

2 hr exam  
Close book and notes

1) 20 pts

Mark the following statements as **TRUE** or **FALSE**. No need to provide any justification except for the question at the bottom of the page.

[ **TRUE/FALSE** ]

In a flow network, if all edge capacities are distinct, then the max flow of this network is unique.

[ **TRUE/FALSE** ]

To find the minimum element in a max heap of  $n$  elements, it takes  $O(n)$  time.

[ **TRUE/FALSE** ]

Let  $T$  be a spanning tree of graph  $G(V, E)$ , let  $k$  be the number of edges in  $T$ , then  $k=O(V)$

[ **TRUE/FALSE** ]

Linear programming problems can be solved in polynomial time.

[ **TRUE/FALSE** ]

Consider problem A: given a flow network, find the maximum flow from a node  $s$  to a node  $t$ . problem A is in NP.

[ **TRUE/FALSE** ]

Given  $n$  numbers, it takes  $O(n)$  time to construct a binary min heap.

[ **TRUE/FALSE** ]

Kruskal's algorithm for finding the MST works with positive and negative edge weights.

[ **TRUE/FALSE** ]

Breadth first search is an example of a divide-and-conquer algorithm.

[ **TRUE/FALSE** ]

If a problem is not in P, then it must be in NP.

[ **TRUE/FALSE** ]

$L1$  can be reduced to  $L2$  in Polynomial time and  $L1$  is in NP, then  $L2$  is in NP