

Hon Pre-Calculus Quiz Algebra Review

Name ~~XXXXXXXXXX~~

Show All Work!!!! No Calculators!!! Circle All Final Answers!!!

45/50

Short Answer

1. Factor Completely.:

$$16b^2 + 60b - 100$$

$$4(4b^2 + 15b - 25)$$

$$4(4b^2 + 20b - 5b - 25)$$

$$4(4b(b+5) - 5(b+5))$$

$$4(4b-5)(b+5)$$

2. Factor Completely.:

$$343b^2 - 7b^4$$

$$7b^2(49 - b^2)$$

$$7b^2(7b+b)(7b-b)$$

$$7b^2(7b+b)(7b-b)$$

3. Factor Completely.:

$$x^{2n} + 9x^n - 10$$

$$(x^n - 1)(x^n + 10)$$

4. Factor Completely.:

$$5nu^8 - 15nu^4 + 40n$$

$$5n(u^8 - 3u^4 + 8)$$

$$5n(u^8 - 3u^4 + 8)$$

5. Factor Completely.:

$$5x^4 - 9x^2 + 4$$

$$5x^4 - 5x^2 - 4x^2 + 4$$

$$5x^2(x^2 - 1) - 4(x^2 - 1)$$

$$(5x^2 - 4)(x^2 - 1)$$

$$(5x+2)(5x-2)(x+1)(x-1)$$

6. Factor Completely.:

$$16x^2c + 8xyd - 16x^2d - 8xyc$$

$$16x^2c - 16x^2d - 8xyc + 8xyd$$

$$16x^2(c-d) - 8xy(c-d)$$

$$(16x^2 - 8xy)(c-d)$$

$$8x(2x-y)(c-d)$$

7. Factor Completely.:

$$x^9 + x^6 - x^3 - 1$$

$$x^6(x^3+1) - 1(x^3+1)$$

$$(x^6-1)(x^3+1)$$

$$(x^2-1)(x^4+x^2+1)(x-1)(x^2+x+1)$$

$$(x+1)(x-1)(x^4+x^2+1)(x-1)(x^2+x+1)$$

8. Solve:

$$10n^2 - 35 = 65n$$

$$10n^2 - 65n - 35 = 0$$

$$2n^2 - 13n - 7 = 0$$

$$2n^2 - 14n + n - 7 = 0$$

$$2n(n-7) + 1(n-7) = 0$$

$$(2n+1)(n-7) = 0$$

$$n = -\frac{1}{2}, n = 7 \left\{ -\frac{1}{2}, 7 \right\}$$

9. Solve by completing the square:

$$4n^2 + 4n = -24$$

$$n^2 + n = -6$$

$$n^2 + n + \frac{1}{4} = -6 + \frac{1}{4}$$

$$\sqrt{\left(n + \frac{1}{2}\right)^2} = \sqrt{-\frac{23}{4}}$$

$$n + \frac{1}{2} = \pm \frac{\sqrt{-23}}{2}$$

$$n = -\frac{1}{2} \pm \frac{i\sqrt{23}}{2}$$

$$n = \frac{-1 + i\sqrt{23}}{2}, \frac{-1 - i\sqrt{23}}{2}$$

10. Solve using the quadratic formula:

$$9x^2 - 11 = 6x$$

$$9x^2 - 6x - 11 = 0$$

$$x = \frac{6 \pm \sqrt{(-6)^2 - 4(9)(-11)}}{18}$$

$$x = \frac{6 \pm \sqrt{36 + 396}}{18}$$

$$x = \frac{6 \pm \sqrt{432}}{18}$$

$$x = \frac{6 \pm 12\sqrt{3}}{18} = \frac{6}{18} \pm \frac{2\sqrt{3}}{3} = \frac{1}{3} \pm \frac{2\sqrt{3}}{3}$$

$$x = \frac{1 \pm 2\sqrt{3}}{3} \left\{ \frac{1+2\sqrt{3}}{3}, \frac{1-2\sqrt{3}}{3} \right\}$$

11. Simplify the following completely:

$$\frac{\frac{1}{2} - \frac{x+5}{4}}{\frac{2x^2}{2} - \frac{5}{2}} = \frac{\frac{2-(x+5)}{4}}{\frac{2x^2-5}{2}}$$

$$= \frac{2-(x+5)}{4} \cdot \frac{2}{2x^2-5}$$

$$= \frac{2-(x+5)}{2(x^2-5)}$$

$$= \frac{2-x-5}{2(x^2-5)}$$

$$\frac{-x-3}{2x^2-10}$$

12. Solve over the reals:

$$4x^2 + 4x - 8 = 1$$

$$4x^2 + 4x - 9 = 0$$

$$x^2 + x - \frac{9}{4} = 0$$

$$\sqrt{\left(x + \frac{1}{2}\right)^2} = \sqrt{\frac{5}{2}}$$

$$x + \frac{1}{2} = \pm \sqrt{\frac{5}{2}}$$

$$x = -\frac{1}{2} \pm \sqrt{\frac{5}{2}}$$

$$\left\{ -\frac{1}{2} + \sqrt{\frac{5}{2}}, -\frac{1}{2} - \sqrt{\frac{5}{2}} \right\}$$

$$\frac{x^b}{x^c} = x^a$$

13. Solve over the reals:

$$\frac{81^{3n+2}}{243^{-n}} = 3^4$$

$$\frac{(3^4)^{3n+2}}{3^{5(-n)}} = 3^4$$

$$\frac{3^{12n+8}}{3^{-5n}} = 3^4$$

$$3^{(12n+8)+5n} = 3^4$$

$$17n + 13 = 4$$

$$\frac{17n}{17} = \frac{-9}{17}$$

$$n = -\frac{9}{17}$$

14. Solve over the reals:

$$\frac{1}{6}^{3x+2} \cdot 216^{3x} = \frac{1}{216}$$

$$6^{-1(3x+2)} \cdot 6^{3(3x)} = 6^{-3}$$

$$6^{-3x-2} \cdot 6^{9x} = 6^{-3}$$

$$6^{6x-2} = 6^{-3}$$

$$6x-2 = -3$$

$$\frac{6x}{6} = \frac{-1}{6}$$

$$x = -\frac{1}{6}$$

15. $\log_4(x^2-3) + \log_4 10 = 1$

$$\log_4 10x^2-30 = 1$$

$$4 = 10x^2-30$$

$$34 = 10x^2$$

$$\frac{34}{10} = x^2$$

$$\sqrt{x^2} = \sqrt{\frac{17}{5}}$$

$$x = \pm \sqrt{\frac{17}{5}}$$

16. Solve for x over the reals:

$$\ln(4x+1) - \ln 3 = 5$$

$$\ln \frac{4x+1}{3} = 5$$

$$3e^5 = \frac{4x+1}{3}$$

$$3e^5 = 4x+1$$

$$\frac{3e^5-1}{4} = \frac{4x}{4}$$

$$x = \frac{3e^5-1}{4}$$