

1) 20 pts

Mark the following statements as **TRUE** or **FALSE**. No need to provide any justification.

[TRUE/FALSE] **True**

Assume $P \neq NP$. Let A and B be decision problems. If A is in NP-Complete and $A \leq_P B$, then B is not in P.

[TRUE/FALSE] **True**

There exists a decision problem X such that for all Y in NP, Y is polynomial time reducible to X.

It is in fact the Cook-Levin theorem that proves that there are problems that are NP-complete. Picking X to be 3-SAT (or any other in problem in NP-complete) ensures that ensures that every Y in NP is reducible to X.

[TRUE/FALSE] **True**

If P equals NP, then NP equals NP-complete.

True. A problem X is NP-hard iff any problem in NP can be reduced in polynomial time to X. If P equals NP, then we can reduce any problem in NP to any other problem by just solving the original problem.

[TRUE/FALSE] **False**

The running time of a dynamic programming algorithm is always $\theta(P)$ where P is the number of sub-problems.

Solution: False. The running time of a dynamic program is the number of subproblems times the time per subproblem. This would only be true if the time per subproblem is $O(1)$.

[TRUE/FALSE] **True**

A spanning tree of a given undirected, connected graph $G=(V,E)$ can be found in $O(|E|)$ time. You can just walk on the graph.

[TRUE/FALSE] **True**

To find the minimum element in a max heap of n elements, it takes $O(n)$ time

[TRUE/FALSE] **True**

Kruskal's algorithm for finding the MST works with positive and negative edge weights.

[TRUE/FALSE] **False**

If a problem is not in P, then it must be in NP.

[TRUE/FALSE] **False**

If an NP-complete problem can be solved in linear time, then all NP-complete problems can be solved in linear time.

[TRUE/FALSE] **True**