

COMP631 Introduction to IR

Homework 2

March 11, 2022

- 1) Submit a single PDF file containing your answers to each question. **You are highly encouraged to use LaTeX or Microsoft Word.**
- 2) For calculation questions, please provide the analysis and calculation steps. An answer with only a resultant value will not receive any score.
– Due Date: March 21, 2022 11:59pm

1 HITS and PageRank (35 pts)

Given the figure including a graph as below:

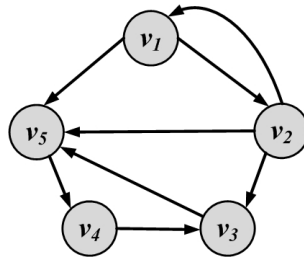


Figure 1: A toy example of a graph

- 1) (8 pts) For each graph node in Figure 1, calculate the degree centrality *normalized by the degree sum*, as well as the rank with respect to the centrality.

- 2) (8 pts) In the context of world wide web or social media, given a concrete real-world example for entities that can be recognized as “authorities”.
- 3) (12 pts) Calculate the PageRank values for the graph in Figure 1 by applying the iterative algorithm. (Please show 2 iteration steps.)
- 4) (7 pts) Explain the limitations of Katz Centrality, and how PageRank overcome these limitations.

2 Graph Analysis (35 pts)

Given the graph as below:

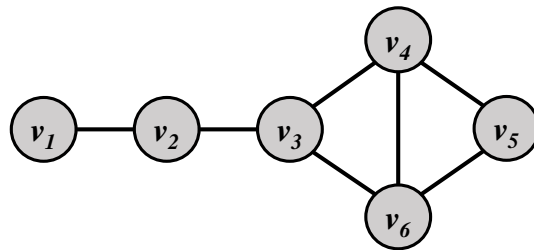


Figure 2: Another toy example of a graph

- 1) (7 pts) Calculate the Closeness centrality of node v_5 .
- 2) (7 pts) Calculate the Betweenness centrality of node v_4 .
- 3) (7 pts) Calculate the Jaccard similarity between v_3 and v_5 .
- 4) (7 pts) Calculate the local clustering coefficient of v_4 .
- 5) (7 pts) Explain how we can use similarity measure or clustering coefficient for friend recommendation in social network.

3 Results Assembly (30 pts)

1) (12 pts) For a multi-term query q , explain why we can only consider high-*idf* query terms for index elimination.

2) (18 pts) Consider a more general form of net score,

$$\text{netscore}(q, d) = \alpha \cdot g(d) + \beta \cdot \text{cosine}(q, d), \quad (1)$$

where α and β are weights, $0 \leq \alpha \leq 1$, $0 \leq \beta \leq 1$, $\alpha + \beta = 1$, explain how the IR system would behave with different relative weighting.