

1) 20 pts

Mark the following statements as **TRUE** or **FALSE**. No need to provide any justification.

[ **TRUE** / ]

Given a minimum cut, we could find the maximum flow value in  $O(E)$  time.

[ / **FALSE** ]

Any NP-hard problem can be solved in time  $O(2^{\text{poly}(n)})$ , where  $n$  is the input size and  $\text{poly}(n)$  is a polynomial.

[ **TRUE** / ]

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[ **TRUE** / ]

If  $3\text{-SAT} \leq_p 2\text{-SAT}$ , then  $P = NP$ .

[ / **FALSE** ]

Assuming  $P \neq NP$ , there can exist a polynomial-time approximation algorithm for the general Traveling Salesman Problem.

[ / **FALSE** ]

Let  $(S, V-S)$  be a minimum  $(s,t)$ -cut in the network flow graph  $G$ . Let  $(u,v)$  be an edge that crosses the cut in the forward direction, i.e.,  $u \in S$  and  $v \in V-S$ . Then increasing the capacity of the edge  $(u, v)$  necessarily increases the maximum flow of  $G$ .

[ / **FALSE** ]

If problem  $X$  can be solved using dynamic programming, then  $X$  belongs to  $P$ .

[ / **FALSE** ]

All instances of linear programming have exactly one optimal solution.

[ / **FALSE** ]

Let  $Y \leq_p X$  and there exists a 2-approximation for  $X$ , then there must exist a 2-approximation for  $Y$ .

[ **TRUE** / ]

There is no known polynomial-time algorithm to solve an integer linear programming.