

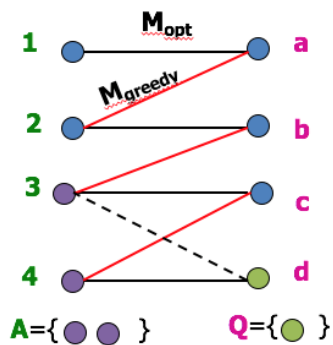
Quiz: Web Advertising

Name: \_\_\_\_\_ ID: \_\_\_\_\_

1) (1 pt) Explain and write the definition of the competitive ratio.

2) (1 pt) Show a case using 4 ads and 4 queries to demonstrate the worst-case scenario in the greedy algorithm.

3) (3 pts) Using the example below to show that the competitive ratio of the greedy algorithm is  $\frac{1}{2}$ . (You need to use the sets  $Q$  and  $A$  in your answer.)



4) (1 pt) Fill up the table below with the Balance algorithm

- ◆ Bidder  $A_1$ : bid  $x_1 = 20$  budget  $b_1 = 40$
- ◆ Bidder  $A_2$ : bid  $x_2 = 10$  budget  $b_2 = 50$
- ◆ Assume ties are broken in favor of  $A_1$

Query q	Assigned to Bidder ( $A_1, A_2$ or No Ad)	Remaining Budget for $A_1$	Remaining Budget for $A_2$
At start	----	40	50
1 <sup>st</sup> query q			
2 <sup>nd</sup> query q			
3 <sup>rd</sup> query q			
4 <sup>th</sup> query q			
5 <sup>th</sup> query q			
6 <sup>th</sup> query q			
7 <sup>th</sup> query q			
8 <sup>th</sup> query q			

5) (4pts) Explain the competitive ratio for Balance algorithm with multiple bidders