Week2: Getting started with R

Overview

What is R?

- R is a programming environment
 - uses a well-developed but simple programming language
 - allows for rapid development of new tools according to user demand
 - these tools are distributed as packages, which any user can download to customize the R environment

Why using R?

- Complete statistical environment and programming language
- Efficient functions and data structures for data analysis
- Powerful graphics
- Access to fast growing number of analysis packages
- Most widely used language in applied statistics
- Is standard for data mining and statistical analysis
- Technical advantages: free, open-source, available for all OSs

R Working Environments

Some R working environments with support for syntax highlighting and utilities to send code to the R console:

- RStudio: excellent choice for beginners (Cheat Sheet)
- Basic R code editors provided by Rguis
- gedit, Rgedit, RKWard, Eclipse, Tinn-R, Notepad++, NppToR
- Vim-R-Tmux: R working environment based on vim and tmux
- Emacs (ESS add-on package)

Example: RStudio

New integrated development environment (IDE) for R. Highly functional for both beginners and advanced.

RStudio IDE

Some userful shortcuts: Ctrl+Enter (send code), Ctrl+Shift+C (comment/uncomment), Ctrl+1/2 (switch window focus)

Getting Started with R

Installation of R and packages

- 1. Base R and most R packages are available for download from the Comprehensive R Archive Network (CRAN)
 - http://www.r-project.org/
 - base R comes with a number of basic data management, analysis, and graphical tools

- R's power and flexibility, however, lie in its array of packages (currently more 8,000!)
- 2. Install RStudio from RStudio.
- 3. Install CRAN Packages from R console like this:

```
install.packages(c("pkg1", "pkg2"))
install.packages("pkg.zip", repos=NULL)
```

Startup and Closing R

- Starting R: The R GUI versions, including RStudio, under Windows and Mac OS X can be opened by double-clicking their icons. Alternatively, one can start it by typing R in a terminal (default under Linux).
- Startup/Closing Behavior: The R environment is controlled by hidden files in the startup directory: .RData, .Rhistory and .Rprofile (optional).
- Closing R:

```
q()
```

Save workspace image? [y/n/c]:

• Note: When responding with y, then the entire R workspace will be written to the .RData file which can become very large. Often it is sufficient to just save an analysis protocol in an R source file. This way one can quickly regenerate all data sets and objects.

Navigating directories

- Create an object with the assignment operator <- or = object <- ...
- List objects in current R session

ls()

• Return content of current working directory

dir()

• Return path of current working directory

```
getwd()
```

• Change current working directory

```
setwd("/home/user")
```

Basic Syntax

• General R command syntax

```
object <- function_name(arguments)
object <- object[arguments]</pre>
```

• Finding help

```
?function_name
```

• Load a library/package

```
library("my_library")
```

• List functions defined by a library

```
library(help="my_library")
```

• Load library manual (PDF or HTML file)

```
vignette("my_library")
```

• Execute an R script from within R

```
source("my_script.R")
```

• Execute an R script from command-line (the first of the three options is preferred)

```
$ Rscript my_script.R
$ R CMD BATCH my_script.R
$ R --slave < my_script.R</pre>
```

Data Types

• Numeric data

```
Example: 1, 2, 3, ...

x <- c(1, 2, 3)

x

## [1] 1 2 3

is.numeric(x)

## [1] TRUE

as.character(x)

## [1] "1" "2" "3"

• Character data

Example: "a", "b", "c", ...

x <- c("1", "2", "3")

x

## [1] "1" "2" "3"

is.character(x)

## [1] TRUE

as.numeric(x)

## [1] 1 2 3
```

• Complex data

Example: mix of both

```
c(1, "b", 3)

## [1] "1" "b" "3"

• Logical data
Example: TRUE of FALSE

x <- 1:10 < 5
x

## [1] TRUE TRUE TRUE TRUE FALSE FALSE FALSE FALSE FALSE FALSE
!x

## [1] FALSE FALSE FALSE FALSE TRUE TRUE TRUE TRUE TRUE
which(x) # Returns index for the 'TRUE' values in logical vector

## [1] 1 2 3 4</pre>
```

Data objects

• Vectors (1D)

class(myMA)

[1] "matrix"

Object types

Definition: numeric or character myVec <- 1:10; names(myVec) <- letters[1:10]</pre> myVec[1:5] ## a b c d e ## 1 2 3 4 5 myVec[c(2,4,6,8)]## b d f h ## 2 4 6 8 myVec[c("b", "d", "f")] ## b d f ## 2 4 6 • Factors (1D) Definition: vectors with grouping information factor(c("dog", "cat", "mouse", "dog", "dog", "cat")) ## [1] dog cat mouse dog dog cat ## Levels: cat dog mouse • Matrices (2D)

Definition: two dimensional structures with data of same type

myMA <- matrix(1:30, 3, 10, byrow = TRUE)

```
myMA[1:2,]
           [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
  ## [1,]
                  2
                         3
                              4
                                    5
                                         6
                                              7
                                                    8
                                                               10
             1
  ## [2,]
                                                   18
             11
                  12
                       13
                             14
                                   15
                                        16
                                              17
                                                         19
                                                               20
  myMA[1, , drop=FALSE]
          [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
  ## [1,]
                   2
                              4
                                    5
                                         6
                         3
• Data Frames (2D)
  Definition: two dimensional objects with data of variable types
  myDF <- data.frame(Col1=1:10, Col2=10:1)</pre>
  myDF[1:2, ]
  ##
       Col1 Col2
  ## 1
          1
               10
  ## 2
           2
                9
• Arrays
  Definition: data structure with one, two or more dimensions
• Lists
  Definition: containers for any object type
  myL <- list(name="Fred", wife="Mary", no.children=3, child.ages=c(4,7,9))</pre>
  myL
  ## $name
  ## [1] "Fred"
  ##
  ## $wife
  ## [1] "Mary"
  ## $no.children
  ## [1] 3
  ##
  ## $child.ages
  ## [1] 4 7 9
  myL[[4]][1:2]
  ## [1] 4 7
• Functions
  Definition: piece of code
  myfct <- function(arg1, arg2, ...) {</pre>
      function_body
  }
```

Subsetting of data objects

• Subsetting by positive or negative index/position numbers

```
myVec <- 1:26; names(myVec) <- LETTERS</pre>
    myVec[1:4]
    ## A B C D
    ## 1 2 3 4
  • Subsetting by same length logical vectors
    myLog <- myVec > 10
    myVec[myLog]
    ## K L M N O P Q R S T U V W X Y Z
    ## 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26
  • Subsetting by field names
    myVec[c("B", "K", "M")]
    ## B K M
    ## 2 11 13
  • Subset with $ sign: references a single column or list component by its name
    iris$Species[1:8]
    ## [1] setosa setosa setosa setosa setosa setosa setosa
    ## Levels: setosa versicolor virginica
Important Utilities
  • Combining Objects
    The c function combines vectors and lists
    c(1, 2, 3)
    ## [1] 1 2 3
    x <- 1:3; y <- 101:103
    c(x, y)
                  2 3 101 102 103
    ## [1]
    iris$Species[1:8]
    ## [1] setosa setosa setosa setosa setosa setosa setosa
    ## Levels: setosa versicolor virginica
    The cbind and rbind functions can be used to append columns and rows, respecively.
    ma <- cbind(x, y)</pre>
    ma
    ##
```

##

[1,] 1 101 ## [2,] 2 102 ## [3,] 3 103 rbind(ma, ma)

```
## [3,] 3 103
  ## [4,] 1 101
  ## [5,] 2 102
  ## [6,] 3 103
• Accessing Dimensions of Objects
  Length and dimension information of objects
  length(iris$Species)
  ## [1] 150
  dim(iris)
  ## [1] 150
               5
• Accessing Name Slots of Objects
   Accessing row and column names of 2D objects
  rownames(iris)[1:8]
  ## [1] "1" "2" "3" "4" "5" "6" "7" "8"
  colnames(iris)
  ## [1] "Sepal.Length" "Sepal.Width" "Petal.Length" "Petal.Width"
  ## [5] "Species"
• Return name field of vectors and lists
  names(myVec)
  ## [1] "A" "B" "C" "D" "E" "F" "G" "H" "I" "J" "K" "L" "M" "N" "O" "P" "Q"
  ## [18] "R" "S" "T" "U" "V" "W" "X" "Y" "Z"
  names(myL)
  ## [1] "name"
                        "wife"
                                       "no.children" "child.ages"
• Sorting Objects
  The function sort returns a vector in ascending or descending order
  sort(10:1)
  ## [1] 1 2 3 4 5 6 7 8 9 10
  The function order returns a sorting index for sorting an object
  sortindex <- order(iris[,1], decreasing = FALSE)</pre>
  sortindex[1:12]
  ## [1] 14 9 39 43 42 4 7 23 48 3 30 12
  iris[sortindex,][1:2,]
  ##
        Sepal.Length Sepal.Width Petal.Length Petal.Width Species
  ## 14
                  4.3
                              3.0
                                                        0.1 setosa
                                            1.1
                              2.9
                                                         0.2 setosa
  sortindex <- order(-iris[,1]) # Same as decreasing=TRUE</pre>
```

Sorting multiple columns

[2,] 2 102

```
iris[order(iris$Sepal.Length, iris$Sepal.Width),][1:2,]

## Sepal.Length Sepal.Width Petal.Length Petal.Width Species
## 14     4.3     3.0     1.1     0.1 setosa
## 9     4.4     2.9     1.4     0.2 setosa
```

Operators and Calculations

• Comparison Operators

```
Comparison operators: ==, !=, <, >, <=, >=
  1==1
  ## [1] TRUE
  Logical operators: AND: &, OR: |, NOT: !
  x <- 1:10; y <- 10:1
  x > y & x > 5
  ## [1] FALSE FALSE FALSE FALSE TRUE TRUE TRUE TRUE TRUE
• Basic Calculations
  To look up math functions, see Function Index here
 x + y
  ## [1] 11 11 11 11 11 11 11 11 11
  sum(x)
  ## [1] 55
 mean(x)
  ## [1] 5.5
  apply(iris[1:6,1:3], 1, mean)
                     2
                              3
                                        4
                                                 5
  ## 3.33333 3.100000 3.066667 3.066667 3.333333 3.666667
```

Reading and Writing External Data

• Import of tabular data

```
Import of a tab-delimited tabular file
```

```
myDF <- read.delim("myData.xls", sep="\t")</pre>
```

Import of Excel file. Note: working with tab- or comma-delimited files is more flexible and preferred.
library(gdata)
myDF <- read.xls("myData.xls")</pre>

• Export of tabular data

```
write.table(myDF, file="myfile.xls", sep="\t", quote=FALSE, col.names=NA)
```

• Line-wise import

```
myDF <- readLines("myData.txt")</pre>
```

• Line-wise export

```
writeLines(month.name, "myData.txt")
```

• Copy and paste into R

On Windows/Linux systems

```
read.delim("clipboard")
```

On Mac OS X systems

```
read.delim(pipe("pbpaste"))
```

• Copy and paste from R

On Windows/Linux systems

```
write.table(iris, "clipboard", sep="\t", col.names=NA, quote=F)
```

On Mac OS X systems

```
zz <- pipe('pbcopy', 'w')
write.table(iris, zz, sep="\t", col.names=NA, quote=F)
close(zz)</pre>
```

Useful R Functions

• Unique entries

Make vector entries unique with unique

```
length(iris$Sepal.Length)
```

```
## [1] 150
length(unique(iris$Sepal.Length))
```

```
## [1] 35
```

• Count occurrences

Count occurrences of entries with table

```
table(iris$Species)
```

```
## setosa versicolor virginica
## 50 50 50
```

• Aggregate data

Compute aggregate statistics with aggregate

```
aggregate(iris[,1:4], by=list(iris$Species), FUN=mean, na.rm=TRUE)
```

```
##
      Group.1 Sepal.Length Sepal.Width Petal.Length Petal.Width
## 1
       setosa
             5.006
                            3.428 1.462
                                                 0.246
## 2 versicolor
                  5.936
                            2.770
                                       4.260
                                                 1.326
                            2.974
## 3 virginica
                  6.588
                                      5.552
                                                 2.026
```

• Intersect data

Compute intersect between two vectors with %in%

```
month.name %in% c("May", "July")

## [1] FALSE FALSE FALSE TRUE FALSE TRUE FALSE FALSE FALSE
```

[12] FALSEMerge data frames

Join two data frames by common field entries with merge (here row names by.x=0). To obtain only the common rows, change all=TRUE to all=FALSE. To merge on specific columns, refer to them by their position numbers or their column names.

```
frame1 <- iris[sample(1:length(iris[,1]), 30), ]</pre>
frame1[1:2,]
##
      Sepal.Length Sepal.Width Petal.Length Petal.Width
                                                              Species
## 11
                5.4
                            3.7
                                          1.5
                                                               setosa
## 61
                5.0
                            2.0
                                          3.5
                                                       1.0 versicolor
dim(frame1)
## [1] 30 5
my_result <- merge(frame1, iris, by.x = 0, by.y = 0, all = TRUE)
dim(my_result)
## [1] 150 11
```

Graphics in R

Advantages

- Powerful environment for visualizing scientific data
- Integrated graphics and statistics infrastructure
- Publication quality graphics
- Fully programmable
- Highly reproducible
- Full LaTeX and Markdown support via knitr and R markdown
- Vast number of R packages with graphics utilities

Documentation for R Graphics

```
** General **
```

- Graphics Task Page URL
- R Graph Gallery URL
- R Graphical Manual URL
- Paul Murrell's book R (Grid) Graphics URL

Interactive graphics

- rggobi' (GGobi) URL
- iplots URL
- Open GL (rgl) URL

Graphics Environments

Viewing and saving graphics in R

- On-screen graphics
- postscript, pdf, svg
- jpeg, png, wmf, tiff, \dots

Four major graphic environments

- (a) Low-level infrastructure
 - R Base Graphics (low- and high-level)
 - grid: Manual
- (b) High-level infrastructure \begin{itemize}
 - lattice: Manual, Intro, Book
 - ggplot2: Manual, Intro, Book

Base Graphics: Overview

Important high-level plotting functions

- plot: generic x-y plotting
- barplot: bar plots
- boxplot: box-and-whisker plot
- hist: histograms
- pie: pie charts
- dotchart: cleveland dot plots
- image, heatmap, contour, persp: functions to generate image-like plots
- qqnorm, qqline, qqplot: distribution comparison plots
- pairs, coplot: display of multivariant data

Help on graphics functions

- ?myfct
- ?plot
- ?par

Preferred Object Types

- Matrices and data frames
- Vectors
- Named vectors

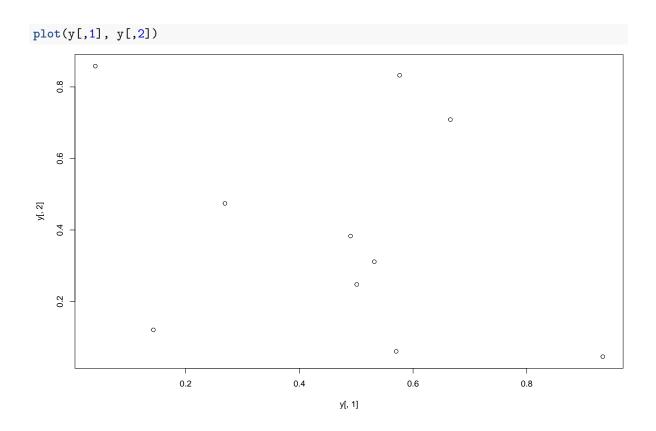
Scatter Plots

Basic Scatter Plot

• Sample data set for subsequent plots

```
set.seed(1410)
y <- matrix(runif(30), ncol=3, dimnames=list(letters[1:10], LETTERS[1:3]))</pre>
```

• Plot data



All pairs

```
pairs(y)
![](Figs/pairs_scatter_plot-1.pdf)<!-- -->
```

With labels

```
plot(y[,1], y[,2], pch=20, col="red", main="Symbols and Labels")
text(y[,1]+0.03, y[,2], rownames(y))

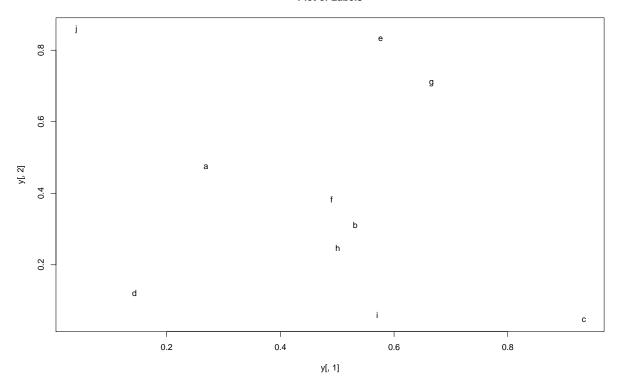
![](Figs/labels_scatter_plot-1.pdf)<!-- -->
```

More examples

• Print instead of symbols the row names

```
plot(y[,1], y[,2], type="n", main="Plot of Labels")
text(y[,1], y[,2], rownames(y))
```

Plot of Labels



• Usage of important plotting parameters

- Important arguments
 - mar: specifies the margin sizes around the plotting area in order: c(bottom, left, top, right)
 - col: color of symbols
 - pch: type of symbols, samples: example(points)
 - lwd: size of symbols
 - cex: control font sizes
 - For details see ?par

Add regression line

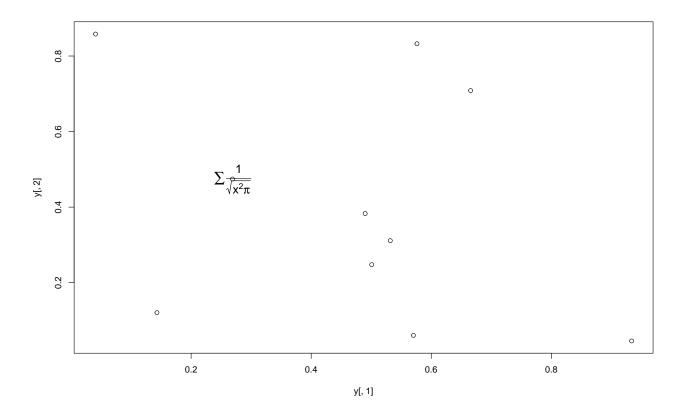
```
plot(y[,1], y[,2])
myline <- lm(y[,2]~y[,1]); abline(myline, lwd=2)

![](Figs/plot_regression-1.pdf)<!-- -->

summary(myline)
```

```
. . .
##
## Call:
## lm(formula = y[, 2] ~ y[, 1])
## Residuals:
##
       Min
                 1Q Median
                                   3Q
                                           Max
## -0.40357 -0.17912 -0.04299 0.22147 0.46623
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.5764
                           0.2110 2.732 0.0258 *
                                            0.3839
               -0.3647
                           0.3959 -0.921
## y[, 1]
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.3095 on 8 degrees of freedom
## Multiple R-squared: 0.09589,
                                  Adjusted R-squared: -0.01712
## F-statistic: 0.8485 on 1 and 8 DF, p-value: 0.3839
Log scale
- Same plot as above, but on log scale
```r
plot(y[,1], y[,2], log="xy")
<!-- -->
Add a mathematical expression
```

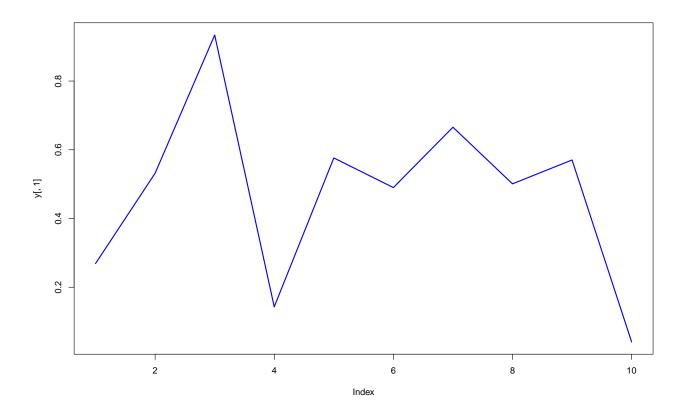
```
plot(y[,1], y[,2]); text(y[1,1], y[1,2], expression(sum(frac(1,sqrt(x^2*pi)))), cex=1.3)
```



## Line Plots

## Single data set

```
plot(y[,1], type="1", lwd=2, col="blue")
```



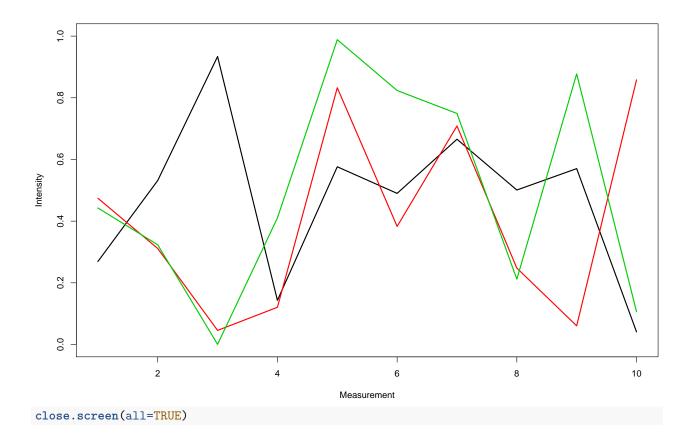
## Many Data Sets

Plots line graph for all columns in data frame y. The split.screen function is used in this example in a for loop to overlay several line graphs in the same plot.

```
split.screen(c(1,1))

[1] 1

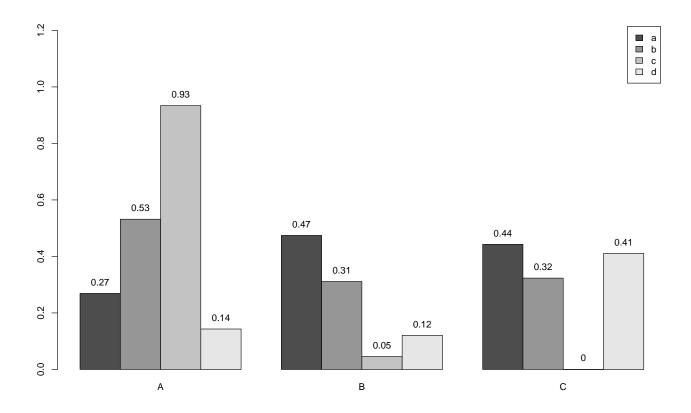
plot(y[,1], ylim=c(0,1), xlab="Measurement", ylab="Intensity", type="1", lwd=2, col=1)
for(i in 2:length(y[1,])) {
 screen(1, new=FALSE)
 plot(y[,i], ylim=c(0,1), type="1", lwd=2, col=i, xaxt="n", yaxt="n", ylab="", xlab="", main="", bty:
}
```



## **Bar Plots**

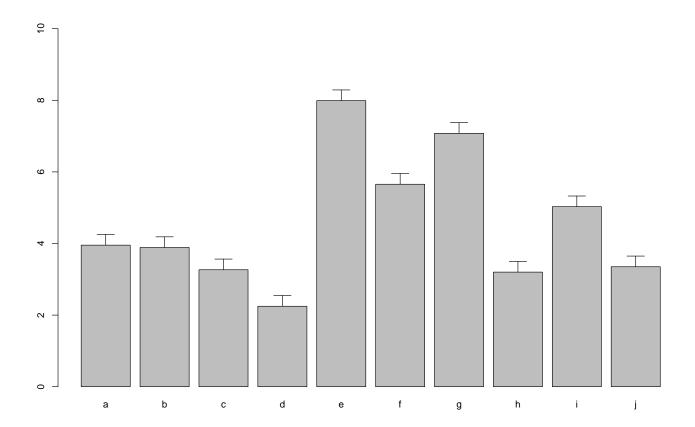
## **Basics**

```
 barplot(y[1:4,], ylim=c(0, max(y[1:4,])+0.3), beside=TRUE, legend=letters[1:4]) \\ text(labels=round(as.vector(as.matrix(y[1:4,])),2), x=seq(1.5, 13, by=1) + sort(rep(c(0,1,2), 4)), y=as(1.5, 13, by=1) +
```



## **Error Bars**

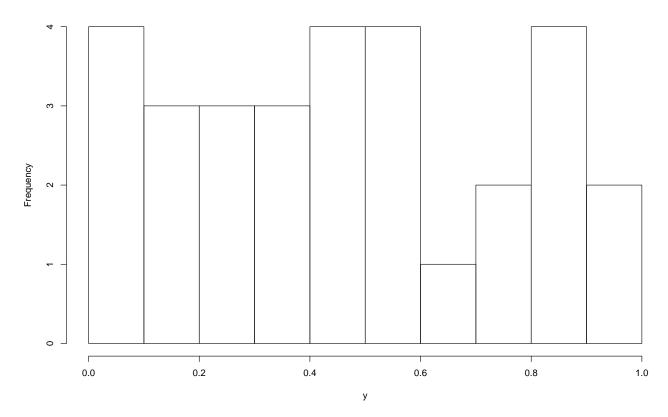
```
bar <- barplot(m <- rowMeans(y) * 10, ylim=c(0, 10))
stdev <- sd(t(y))
arrows(bar, m, bar, m + stdev, length=0.15, angle = 90)</pre>
```



## ${\bf Histograms}$

hist(y, freq=TRUE, breaks=10)

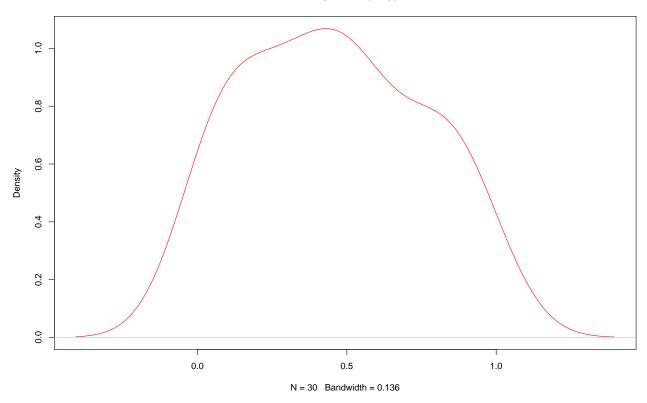




## Density Plots

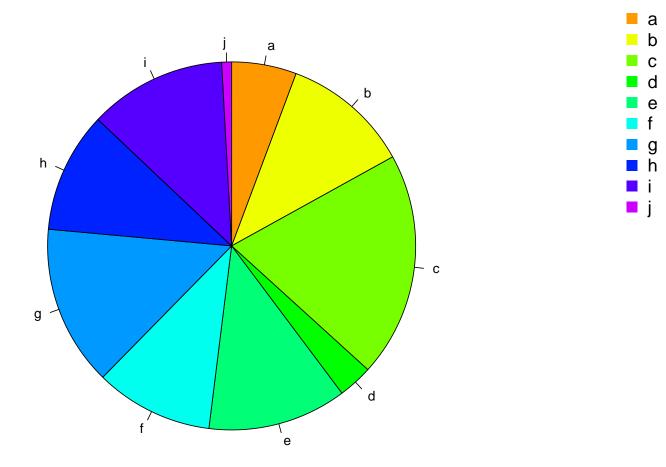
plot(density(y), col="red")

## density.default(x = y)



## Pie Charts

```
pie(y[,1], col=rainbow(length(y[,1]), start=0.1, end=0.8), clockwise=TRUE)
legend("topright", legend=row.names(y), cex=1.3, bty="n", pch=15, pt.cex=1.8,
col=rainbow(length(y[,1]), start=0.1, end=0.8), ncol=1)
```



## Color Selection Utilities

• Default color palette and how to change it

```
palette()

[1] "black" "red" "green3" "blue" "cyan" "magenta" "yellow"

[8] "gray"

palette(rainbow(5, start=0.1, end=0.2))
palette()

[1] "#FF9900" "#FFBF00" "#FFE600" "#F2FF00" "#CCFF00"

palette("default")
```

• The gray function allows to select any type of gray shades by providing values from 0 to 1 gray(seq(0.1, 1, by= 0.2))

```
[1] "#1A1A1A" "#4D4D4D" "#808080" "#B3B3B3" "#E6E6E6"
```

• Color gradients with colorpanel function from gplots library

```
library(gplots)
colorpanel(5, "darkblue", "yellow", "white")
```

```
[1] "#00008B" "#808046" "#FFFF00" "#FFFF80" "#FFFFFF"
```

Much more on colors in R see Earl Glynn's color chart here

### Saving Graphics to File

• After the pdf() command all graphs are redirected to file test.pdf. Works for all common formats similarly: jpeg, png, ps, tiff, ...

```
pdf("test.pdf")
plot(1:10, 1:10)
dev.off()
```

• Generates Scalable Vector Graphics (SVG) files that can be edited in vector graphics programs, such as InkScape.

```
library("RSvgDevice")
devSVG("test.svg")
plot(1:10, 1:10)
dev.off()
```

## **Basic Statistics**

• summary is a generic function to summarize many types of R objects, including datasets.

```
summary(iris)
```

```
##
 Sepal.Length
 Sepal.Width
 Petal.Length
 Petal.Width
 :1.000
 :4.300
 :2.000
 :0.100
##
 Min.
 Min.
 Min.
 Min.
##
 1st Qu.:5.100
 1st Qu.:2.800
 1st Qu.:1.600
 1st Qu.:0.300
Median :5.800
 Median :3.000
 Median :4.350
 Median :1.300
Mean
 :5.843
 :3.057
 :3.758
 :1.199
 Mean
 Mean
 Mean
##
 3rd Qu.:6.400
 3rd Qu.:3.300
 3rd Qu.:5.100
 3rd Qu.:1.800
##
 {\tt Max.}
 :7.900
 Max.
 :4.400
 Max.
 :6.900
 :2.500
 Max.
##
 Species
##
 setosa
 :50
##
 versicolor:50
##
 virginica:50
##
##
##
```

• Compare the mean of two groups

```
s=iris[which(iris$Species=='setosa'), 1];
v=iris[which(iris$Species=='virginica'), 1];
t.test(s,v, paired=T)
```

```
##
Paired t-test
##
data: s and v
t = -16.344, df = 49, p-value < 2.2e-16
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
-1.776513 -1.387487
sample estimates:</pre>
```

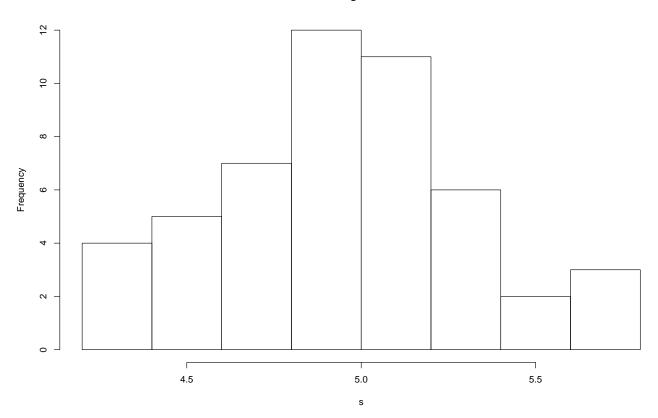
```
mean of the differences
-1.582
```

• Check the normality of my data

```
s=iris[which(iris$Species=='setosa'), 1];
shapiro.test(s);

##
Shapiro-Wilk normality test
##
data: s
W = 0.9777, p-value = 0.4595
hist(s, breaks=10);
```

#### Histogram of s



• Test correlation between two data sets

## 0.5851391 0.8460314

```
s=iris[which(iris$Species=='setosa'), 1];
v=iris[which(iris$Species=='setosa'), 2];
cor.test(s,v)

##
Pearson's product-moment correlation
##
data: s and v
t = 7.6807, df = 48, p-value = 6.71e-10
alternative hypothesis: true correlation is not equal to 0
95 percent confidence interval:
```

```
sample estimates:
##
 cor
0.7425467
 • Build a linear model
myModel = lm(iris[,1] - iris[, 2] + iris[, 3] + iris[, 4])
summary(myModel)
##
Call:
lm(formula = iris[, 1] ~ iris[, 2] + iris[, 3] + iris[, 4])
Residuals:
##
 Min
 1Q
 Median
 ЗQ
 Max
-0.82816 -0.21989 0.01875 0.19709 0.84570
##
Coefficients:
 Estimate Std. Error t value Pr(>|t|)
##
(Intercept) 1.85600
 0.25078
 7.401 9.85e-12 ***
iris[, 2]
 0.65084
 0.06665
 9.765 < 2e-16 ***
iris[, 3]
 0.70913
 0.05672 12.502 < 2e-16 ***
iris[, 4]
 -0.55648
 0.12755 -4.363 2.41e-05 ***

Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
Residual standard error: 0.3145 on 146 degrees of freedom
Multiple R-squared: 0.8586, Adjusted R-squared: 0.8557
F-statistic: 295.5 on 3 and 146 DF, p-value: < 2.2e-16
step(myModel, direction="backward")
Start: AIC=-343.04
iris[, 1] ~ iris[, 2] + iris[, 3] + iris[, 4]
##
##
 Df Sum of Sq
 RSS
 AIC
<none>
 14.445 -343.04
- iris[, 4] 1
 1.8834 16.329 -326.66
- iris[, 2] 1
 9.4353 23.881 -269.63
- iris[, 3] 1
 15.4657 29.911 -235.86
##
Call:
lm(formula = iris[, 1] ~ iris[, 2] + iris[, 3] + iris[, 4])
##
Coefficients:
(Intercept)
 iris[, 2]
 iris[, 3]
 iris[, 4]
##
 1.8560
 0.6508
 0.7091
 -0.5565

 ANOVA

myAnova<-aov(iris[,1] ~ iris[, 5])</pre>
summary(myAnova)
 Df Sum Sq Mean Sq F value Pr(>F)
iris[, 5]
 2 63.21 31.606
 119.3 <2e-16 ***
Residuals
 147 38.96
 0.265

```

## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.05 '.' 0.1 ' ' 1