| Name: | USC | CID: |
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INF 553 - Spring 2018

Quiz 4: Jaccard & Minhash signatures (10 points), 15 minutes

Consider three sets: S1, S2, and S3 whose characteristic matrix is shown in columns 1-4 of the table below.

| Row # | S1 | S2 | S3 | f1(x)=(x+3)%5 | f2(x)=(3x+1)%5 |
|-------|-----------|-----------|-----------|---------------|----------------|
| 0 | 0 | 1 | 1 | 3 | 1 |
| 1 | 1 | 1 | 0 | 4 | 4 |
| 2 | 0 | 0 | 1 | 0 | 2 |
| 3 | 1 | 1 | 0 | 1 | 0 |
| 4 | 0 | 1 | 1 | 2 | 3 |

- 1. [3 points] Suppose we generate signatures of the sets using hash functions f1(x) and f2(x) shown in the table above. Recall that x is the old row #. Fill in the blanks with the new row numbers generated by each hash function.
- 2. [3 points] Fill in the signature matrix below with minHash values generated by f1 and f2 for the three sets.

| | S1 | S2 | S3 |
|----|----|-----------|-----------|
| f1 | 1 | 1 | 0 |
| f2 | 0 | 0 | 1 |

3. [4 points] Fill in the table below with the actual similarity of pairs (i.e., their Jaccard similarity) and their similarity estimated using the signatures.

| Pair | Actual Sim. | Estimated Sim. |
|----------|-------------|----------------|
| (S1, S2) | | |
| (S1, S3) | | |
| (S2, S3) | | |

| Pair | Actual Sim | Estimated Sim |
|---------|------------|---------------|
| (S1,S2) | 1/2 | 1 |
| (S1,S3) | 0 | 0 |
| (S2,S3) | 2/5 | 0 |

Actual Sim worth 2 points
Estimated Sim worth 2 points