

1) 20 pts

Mark the following statements as **TRUE**, **FALSE**, or **UNKOWN**. No need to provide any justification.

[**TRUE/FALSE**]

Given a network $G(V, E)$ and flow f , and the residual graph $G_f(V', E')$, then $|V|=|V'|$ and $2|E| \geq |E'|$.

[**TRUE/FALSE**]

The Ford-Fulkerson Algorithm terminates when the source s is not reachable from the sink t in the residual graph.

[**TRUE/FALSE/UNKOWN**]

NP is the class of problems that are not solvable in polynomial time.

[**TRUE/FALSE/UNKOWN**]

If problem A is NP complete, and problem B can be reduced to problem A in quadratic time. Then problem B is also NP complete

[**TRUE/FALSE/UNKOWN**]

If X can be reduced in polynomial time to Y and Z can be reduced in polynomial time to Y, then X can be reduced in polynomial time to Z.

[**TRUE/FALSE**]

Let $G(V, E)$ be a weighted graph and let T be a minimum spanning tree of G obtained using Prim's algorithm. The path in T between s (the root of the MST) and any other node in the tree must be a shortest path in G.

[**TRUE/FALSE**]

DFS can be used to find the shortest path between any two nodes in a non-weighted graph.

[**TRUE/FALSE**]

The Bellman-Ford algorithm cannot be parallelized if there are negative cost edges in the network.

[**TRUE/FALSE**]

A perfect matching in a bipartite graph can be found using a maximum-flow algorithm.

[**TRUE/FALSE**]

Max flow in a flow network with integer capacities can be found exactly using linear programming.