

1) 20 pts

Mark the following statements as **TRUE** or **FALSE**. No need to provide any justification.

[ **TRUE/FALSE** ]

To prove that a problem X is NP-complete, it is sufficient to prove that 3SAT is polynomial time reducible to X.

[ **TRUE/FALSE** ]

Finding the minimum element in a binary max heap of n elements takes  $O(\log n)$  time

[ **TRUE/FALSE** ]

We are told that in the worst case, algorithm A runs in  $O(n \log n)$  and algorithm B runs in  $O(n^2)$ . Based on these facts, there must be some N that when  $n > N$ , algorithm A runs faster than algorithm B.

[ **TRUE/FALSE** ]

The following recurrence equation  $T(n) = 3T(n/3) + 0.1n$  has the solution:  
 $T(n) = \Theta(n \log(n))$ .

[ **TRUE/FALSE** ]

Every problem in NP can be solved in exponential time by a deterministic Turing machine

[ **TRUE/FALSE** ]

In Kruskal's MST algorithm, if we choose edges in decreasing (instead of increasing) order of cost, we will end up with a spanning tree of maximum total cost

[ **TRUE/FALSE** ]

If all edges in a graph have capacity 1, then Ford-Fulkerson runs in linear time.

[ **TRUE/FALSE** ]

If problem X can be solved using dynamic programming, then X belongs to P.

[ **TRUE/FALSE** ]

If  $\text{Vertex-Cover} \in P$  then  $\text{SAT} \in P$ .

[ **TRUE/FALSE** ]

Assuming  $P \neq NP$ , and X is a problem belonging to class NP. There is no polynomial time algorithm for X.