/android/app/FragmentManager.java
2178 private void executeOpsTogether(ArrayList<BackStackRecord> records,
2179     ArrayList<Boolean> isRecordPop, int startIndex, int endIndex) {
...
2189 for (int recordNum = startIndex; recordNum < endIndex; recordNum++) {
2190     final BackStackRecord record = records.get(recordNum);
2191     final boolean isPop = isRecordPop.get(recordNum);
2192     if (!isPop) {
2193         oldPrimaryNav = record.expandOps(mTmpAddedFragments, oldPrimaryNav);
2194     } else {
2195         record.trackAddedFragmentsInPop(mTmpAddedFragments);
2196     }
...
2205     executeOps(records, isRecordPop, startIndex, endIndex);
2206 }
...
2236 }

// +/master/core/java/android/app/BackStackRecord.java
892 Fragment expandOps(ArrayList<Fragment> added, Fragment oldPrimaryNav) {
893     for (int opNum = 0; opNum < mOps.size(); opNum++) {
894         final Op op = mOps.get(opNum);
895         switch (op.cmd) {
...
910             case OP_REPLACE: {
911                 final Fragment f = op.fragment;
...
914                 for (int i = added.size() - 1; i >= 0; i--) {
915                     final Fragment old = added.get(i);
916                     if (old.mContainerId == containerId) {
...
927                         final Op removeOp = new Op(OP_REMOVE, old);
...
932                         mOps.add(opNum, removeOp);
933                         added.remove(old);
...
937                     }
...
942                     op.cmd = OP_ADD;
943                     added.add(f);
...
959             }
...
968     void trackAddedFragmentsInPop(ArrayList<Fragment> added) {
969         for (int opNum = 0; opNum < mOps.size(); opNum++) {
970             final Op op = mOps.get(opNum);
971             switch (op.cmd) {
972                 case OP_ADD:
973                 case OP_ATTACH:
974                     added.remove(op.fragment);
975                     break;
976                 case OP_REMOVE:
977                 case OP_DETACH:
978                     added.add(op.fragment);
979                     break;
980             }
981         }
982     }
}

```

Fig. 24. Source code of executeOpsTogether(), expandOps(), and trackAddedFragmentsInPop().

constrain the source configurations very much. To validate the semantics of $\tau = A \xrightarrow{\mu} T$, we fix the values of the following parameters and generate configurations as well as transition rules with these values:

- The number of containers associated with A is 1 for each $A \in \text{Act}$.
- The maximum number of fragment transactions in the transaction stack is 1.
- The maximum number of actions in a fragment transaction is 2.
- The identifiers in (concretized) actions in a fragment transaction are from the set $\{1, 2\}$.

Note that the maximum number of fragments in a container is bounded by $\hbar = 6$ (i.e., the bound on the height of the stacks). In total, there are 4,032 different configurations to be considered. In the

```

// +/master/core/java/android/app/FragmentManager.java
2397  private static void executeOps(ArrayList<BackStackRecord> records,
2398      ArrayList<Boolean> isRecordPop, int startIndex, int endIndex) {
2399
2400      if (isPop) {
2401          ...
2402          record.executePopOps(moveToState);
2403      } else {
2404          ...
2405          record.executeOps();
2406      }
2407      ...
2408  }

// +/master/core/java/android/app/BackStackRecord.java
759  void executeOps() {
760      final int numOps = mOps.size();
761      for (int opNum = 0; opNum < numOps; opNum++) {
762
763          switch (op.cmd) {
764              case OP_ADD:
765                  f.setNextAnim(op.enterAnim);
766                  mManager.addFragment(f, false);
767                  break;
768              case OP_REMOVE:
769                  f.setNextAnim(op.exitAnim);
770                  mManager.removeFragment(f);
771                  break;
772              ...
773          }
774      }
775  }

// +/master/core/java/android/app/BackStackRecord.java
818  void executePopOps(boolean moveToState) {
819      for (int opNum = mOps.size() - 1; opNum >= 0; opNum--) {
820          final Op op = mOps.get(opNum);
821          Fragment f = op.fragment;
822
823          switch (op.cmd) {
824              case OP_ADD:
825                  f.setNextAnim(op.popExitAnim);
826                  mManager.removeFragment(f);
827                  break;
828              case OP_REMOVE:
829                  f.setNextAnim(op.popEnterAnim);
830                  mManager.addFragment(f, false);
831                  break;
832              ...
833          }
834      }
835  }

```

Fig. 25. Source code of `FragmentManager.executeOps()`, `BackStackRecord.executeOps()`, and `BackStackRecord.executePopOps()`.

end, we generate 4,032 configurations for ValApp. We also generate 576 (288 if only $\tau = A \xrightarrow{\mu} T$ is counted) transition rules for ValApp. Therefore, the total number of (configuration, transition rule) pairs for ValApp is 1,741,824 (1,161,824 if $\tau = A \xrightarrow{\mu} T$ is counted). Then for all these pairs, we apply the transition rules on the configurations to validate the formal semantics. Through experiments, we discover that for each configuration and each transition rule, the configuration obtained by applying the transition rule according to the formal semantics and the actual configuration returned by ADB are equal, thus the formal semantics of AMASS models in this case for Android 13.0 are confirmed to be consistent with the actual behaviors of Android apps.

Validation of the Semantics of the Transition Rule $\tau = \text{back}$. According to the definition of semantics of AMASS models in Appendix C, there are only two constraints on the configurations: $\eta = \epsilon$ and $\eta \neq \epsilon$. Because the aforementioned 4,032 configurations generated for $\tau = A \xrightarrow{\mu} T$ or $F \xrightarrow{\mu} T$

cover both constraints $\eta = \epsilon$ and $\eta \neq \epsilon$. Hence, we could reuse these 4,032 configurations for the validation of the semantics for $\tau = \text{back}$. Then for all these configurations, we apply the transition rule $\tau = \text{back}$ on the configurations to validate the formal semantics. Through experiments, we discover that for each configuration and each transition rule, the configuration obtained by applying the transition rule according to the formal semantics and the actual configuration returned by ADB are equal, thus the formal semantics of AMASS models in this case for Android 13.0 are confirmed to be consistent with the actual behaviors of Android apps.

All the results of the validation experiments for AMASS models are available at <https://github.com/Jinlong-He/TaskDroid/blob/master/semanticsVal.md>.

G Information about Randomly Selected Task/Fragment Container Unbounded Apps

Table 20. Statistics of 25 Randomly Selected “Task-Unbounded” Apps from F-Droid

Package name	Act	Frg	$ \Delta $	Size (MB)
org.gnucash.android	10	2	32	2.71
systems.byteswap.apiroute	3	0	3	1.08
max.music_cyclon	2	0	2	1.81
com.matburt.mobileorg	8	0	9	1.36
org.npr.android.news	5	0	8	0.92
com.commonsware.android.arXiv	8	0	12	0.52
net.mabako.steamgifts	6	1	24	2.66
com.app.Zensuren	17	0	22	0.17
uk.co.busydoingnothing.prevo	4	0	5	11.79
de.drhoffmannsoftware.calcvac	14	0	24	0.9
org.sasehash.burgerwp	2	0	3	1.76
com.mikifus.padland	6	1	18	1.07
org.evilsoft.pathfinder.reference	5	0	8	22.02
com.android.keepass	4	0	6	1.65
de.bloosberg.basti.childresuscalc	2	0	2	1.41
com.samebits.beacon.locator	2	0	2	1.98
ohm.quickdice	9	0	14	1.41
org.saiditnet.redreader	11	1	51	4.99
com.gianlu.aria2app	13	0	31	21.11
net.artificialworlds.rabbitescape	3	0	3	18.81
com.sam.hex	10	0	23	0.76
com.kaliturin.blacklist	2	0	2	2.06
de.schildbach.oeffi	10	0	35	1.79
com.aurora.store	22	0	56	5.47
com.adrienpoupa.attestationcoronavirus	2	0	2	3.58

Table 21. Statistics of 25 Randomly Selected “Task-Unbounded” Apps from Google Play

Package name	 Act 	 Frg 	 Δ 	Size (MB)
com.abdulqawi.ali.mosabqa	8	0	25	2.84
com.music.star.player	3	3	25	2.38
com.drclabs.android.wootchecker	11	0	18	0.84
com.hotels.hotelsmecca	6	1	16	16.43
com.airg.hookt	6	0	12	10.59
com.holidu.holidu	2	0	2	4.04
com.appkey.english3000freakata	28	0	97	1.06
socials.com.application	34	0	122	3.75
www.genting.rwggenting	3	0	5	12.78
com.goldenhammer.beisboldominicana	3	1	10	4.58
com.travolution.seoultravelpass	5	0	10	4.58
com.ic.myMoneyTracker	25	0	60	3.39
tekcarem.gebeliktakibi	59	0	255	3.15
de.fckoeln.app	22	0	45	40.77
de.twokit.castbrowser	5	0	8	3.79
com.TWTD.FLIXMOVIE	6	0	10	7.73
com.emeint.android.mwallet.tub	10	0	95	59.02
com.ctt.celltrak2	22	0	80	11.31
biz.mobinex.android.apps.cep_sifrematik	11	0	34	3.54
com.linesmarts.linesmartsfree	4	0	4	28.47
com.nhiApp.v1	8	9	107	26.6
com.alfarooqislamicresearchcenter	34	0	78	13.83
com.objectremover.touchretouch	14	0	19	11.28
com.vwfs.phototan	3	0	5	27.23
com.sg.apphelperstore	5	0	6	6.56

Table 22. Statistics of 25 Randomly Selected “Fragment Container Unbounded” Apps from F-Droid

Package name	Act	Frg	\Delta	Size (MB)
org.ligi.fahrplan	6	5	46	1.83
io.gitlab.allenb1.todolist	6	3	11	1.05
naman14.timber	5	3	15	5.8
me.anon.grow	4	3	30	6.46
com.wikijourney.wikijourney	1	2	7	4.27
com.mattallen.loaned	3	1	5	1.01
com.ymber.eleven	1	2	15	10.38
com.syncedsynapse.kore2	2	1	5	2.22
net.momodalapp.vimtouch	5	1	9	3.44
com.csipsimple	12	2	22	11.56
ch.corten.aha.worldclock	4	3	13	1.4
org.wikimedia.commons.wikimedia	3	6	44	15.0
com.llamacorp.equate	1	1	3	0.39
koeln.mop.elpeefpe	4	2	11	1.59
fr.kwiatkowski.ApkTrack	1	2	13	2.32
eu.siacs.conversations.legacy	17	2	88	11.12
com.artifex.mupdfdemo	4	2	5	25.68
org.osmdroid	15	3	28	4.62
com.haha01haha01.harail	4	1	6	0.69
com.owncloud.android	11	4	40	3.8
org.cipherdyne.fwknop2	5	2	12	2.63
edu.cmu.cylab.starslinger.demo	4	1	8	1.21
com.commonslab.commonslab	4	6	45	14.72
hans.b.skewy1_0	1	6	19	6.45
com.twobuntu.twobuntu	4	3	12	0.75

Table 23. Statistics of 25 Randomly Selected “Fragment Container Unbounded” Apps from GooglePlay

Package name	 Act 	 Frg 	 \Delta 	Size (MB)
com.schoola2zlive	11	1	40	4.77
com.endless.smoothierecipes	3	9	110	7.57
com.traderumors	5	6	28	5.53
com.rakuten.room	20	19	87	20.1
com.hotels.hotelsmecca	6	1	16	16.43
br.com.prevapp03	34	1	80	5.15
com.star.mobile.video	21	1	55	7.98
fr.elol.yams	4	6	93	8.75
music.symphony.com.materialmusicv2	7	3	14	3.39
ru.sports.rfpl	6	1	9	8.33
com.discsoft.daemonsync	7	1	10	10.06
com.accuvally.android.accupass	8	1	21	11.62
com.directv.navigator	10	7	68	41.66
com.ldf.gulli.view	13	8	49	15.62
kvp.jjy.MispAndroid320	14	6	51	31.34
de.wirfahrlehrer.easytheory	3	12	144	3.6
com.mmb.mamitalk	5	4	22	8.19
ch.swissdevelopment.android	3	1	8	20.55
tw.com.iobear.medicalcalculator	1	1	3	2.49
com.gn.apkmanager	2	1	4	2.92
com.piradevrcostagen.strobo	2	1	4	2.48
com.gqueues.android.app	13	3	34	4.68
com.reverb.app	14	9	96	13.82
com.xnview.hypocam	4	8	36	26.23
de.stefanpled.localcast	1	16	95	13.94

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