

```

(load "chapl.scm")

;;Exercise 2.1
(define better-make-rat
  (lambda (x y)
    (let ((g (gcd x y)))
      (if (or (and (> x 0) (> y 0)) (and (< x 0) (< y 0)))
          (cons (abs (/ x g)) (abs (/ y g)))
          (cons (- (abs (/ x g))) (abs (/ y g)))))))
(define (numer x) (car x))
(define (denom x) (cdr x))

(define (print-rat x)
  (newline)
  (display (numer x))
  (display "/" )
  (display (denom x)))

;;Exercise 2.2
(define (print-p p)
  (newline)
  (display "(")
  (display (x-point p))
  (display "," )
  (display (y-point p))
  (display ")"))

(define make-point
  (lambda (x y)
    (cons x y)))
(define x-point
  (lambda (point)
    (car point)))
(define y-point
  (lambda (point)
    (cdr point)))

(define make-segment
  (lambda (start-point end-point)
    (cons start-point end-point)))
(define start-segment
  (lambda (segment)
    (car segment)))
(define end-segment

```

```

(lambda (segment)
  (cdr segment)))

(define mid-point
  (lambda (segment)
    (make-segment (/ (+ (x-point (start-segment segment))
                        (x-point (end-segment segment)))
                     2)
                  (/ (+ (y-point (start-segment segment))
                        (y-point (end-segment segment)))
                     2))))

```

;;Exercise 2.3

```

(define make-rect
  (lambda (width height)
    (cons width height)))
(define (width a-rect)
  (car a-rect))
(define (height a-rect)
  (cdr a-rect))
(define perimeter
  (lambda (a-rect)
    (* 2 (+ (width a-rect)
            (height a-rect)))))
(define area
  (lambda (a-rect)
    (* (width a-rect)
       (height a-rect))))

```

;;Version2 : using points representation

;;Exercise 2.4

```

(define (my-cons x y)
  (lambda (m) (m x y)))

(define (my-car z)
  (z (lambda (p q) p)))

```

```

;(my-car (my-cons 1 2))
(define (my-cdr z)
  (z (lambda (p q) q)))
;(my-cdr (my-cons 1 2))

```

;;Exercise 2.5

;;Because an Integer can and represent by $(2^a) \cdot (3^b)$

```

(define my-cons
  (lambda (a b)
    (* (expt 2 a) (expt 3 b))))
(define my-car
  (lambda (a-pair)
    (define (loop input value)
      (if (= (remainder input 2) 0)
          (loop (/ input 2) (+ value 1))
          value))
      (loop a-pair 0)))
(define my-cdr
  (lambda (a-pair)
    (define (loop input value)
      (if (= (remainder input 3) 0)
          (loop (/ input 3) (+ value 1))
          value))
      (loop a-pair 0)))

```

;;Exercise 2.6

;丘齐数里，所有的数字都是两个参数的函数：

;零是 $\lambda s z . z$

;一是 $\lambda s z . s z$

;二是 $\lambda s z . s (s z)$

;对任意一个数“n”，它的丘齐数都是一个函数。这个函数把它的第一个参数应用到第二个参数上 n 次。

;加法函数 $\text{plus}(m,n) = m + n$ 利用了恒等式 $f(m + n)(x) = fm(fn(x))$ 。

;

; $\text{plus} \equiv \lambda m. \lambda n. \lambda f. \lambda x. m f (n f x)$

;后继函数 $\text{succ}(n) = n + 1$ β -等价于 $(\text{plus } 1)$ 。

;

; $\text{succ} \equiv \lambda n. \lambda f. \lambda x. f (n f x)$

;乘法函数 $\text{times}(m,n) = m * n$ 利用了恒等式 $f(m * n) = (fm)n$ 。

;

; $\text{mult} \equiv \lambda m. \lambda n. \lambda f. n (m f)$

;指数函数 $\text{exp}(m,n) = mn$ 由 Church 数定义直接给出。

;

; $\text{exp} \equiv \lambda m. \lambda n. n m$

```

(define zero
  (lambda (f)
    (lambda (x)
      x)))

```

;;zero 是一个函数，这个函数接受参数，返回参数，不做任何处理

```
;;use substitution model to evaluate (add-1 zero)
;;(add-1 one) to get two
;;(add-1 two) to get three
```

```
(define one
  (lambda (f)
    (lambda (x)
      (f x))))
```

```
(define two
  (lambda (f)
    (lambda (x)
      (f (f x))))))
```

```
(define (add-1 n)
  (lambda (f)
    (lambda (x)
      (f ((n f) x))))))
```

```
;;operate one more time than before
```

```
(define (church-add n m)
  (lambda (f)
    (lambda (x)
      (((n add-1) m) f) x))))
```

```
;;using repeated add-1
```

```
(define (my-church-add n m)
  (lambda (f)
    (lambda (x)
      ((m f) ((n f) x))))))
```

```
(define (church-mul n m)
  (lambda (f)
    (n (m f))))
```

```
(define (church-expt m n)
  (n m))
```

```
(define f
  (lambda (x)
    (cons "a" x)))
```

```
;(((add-1 two) f) '())
```

```
;(((my-church-add one two) f) '())
```

```
;A better test version: (define (inc x) (+ 1 x))
```

```

(define (inc x) (+ x 1))
(define (check n)
  ((n inc) 0))

```

;;Extended Exercise: Interval Arithmetic

```

(define (add-interval x y)
  (make-interval (+ (lower-bound x) (lower-bound y))
                  (+ (upper-bound x) (upper-bound y))))

```

```

(define (mul-interval x y)
  (let ((p1 (* (lower-bound x) (lower-bound y)))
        (p2 (* (lower-bound x) (upper-bound y)))
        (p3 (* (upper-bound x) (lower-bound y)))
        (p4 (* (upper-bound x) (upper-bound y))))
    (make-interval (min p1 p2 p3 p4)
                    (max p1 p2 p3 p4))))

```

```

(define (div-interval x y)
  (mul-interval x
                (make-interval (/ 1.0 (upper-bound y))
                                (/ 1.0 (lower-bound y)))))

```

;;Exercise 2.7

```

(define make-interval
  (lambda (low up)
    (cons low up)))
(define (upper-bound a)
  (cdr a))
(define (lower-bound a)
  (car a))

```

;;Exercise 2.8

```

(define (sub-interval x y)
  (make-interval (- (upper-bound x) (lower-bound y))
                  (- (lower-bound x) (upper-bound y))))

```

;;Exercise 2.9

;For interval (4 6) and (7 11) width-add= (6-4)/2 + (11-7)/2 width-sub=width-add

;For mul and div doesn't stand

;概率与统计: $E(X+Y)=E(X)+E(Y)$

;X与Y相互独立时: $E(XY)=E(X)E(Y)$

;;Exercise 2.10

```

(define check-div-interval
  (lambda (a-interval b-interval)
    (if (and(> (upper-bound b-interval) 0)

```

```

    (< (lower-bound b-interval) 0))
  (display "Error occurred!")
  (div-interval a-interval b-interval))))

```

;;Exercise 2.11

```

(define mul-interval
  (lambda (x y)
    (cond ((>= (lower-bound x) 0)
      (cond ((>= (lower-bound y) 0)
        (make-interval (* (lower-bound x) (lower-bound y)) (* (upper-bound x) (upper-bound y))))
      ((<= (upper-bound y) 0)
        (make-interval (* (upper-bound x) (lower-bound y)) (* (lower-bound x) (upper-bound y))))
      (else
        (make-interval (* (upper-bound x) (lower-bound y)) (* (lower-bound x) (upper-bound y))))))
    ((<= (upper-bound x) 0)
      (cond ((>= (lower-bound y) 0)
        (make-interval (* (lower-bound x) (upper-bound y)) (* (upper-bound x) (lower-bound y))))
      ((<= (upper-bound y) 0)
        (make-interval (* (lower-bound x) (lower-bound y)) (* (upper-bound x) (upper-bound y))))
      (else
        (make-interval (* (lower-bound x) (upper-bound y)) (* (lower-bound x) (lower-bound y))))))
    (else
      (cond ((>= (lower-bound y) 0)
        (make-interval (* (lower-bound x) (upper-bound y)) (* (upper-bound x) (upper-bound y))))
      ((<= (upper-bound y) 0)
        (make-interval (* (upper-bound x) (lower-bound y)) (* (lower-bound x) (lower-bound y))))
      (else
        (make-interval (min (* (lower-bound x) (upper-bound y))
          (* (upper-bound x) (lower-bound y)))
          (max (* (lower-bound x) (lower-bound y))
            (* (upper-bound x) (upper-bound y))))))))))

```

;;Exercise 2.12

```

(define (make-center-width c w)
  (make-interval (- c w) (+ c w)))
(define (center i)

```

```

(/ (+ (lower-bound i) (upper-bound i)) 2))
(define (width i)
  (/ (- (upper-bound i) (lower-bound i)) 2))

(define make-center-percent
  (lambda (center percent)
    (let ((balance (/ (* center percent) 100)))
      (make-interval (- center balance) (+ center balance)))))

(define center
  (lambda (a-interval)
    (/ (+ (lower-bound a-interval) (upper-bound a-interval))
       2)))

(define percent
  (lambda (a-interval)
    (let ((value (- (upper-bound a-interval) (center a-interval))))
      (* (/ value (center a-interval)) 100))))

```

;;Exercise 2.13

```

;interval A: (a-a*p/100, a+a*p/100)
;interval B: (b-b*p/100, b+b*p/100)
;A*B = ab * (1 + pq/10000) ± (p+q)/100
;for small p and q, pq/1000=0
;A*B= ab±(p+q)/100

```

;;Exericse 2.14

```

(define (par1 r1 r2)
  (div-interval (mul-interval r1 r2)
    (add-interval r1 r2)))

(define (par2 r1 r2)
  (let ((one (make-interval 1 1)))
    (div-interval one
      (add-interval (div-interval one r1)
        (div-interval one r2)))))

(define x (make-interval 9.5 10.5)) ;; 10.0 ±0.5 = 10.0 ±5%
(define y (make-interval 5 6))      ;; 6.5 ±0.5 = 6.5 ±7.69%
(define z (make-interval 2 2.5))    ;; 2.25±0.25 = 2.25±11.1%
(define A (make-interval 8.999 9.001))
(define B (make-interval 7.999 8.000))

; Lem is right
;(par1 x y)
;(par2 x y) the width of par2 is smaller

```

```
;(div-interval A A)
;(0.9997778024663928 . 1.0002222469163238)
```

```
;;Exercise 2.15 and 2.16...
```

```
;(par1 x y)
;(2.878787878787879 . 4.344827586206897)
;(par2 x y)
;(3.2758620689655173 . 3.818181818181819)
```

```
;par2 produce a smaller width...
```

```
;there is some difference between interval-arithmetic and it's equivalent
algebraic expressions
```

```
;;Exercise 2.17
```

```
(define my-last-pair
  (lambda (a-pair)
    (define (loop list)
      (if (empty? (cdr list))
          (cons (car list) '())
          (loop (cdr list))))
    (loop a-pair)))
```

```
;;Exercise 2.18
```

```
(define my-reverse
  (lambda (a-list)
    (define (loop list list-now)
      (if (empty? list)
          list-now
          (loop (cdr list) (cons (car list) list-now))))
    (loop a-list '())))
```

```
;;Exercise 2.19
```

```
(define first-denomination
  (lambda (value-list)
    (car value-list)))
(define except-first-denomination
  (lambda (value-list)
    (cdr value-list)))
```

```
(define no-more?
  (lambda (value-list)
    (empty? value-list)))
```

```
(define (cc amount coin-values)
```



```

(cond ((= amount 0) 1)
      ((or (< amount 0) (no-more? coin-values)) 0)
      (else
       (+ (cc amount
              (except-first-denomination coin-values))
          (cc (- amount
                 (first-denomination coin-values))
              coin-values))))))

;;Exercise 2.20
(define (same-parity . w)
  (let ((first-even? (even? (car w))))
    (define (same-parity? item)
      (let ((this-even? (even? item)))
        (or (and this-even? first-even?)
            (and (not this-even?) (not first-even?)))))
    (define (loop items result)
      (cond ((empty? items) result)
            ((same-parity? (car items))
             (cons (car items) (loop (cdr items) result)))
            (else
             (loop (cdr items) result))))
    (loop w '())))

;(define nil '())
;;Exercise 2.21
;Version 1
(define (square-list items)
  (if (null? items)
      '()
      (cons (square (car items)) (square-list (cdr items)))))

;Version 2
(define (my-map proc items)
  (if (null? items)
      '()
      (cons (proc (car items))
            (map proc (cdr items)))))

(define (square-list items)
  (my-map square items))

;;Exercise 2.22
;This is the correct version
(define (square-list items)

```

```

(define (iter things answer)
  (if (null? things)
      answer
      (cons (square (car things))
            (square-list (cdr things)))))
(iter items '())

```

;;Exercise 2.23

```

(define my-for-each
  (lambda (proc items)
    (define (loop things)
      (if (null? things)
          (display "\nOK")
          (begin
             (proc (car things))
             (loop (cdr things)))))
    (loop items)))

```

;;Exercise 2.24

```

;(1 (2 (3 4)))

```

;;Exercise 2.25

```

;(cadaddr '(1 3 '(5 7) 9))
;(car (cdaddr '(1 3 (5 7) 9)))
;(caar '((7)))
;(car (cdr (car (cdr (car (cdr (car (cdr (cadadr '(1 (2 (3 (4 (5 (6
7))))))))))))))

```

;;Exercise 2.26

```

(define x (list 1 2 3))
(define y (list 4 5 6))
;(append x y)
;(cons x y)
;(list x y)
;(1 2 3 4 5 6)
;((1 2 3) 4 5 6)
;((1 2 3) (4 5 6))

```

;;Exercise 2.27

```

(define x (list (list 1 2) (list 3 4)))
(define deep-reverse
  (lambda (items)
    (define (loop things now)
      (cond ((null? things) now)

```

```

        ((pair? (car things))
         (let ((temp (reverse (car things))))
           (loop (cdr things) (cons temp now))))
        (else
         (loop (cdr things) (cons (car things) now))))
(loop items '()))

```

;;Exercise 2.28

```

(define fringe
  (lambda (tree)
    (cond ((null? tree) '())
          ((pair? (car tree))
           (append (fringe (car tree)) (fringe (cdr tree))))
          (else
           (cons (car tree) (fringe (cdr tree)))))))

```

;;Exercise 2.29

```

(define (make-mobile left right)
  (cons left right))

```

```

(define (make-branch length structure)
  (cons length structure))

```

;a

```

(define (left-branch mobile)
  (car mobile))
(define (right-branch mobile)
  (cadr mobile))

```

```

(define (branch-length branch)
  (car branch))
(define (branch-structure branch)
  (cadr branch))

```

;b

```

(define (total-weight mobile)
  (define (branch-weight branch)
    (if(not (pair? (branch-structure branch)))
        (branch-structure branch)
        (total-weight (branch-structure branch))))
  (+ (branch-weight (left-branch mobile))
     (branch-weight (right-branch mobile))))

```

;c Design a predicate that tests whether a binary mobile is balanced.

```

(define (branch-weight branch)
  (if(not (pair? (branch-structure branch)))
      (branch-structure branch)

```

```

    (total-weight (branch-structure branch))))

(define (structure-is-mobile? branch)
  (pair? (branch-structure branch)))

(define (troque branch)
  (* (branch-length branch)
     (branch-weight branch)))

(define (balanced-branch? branch)
  (if (structure-is-mobile? branch)
      (balanced-mobile? (branch-structure branch))
      #t))

(define (balanced-mobile? mobile)
  (let ((left (left-branch mobile))
        (right (right-branch mobile)))
    (if (= (troque left) (troque right))
        (and (balanced-branch? left)
              (balanced-branch? right))
        #f)))

;d
;change
(define (make-mobile left right)
  (cons left right))
(define (make-branch length structure)
  (cons length structure))

(define (right-branch mobile)
  (cdr mobile))
(define (branch-structure branch)
  (cdr branch))

;;Exercise 2.30
(define square-tree
  (lambda (tree)
    (cond ((null? tree) '())
          ((not (pair? tree)) (* tree tree))
          (else (cons (square-tree (car tree))
                      (square-tree (cdr tree)))))))

(define (square-tree tree)
  (map (lambda (sub-tree)
        (if (pair? sub-tree)
            (square-tree sub-tree)
            (* sub-tree sub-tree)))
       tree))

```

```

        (square-tree sub-tree)
        (* sub-tree sub-tree)))
    tree))

```

;;Exercise 2.31

```

(define (tree-map proc tree)
  (map (lambda (sub-tree)
        (if(pair? sub-tree)
            (tree-map proc sub-tree)
            (proc sub-tree)))
    tree))

```

;;Exercise 2.32

```

(define (subsets s)
  (if (null? s)
      (list '())
      (let ((rest (subsets (cdr s))))
        (append rest (map (lambda(a-list)
                           (cons (car s) a-list))
                          rest)))))

```

;;For example: (subsets (list 1 2 3))

;(())

;((cons 3 ()) ()) ==> ((3) ())

;((cons 2 (3)) (cons 2 ()) (3) ()) ==> ((2 3) (2) (3) ())

;((cons 1 (2 3)) (cons 1 (2)) (cons 1 (3)) (cons 1 ()) (2 3) (2) (3) ()) ==>((1 2 3) (1 2) (1 3) (1) (2 3) (2) (3) ())

;;Exercise 2.33

```

(define (accumulate op initial sequences)
  (if (null? sequences)
      initial
      (op (car sequences)
          (accumulate op initial (cdr sequences)))))

```

```

(define (my-map p sequences)
  (accumulate
    (lambda (x y)
      (cons (p x) y))
    '()
    sequences))

```

```

(define (my-append seq-a seq-b)
  (accumulate
    cons
    seq-b

```

```
seq-a))
```

```
(define (my-length seq)
  (accumulate
    (lambda (x y)
      (+ y 1))
    0
    seq))
```

```
;;Exercise 2.34
```

```
(define (horner-eval x coefficient-sequence)
  (accumulate
    (lambda (this-coeff higher-terms)
      (+ (* higher-terms x)
         this-coeff))
    0
    coefficient-sequence))
```

```
;;Exercise 2.35
```

```
(define (count-leaves tree)
  (accumulate
    (lambda (x y)
      (+ x y))
    0
    (map (lambda (node)
          (cond ((null? node) 0)
                ((pair? node) (count-leaves node))
                (else 1)))
         tree)))
```

```
;;Exercise 2.36
```

```
(define (accumulate-n op init seqs)
  (if (null? (car seqs))
      '()
      (cons (accumulate op init (map car seqs))
            (accumulate-n op init (map cdr seqs)))))
```

```
;;Exercise 2.37
```

```
(define (dot-product v w)
  (accumulate + 0 (map * v w)))
```

```
(define (matrix-*-vector m v)
  (map
```

```

(lambda (a-vector)
  (dot-product a-vector v))
m))

```

```

(define (transpose mat)
  (accumulate-n
   cons
   '()
   mat))

```

```

(define (matrix-*-matrix m n)
  (let ((cols (transpose n)))
    (map
     (lambda (a-vector)
       (map (lambda (cols-vector)
              (dot-product cols-vector a-vector))
            cols))
     m)))

```

;;Exercise 2.38

```

(define fold-right accumulate)

```

```

(define (fold-right op initial sequences)
  (if (null? sequences)
      initial
      (op (car sequences)
          (accumulate op initial (cdr sequences))))))

```

```

(define (fold-left op initial sequences)
  (define (iter result rest)
    (if (null? rest)
        result
        (iter (op result (car rest))
              (cdr rest))))
  (iter initial sequences))

```

```

;;(fold-right / 1 (list 1 2 3)) ==> 3/2
;;(fold-left / 1 (list 1 2 3)) ==> 1/6
;;(fold-right list '() (list 1 2 3)) ==> (1 (2 (3 ())))
;;(fold-left list '() (list 1 2 3)) ==> (((() 1) 2) 3)
;;Associative

```

;;Exercise 2.39

```

(define nil '())

```

```

(define (my-reverse sequences)

```

```
(fold-right
  (lambda (x y)
    (append y (list x)))
  nil sequences))
```

```
(define (my-reverse sequences)
  (fold-left
    (lambda (x y)
      (cons y x))
    nil
    sequences))
```

;;Exercise 2.40

```
(define (flatmap proc seq)
  (accumulate append nil (map proc seq)))
```

```
(define (enumerate-interval low high)
  (define (loop index now)
    (if (> index high)
        now
        (loop (+ index 1)
              (append now (list index)))))
  (loop low nil))
```

```
(define (unique-pairs n)
  (flatmap
    (lambda (index)
      (map (lambda (x)
            (list index x))
          (enumerate-interval 1 index)))
    (enumerate-interval 1 n)))
```

;;Exercise 2.41

```
(define (ordered-one-triple n)
  (map
    (lambda (a-list)
      (cons n a-list))
    (unique-pairs (- n 1))))
```

```
(define (ordered-triples n)
  (flatmap
    ordered-one-triple
    (enumerate-interval 1 n)))
```

```
(define (S-triple n s)
```



```

(define (Ok? a-triple)
  (= (+ (car a-triple) (cadr a-triple) (caddr a-triple))
     s))
(let ((sequences (ordered-triples n)))
  (filter
   Ok?
   sequences)))

```

;;Exercise 2.42

```

(define (queens board-size)
  (define (queen-cols k)
    (if (= k 0)
        (list empty-board)
        (filter
         (lambda (positions) (safe? k positions))
         (flatmap
          (lambda (rest-of-queens)
            (map (lambda (new-row)
                    (adjoin-position new-row k rest-of-queens))
                 (enumerate-interval 1 board-size))))
         (queen-cols (- k 1))))))
  (queen-cols board-size))

```

```

(define empty-board nil)

```

```

(define (adjoin-position new-row k rest-of-queens)
  (cons (list new-row k) rest-of-queens))

```

```

(define (safe? k positions)
  (let ((k-th (car positions)))
    (define (conflicts? a b)
      (let ((dx (abs (- (car a) (car b))))
            (dy (abs (- (cadr a) (cadr b)))))
        (cond ((= dx 0) #t)
              ((= dy 0) #t)
              ((= dx dy) #t)
              (else #f)))))
    (define (Test pos)
      (cond((null? pos) #t)
            ((conflicts? (car pos) k-th) #f)
            (else
             (Test (cdr pos)))))
    (Test (cdr positions)))))

```

```
;;Exercise 2.43
```

```
;速度会慢得很多, 因为随着k 值增大, rest-of-queens 增大很多,
```

```
;;=====Example: A Picture
```

```
Language=====
```

```
;;=====2.3 Symbolic Data=====
```

```
;;Exercise 2.53
```

```
;(list 'a 'b 'c)
```

```
;(list (list 'george)) ;(a b c)
```

```
;(cdr '((x1 x2) (y1 y2))) ;((george))
```

```
;(cadr '((x1 x2) (y1 y2))) ;((y1 y2)) (y1 y2)
```

```
;(pair? (car '(a short list))) ;#f
```

```
;(memq 'red '((red shoes) (blue socks))) ;#f
```

```
;(memq 'red '(red shoes blue socks)) ;(red shoes blue socks)
```

```
;;Exercise 2.54
```

```
(define (my-equal? a b)
```

```
  (cond ((and (symbol? a) (symbol? b))
```

```
    (if (eq? a b)
```

```
        #t
```

```
        #f))
```

```
    ((and (number? a) (number? b))
```

```
      (= a b))
```

```
    ((and (null? a) (null? b)) #t)
```

```
    ((and (list? a) (list? b))
```

```
      (if (my-equal? (car a) (car b))
```

```
          (my-equal? (cdr a) (cdr b))
```

```
          #f))
```

```
    (else
```

```
      #f)))
```

```
;;Exercise 2.55
```

```
;(car '(quote abracadabra))
```

```
;;Example: Symbolic Differentiation
```

```
(define (variable? x) (symbol? x))
```

```
(define (same-variable? v1 v2)
```

```
  (and (variable? v1) (variable? v2) (eq? v1 v2)))
```

```
(define (make-sum a1 a2)
```

```
  (cond ((=number? a1 0) a2)
```

```

      ((=number? a2 0) a1)
      ((and (number? a1) (number? a2)) (+ a1 a2))
      (else (list '+ a1 a2))))
(define (=number? exp num)
  (and (number? exp) (= exp num)))

```

```

(define (make-product m1 m2)
  (cond ((or (=number? m1 0) (=number? m2 0)) 0)
        ((=number? m1 1) m2)
        ((=number? m2 1) m1)
        ((and (number? m1) (number? m2)) (* m1 m2))
        (else (list '* m1 m2))))

```

```

(define (sum? x)
  (and (pair? x) (eq? (car x) '+)))
(define (addend s) (cadr s))
(define (augend s) (caddr s))

```

```

(define (product? x)
  (and (pair? x) (eq? (car x) '*)))

```

```

(define (multiplier p) (cadr p))
(define (multiplicand p) (caddr p))

```

;;Exercise 2.56

```

(define (exponentiation? x)
  (and (pair? x) (eq? (car x) '**)))
(define (base p)
  (cadr p))
(define (exponent p)
  (caddr p))
(define (make-exponentiation base expt)
  (cond ((= expt 0) 1)
        ((= expt 1) base)
        (else
         (list '** base expt))))

```

```

(define (deriv exp var)
  (cond ((number? exp) 0)
        ((variable? exp)
         (if (same-variable? exp var) 1 0))
        ((sum? exp)

```

```

      (make-sum (deriv (addend exp) var)
                 (deriv (augend exp) var)))
    ((product? exp)
     (make-sum
      (make-product (multiplier exp)
                    (deriv (multiplicand exp) var))
      (make-product (deriv (multiplier exp) var)
                    (multiplicand exp))))
    ((exponentiation? exp)
     (make-product (make-product (exponent exp)
                                 (make-exponentiation (base exp) (- (exponent
exp) 1)))
                   (deriv (base exp) var)))
    (else
     (error "unknown expression type -- DERIV" exp))))

```

;;Exercise 2.57

```

(define (sum? x)
  (and (pair? x) (eq? (car x) '+)))
(define (addend s) (cadr s))
(define (augend s)
  (if (null? (cdddr s))
      (caddr s)
      (cons '+ (cddr s))))

```

```

(define (product? x)
  (and (pair? x) (eq? (car x) '*)))
(define (multiplier p) (cadr p))
(define (multiplicand p)
  (if (null? (cdddr p))
      (caddr p)
      (cons '* (cddr p))))

```

;;Exericse 2.58

;;a

```

(define (sum? x)
  (and (pair? x) (eq? (cadr x) '+)))
(define (addend s)
  (car s))
(define (augend s)
  (caddr s))

```

```

(define (make-sum a1 a2)
  (cond ((=number? a1 0) a2)

```

```

((=number? a2 0) a1)
((and (number? a1) (number? a2)) (+ a1 a2))
(else (list a1 '+ a2))))

```

```

(define (product? x)
  (and (pair? x) (eq? (cadr x) '*)))
(define (multiplier p) (car p))
(define (multiplicand p)
  (caddr p))

```

```

(define (make-product m1 m2)
  (cond ((or (=number? m1 0) (=number? m2 0)) 0)
        ((=number? m1 1) m2)
        ((=number? m2 1) m1)
        ((and (number? m1) (number? m2)) (* m1 m2))
        (else (list m1 '* m2))))

```

```

(define (exponentiation? x)
  (and (pair? x) (eq? (cadr x) '**)))
(define (base p)
  (car p))
(define (exponent p)
  (caddr p))
(define (make-exponentiation base expt)
  (cond ((= expt 0) 1)
        ((= expt 1) base)
        (else
         (list base '** expt))))

```

;b ;;This is two harder, i will solve this latter =_=!!

;;Exercise 2.59

```

(define (element-of-set? x set)
  (cond ((null? set) false)
        ((equal? x (car set)) true)
        (else (element-of-set? x (cdr set)))))

```

```

(define (adjoin-set x set)
  (if (element-of-set? x set)
      set
      (cons x set)))

```

```

(define (union-set set1 set2)
  (define (loop a-set set-now)

```

```

    (if(null? a-set)
        set-now
        (loop (cdr a-set)
                (adjoin-set (car a-set) set-now))))
(loop set1 set2))

```

;;Exercise 2.60

```

(define (element-of-set? x set)
  (cond ((null? set) false)
        ((equal? x (car set)) true)
        (else
         (element-of-set? x (cdr set)))))
(define (adjoin-set x set)
  (cons x set))
(define (union-set set1 set2)
  (append set1 set2))

(define (intersection-set set1 set2)
  (cond ((or (null? set1) (null? set2)) '())
        ((element-of-set? (car set1) set2)
         (cons (car set1)
                (intersection-set (cdr set1) set2)))
        (else (intersection-set (cdr set1) set2))))

```

;;Exericse 2.61

```

(define (element-of-set? x set)
  (cond ((null? set) false)
        ((= x (car set)) true)
        ((< x (car set)) false)
        (else (element-of-set? x (cdr set)))))

(define (adjoin-set x set)
  (cond ((< x (car set)) (cons x set))
        ((= x (car set)) set)
        (else
         (cons (car set) (adjoin-set x (cdr set))))))

```

;;Exercise 2.62

```

(define (union-set set1 set2)
  (cond ((null? set1) set2)
        ((null? set2) set1)
        (else
         (let((x1 (car set1))
              (x2 (car set2)))

```

[illegible]

```

(make-tree 7 nil nil)))))))))
;;the two version tree-list visit tree in the same order
;b: Version1 grows slowly

;;Exercise 2.64
(define (list->tree elements)
  (car (partial-tree elements (length elements))))

(define (partial-tree elts n)
  (if (= n 0)
      (cons '() elts)
      (let ((left-size (quotient (- n 1) 2)))
        (let ((left-result (partial-tree elts left-size)))
          (let ((left-tree (car left-result))
                (non-left-elts (cdr left-result))
                (right-size (- n (+ left-size 1))))
            (let ((this-entry (car non-left-elts))
                  (right-result (partial-tree (cdr non-left-elts)
                                              right-size)))
              (let ((right-tree (car right-result))
                    (remaining-elts (cdr right-result)))
                (cons (make-tree this-entry left-tree right-tree)
                      remaining-elts))))))))))

;a partial-tree uses a tree recursive style
;b  $O(n)$  growth

;;Exercise 2.65
(define (union-set-1 tree1 tree2)
  (list->tree (union-set (tree->list-2 tree1)
                        (tree->list-2 tree2))))

(define (intersection-set-1 tree1 tree2)
  (list->tree (intersection-set (tree->list-2 tree1)
                              (tree->list-2 tree2))))

;;Exercise 2.73
(define (put-get-gen)
  (define (make-record key1 key2 value)
    (list key1 key2 value))
  (define (key1-record rec) (car rec))
  (define (key2-record rec) (cadr rec))
  (define (value-record rec) (caddr rec))
  (define (match-record? rec key1 key2)
    (and (equal? (key1-record rec) key1)
          (equal? (key2-record rec) key2)
          (equal? (value-record rec) value))))

```



```

(equal? (key2-record rec) key2)))
(define table '())
(list
  (lambda (op type item)
    (define (delete-from tbl key1 key2 result)
      (if (null? tbl)
          result
          (let ((rec (car tbl)))
            (if (match-record? rec key1 key2)
                (delete-from (cdr tbl) key1 key2 result)
                (delete-from (cdr tbl) key1 key2 (cons (car tbl) result))
            ))))
    (let ((new-rec (make-record op type item)))
      (set! table (cons new-rec (delete-from table op type '()))))

      new-rec))
(lambda (op type)
  (define (select-from tbl key1 key2)
    (if (null? tbl)
        #f
        (let ((rec (car tbl)))
          (if (match-record? rec key1 key2)
              (value-record rec)
              (select-from (cdr tbl) key1 key2))))
    )
  (select-from table op type))
(lambda () table)
))

```

```

(define put-get (put-get-gen))
(define put (car put-get))
(define get (cadr put-get))
(define table (caddr put-get))

```

```

(define (install-sum-package)
  (define (addend operands)
    (cadr operands))
  (define (augend operands)
    (let ((rest (cdr operands)))
      (if (null? (cddr rest))
          (cadr rest)
          (cons '+ (cdr rest)))))
  (define (make-sum a1 a2)
    (cond ((=number? a1 0) a2)

```

```

      ((=number? a2 0) a1)
      ((and (number? a1) (number? a2)) (+ a1 a2))
      (else (list '+ a1 a2))))
(define (deriv-sum exp var)
  (make-sum (deriv (addend exp) var)
             (deriv (augend exp) var)))
(put 'make '+ make-sum)
(put 'deriv '+ deriv-sum)
'done
)

```

```

(define (install-product-package)
  (define (multiplier operands)
    (cadr operands))
  (define (multiplicand operands)
    (let ((rest (cdr operands)))
      (if (null? (cddr rest))
          (cadr rest)
          (cons '* (cdr rest)))))
  (define (make-product m1 m2)
    (cond ((or (=number? m1 0) (=number? m2 0)) 0)
          ((=number? m1 1) m2)
          ((=number? m2 1) m1)
          ((and (number? m1) (number? m2)) (* m1 m2))
          (else (list '* m1 m2))))
  (define (deriv-product exp var)
    ((get 'make '+)
     (make-product (multiplier exp)
                   (deriv (multiplicand exp) var))
     (make-product (deriv (multiplier exp) var)
                   (multiplicand exp))))
  (put 'make '* make-product)
  (put 'deriv '* deriv-product)
)

```

```

(define (install-exponent-package)
  (define (base operands)
    (cadr operands))
  (define (expt operands)
    (caddr operands))
  (define (make-exponent base expt)
    (cond ((= expt 0) 1)
          ((= expt 1) base)
          (else (list '** base expt))))

```

```

(define (deriv-expt exp var)
  ((get 'make '*))
  ((get 'make '*) (expt exp)
   (make-exponent (base exp) (- (expt exp) 1)))
  (deriv (base exp) var)))
(put 'make '** make-exponent)
(put 'deriv '** deriv-expt)
'done)

```

```

(install-sum-package)
(install-product-package)
(install-exponent-package)
(define (deriv exp var)
  (cond ((number? exp) 0)
        ((variable? exp)
         (if (same-variable? exp var) 1 0))
        ((sum? exp)
         ((get 'deriv '+) exp var))
        ((product? exp)
         ((get 'deriv '*) exp var))
        ((exponentiation? exp)
         ((get 'deriv '**) exp var))
        (else
         (error "unknown expression type -- DERIV" exp))))

```

```

(define (sum? x)
  (and (pair? x) (eq? (car x) '+)))

```

```

(define (product? x)
  (and (pair? x) (eq? (car x) '*)))

```

```

(define (exponentiation? x)
  (and (pair? x) (eq? (car x) '**)))

```