

1) 20 pts

Mark the following statements as **TRUE** or **FALSE**. No need to provide any justification.

[**TRUE/FALSE**]

Let X be a decision problem. If we prove that X is in the class NP and give a poly-time reduction from X to 3-SAT, we can conclude that X is NP-complete.

[**TRUE/FALSE**]

Let A be an algorithm that operates on a list of n objects, where n is a power of two. A spends $\Theta(n^2)$ time dividing its input list into two equal pieces and selecting one of the two pieces. It then calls itself recursively on that list of $n/2$ elements. Then A 's running time on a list of n elements is $O(n)$.

[**TRUE/FALSE**]

If there is a polynomial time algorithm to solve problem A then A is in NP.

[**TRUE/FALSE**]

A pseudo-polynomial time algorithm is always slower than a polynomial time algorithm.

[**TRUE/FALSE**]

In a dynamic programming formulation, the sub-problems must be non-overlapping.

[**TRUE/FALSE**]

A spanning tree of a given undirected, connected graph $G = (V, E)$ can be found in $O(E)$ time.

[**TRUE/FALSE**]

Ford-Fulkerson can return a zero maximum flow for flow networks with non-zero capacities.

[**TRUE/FALSE**]

If $f(n) = \Theta(g(n))$ and $g(n) = \Theta(h(n))$, then $h(n) = \Theta(f(n))$

[**TRUE/FALSE**]

There is a polynomial-time solution for the 0/1 Knapsack problem if all items have the same weight but different values.

[**TRUE/FALSE**]

If there are negative cost edges in a graph but no negative cost cycles, Dijkstra's algorithm still runs correctly.