

Study of χ_b production at $\sqrt{s} = 7$ and 8 TeV

I. Belyaev^{1,2}, C. Bozzi³, H. Dijkstra¹, A. Mazurov^{1,4}.

¹CERN, ²ITEP, Moscow, ³INFN Sezione di Ferrara, ⁴Università di Ferrara

Abstract

A study of χ_b production at LHCb is performed on data collected during 2011 and 2012, by reconstructing $\chi_b(1P,2P,3P) \to \Upsilon(1S)\gamma$ decays. The differential production cross sections, relative to the $\Upsilon(1S)$, are measured as a function of $\Upsilon(1S)$ transverse momentum and rapidity. The $\chi_b \to \Upsilon(2S)\gamma$ and $\chi_b \to \Upsilon(3S)\gamma$ decays are also investigated. The $\chi_b(3P)$ mass is measured.

1 Introduction

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It is expected that a significant fraction of the production cross-section of J/ψ and Υ states in hadron collisions is due to feed-down from heavier quarkonium states. A study of this effect is important for the interpretation of onia production cross section and polarization measurements in hadron collisions. For P-wave quarkonia, measurements of χ_c have been reported by CDF [?], HERA-B [?] and LHCb [?], whereas CDF [?] and ATLAS [?] have performed measurements involving χ_b states. LHCb has reported [?] a preliminary measurement of the χ_b production cross-section, and subsequent decay into $\Upsilon(1S)$ γ , relative to the $\Upsilon(1S)$ production. This measurement was performed on 2011 data, in a region defined by $6 \text{ GeV}/c < p_T(\Upsilon(1S)) < 15 \text{ GeV}/c$ and 2.0 < y < 4.5.

This note presents an update of the previous LHCb study. Data collected in 2012 were also analyzed, allowing for cross-section measurements at \sqrt{s} =8 TeV. Using the full integrated luminosity allows for a measurement of the differential cross-section in $p_{\rm T}$ and rapidity bins of the $\Upsilon(1S)$, and to study the production of $\chi_b(2P)$ And $\chi_b(3P)$. A measurement of the $\chi_b(3P)$ mass is also performed by combining data collected in 2011 and 2012.

The analysis proceeds through the reconstruction of $\Upsilon(nS)$ candidates via their dimuon decays, and their subsequent pairing with a photon to look for $\chi_b(mP) \to \Upsilon(nS)\gamma$ decays. Ratios of $\chi_b(mP)$ to $\Upsilon(nS)$ production cross section can be written as

$$\frac{\sigma(pp \to \chi_b(mP) \to \Upsilon(nS)\gamma)}{\sigma(pp \to \Upsilon(nS))} = \frac{N_{\chi_b(mP) \to \Upsilon(nS)\gamma}}{N_{\Upsilon(nS)}} \times \frac{\epsilon_{\Upsilon(nS)}}{\epsilon_{\chi_b(mP) \to \Upsilon(nS)\gamma}} = \frac{N_{\chi_b(mP) \to \Upsilon(nS)\gamma}}{N_{\Upsilon(nS)}} \times \frac{1}{\epsilon_{\gamma}^{reco}}$$
(1)

where $N_{\Upsilon(nS)}$ and $N_{\chi_b(mP)\to\Upsilon(nS)\gamma}$ are the $\Upsilon(nS)$ and $\chi_b(mP)$ yields, $\epsilon_{\Upsilon(nS)}$ and $\epsilon_{\chi_b(mP)\to\Upsilon(nS)\gamma}$ are their corresponding selection efficiencies. The latter are the product of geometric acceptance, trigger efficiency and reconstruction efficiency. Since the selection criteria for the two samples differ only in the reconstruction of a photon, the efficiency ratio can be replaced by $1/\epsilon_{\gamma}$, the reconstruction efficiency for the photon from the χ_b decay. Similar expressions may be used to compute differential cross sections in Υ $p_{\rm T}$ and rapidity bins.

2 Data and Monte-Carlo samples

The data sample used in this analysis has been collected by LHCb in 2011 and 2012, at center-of-mass energies of \sqrt{s} =7 TeV and 8 TeV, respectively. For 2011, both Reco12 (?) and Reco14/Stripping 20 samples were used. The former was privately stripped by Vanya (?).

The corresponding integrated luminosities are...

Events are triggered by...

and subsequently stripped by StrippingMicroDSTDiMuonDiMuonIncLine. This line takes StdLooseDiMuon as input, applies requirements on muon momentum, transverse

 36 momentum, track and vertex chisquares, and transverse momentum of the composite 37 particle

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(MINTREE('mu+'==ABSID,PT) > 650.0 *MeV) & (MINTREE('mu+'==ABSID,P)

39 > -8000.0 *MeV) & (MAXTREE('mu+'==ABSID,TRCHI2DOF) < 5.0) & (in_range(
40 3000.0 *MeV, MM, 100000000.0 *MeV)) & (VFASPF(VCHI2PDOF) < 20.0) & (PT >
41 2000.0)
```

and saves the output in MicroDST format. The StdLooseDiMuon list contains pairs of oppositely charged muon from the StdAllLooseMuons list with the additional requirement CombinationCut (ADOCACHI2CUT(30, ")), MotherCut (VFASPF(VCHI2); 25)

Simulated data were produced with 2011 conditions. Six samples of XX million events each were generated, each corresponding to a different decay under study. Table ?? summarizes the various samples used in this analysis.

3 Event Selection criteria

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Pairs of opposite charge tracks are used to form Υ candidates. Both tracks are identified as muons and must originate from a common vertex Put selection criteria here, discuss discriminating variables, put all cuts in a table.

4 Data - Monte Carlo comparison

A comparison of the distribution of the relevant observables used in this analysis was performed on real and simulated data, in order to assess the reliability of Monte Carlo in computing efficiencies. It should be stressed that, since a relative branching fraction is measured, systematic effects cancel at first order.

Combinatorial background has been subtracted in real data by using an *sPlot*technique, where the discriminant distribution is... The resulting signal weights are used to obtain the signal distribution for each relevant variable. These distributions are then compared with simulation, as shown in Figures ??-??. The agreement is generally very good, giving confidence that the Monte Carlo describes correctly the decays under study.

$_{52}$ 5 Determination of Υ yields

The yields of $\Upsilon(1S)$, $\Upsilon(2S)$ and $\Upsilon(3S)$ particles are determined by fitting the dimuon invariant mass distribution. The combinatorial background is described by... The Υ peaks are parameterized with... The α and n parameters of the Crystal Ball function are fixed to... etc... the floating parameters in the fit are... Figure XX and YY show the invariant mass distribution in 2011 and 2012 data, respectively. The event yields and other fit parameters are reported in Table ZZ. The systematic uncertainties in the Υ yields are determined by... They are discussed in ??.

$_{\circ}$ 6 Determination of the χ_b yields

The yields of $\chi_b(1S, 2S, 3S) \to \Upsilon(1S) \gamma$ are determined with fits to the $m(\mu^+\mu^-\gamma)$ – $m(\mu^+\mu^-)$ invariant mass difference. Combinatorial background is described by ..., signal are parametrized with ... Mention how you fix and float the various parameters of this fit... Figure XX and Table YY show the results...

⁵ 7 Determination of selection efficiencies

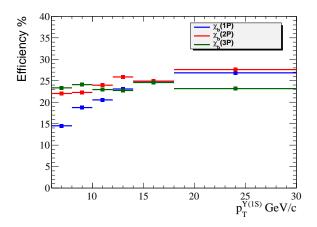


Figure 1: Monte-Carlo data. Fraction of $\Upsilon(1S)$ originating from χ_b decays for different $p_T^{\Upsilon(1S)}$ intervals.

⁶ 8 Determination of the χ_b production cross section

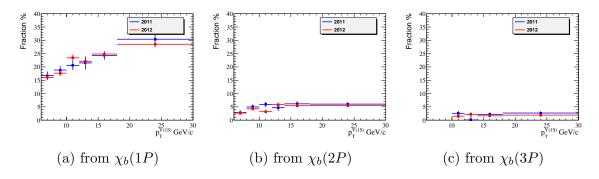


Figure 2: Fraction of $\Upsilon(1S)$ originating from χ_b decays for different $p_T^{\Upsilon(1S)}$ intervals.

- 9 Systematic Uncertainties
- 78 10 Determination of the χ_b masses
- 79 11 Conclusion

Appendices

${f a}$ A Fitting parameters summary

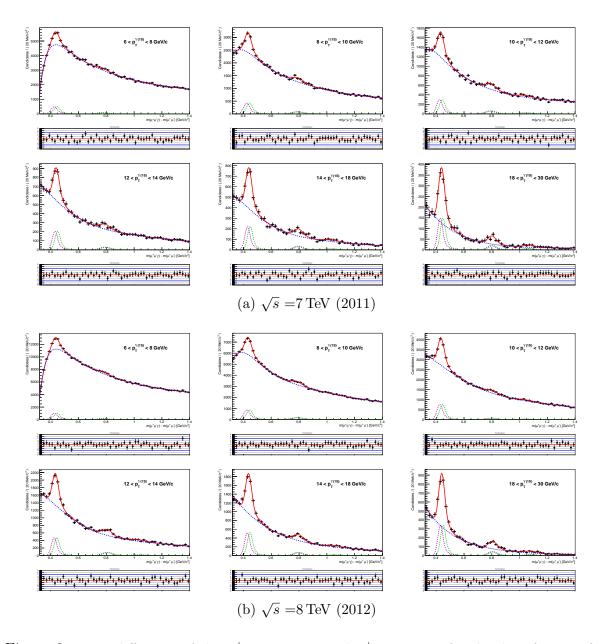


Figure 3: Mass difference of the $\mu^+\mu^-\gamma$ system and $\mu^+\mu^-$ system for the data for specified interval of transverse momentum of the $\Upsilon(1S)$. The red solid line is the result of the fit described in the text. Blue dashed line is the background contribution obtained from the fit. Magenta and green dashed lines are χ_{b1} and χ_{b2} signal contribution obtained from the fit.

Table 1: Summary of fraction determination.

	20/4	α\ .							
	6 - 8	S) transverse mo 8 - 10	10 - 12	12 - 14	14 - 18	18 - 30			
		obtained by fitt:							
$N_{\chi_b(1P)}^{rec}$ $N_{\chi_b(2P)}^{rec}$ $N_{\chi_b(2P)}^{rec}$ $N_{\chi_b(3P)}^{rec}$	3130 ± 280	2610 ± 220	1750 ± 140	1130 ± 130	1190 ± 80	780 ± 40			
$N_{\chi_b(2P)}^{rec}$	820 ± 230	820 ± 150	590 ± 100	280 ± 70	300 ± 50	160 ± 21			
$N_{\chi_h(3P)}^{rec}$			240 ± 90	0 ± 140	100 ± 40	60 ± 15			
$\Delta m_{\chi_{h1}(1P)}$ in MeV/ c^2	425.3 ± 2.1	424.1 ± 1.9	424.0 ± 1.9	430.4 ± 1.9	429.0 ± 1.5	429.3 ± 1.5			
$\Delta m_{\chi_{b1}(2P)}$ in MeV/ c^2	770 ± 12	784 ± 6	787 ± 6	786 ± 13	790 ± 6	796 ± 5			
$\Delta m_{(\chi_{b1}3P)}$ in MeV/ c^2			1040 ± 15	1030 ± 40	1030 ± 40	1059 ± 12			
$N_{\Upsilon(1S)}^{rec}$	$128,900 \pm 400$	$73,940 \pm 320$	$41,390 \pm 230$	$22,790 \pm 170$	$19,660 \pm 160$	9610 ± 110			
	Parameters	obtained by fitt:	ing data distribi	itions $\sqrt{s} = 8 \mathrm{T}$	eV				
$N_{\chi_b(1P)}^{rec}$	6500 ± 400	5380 ± 320	4410 ± 230	2610 ± 140	2800 ± 110	1800 ± 70			
$N_{\chi_b(2P)}^{rec}$	1600 ± 400	1550 ± 230	700 ± 150	780 ± 100	610 ± 70	355 ± 35			
$N_{\chi_b(3P)}^{rec}$			320 ± 150	250 ± 90	180 ± 60	104 ± 22			
$\Delta m_{\chi_{b1}(1P)}$ in MeV/ c^2	426.0 ± 1.6	425.4 ± 1.4	425.9 ± 1.1	424.3 ± 1.2	427.6 ± 1.0	430.6 ± 1.0			
$\Delta m_{\chi_{b1}(2P)}$ in MeV/ c^2	775 ± 9	782 ± 6	795 ± 9	801 ± 5	790 ± 4	801 ± 4			
$\Delta m_{(\chi_{b1}3P)}$ in MeV/ c^2			1043 ± 19	1031 ± 27	1061 ± 16	1074 ± 4			
$N_{\Upsilon(1S)}^{rec}$	$277,000 \pm 600$	$162,500 \pm 500$	$91,610 \pm 350$	$51,270 \pm 260$	$45,350 \pm 240$	$23,540 \pm 18$			
	Parameters obta	ined by counting	MC matched e	vents for $\chi_{b1}(1F$) decay				
	6172	5345	3653	2266	2131	1113			
$N_{\chi_{b1}(1P)}^{MC}$ $N_{\Upsilon(1S)}^{MC}$ $\varepsilon_{\mu\nu}^{MC}$ $\%$	42,587	28,398	17,078	9632	8237	3922			
$\varepsilon_{\chi_{b1}(1P)}^{I(1S)}$ %	14.5	18.8	21.4	23.5	25.9	28.4			
Parameters obtained by counting MC matched events for $\chi_{b2}(1P)$ decay									
	4327	2676	1298	645	467	164			
$\chi_{b2}(1P)$ χMC	29,792	14,325	6594	2850	1952	648			
_MC 07	14.5	18.7	19.7	22.6	23.9	25.3			
$\chi_{b2}(1F)$						20.0			
	Parameters obta 4648		2041			524			
$\chi_{b1}(2P)$		3273		1155	1016				
$N^{MC}_{\chi_{b1}(2P)}$ $N^{MC}_{\Upsilon(1S)}$ $\in {}^{MC}_{Y_{b1}(2P)}$ $\%$	20,091	13,810	8176	4426	3974	1898			
A81(=-)	23.1	23.7	25.0	26.1	25.6	27.6			
	Parameters obta								
$N_{\chi_{b2}(2P)}^{MC}$	3712	1712	848	431	269	106			
$N_{\Upsilon(1S)}^{MC}$	17,731	8212	3694	1679	1110	384			
$N_{\chi_{b_{2}(2P)}}^{MC}$ $N_{\Upsilon(1S)}^{MC}$ $\varepsilon_{\chi_{b_{2}(2P)}}^{MC}$ %	20.9	20.8	23.0	25.7	24.2	27.6			
Parameters obtained by counting MC matched events for ($v_{ij}3P$) decay									
$N_{(\gamma_b,3P)}^{MC}$	4629	3120	1772	1066	884	415			
$N_{(\chi_{b1}3P)}^{MC}$ $N_{\Upsilon(1S)}^{MC}$ M_{C}^{MC}	18,486	12,359	7298	4174	3581	1646			
$\varepsilon_{(\chi_{b1}3P)}^{MC}$ %	25.0	25.2	24.3	25.5	24.7	25.2			
	Parameters obta	ined by counting	MC matched e	vents for $\chi_{k2}(3F)$	e) decay				
	2598	1282	524	223	192	49			
N_{MC}^{MC}	12,003	5587	2425	1119	784	232			
$N_{\chi_{b2}(3P)}^{MC}$ $N_{\Upsilon(1S)}^{MC}$ $\varepsilon_{\chi_{b2}(3P)}^{MC}$	21.6	22.9	21.6	19.9	24.5	21.1			
$\varepsilon_{\chi_{b2}(3P)}^{m}$ %					24.0	21.1			
Average MC efficiency of χ_{b1} and χ_{b2} MeV/ c^2 in % $\varepsilon_{0.0}^{MC}$ 14.5 18.8 20.5 23.1 24.9 26.8									
$\varepsilon_{\chi_b(1P)}^{m}$ ε_{MC}^{mC}	22.0	22.3	24.0	25.9	24.9	27.6			
$\chi_b(2P)$ MC	23.3	24.1	22.9	22.7	24.6	23.2			
$\varepsilon_{\chi_b(3P)}$						23.2			
Parameters obtained by fitting MC distributions in MeV/ c^2									
$\Delta m_{\chi_{b1}(1P)}$	428.18 ± 0.34	427.5 ± 0.4	427.3 ± 0.4	427.2 ± 0.5	427.4 ± 0.5	428.0 ± 0.6			
$\Delta m_{\chi_{b2}(1P)}$ $\Delta m_{\chi_{b2}(1P)}$	448.2 ± 0.5 786.4 ± 0.6	447.2 ± 0.6 786.5 ± 0.7	447.3 ± 0.7 786 7 ± 0.0	447.0 ± 0.9 786.5 ± 1.0	446.1 ± 1.1 780.0 ± 1.0	446.1 ± 1.4 700.2 ± 1.3			
$\Delta m_{\chi_{b1}(2P)}$ $\Delta m_{\chi_{b1}(2P)}$	180.4 ± 0.6 800.8 ± 0.7	786.5 ± 0.7 800.9 ± 1.0	786.7 ± 0.9 799.5 ± 1.2	786.5 ± 1.0 802.5 ± 1.7	789.0 ± 1.0 799.9 ± 1.9	790.2 ± 1.3 802.8 ± 3.2			
$\Delta m_{\chi_{b2}(2P)}$ Δm_{-}	1046.2 ± 0.7	1046.8 ± 0.8	199.3 ± 1.2 1047.9 ± 1.0	1047.4 ± 1.3	1049.5 ± 1.3	1050.9 ± 1.9			
	1040.2 ± 0.7	10-10.0 ± 0.0		1047.4 ± 1.3 1059.6 ± 2.8	1049.9 ± 1.3 1063.9 ± 2.8	$1050.9 \pm 1.$ 1061 ± 7			
$\Delta m_{(\chi_{b1}3P)}$ $\Delta m_{rec(2P)}$	1058.0 ± 1.0	1055.9 ± 1.9							
$\Delta m_{\chi_{b2}(3P)}$	1058.0 ± 1.0 23.14 ± 0.35	1055.9 ± 1.2 22.3 ± 0.4	1058.1 ± 2.1 21.1 ± 0.4						
$\frac{\Delta m_{\chi_{b2}(3P)}}{\sigma_{\chi_{b1}(1P)}}$	23.14 ± 0.35	22.3 ± 0.4	21.1 ± 0.4	19.9 ± 0.5	19.4 ± 0.5	19.0 ± 0.6			
$\frac{\Delta m_{\chi_{b2}(3P)}}{\sigma_{\chi_{b1}(1P)}}$ $\sigma_{\chi_{b2}(1P)}$	23.14 ± 0.35 24.2 ± 0.5	22.3 ± 0.4 23.3 ± 0.6	21.1 ± 0.4 21.4 ± 0.7	19.9 ± 0.5 20.7 ± 1.0	19.4 ± 0.5 22.4 ± 0.9	19.0 ± 0.6 15.8 ± 1.3			
$\Delta m_{\chi_{b2}(3P)}$ $\sigma_{\chi_{b1}(1P)}$ $\sigma_{\chi_{b2}(1P)}$ $\sigma_{\chi_{b2}(2P)}$	23.14 ± 0.35 24.2 ± 0.5 34.2 ± 0.8	22.3 ± 0.4 23.3 ± 0.6 33.5 ± 0.8	21.1 ± 0.4 21.4 ± 0.7 32.9 ± 1.0	19.9 ± 0.5 20.7 ± 1.0 32.3 ± 0.8	19.4 ± 0.5 22.4 ± 0.9 30.7 ± 0.8	19.0 ± 0.6 15.8 ± 1.3 29.2 ± 1.2			
$\Delta m_{\chi_{b2}(3P)}$ $\sigma_{\chi_{b1}(1P)}$ $\sigma_{\chi_{b2}(1P)}$ $\sigma_{\chi_{b2}(1P)}$ $\sigma_{\chi_{b1}(2P)}$ $\sigma_{\chi_{b2}(2P)}$	23.14 ± 0.35 24.2 ± 0.5 34.2 ± 0.8 37.5 ± 0.7	$\begin{array}{c} 22.3 \pm 0.4 \\ 23.3 \pm 0.6 \\ 33.5 \pm 0.8 \\ 33.5 \pm 1.1 \end{array}$	$\begin{array}{c} 21.1 \pm 0.4 \\ 21.4 \pm 0.7 \\ 32.9 \pm 1.0 \\ 32.6 \pm 1.0 \end{array}$	19.9 ± 0.5 20.7 ± 1.0 32.3 ± 0.8 33.1 ± 1.5	19.4 ± 0.5 22.4 ± 0.9 30.7 ± 0.8 31.6 ± 1.5	19.0 ± 0.6 15.8 ± 1.3 29.2 ± 1.2 32.1 ± 2.6			
$\begin{array}{c} \Delta m_{\chi_{b2}(3P)} \\ \sigma_{\chi_{b1}(1P)} \\ \sigma_{\chi_{b2}(1P)} \\ \sigma_{\chi_{b1}(2P)} \\ \sigma_{\chi_{b1}(2P)} \\ \sigma_{\chi_{b2}(2P)} \\ \sigma_{(\chi_{b1}3P)} \end{array}$	23.14 ± 0.35 24.2 ± 0.5 34.2 ± 0.8 37.5 ± 0.7 47.2 ± 0.6	$\begin{array}{c} 22.3 \pm 0.4 \\ 23.3 \pm 0.6 \\ 33.5 \pm 0.8 \\ 33.5 \pm 1.1 \\ 45.9 \pm 0.7 \end{array}$	21.1 ± 0.4 21.4 ± 0.7 32.9 ± 1.0 32.6 ± 1.0 43.4 ± 0.9	19.9 ± 0.5 20.7 ± 1.0 32.3 ± 0.8 33.1 ± 1.5 43.3 ± 1.1	19.4 ± 0.5 22.4 ± 0.9 30.7 ± 0.8 31.6 ± 1.5 42.3 ± 1.0	19.0 ± 0.6 15.8 ± 1.3 29.2 ± 1.2 32.1 ± 2.6 40.2 ± 1.5			
$\begin{array}{c} \Delta m_{\chi_{b2}(3P)} \\ \sigma_{\chi_{b1}(1P)} \\ \sigma_{\chi_{b2}(1P)} \\ \sigma_{\chi_{b2}(1P)} \\ \sigma_{\chi_{b1}(2P)} \\ \sigma_{\chi_{b2}(2P)} \\ \sigma_{(\chi_{b1}3P)} \end{array}$	23.14 ± 0.35 24.2 ± 0.5 34.2 ± 0.8 37.5 ± 0.7 47.2 ± 0.6 49.0 ± 0.9	22.3 ± 0.4 23.3 ± 0.6 33.5 ± 0.8 33.5 ± 1.1 45.9 ± 0.7 42.0 ± 1.2	21.1 ± 0.4 21.4 ± 0.7 32.9 ± 1.0 32.6 ± 1.0 43.4 ± 0.9 43.1 ± 2.1	19.9 ± 0.5 20.7 ± 1.0 32.3 ± 0.8 33.1 ± 1.5 43.3 ± 1.1 40.2 ± 3.0	19.4 ± 0.5 22.4 ± 0.9 30.7 ± 0.8 31.6 ± 1.5	19.0 ± 0.6 15.8 ± 1.3 29.2 ± 1.2 32.1 ± 2.6			
$\Delta m_{\chi_{b2}(3P)}$ $\sigma_{\chi_{b1}(1P)}$ $\sigma_{\chi_{b2}(1P)}$ $\sigma_{\chi_{b2}(1P)}$ $\sigma_{\chi_{b1}(2P)}$ $\sigma_{\chi_{b1}(2P)}$ $\sigma_{\chi_{b2}(3P)}$ $\sigma_{\chi_{b2}(3P)}$	23.14 ± 0.35 24.2 ± 0.5 34.2 ± 0.8 37.5 ± 0.7 47.2 ± 0.6 49.0 ± 0.9	22.3 ± 0.4 23.3 ± 0.6 33.5 ± 0.8 33.5 ± 1.1 45.9 ± 0.7 42.0 ± 1.2 Fraction of $\Upsilon(1.5)$	21.1 ± 0.4 21.4 ± 0.7 32.9 ± 1.0 32.6 ± 1.0 43.4 ± 0.9 43.1 ± 2.1 8) in % for $\sqrt{s} = \frac{1}{2}$	19.9 ± 0.5 20.7 ± 1.0 32.3 ± 0.8 33.1 ± 1.5 43.3 ± 1.1 40.2 ± 3.0 $= 7 \text{ TeV}$	19.4 ± 0.5 22.4 ± 0.9 30.7 ± 0.8 31.6 ± 1.5 42.3 ± 1.0 38.1 ± 2.4	19.0 ± 0.6 15.8 ± 1.3 29.2 ± 1.2 32.1 ± 2.6 40.2 ± 1.5 41 ± 6			
$\Delta m_{(\chi_{b1}3P)}$ $\Delta m_{\chi_{b2}(3P)}$ $\Delta m_{\chi_{b2}(3P)}$ $\sigma_{\chi_{b1}(1P)}$ $\sigma_{\chi_{b1}(2P)}$ $\sigma_{\chi_{b1}(2P)}$ $\sigma_{\chi_{b1}(2P)}$ $\sigma_{\chi_{b2}(2P)}$ $\sigma_{\chi_{b2}(3P)}$ $\sigma_{\chi_{b2}(3P)}$ from $\chi_{b}(1P)$ from $\chi_{b}(2P)$	23.14 ± 0.35 24.2 ± 0.5 34.2 ± 0.8 37.5 ± 0.7 47.2 ± 0.6 49.0 ± 0.9 16.8 ± 1.5	$\begin{array}{c} 22.3 \pm 0.4 \\ 23.3 \pm 0.6 \\ 33.5 \pm 0.8 \\ 33.5 \pm 1.1 \\ 45.9 \pm 0.7 \\ 42.0 \pm 1.2 \\ \hline \text{Fraction of } \varUpsilon(18) \\ 18.8 \pm 1.6 \end{array}$	$\begin{array}{c} 21.1 \pm 0.4 \\ 21.4 \pm 0.7 \\ 32.9 \pm 1.0 \\ 32.6 \pm 1.0 \\ 43.4 \pm 0.9 \\ 43.1 \pm 2.1 \\ \hline s) \text{ in } \% \text{ for } \sqrt{s} = \\ 20.6 \pm 1.7 \end{array}$	19.9 ± 0.5 20.7 ± 1.0 32.3 ± 0.8 33.1 ± 1.5 43.3 ± 1.1 40.2 ± 3.0 $= 7 \text{ TeV}$ 21.5 ± 2.4	19.4 ± 0.5 22.4 ± 0.9 30.7 ± 0.8 31.6 ± 1.5 42.3 ± 1.0 38.1 ± 2.4 24.3 ± 1.6	19.0 ± 0.6 15.8 ± 1.3 29.2 ± 1.2 32.1 ± 2.6 40.2 ± 1.5 41 ± 6 30.4 ± 1.7			
$\Delta m_{\chi_{b2}(3P)}$ $\sigma_{\chi_{b1}(1P)}$ $\sigma_{\chi_{b2}(1P)}$ $\sigma_{\chi_{b2}(2P)}$ $\sigma_{\chi_{b2}(2P)}$ $\sigma_{\chi_{b2}(2P)}$ $\sigma_{\chi_{b3}(3P)}$ from $\chi_{b}(1P)$ from $\chi_{b}(2P)$	23.14 ± 0.35 24.2 ± 0.5 34.2 ± 0.8 37.5 ± 0.7 47.2 ± 0.6 49.0 ± 0.9	22.3 ± 0.4 23.3 ± 0.6 33.5 ± 0.8 33.5 ± 1.1 45.9 ± 0.7 42.0 ± 1.2 Fraction of $\Upsilon(1.5)$	21.1 ± 0.4 21.4 ± 0.7 32.9 ± 1.0 32.6 ± 1.0 43.4 ± 0.9 43.1 ± 2.1 $5) \text{ in } \% \text{ for } \sqrt{s} = \frac{20.6 \pm 1.7}{5.9 \pm 1.0}$	19.9 ± 0.5 20.7 ± 1.0 32.3 ± 0.8 33.1 ± 1.5 43.3 ± 1.1 40.2 ± 3.0 $= 7 \text{ TeV}$ 21.5 ± 2.4 4.7 ± 1.3	19.4 ± 0.5 22.4 ± 0.9 30.7 ± 0.8 31.6 ± 1.5 42.3 ± 1.0 38.1 ± 2.4 24.3 ± 1.6 6.1 ± 0.9	19.0 ± 0.6 15.8 ± 1.3 29.2 ± 1.2 32.1 ± 2.6 40.2 ± 1.5 41 ± 6 30.4 ± 1.7 6.0 ± 0.8			
$\Delta m_{\chi_{b2}(3P)}$ $\sigma_{\chi_{b1}(1P)}$ $\sigma_{\chi_{b2}(1P)}$ $\sigma_{\chi_{b2}(2P)}$ $\sigma_{\chi_{b2}(2P)}$ $\sigma_{\chi_{b2}(2P)}$ $\sigma_{\chi_{b3}(3P)}$ from $\chi_{b}(1P)$ from $\chi_{b}(2P)$	23.14 ± 0.35 24.2 ± 0.5 34.2 ± 0.8 37.5 ± 0.7 47.2 ± 0.6 49.0 ± 0.9 16.8 ± 1.5 2.9 ± 0.8	$\begin{array}{c} 22.3 \pm 0.4 \\ 23.3 \pm 0.6 \\ 33.5 \pm 0.8 \\ 33.5 \pm 1.1 \\ 45.9 \pm 0.7 \\ 42.0 \pm 1.2 \\ \hline \text{Fraction of } \varUpsilon (1S) \\ 18.8 \pm 1.6 \\ 5.0 \pm 0.9 \\ \end{array}$	21.1 ± 0.4 21.4 ± 0.7 32.9 ± 1.0 32.6 ± 1.0 43.4 ± 0.9 43.1 ± 2.1 $5) \text{ in } \% \text{ for } \sqrt{s} = 20.6 \pm 1.7$ 5.9 ± 1.0 2.6 ± 0.9	19.9 ± 0.5 20.7 ± 1.0 32.3 ± 0.8 33.1 ± 1.5 43.3 ± 1.1 40.2 ± 3.0 $= 7 \text{ TeV}$ 21.5 ± 2.4 4.7 ± 1.3 0.1 ± 2.7	19.4 ± 0.5 22.4 ± 0.9 30.7 ± 0.8 31.6 ± 1.5 42.3 ± 1.0 38.1 ± 2.4 24.3 ± 1.6	19.0 ± 0.6 15.8 ± 1.3 29.2 ± 1.2 32.1 ± 2.6 40.2 ± 1.5 41 ± 6 30.4 ± 1.7			
$ \Delta m_{\chi_{b2}(3P)} $ $ \sigma_{\chi_{b1}(1P)} $ $ \sigma_{\chi_{b1}(2P)} $ $ \sigma_{\chi_{b2}(2P)} $ $ \sigma_{\chi_{b2}(2P)} $ $ \sigma_{\chi_{b2}(2P)} $ $ \sigma_{\chi_{b2}(3P)} $ $ \sigma_{\chi_{b2}(3P)} $ $ from \chi_{b}(1P) $ $ from \chi_{b}(2P) $ $ from \chi_{b}(3P) $	23.14 ± 0.35 24.2 ± 0.5 34.2 ± 0.8 37.5 ± 0.7 47.2 ± 0.6 49.0 ± 0.9 16.8 ± 1.5 2.9 ± 0.8	$\begin{array}{c} 22.3 \pm 0.4 \\ 23.3 \pm 0.6 \\ 33.5 \pm 0.8 \\ 33.5 \pm 1.1 \\ 45.9 \pm 0.7 \\ 42.0 \pm 1.2 \\ \hline \text{Fraction of } \varUpsilon(1.5) \\ 18.8 \pm 1.6 \\ 5.0 \pm 0.9 \\ \hline \end{array}$	21.1 ± 0.4 21.4 ± 0.7 32.9 ± 1.0 32.6 ± 1.0 43.4 ± 0.9 43.1 ± 2.1 $5) \text{ in } \% \text{ for } \sqrt{s} = \frac{20.6 \pm 1.7}{2.6 \pm 0.9}$ $6) \text{ in } \% \text{ for } \sqrt{s} = \frac{3.0 \pm 1.0}{2.6 \pm 0.9}$ 2.6 ± 0.9 2.6 ± 0.9 2.6 ± 0.9	$\begin{array}{c} 19.9 \pm 0.5 \\ 20.7 \pm 1.0 \\ 32.3 \pm 0.8 \\ 33.1 \pm 1.5 \\ 43.3 \pm 1.1 \\ 40.2 \pm 3.0 \\ \hline = 7 \text{TeV} \\ 21.5 \pm 2.4 \\ 4.7 \pm 1.3 \\ 0.1 \pm 2.7 \\ \hline = 8 \text{TeV} \end{array}$	19.4 ± 0.5 22.4 ± 0.9 30.7 ± 0.8 31.6 ± 1.5 42.3 ± 1.0 38.1 ± 2.4 24.3 ± 1.6 6.1 ± 0.9 2.1 ± 0.8	19.0 ± 0.6 15.8 ± 1.3 29.2 ± 1.2 32.1 ± 2.6 40.2 ± 1.5 41 ± 6 30.4 ± 1.7 6.0 ± 0.8 2.7 ± 0.7			
$\Delta m_{\chi_{b2}(3P)}$ $\sigma_{\chi_{b1}(1P)}$ $\sigma_{\chi_{b2}(1P)}$ $\sigma_{\chi_{b2}(2P)}$ $\sigma_{\chi_{b2}(2P)}$ $\sigma_{\chi_{b2}(2P)}$ $\sigma_{\chi_{b3}(3P)}$ from $\chi_{b}(1P)$ from $\chi_{b}(2P)$	23.14 ± 0.35 24.2 ± 0.5 34.2 ± 0.8 37.5 ± 0.7 47.2 ± 0.6 49.0 ± 0.9 16.8 ± 1.5 2.9 ± 0.8	$\begin{array}{c} 22.3 \pm 0.4 \\ 23.3 \pm 0.6 \\ 33.5 \pm 0.8 \\ 33.5 \pm 1.1 \\ 45.9 \pm 0.7 \\ 42.0 \pm 1.2 \\ \hline \text{Fraction of } \varUpsilon (1S) \\ 18.8 \pm 1.6 \\ 5.0 \pm 0.9 \\ \end{array}$	21.1 ± 0.4 21.4 ± 0.7 32.9 ± 1.0 32.6 ± 1.0 43.4 ± 0.9 43.1 ± 2.1 $5) \text{ in } \% \text{ for } \sqrt{s} = 20.6 \pm 1.7$ 5.9 ± 1.0 2.6 ± 0.9	19.9 ± 0.5 20.7 ± 1.0 32.3 ± 0.8 33.1 ± 1.5 43.3 ± 1.1 40.2 ± 3.0 $= 7 \text{ TeV}$ 21.5 ± 2.4 4.7 ± 1.3 0.1 ± 2.7	19.4 ± 0.5 22.4 ± 0.9 30.7 ± 0.8 31.6 ± 1.5 42.3 ± 1.0 38.1 ± 2.4 24.3 ± 1.6 6.1 ± 0.9	19.0 ± 0.6 15.8 ± 1.3 29.2 ± 1.2 32.1 ± 2.6 40.2 ± 1.5 41 ± 6 30.4 ± 1.7 6.0 ± 0.8			

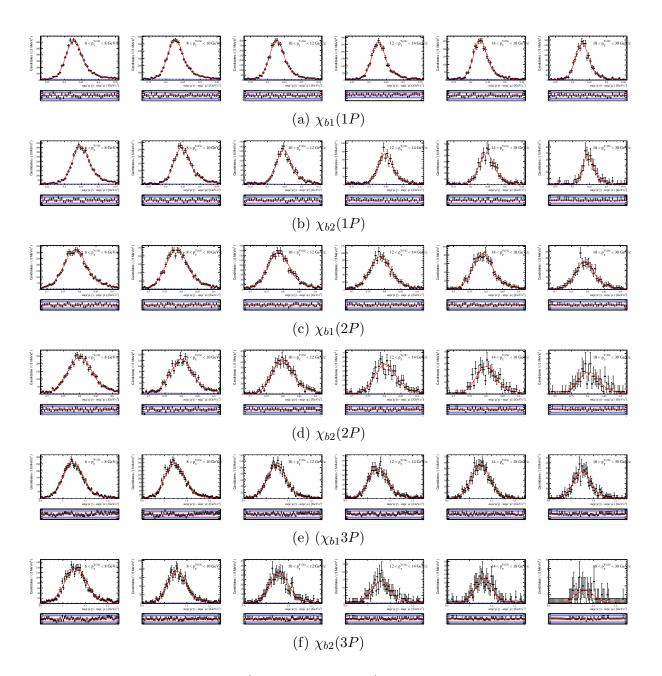


Figure 4: Mass difference of the $\mu^+\mu^-\gamma$ system and $\mu^+\mu^-$ system for the Monte Carlo data for specified interval of transverse momentum of the $\Upsilon(1S)$. The red solid line is the result of the fit described in the text.