

# refinemesh

Refine triangular mesh

**⚠** This page describes the legacy workflow. New features might not be compatible with the legacy workflow. For the corresponding step in the recommended workflow, see [generateMesh](#).

## Syntax

```
[p1,e1,t1] = refinemesh(g,p,e,t)
[p1,e1,t1,u1] = refinemesh(g,p,e,t,u)
[ ___ ] = refinemesh( ___,it)
[ ___ ] = refinemesh( ___, 'longest')
```

## Description



### Note

This function does not support quadratic 2-D elements.

[example](#)

`[p1,e1,t1] = refinemesh(g,p,e,t)` returns a refined version of the triangular mesh given by the mesh data `p`, `e`, and `t`. For details on the mesh data representation, see [Mesh Data as \[p,e,t\] Triples](#).

`[p1,e1,t1,u1] = refinemesh(g,p,e,t,u)` refines the mesh and extends the solution `u` to the new mesh nodes by linear interpolation. The number of rows in `u` must correspond to the number of columns in `p`, and `u1` has as many rows as there are points in `p1`.

`refinemesh` interpolates each column of `u` separately.

`[ ___ ] = refinemesh( ___,it)` uses the input and output arguments from the previous syntaxes and specifies the list `it` of geometric faces or triangles to refine. A scalar or a row vector specifies faces. A column vector specifies triangles.

[example](#)

`[ ___ ] = refinemesh( ___, 'longest')` uses the longest edge refinement, where the longest edge of each triangle is bisected. By default, `refinemesh` uses the regular refinement, where all triangles are divided into four triangles of the same shape. You also can explicitly specify 'regular' instead of 'longest'. If you use a column vector `it` to specify the triangles to refine, then `refinemesh` can refine some triangles outside of the specified set to preserve the triangulation and its quality.

## Examples

[collapse all](#)



### Mesh Refinement

Refine the mesh of the L-shaped membrane several times.  
Plot the initial mesh and refined meshes at each step.

[Open Live Script](#)

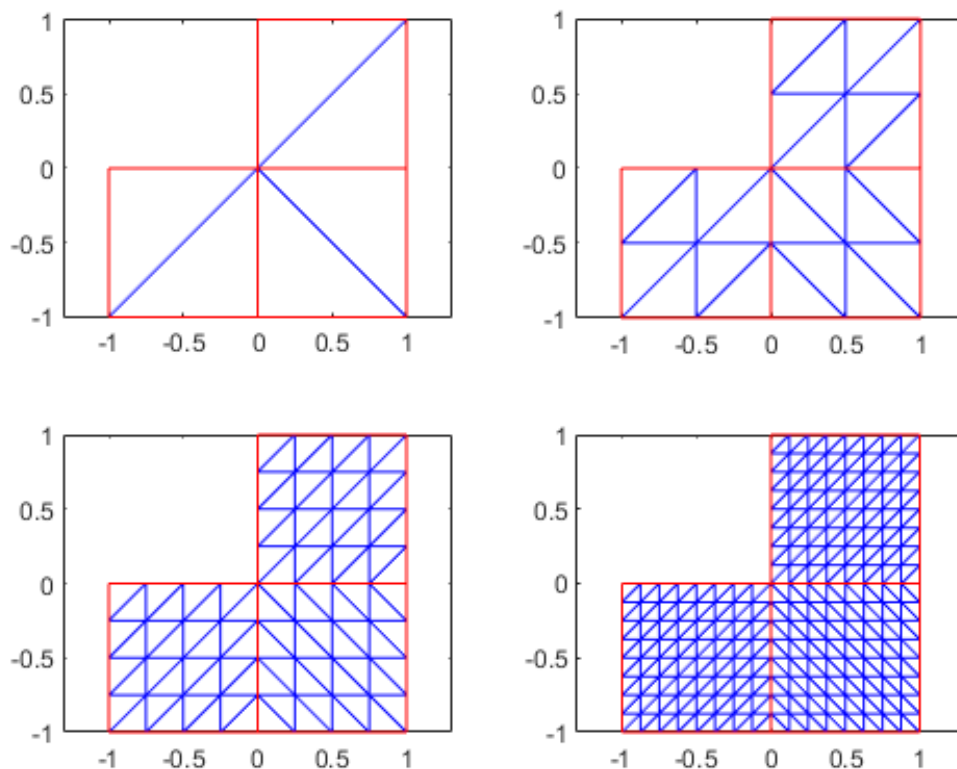
```
[p,e,t] = initmesh('lshaped','Hmax',Inf);
subplot(2,2,1)
```

```
pdemesh(p,e,t)
```

```
[p,e,t] = refinemesh('lshaped',p,e,t);  
subplot(2,2,2)  
pdemesh(p,e,t)
```

```
[p,e,t] = refinemesh('lshaped',p,e,t);  
subplot(2,2,3)  
pdemesh(p,e,t)
```

```
[p,e,t] = refinemesh('lshaped',p,e,t);  
subplot(2,2,4)  
pdemesh(p,e,t)
```



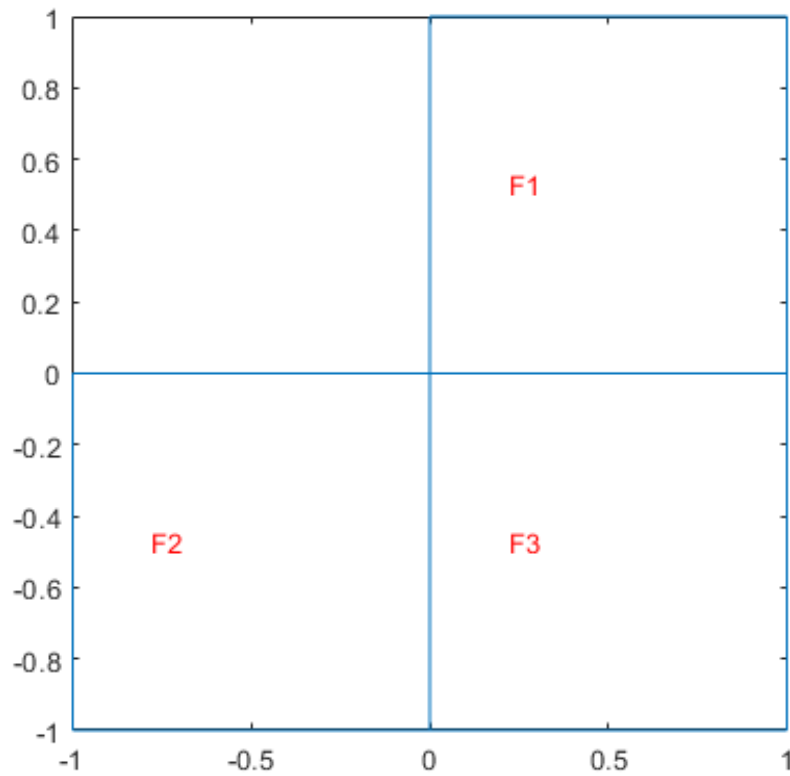
## Mesh Refinement for Specified Faces

Refine the mesh for a particular face of the L-shaped membrane.

[Open Live Script](#)

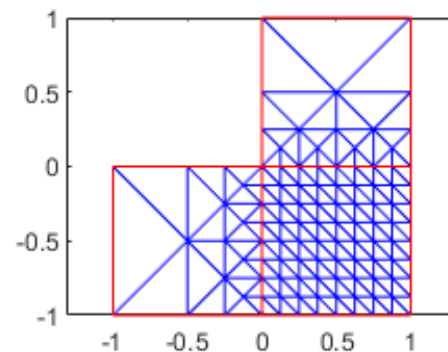
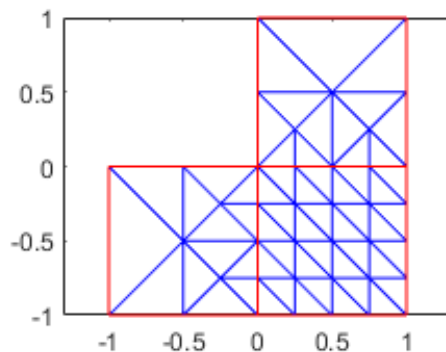
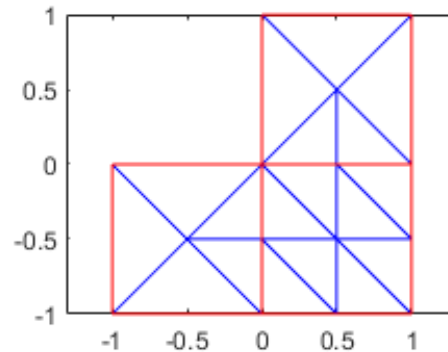
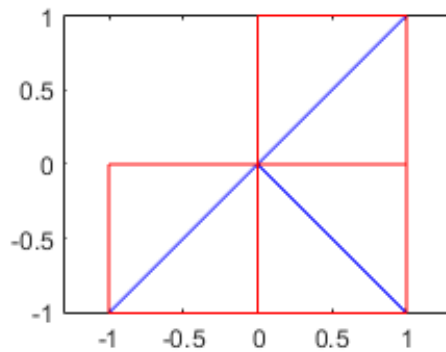
Plot the L-shaped membrane to identify the face numbers.

```
pdgplot('lshaped','FaceLabels','on')
```



Create the initial mesh for the entire geometry, then refine the mesh for face 3 several times. Plot the initial mesh and refined meshes at each step.

```
[p,e,t] = initmesh('lshapedeg', 'Hmax', Inf);  
subplot(2,2,1)  
pdemesh(p,e,t)  
  
[p,e,t] = refinemesh('lshapedeg', p,e,t,3);  
subplot(2,2,2)  
pdemesh(p,e,t)  
  
[p,e,t] = refinemesh('lshapedeg', p,e,t,3);  
subplot(2,2,3)  
pdemesh(p,e,t)  
  
[p,e,t] = refinemesh('lshapedeg', p,e,t,3);  
subplot(2,2,4)  
pdemesh(p,e,t)
```



## Input Arguments

[collapse all](#)

### ✓ **g — Geometry description**

decomposed geometry matrix | geometry function | handle to geometry function

Geometry description, specified as a decomposed geometry matrix, a geometry function, or a handle to the geometry function. For details about a decomposed geometry matrix, see [decsg](#). For details about a geometry function, see [Parametrized Function for 2-D Geometry Creation](#).

A geometry function must return the same result for the same input arguments in every function call. Thus, it must not contain functions and expressions designed to return a variety of results, such as random number generators.

**Data Types:** double | char | string | function\_handle

### ✓ **p — Mesh points**

2-by-Np matrix

Mesh points, specified as a 2-by-Np matrix. Np is the number of points (nodes) in the mesh. Column k of p consists of the x-coordinate of point k in p(1,k) and the y-coordinate of point k in p(2,k). For details, see [Mesh Data as \[p,e,t\] Triples](#).

### ✓ **e — Mesh edges**

7-by-Ne matrix

Mesh edges, specified as a 7-by-Ne matrix, where Ne is the number of edges in the mesh. An edge is a pair of points in p containing a boundary between subdomains, or containing an outer boundary. For details, see [Mesh Data as \[p,e,t\] Triples](#).

✓ **t — Mesh elements**

4-by-Nt matrix

Mesh elements, specified as a 4-by-Nt matrix. Nt is the number of triangles in the mesh.

The  $t(i,k)$ , with  $i$  ranging from 1 through  $\text{end} - 1$ , contain indices to the corner points of element  $k$ . For details, see [Mesh Data as \[p,e,t\] Triples](#). The last row,  $t(\text{end},k)$ , contains the subdomain number of the element.

✓ **u — PDE solution**

vector

PDE solution, specified as a vector.

- If the PDE is scalar, meaning that it has only one equation, then  $u$  is a column vector representing the solution  $u$  at each node in the mesh.
- If the PDE is a system of  $N > 1$  equations, then  $u$  is a column vector with  $N \times N_p$  elements, where  $N_p$  is the number of nodes in the mesh. The first  $N_p$  elements of  $u$  represent the solution of equation 1, the next  $N_p$  elements represent the solution of equation 2, and so on.

✓ **it — Faces or triangles to refine**

positive number | vector of positive numbers

Faces or triangles to refine, specified as a positive number or a row or column vector of positive numbers. A scalar or a row vector specifies faces. A column vector specifies triangles.

## Output Arguments

[collapse all](#)

✓ **p1 — Refined mesh points**

2-by-Np matrix

Refined mesh points, returned as a 2-by-Np matrix. Np is the number of points (nodes) in the mesh. Column  $k$  of  $p$  consists of the  $x$ -coordinate of point  $k$  in  $p(1,k)$  and the  $y$ -coordinate of point  $k$  in  $p(2,k)$ . For details, see [Mesh Data as \[p,e,t\] Triples](#).

✓ **e1 — Refined mesh edges**

7-by-Ne matrix

Refined mesh edges, returned as a 7-by-Ne matrix, where Ne is the number of edges in the mesh. An edge is a pair of points in p containing a boundary between subdomains, or containing an outer boundary. For details, see [Mesh Data as \[p,e,t\] Triples](#).

✓ **t1 — Refined mesh elements**

4-by-Nt matrix

Refined mesh elements, returned as a 4-by-Nt matrix. Nt is the number of triangles in the mesh.

The  $t(i,k)$ , with  $i$  ranging from 1 through end-1, contain indices to the corner points of element  $k$ . For details, see [Mesh Data as \[p,e,t\] Triples](#). The last row,  $t(end,k)$ , contains the subdomain number of the element.

✓ **u1 — PDE solution**

vector

PDE solution, returned as a vector.

- If the PDE is scalar, meaning that it has only one equation, then u1 is a column vector representing the solution  $u1$  at each node in the mesh.
- If the PDE is a system of  $N > 1$  equations, then u1 is a column vector with  $N*Np$  elements, where  $Np$  is the number of nodes in the mesh. The first  $Np$  elements of u1 represent the solution of equation 1, the next  $Np$  elements represent the solution of equation 2, and so on.

## Algorithms

The refinement algorithm follows these steps:

1. Pick the initial set of triangles to refine.
2. Divide all edges of the selected triangles in half (regular refinement) or divide the longest edge in half (longest edge refinement).
3. Divide the longest edge of any triangle that has a divided edge.
4. Repeat step 3 until no more edges are divided.
5. Introduce new points of all divided edges, and replace all divided entries in e by two new entries.
6. Form the new triangles. If all three sides are divided, new triangles are formed by joining the side midpoints. If two sides are divided, the midpoint of the longest edge is joined with the opposing corner and with the other midpoint. If only the longest edge is divided, its midpoint is joined with the opposing corner.

## See Also

[initmesh](#)

## Topics

[Mesh Data as \[p,e,t\] Triples](#)

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**Introduced before R2006a**

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