

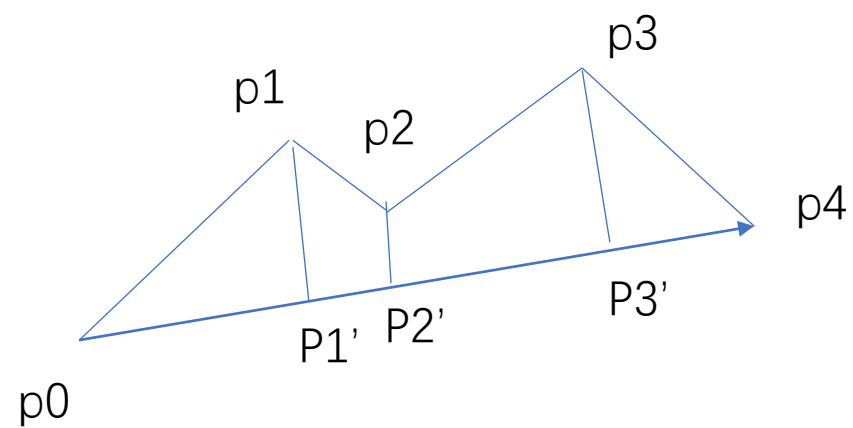
# Direction-Preserving Trajectory Simplification

$$\triangle(\theta_1, \theta_2) = \min\{|\theta_1 - \theta_2|, 2\pi - |\theta_1 - \theta_2|\} \quad (1)$$

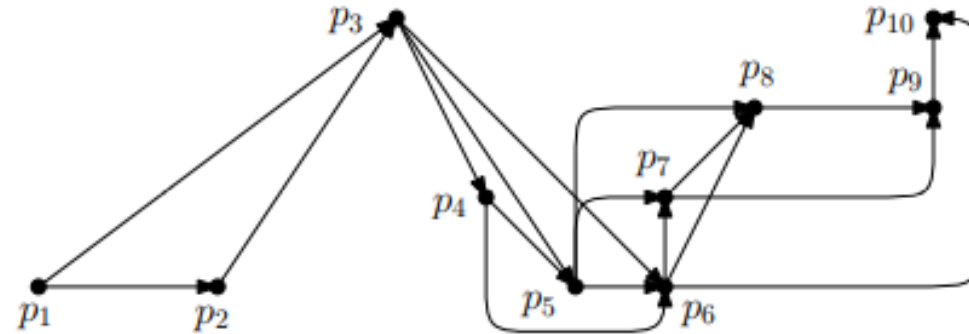
$$\epsilon(\overline{p_{s_k} p_{s_{k+1}}}) = \max_{s_k \leq h < s_{k+1}} \triangle(\theta(\overline{p_{s_k} p_{s_{k+1}}}), \theta(\overline{p_h p_{h+1}}))$$

$$\epsilon(T') = \max_{1 \leq k < m} \epsilon(\overline{p_{s_k} p_{s_{k+1}}}) \quad (2)$$

Closest Euclidean distance:



Algorithm SP:



**Figure 5: The graph  $G_{\epsilon_t}$  constructed based on the running example when  $\epsilon_t$  is set to be  $\pi/4 = 0.785$**

The SP algorithm with the practical enhancement:

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**Algorithm 1** The *SP* algorithm with the practical enhancement

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**Input:** A trajectory  $T = (p_1, p_2, \dots, p_n)$  and the error tolerance  $\epsilon_t$

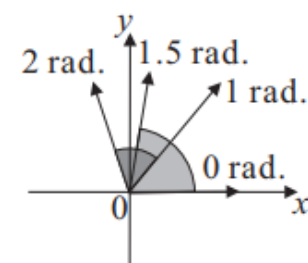
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1:  $H_0 \leftarrow \{p_1\}; U \leftarrow \{p_2, p_3, \dots, p_n\}; l \leftarrow 1$ 
2: while true do
3:    $H_l \leftarrow \emptyset$ 
4:   //process the positions in  $H_{l-1}$  and  $U$  in a reversed order
5:   for each  $p_i$  in  $H_{l-1}$  and each  $p_j$  in  $U$  where  $i < j$  do
6:     if  $\epsilon(\overline{p_i p_j}) \leq \epsilon_t$  then
7:       if  $p_j = p_n$  then
8:         return the trajectory corresponding to the shortest
           path from  $p_1$  to  $p_n$ 
9:        $U \leftarrow U \setminus \{p_j\}; H_l \leftarrow H_l \cup \{p_j\}$ 
10:   $l \leftarrow l + 1$ 
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Trick!

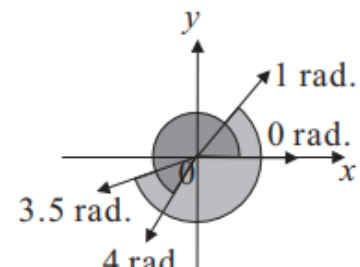
Feasible direction range:

$$fdr(\overline{p_h p_{h+1}} | \epsilon_t) = [\theta(\overline{p_h p_{h+1}}) - \epsilon_t, \theta(\overline{p_h p_{h+1}}) + \epsilon_t] \mod 2\pi \quad (3)$$

$$fdr(T[i, j] | \epsilon_t) = \cap_{i \leq h < j} fdr(\overline{p_h p_{h+1}} | \epsilon_t) \quad (4)$$



(a)  $[0, 1.5] \cap [1.0, 2.0]$



(b)  $[0, 4.0] \cap [3.5, 1.0]$

**Figure 7: Illustration of intersection operations between two angular ranges**

$||fdr(T[i, j])||$  is bounded by  $\min\{1 + \lfloor \frac{\epsilon_t}{(\pi - \epsilon_t)} \rfloor, j - i\}$ .

1,1	1,2	1,3	1,4
2,1	2,2	2,3	2,4
3,1	3,2	3,3	3,4
4,1	4,2	4,3	4,4

$fdr(T[i, j]) \rightarrow fdr(T[i, j-1]) \rightarrow \dots$

The intersect algorithm:

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**Algorithm 2** The *Intersect* Algorithm

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**Input:** A trajectory  $T = (p_1, p_2, \dots, p_n)$ ; an error tolerance  $\epsilon_t$

**Output:** An  $\epsilon_t$ -simplification of  $T'$

- 1:  $T' \leftarrow (p_1)$ ;  $e \leftarrow 1$ ;  $h \leftarrow 2$
  - 2: **while**  $h \leq n$  **do**
  - 3:     **while**  $h \leq n$  and  $\overline{p_e p_h}$  is  $\frac{\epsilon_t}{2}$ -feasible **do**
  - 4:         increment  $h$  by 1
  - 5:     append  $p_{h-1}$  to  $T'$ ;  $e \leftarrow h - 1$
  - 6: **return**  $T'$
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