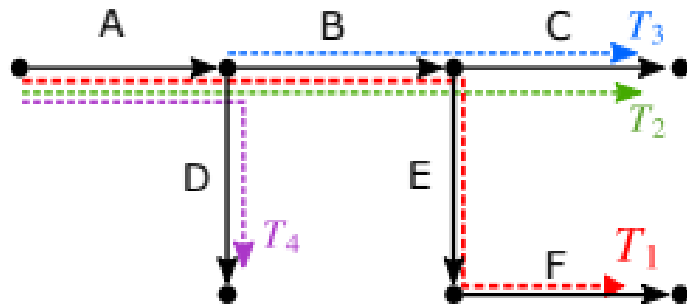


# (2018IEEE ICDE)CiNCT Compression and Retrieval for Massive Vehicular Trajectories via Relative Movement Labeling

Definition:



(a) Network-constrained trajectories (NCTs)

$$T = \underbrace{FEBA}_{T_1^{\text{rev}}} \$ \underbrace{CBA}_{T_2^{\text{rev}}} \$ \underbrace{CB}_{T_3^{\text{rev}}} \$ \underbrace{DA}_{T_4^{\text{rev}}} \$ \# . \quad (1)$$

## BWT(Burrows-Wheeler transform)

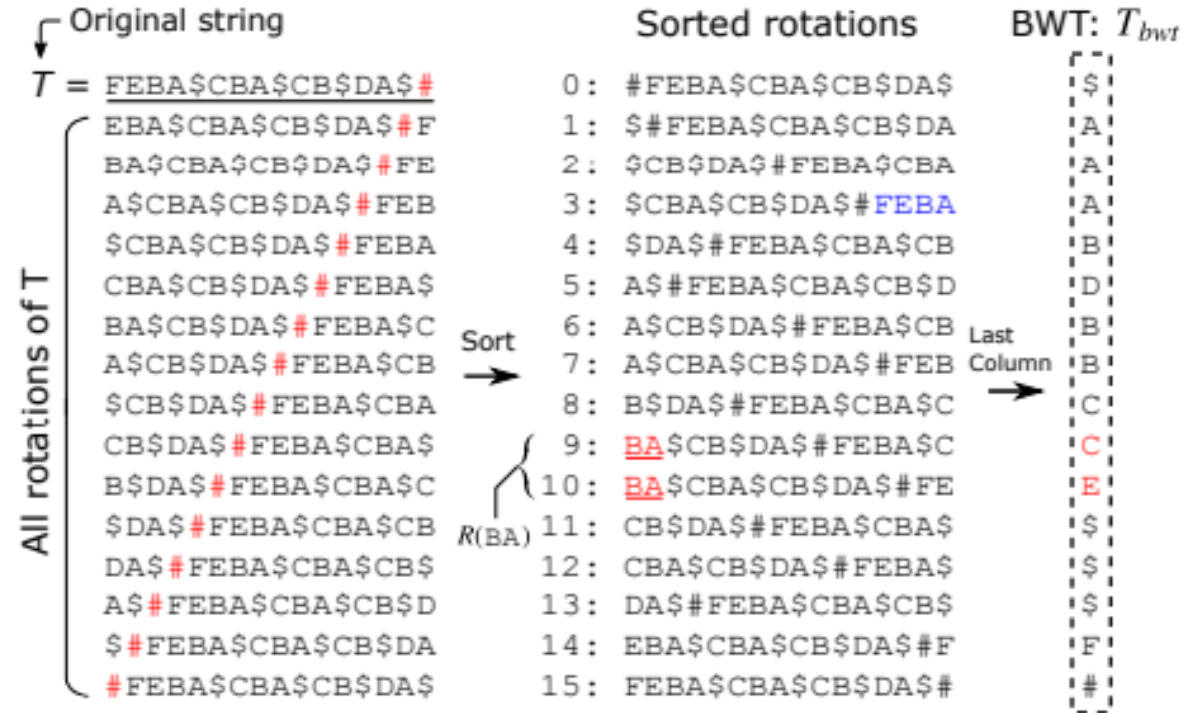
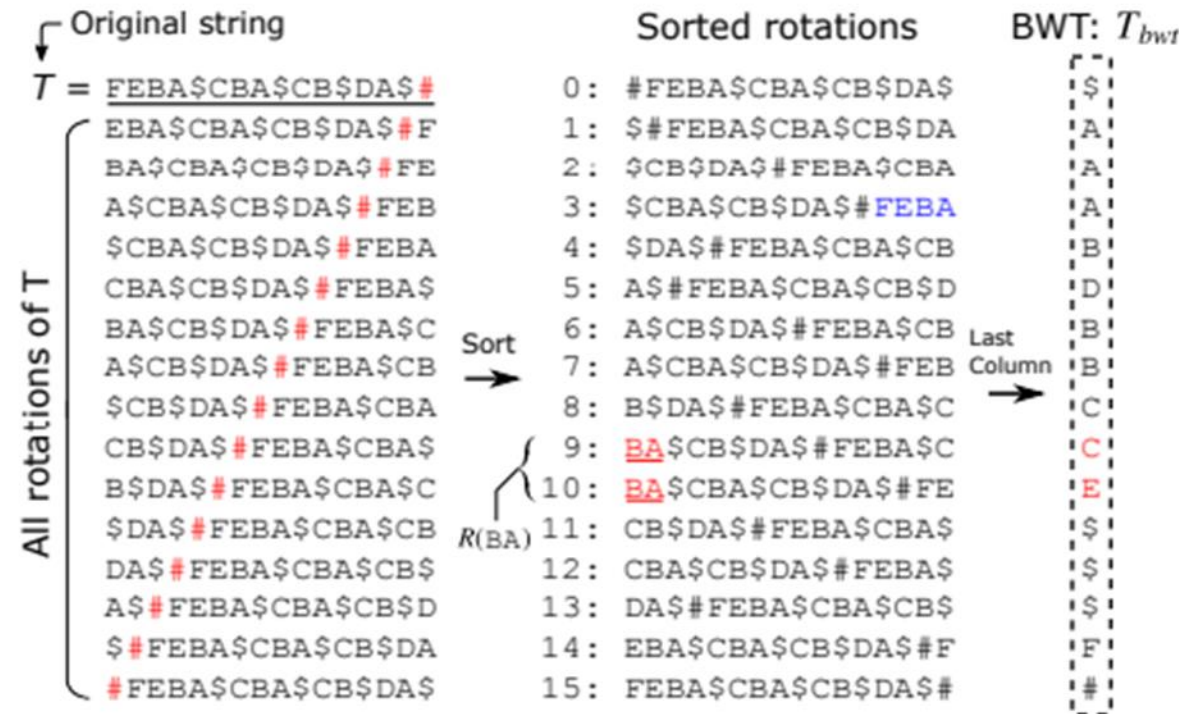


Fig. 2. The BWT of  $T$  is defined to be the last column of the sorted rotations of  $T$ . This example is based on the trajectory string  $T$  in Eq. (1).



$$C[A] = 5 \text{ and } C[B] = 8$$

$$\text{rank}_B(T_{bwt}, 5) = 1$$

Fig. 2. The BWT of  $T$  is defined to be the last column of the sorted rotations of  $T$ . This example is based on the trajectory string  $T$  in Eq. (1).

$P = \text{BA}$ .  $w = \text{A}$ ,  $sp = 5$ ,  $ep = 8$ .

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**Algorithm 1:** Finding the suffix range  $R(P) = [sp, ep)$  for a given query  $P$  of length  $m$  based on  $T_{bwt}$  (*SearchFM*)

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**Input:** BWT string:  $T_{bwt}$ , Query string:  $P$ ,  
Integer array:  $C$

**Output:** Range of  $T_{bwt}$  that matches to  $P$

```
1  $w \leftarrow P[m - 1]$ ;  $sp \leftarrow C[w]$ ;  $ep \leftarrow C[w + 1]$ 
2 for  $i \leftarrow 2$  to  $m$  do
3    $w \leftarrow P[m - i]$ 
4    $sp \leftarrow C[w] + \text{rank}_w(T_{bwt}, sp)$ 
5    $ep \leftarrow C[w] + \text{rank}_w(T_{bwt}, ep)$ 
6   if  $sp \geq ep$  then return NotFound
7 return  $[sp, ep)$ 
```

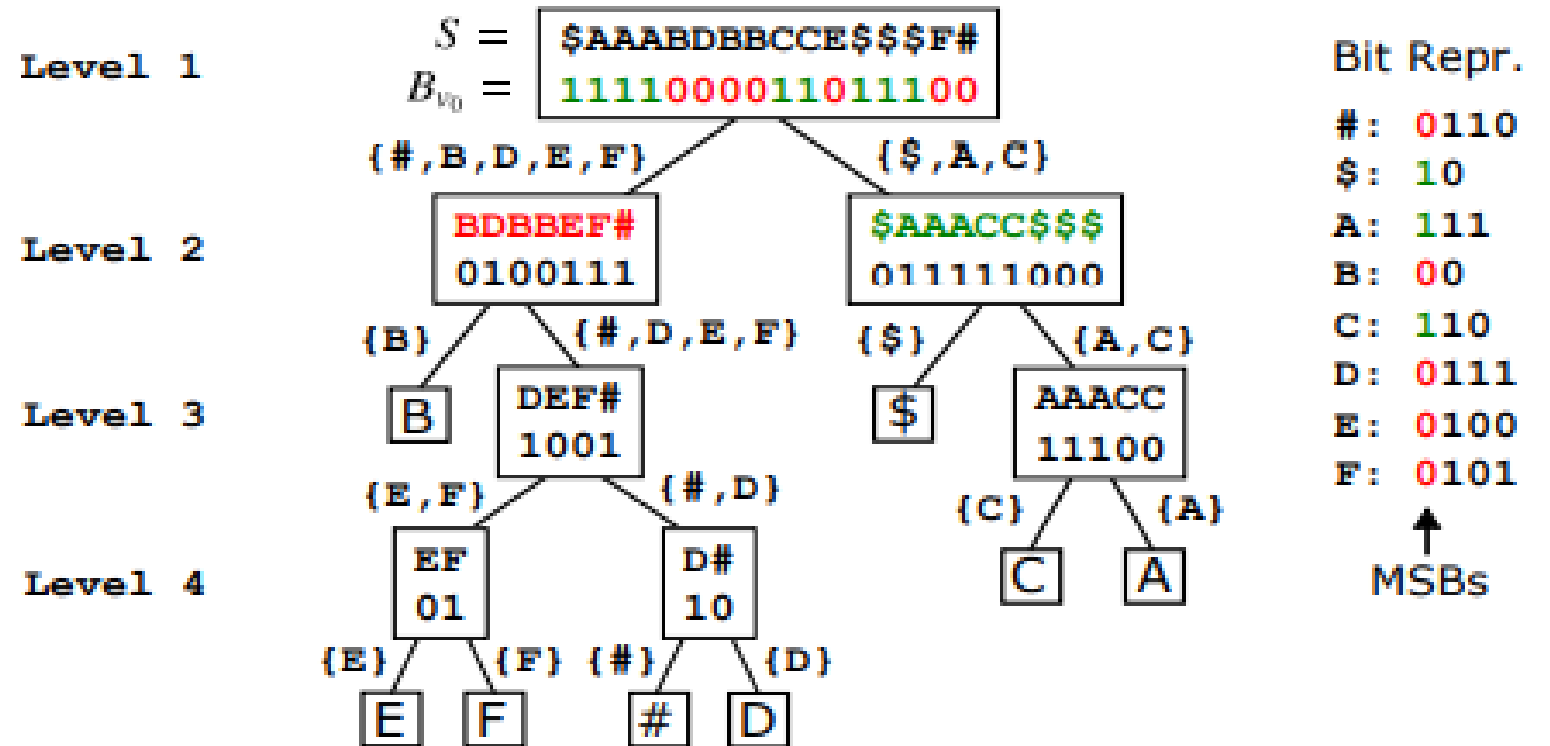
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$$sp = C[\text{B}] + 1 = 9$$

$$ep = C[\text{B}] + 3 = 11$$

9:	<u>BA</u> \$CB\$DA\$#FEBA\$C	<u>C</u>
10:	<u>BA</u> \$CBA\$CB\$DA\$#FE	<u>E</u>

1. Huffman tree
2. Huffman-shaped wavelet tree (HWT)

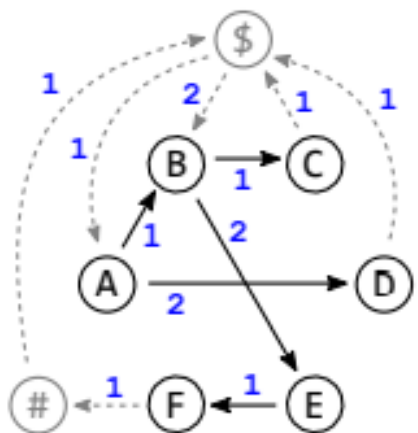


$$\text{rank}_B(T_{bwt}, 5) = 1$$

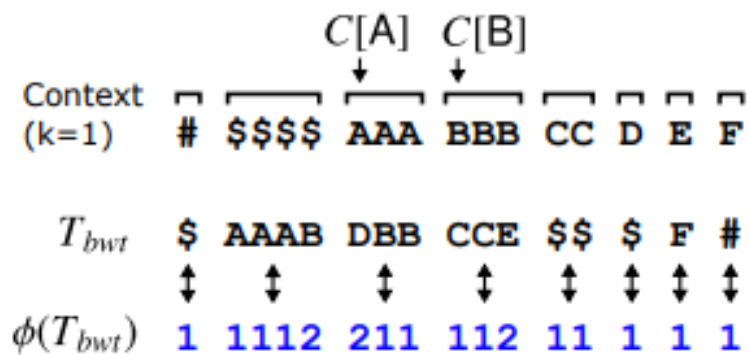
$$\text{Rank0}(B, T_{bwt}, 5) = 1$$

$$\text{Rank0}(B, T_{bwt}, 1) = 1$$

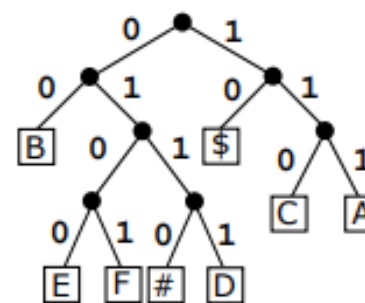
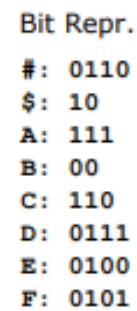
## Relative movement labeling (RML)



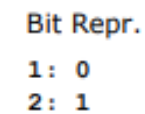
(a) ET-graph and RML



(b) Labeling  $T_{bwt}$  with RML



(a)  $T_{bwt}$



(b)  $\phi(T_{bwt})$ : CiNCT

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**Algorithm 2:** Emulating  $rank_w(T_{bwt}, j)$  by using only  $\phi(T_{bwt})$  ( $PseudoRank(\phi(T_{bwt}), j, w, w', Z_{w'w})$ )

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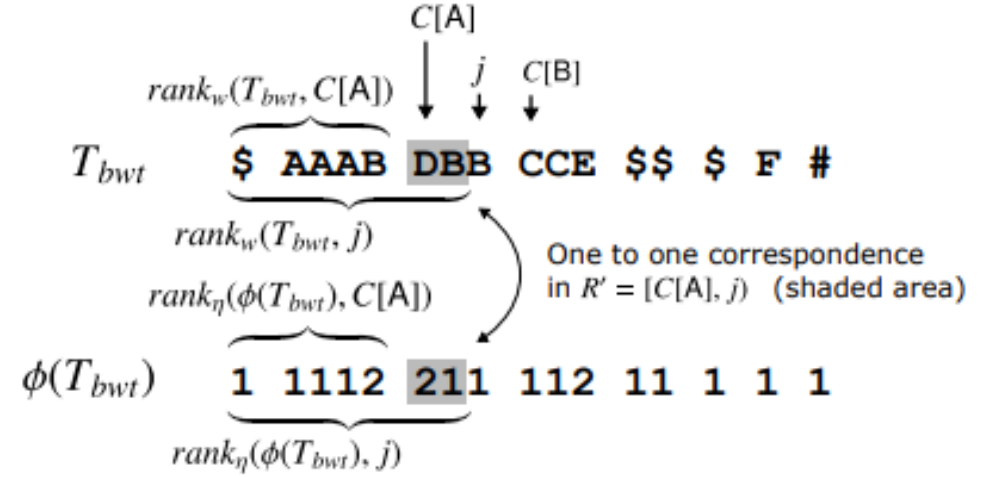
**Input:** Labeled BWT string of length  $n$ :  $\phi(T_{bwt})$ ,  
 Location of rank  $j$ , Correction term  $Z_{w'w}$ ,  
 Target symbol  $w$ , Previous symbol  $w'$

**Output:** The value of  $rank_w(T_{bwt}, j)$

```

1 if  $w \in N_{out}(w')$  and  $C[w'] \leq j \leq C[w' + 1]$  then
2    $\eta \leftarrow \phi(w|w')$  // RML
3   return  $rank_\eta(\phi(T_{bwt}), j) - Z_{w'w}$ 
4 return NotFound
  
```

---



$$rank_w(T_{bwt}, j) - rank_w(T_{bwt}, C[w']) = rank_\eta(\phi(T_{bwt}), j) - rank_\eta(\phi(T_{bwt}), C[w']). \quad (5)$$

$$Z_{w'w} := rank_\eta(\phi(T_{bwt}), C[w']) - rank_w(T_{bwt}, C[w']). \quad (7)$$

$$rank_w(T_{bwt}, j) = rank_\eta(\phi(T_{bwt}), j) - Z_{w'w}, \quad (6)$$



---

**Algorithm 3:** Finding the suffix range  $[sp, ep)$  for a given query  $P$  of length  $m$  based on  $\phi(T_{bwt})$  (*LabeledSearchFM*)

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**Input:** Labeled BWT string of length  $n$ :  $\phi(T_{bwt})$ ,  
Query of length  $m$ :  $P[0, m)$ ,  
Correction terms:  $\{Z_{w'w}\}$

**Output:** Range of  $T_{bwt}$  that matches to  $P$

```
1  $w \leftarrow P[m - 1]$ ;  $sp \leftarrow C[w]$ ;  $ep \leftarrow C[w + 1]$ 
2 for  $i \leftarrow 2$  to  $m$  do
3    $w' \leftarrow w$  // Save the previous symbol
4    $w \leftarrow P[m - i]$ 
5   if  $w \notin N_{out}(w')$  then
6     return NotFound
7    $sp \leftarrow C[w] + PseudoRank(\phi(T_{bwt}), sp, w, w', Z_{w'w})$ 
8    $ep \leftarrow C[w] + PseudoRank(\phi(T_{bwt}), ep, w, w', Z_{w'w})$ 
9   if  $sp \geq ep$  then
10    return NotFound
11 return  $[sp, ep)$ 
```

---



$$T = \underbrace{\text{FEBA}}_{T_1^{\text{rev}}} \$ \underbrace{\text{CBA}}_{T_2^{\text{rev}}} \$ \underbrace{\text{CB}}_{T_3^{\text{rev}}} \$ \underbrace{\text{DA}}_{T_4^{\text{rev}}} \$ \# . \quad (1)$$

---

**Algorithm 4:** Extracting a sub-path  $T[i-l, i]$  for given  $j = ISA[i]$  and  $l > 0$  (*extract*)

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**Input:** Labeled BWT:  $\phi(T_{bwt})$ , Position on  $T_{bwt}$ :  $j$ ,  
Extraction length:  $l$ , Correction terms:  $\{Z_{w'w}\}$

**Output:** A substring  $S := T[i-l, i]$

```

1  $w' \leftarrow \text{BinarySearch}(j, \{C[w']\})$  //  $T[i]$ 
2 for  $k \leftarrow 1$  to  $l$  do
3    $\eta \leftarrow \phi(T_{bwt})[j]; w \leftarrow \text{decode}(\eta|w'); S[l-k] \leftarrow w$ 
4    $j \leftarrow C[w] + \text{PseudoRank}(\phi(T_{bwt}), j, w, w', Z_{w'w})$ 
5    $w' \leftarrow w$  // Save previous symbol
6 return  $S$ 

```

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